

Lab 2 Due: Oct 20, 2020

Instructions:

- Your R code shall be written in a single script file.
- Name the script file lab2_[your_id].R. For example, lab2_5123700044.R.
- Separate your answers/code into sections according to task_id and part_id.

Task 1 (16 points)

This task is about running linear regression in R. The dataset debonding.txt is about cathodic debonding of elastomeric metal bonds. The variables measured were:

debonding the amount of debonding measured in centimetres

time used measured in minutes

voltage voltage used measured in volts

ph pH at time of bonding

temp temperature measured in Fahrenheit

- (a) (1 point) Use R function read.table to load the contents of the data file debonding.txt into a R data frame called deb.df.
- (b) (1 point) Use R function 1m to construct the full model, name it as deb.full.LM,

debonding =
$$\beta_0 + \beta_1$$
time + β_2 voltage + β_3 ph + β_4 temp + ε

- (c) (1 point) What is the proportion of variability in debonding explained by our model?
- (d) (1 point) Use R to plot the standardised residual \hat{e}'_i against the fitted value \hat{y}_i .
- (e) (1 point) Use R to plot the residual \hat{e}_i against the previous residual \hat{e}_{i-1} .
- (f) (1 point) Use R to plot the estimated autocorrelation function of \hat{e}_i , i.e. the acf plot.
- (g) (1 point) Use R to plot the sample quantiles of \hat{e}_i against the theoretical quantiles of

(h) (1 point) Use R to plot the sample quantiles of \hat{e}'_i against the theoretical quantiles of

- (i) (1 point) Perform a Box-Cox transformation on the response by choosing an appropriate λ from its 95% confidence interval, name the transformed response as debonding.bc.
- (j) (1 point) Construct the following model, name it as deb.full.bc.LM,

$$\texttt{debonding.bc} = \beta_0^* + \beta_1^* \texttt{time} + \beta_2^* \texttt{voltage} + \beta_3^* \texttt{ph} + \beta_4^* \texttt{temp} + \varepsilon$$

Is there any evidence that working with the transformed response is better?

- (k) (1 point) Suppose assumptions are satisfied, what does F-test say about the models.
- (l) (1 point) Suppose assumptions are satisfied, comment on the significance of ph in the presence of the other three regressors.
- (m) (1 point) Use R to find the 95% confidence interval of β_1 .



Lab 2Due: Oct 13, 2020

(n) (1 point) Use R to find the 95% confidence interval of the mean debonding when

```
time = 30.00, voltage = 1350, ph = 4.00,
                                        temp = 300
```

(o) (1 point) Use R to find the 95% prediction interval of debonding when

```
time = 30.00, voltage = 1350, ph = 4.00, temp = 300
```

(p) (1 point) Construct the following two, name them as deb.no.v.LM and deb.no.v.p.LM

$$\begin{aligned} & \texttt{debonding} = \beta_0^{**} + \beta_1^{**} \texttt{time} + \beta_3^{**} \texttt{ph} + \beta_4^{**} \texttt{temp} + \varepsilon \\ & \texttt{debonding} = \beta_0^{***} + \beta_1^{***} \texttt{time} + \beta_4^{***} \texttt{temp} + \varepsilon \end{aligned}$$

Suppose the residual analysis has provided no evidence that model assumptions are violated by the two models above. Is there anything in the output of summary (deb.no.v.LM) and summary(deb.no.v.p.LM) that can be used as the basis for deciding which of the two models is better? If so, how to use it. And can we use it to compare amongst all four models?

Task 2 (4 points)

This task is about categorical regressors and partial F-test.

(a) (1 point) Load sim_lab2.csv.bz2 into a R data frame, name it as sim.df, then run $> sim.LM = lm(y^{-}.+x1*x3+x1*x4+x2*x3+x2*x4+x3*x4, data = sim.df)$ > summary(sim.LM)

Explain why there are NAs in the summary output.

- (b) (1 point) Suppose there is no evidence against model assumptions being satisfied. According to our model, is the conditional mean of Y significantly different for x4=B and x4=C given other regressors take the same value. Justify your answer.
- (c) (1 point) Read the help documentation on anova. 1m, then comment on the meaning of having a large p-value in the following output

> anova(sim.LM)

```
Analysis of Variance Table
Response: y
             Df
                    Sum Sq
                              Mean Sq
                                          F value Pr(>F)
x1
              1 388292353
                           388292353 60154.2397 <2e-16
x2
                 36089461
                             36089461
                                        5590.9782 <2e-16
              1
                                                           ***
x3
              3
                     16007
                                 5336
                                           0.8266 0.4790
              2
                 20440965
                             10220482
                                        1583.3568 <2e-16
x4
x1:x3
              3
                     30274
                                10091
                                           1.5633 0.1961
              2
                   6467655
                              3233828
                                         500.9845 <2e-16
x1:x4
              3
x2:x3
                     17517
                                 5839
                                           0.9046 0.4380
              2
                                           1.9963 0.1360
x2:x4
                     25772
                                12886
              4
                      6405
                                           0.2481 0.9109
x3: x4
                                 1601
Residuals 3978
                 25677774
                                 6455
```

(d) (1 point) What can we learn from the following?

```
> source("~/Desktop/lab2_func.R")
> f.vec = replicate(1e4, sim.p.func(n=200)); sim.plot()
```