Data Introduction Exploratory Analysis Three-level Models Random Effects Diagnostic Check Discussion

The Effects of a Stress-Relieving Program in Hospital Nurses: A Three-Level Analysis

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Data Introduction

- The dataset is from the Multilevel analysis: Techniques and applications (Hox, J. J., Moerbeek, M., & Schoot, R, 2018), which contains data from a cross-sectional hypothetical study on stress experienced by nurses in hospitals.
- In each of 25 hospitals, four wards were selected and randomly assigned to an experimental or control condition, where the intervention included a training program to cope with job-related stress. After the intervention was implemented, a random sample of 10 nurses from each ward completed a survey to test job-related stress level.

Variables in the dataset

- hospital: ID number for a hospital (1, ..., 25), a total of 25 hospitals
- ward: ward numbering within a hospital (1, 2, 3, 4), a total of 4 wards from each hospital
- nurse: ID number for a nurse (1, ..., 1000), a total of 1000 nurses (not used in programming)
- age: nurse's age in years gender: nurse's gender (0 = male, 1 = female)
- experience: nurse's years of experience working stress: outcome variable, a scale from 1 to 7
- wardtype: type of hospital ward ('general care', 'special care')
- hospize: hospital size ('small', 'medium', 'large')
- expcon: intervention indicator variable ('control', 'experiment')

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Variables overview

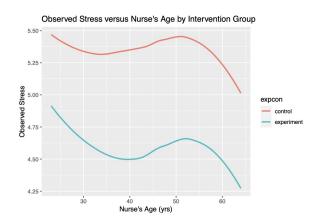
hospital <dbl></dbl>	ward <dbl></dbl>	wardid <dbl></dbl>	nurse <dbl></dbl>	age <dbl></dbl>	gend <db< th=""><th></th><th>experience <dbl></dbl></th><th>stress <dbl></dbl></th><th>wardtype <chr></chr></th><th></th><th>hospsize <chr></chr></th></db<>		experience <dbl></dbl>	stress <dbl></dbl>	wardtype <chr></chr>		hospsize <chr></chr>
1	1	11	1	36		0	11	7	general care		large
1	1	11	2	45		0	20	7 general care		are	large
1	1	11	3	32		0	7	7 general care		ire	large
1	1	11	4	57		1	25	6 general care		ire	large
1	1	11	5	46		1	22	6 general care		large	
1	1	11	6	60		1	22	6 general care		large	
expcon <chr></chr>		hospsize.n <dbl></dbl>	wardty	pe.n dbl>	expcon.n <dbl></dbl>	cgender <chr></chr>	age.C <dbl></dbl>	exper	ience.C <dbl></dbl>	Chospsize <dbl></dbl>	Cexpcon <dbl></dbl>
experiment		2		0	1	Male	-7.005		-6.057	1	0.5
experiment		2		0	1	Male	1.995		2.943	1	0.5
experiment		2		0	1	Male	-11.005	-	10.057	1	0.5
experiment		2		0	1	Female	13.995		7.943	1	0.5
experiment		2		0	1	Female	2.995		4.943	1	0.5
experiment		2		0	1	Female	16.995		4.943	1	0.5

Statistic	N	Mean	St. Dev.	Min	Max
hospital	1,000	13.016	6.947	1	25
ward	1,000	2.493	1.119	1	4
wardid	1,000	132.653	69.476	11	254
nurse	1,000	500.500	288.819	1	1,000
age	1,000	43.005	12.042	23	64
gender	1,000	0.735	0.442	0	1
experience	1,000	17.057	6.042	1	38
stress	1,000	4.977	0.980	1	7
hospsize.n	1,000	0.776	0.689	0	2
wardtype.n	1,000	0.501	0.500	0	1
expcon.n	1,000	0.504	0.500	0	1
age.C	1,000	-0.000	12.042	-20.005	20.995
experience.C	1,000	0.000	6.042	-16.057	20.943
Chospsize	1,000	-0.224	0.689	-1	1
Cexpcon	1,000	0.004	0.500	-0.500	0.500

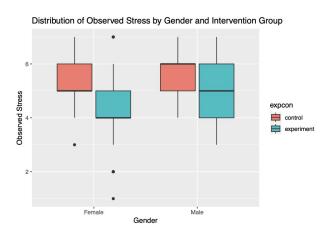
: observation index

: outcome

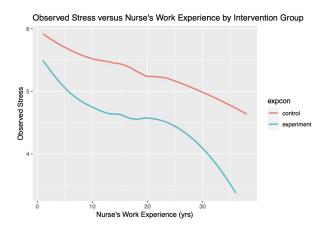
: covariates



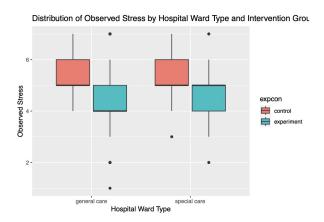
- It can be viewed as approximately linear, considering that the lower number of nurses in older age groups may be an artifact of the data.
- Given that both lines are simply parallel to each other, there is no moderating effect of intervention on this association.



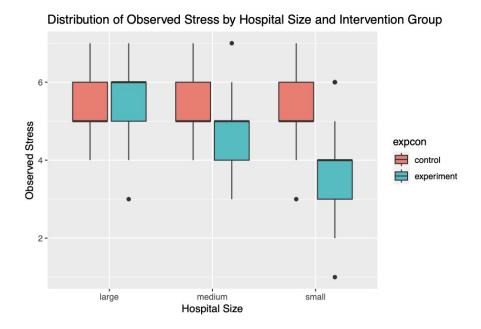
- Among males, there is a large overlaps in stress, and it is unclear whether there is an intervention effect among females.
- The plot does not suggest a moderating effect of intervention on the association between stress and gender.



- There appears to be a liner relationship between observed stress and nurse's experience in years.
- Given that the two trajectories behave in parallel, this does not suggest a moderating effect of intervention on this association.



• Since the intervention effect size seems to be the same within each ward type, therefore, there does not seem to be a moderating effect.



- It seems that there is a linear decline in stress across the hospital size;
- Because the effect size of intervention is different between the hospital sizes, there is a potential moderating effect.

Model1: Three-level model using only a random intercept at each appropriate level of hierarchy

```
Level 1 (nurse): Y_{ijk} = \gamma_{0jk} + \gamma_{1jk} \operatorname{Sex}_{ijk} + \gamma_{2jk} \operatorname{Cexp}_{ijk} + \gamma_{3jk} \operatorname{Cage}_{ijk} + \epsilon_{ijk}

Level 2 (ward): \gamma_{0jk} = \gamma_{00k} + b_{0jk} + \gamma_{01k} \operatorname{Nwardtype}_{jk} + \gamma_{02k} \operatorname{Cexpcon}_{ik}

Level 3 (hospital): \gamma_{00k} = \beta_{000} + b_{0k} + \beta_{001} \operatorname{Chospsize}_{k};
```

$$\gamma_{02k} = \beta_{020} + \beta_{021} \text{Chospsize}_k; \gamma_{01k} = \beta_{010}; \gamma_{1jk} = \beta_{100}; \gamma_{2jk} = \beta_{200}; \gamma_{3jk} = \beta_{300}$$

Combined Model:
$$Y_{ijk} = \beta_{000} + b_{0k} + b_{0jk} + \beta_{001} \text{Chospsize}_k + \beta_{010} \text{Nwardtype}_{ik} + (\beta_{020} + \beta_{021} \text{Chospsize}_k) \text{Cexpcon}_{jk} + \beta_{100} \text{Sex}_{ijk} + \beta_{200} \text{Cexp}_{ijk} + \beta_{300} \text{Cage}_{ijk} + \epsilon_{ijk}$$

Conditional ICCs:

- The ICC within the same ward and the same hospital is 58.42%.
- The ICC from the same hospital regardless of ward type is 26.20%.

Model2: Three-level model adding a random slope for centered intervention indicator variable due to hospital

Level 1 (nurse):
$$Y_{ijk} = \gamma_{0jk} + \gamma_{1jk} \operatorname{Sex}_{ijk} + \gamma_{2jk} \operatorname{Cexp}_{ijk} + \gamma_{3jk} \operatorname{Cage}_{ijk} + \epsilon_{ijk}$$

Level 2 (ward): $\gamma_{0jk} = \gamma_{00k} + b_{0jk} + \gamma_{01k} \operatorname{Nwardtype}_{ik} + \gamma_{02k} \operatorname{Cexpcon}_{ik}$
Level 3 (hospital): $\gamma_{00k} = \beta_{000} + b_{0k} + \beta_{001} \operatorname{Chospsize}_{k}$;

$$\gamma_{02k} = \beta_{020} + \beta_{021} \text{Chospsize}_k + b_{02k}; \gamma_{01k} = \beta_{010}; \gamma_{1jk} = \beta_{100}; \gamma_{2jk} = \beta_{200}; \gamma_{3jk} = \beta_{300}$$

Combined Model:
$$Y_{ijk} = \beta_{000} + b_{0k} + b_{0jk} + \beta_{001} \text{Chospsize}_k + \beta_{010} \text{Nwardtype}_{jk} + (\beta_{020} + \beta_{021} \text{Chospsize}_k + b_{02k}) \text{Cexpcon}_{jk} + \beta_{100} \text{Sex}_{ijk} + \beta_{200} \text{Cexp}_{ijk} + \beta_{300} \text{Cage}_{ijk} + \epsilon_{ijk}$$

Conditional ICCs:

- The ICC within the same ward, the same hospital, and same condition is 68.86%.
- The ICC within the same ward and the same hospital is 39.74%.
- The ICC within the same hospital is 23.81%.

Model Comparison

• To compare the two models, the only difference between them is in the covariance matrix – therefore, we need to conduct a LRT using REML: The hypotheses are:

$$H_0: \sigma_{b_{02k}}^2 = 0$$

$$H_1: \sigma_{b_{02k}}^2 \neq 0$$

- The likelihood ratio test (LRT), implemented via REML, with df=2, G2=8.406 and p=0.0149 (smaller than 0.10), indicates that the addition of the random effect of intervention across different hospitals is significantly improving the fit of the model to the data.
- Hence, we choose Model2 as our final model.

Fixed effects of the final model

```
Value Std.Error DF t-value p-value
(Intercept)
                  5.399858 0.10327271 897
                                          52.28737 0.0000
age.C
                  0.022300 0.00219598 897
                                         10.15512 0.0000
                 -0.454716 0.03489625 897 -13.03050 0.0000
gender
experience.C
                 -0.061804 0.00446073 897 -13.85515 0.0000
wardtype.n
                 0.053069 0.07304260 72 0.72655 0.4699
Chospsize
                 0.458206 0.12922692 23 3.54575 0.0017
Cexpcon
                 -0.498967 0.12074955 72 -4.13225 0.0001
Chospsize: Cexpcon 0.998592 0.16741718 72 5.96469 0.0000
```

As hospital size increased from small to medium to large, the significant reduction in mean stress level due to intervention was significantly diminished/diluted:

There are

- a significant reduction in mean stress level due to intervention at **small** hospitals (an estimated reduction of $\beta_{Cexpon} \beta_{Chospsize:Cexpcon} = -0.499 0.998 = -1.5$);
- a significant reduction in mean stress level due to intervention in **medium-sized hospitals** (an estimated reduction of β_{Cexpon} =-0.499 points);
- a non-significant increase in large-sized hospitals (an estimated increase of $\beta_{Cexpon} + \beta_{Chospsize:Cexpcon} = -0.499 + .998 = 0.499$), meaning that intervention did not seem to significantly impact mean stress level among nurses in large hospitals.

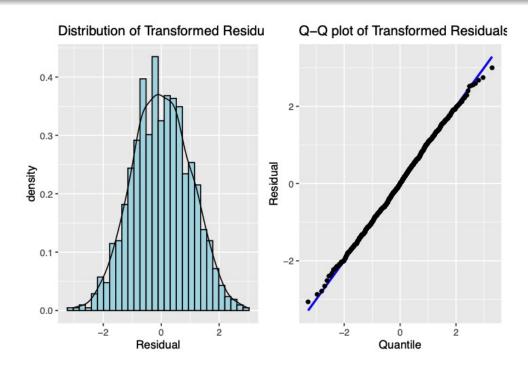
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Random effects of the final model

```
Random Effects:
  Level: hospital
                               lower
                                                   upper
sd((Intercept))
                          0.2771991 0.3893819 0.5469652
sd(Cexpcon)
                          0.2554489 0.4223545 0.6983133
cor((Intercept), Cexpcon) -0.2634529 0.3238953 0.7360486
  Level: ward
                    lower
                                est.
                                         upper
sd((Intercept)) 0.2605456 0.3297284 0.4172812
 Within-group standard error:
    lower
               est.
                        upper
0.4444111 0.4654225 0.4874272
```

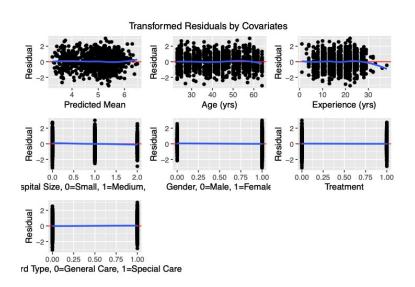
- Estimated correlation between b_{0k} and b_{02k} is 0.34, which means the larger the deviation of a hospital's mean for nurses' stress from the overall mean of stress averaged across all hospitals, the larger the deviation for that hospital's intervention effect from the overall intervention effect size averaged across all hospitals.
- Similar to M1, the majority of heterogeneity in stress (response variable) is explained by the correlation among responses from the same ward within a hospital, but it is now composed of an additional source of heterogeneity due to the varying effect sizes of intervention across different hospitals.

Histogram and Q-Qplot for the transformed residuals



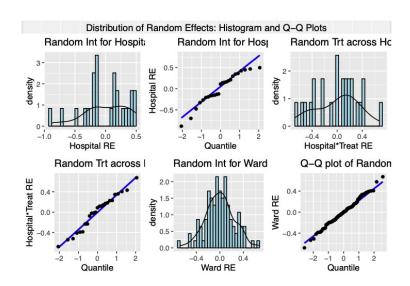
The histogram of residuals looks pretty normal, and the Q-Q plot indicates no significant departures from the Normality.

Marginal transformed residuals



The residuals are approximately 0 on average and their variability is approximately half above and half below the average of 0.

Histograms and Q-Q plots of the random effects BLUPS



Despite the small number of hospitals and in the study, the residuals appear to follow a normal distribution.

Discussion

- Conclusion: This intervention lowered stress among nurses working in small hospitals and to a smaller degree in medium sized hospitals. The intervention did not exhibit an effect in large hospitals.
- Strength:
 - This analysis was able to incorporated all three levels of clustering while additionally controlling for many covariates, both categorical (nurse gender and ward type) and continuous (nurse age and experience in years).
 - Heterogeneity was accounted for in terms of the intervention's effect at various hospitals. This would NOT be possible via any ANOVA type analysis.

Additional works

- Two levels or three levels?: Use LRT via REML to compare the null models with and without the nesting of wards in hospitals; We choose three levels;
- Use centered variables or not? We choose centered;
- What fixed effects are significant to be included? We choose fixed effects in the final model;
- What cross-level interactions are significant to be included? We choose *Chospsize* × *Cexpcon*;
- What random slope should be included? This is the slice I show today.