

# Edges, Contours and Lines

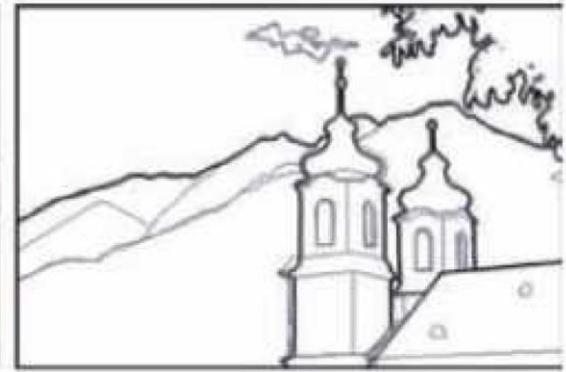
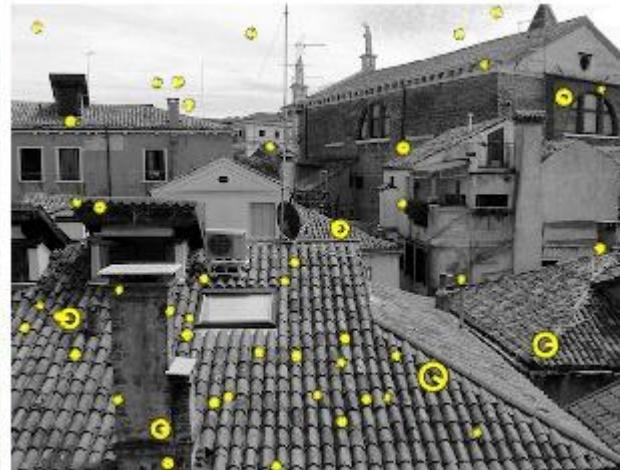
CS 6384 Computer Vision

Professor Yu Xiang

The University of Texas at Dallas

Some slides of this lecture are courtesy Robert Collins (PSU)

# Keypoint Features vs. Edge Points



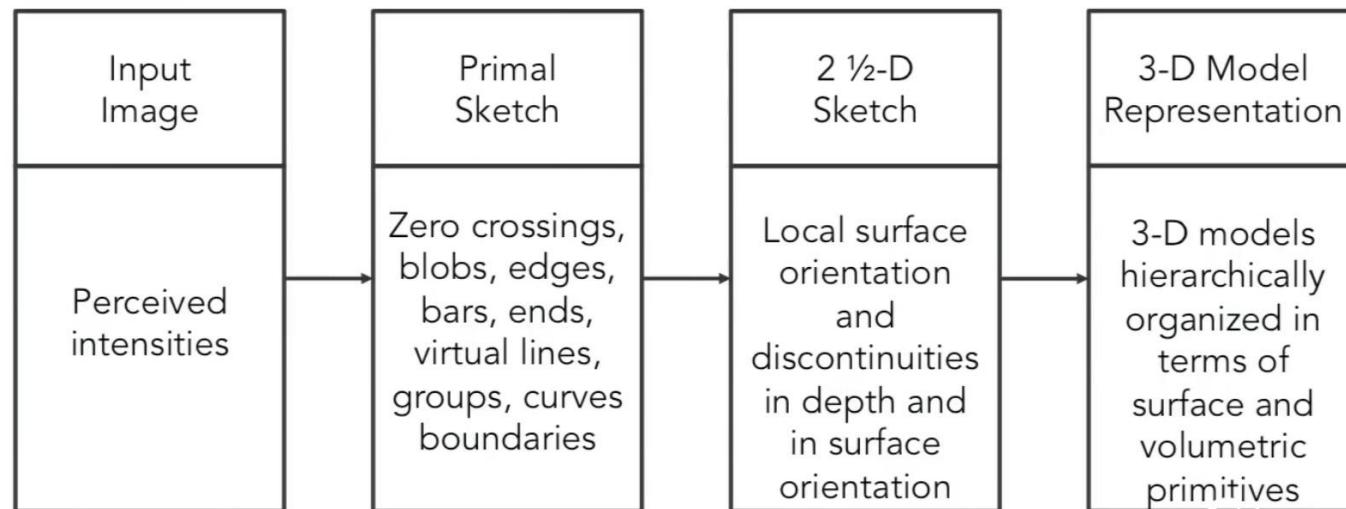
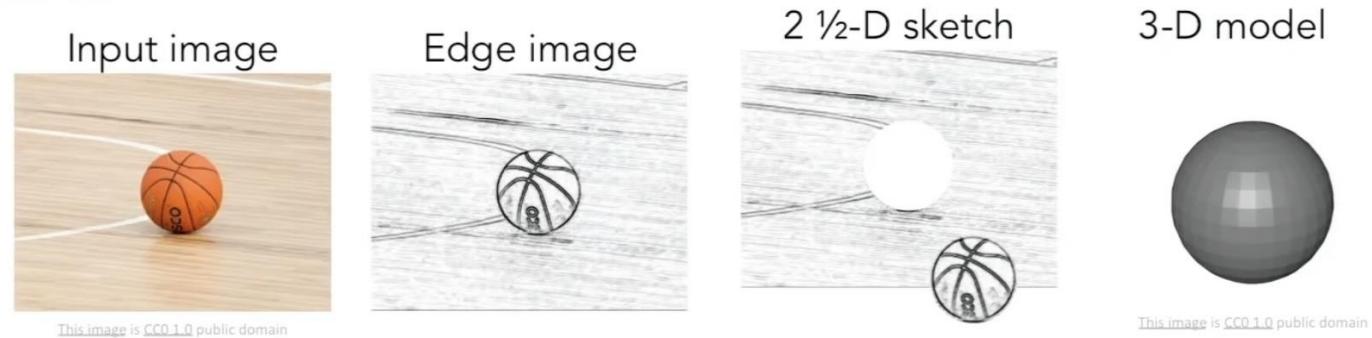
## Keypoints

- Good for feature matching
- Less or no semantic meaning

## Edges

- Not robust for feature matching
- With semantic meanings (object boundaries, occlusion boundaries, shadows, etc.)

# David Marr's Theory of Vision (Neuroscientist)

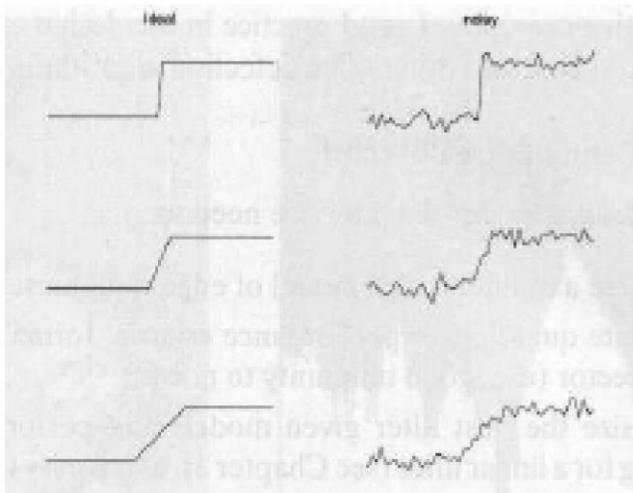
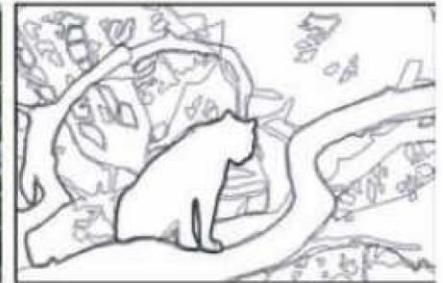


Stages of Visual Representation, David Marr, 1970s

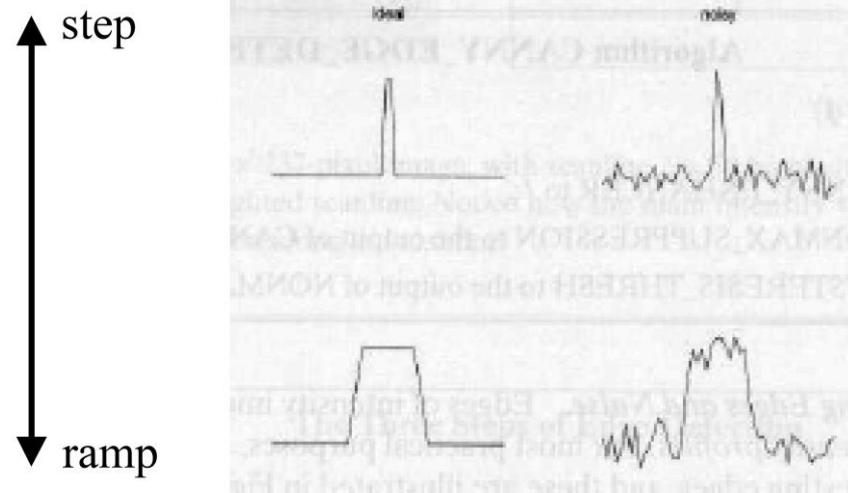
D. Marr. Vision. W. H. Freeman and Co., 1982.

# Edges

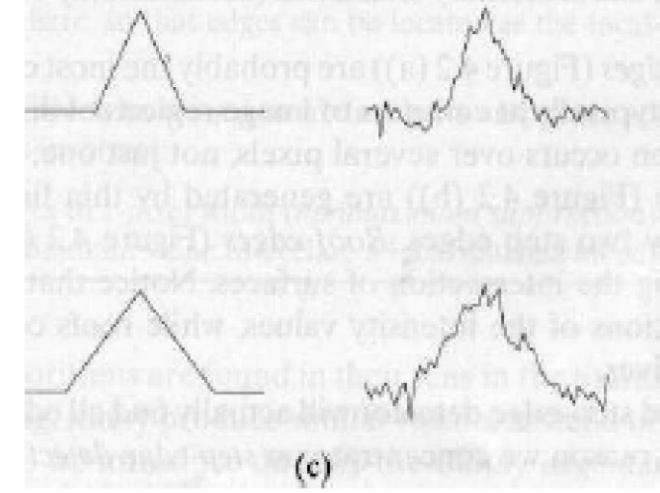
- Edges occur at boundaries between regions of different color, intensity or texture



Step Edge, Ramp Edge



Ridge Edge

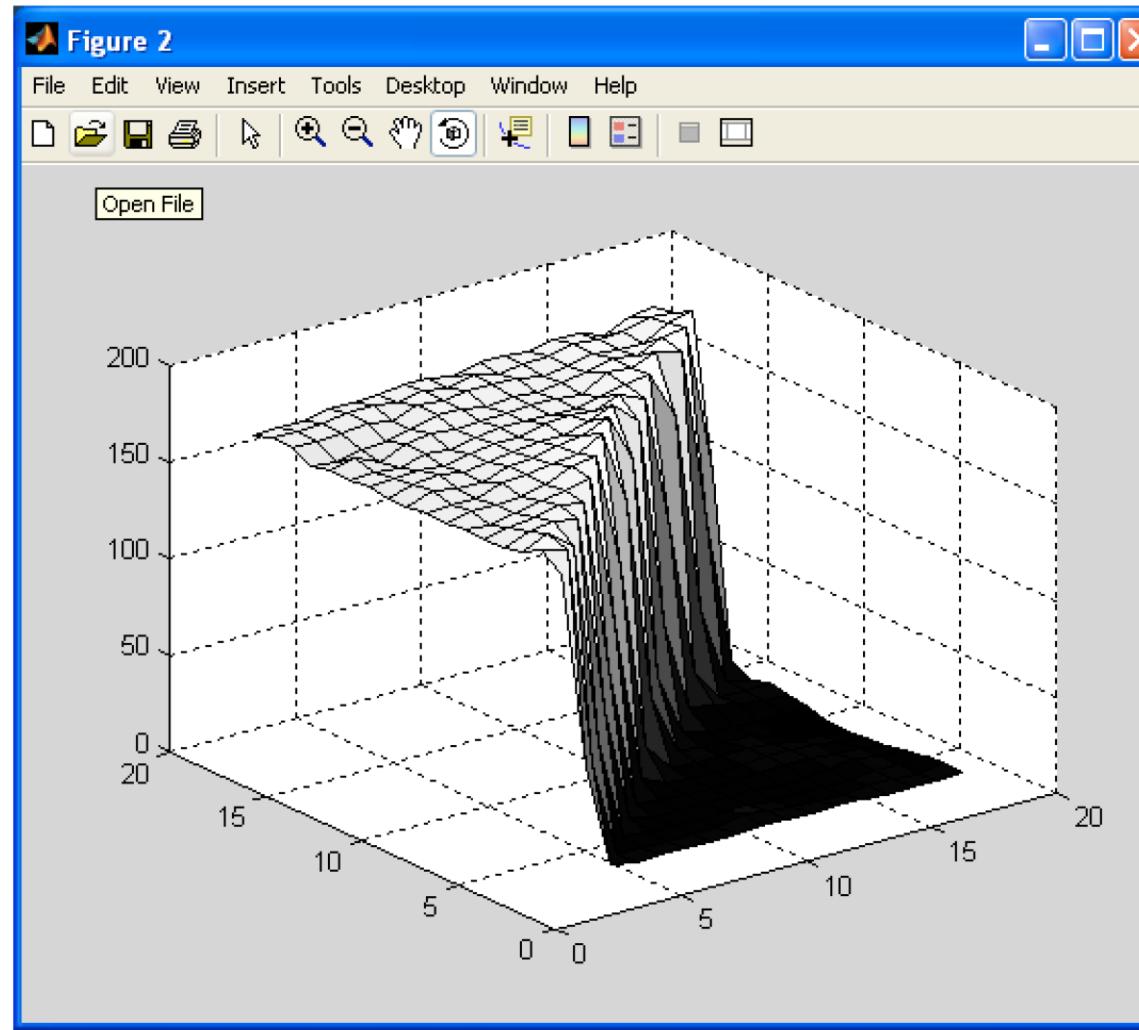


Roof Edge

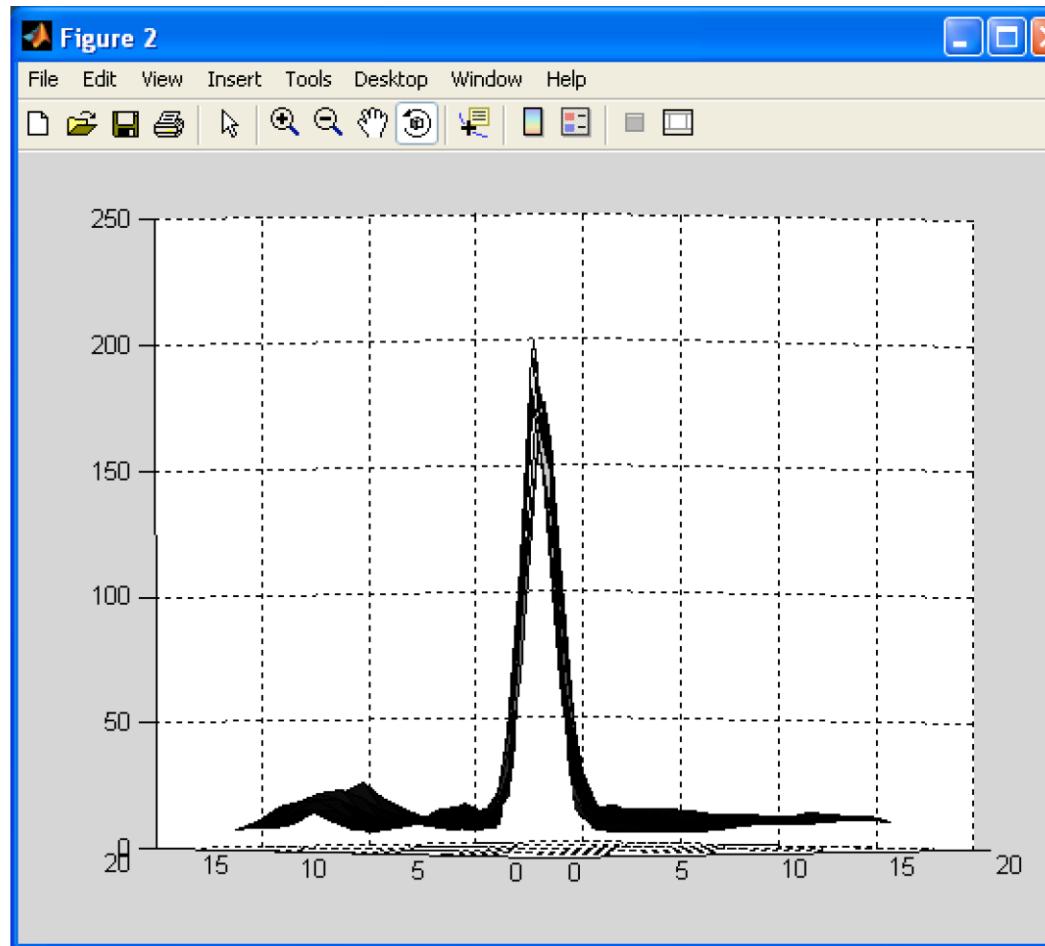
# Step Edge and Ramp Edge



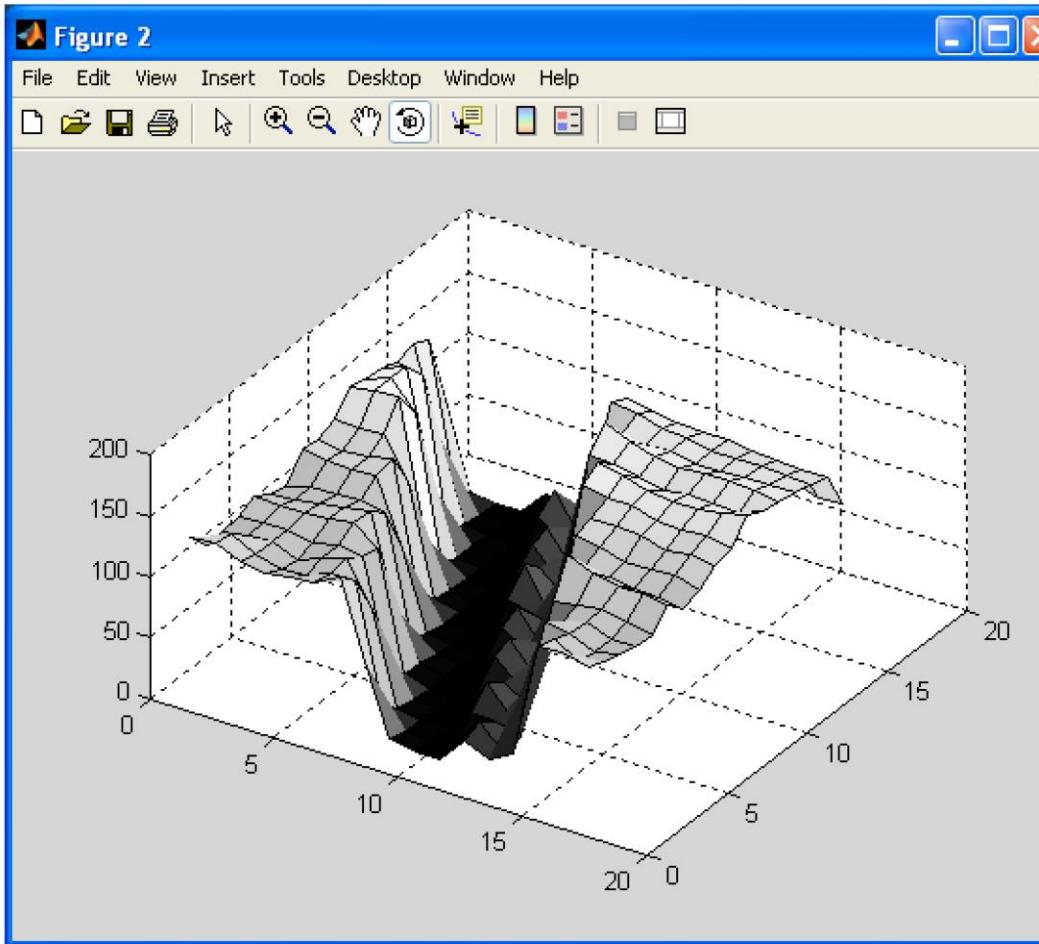
Step Edge, Ramp Edge



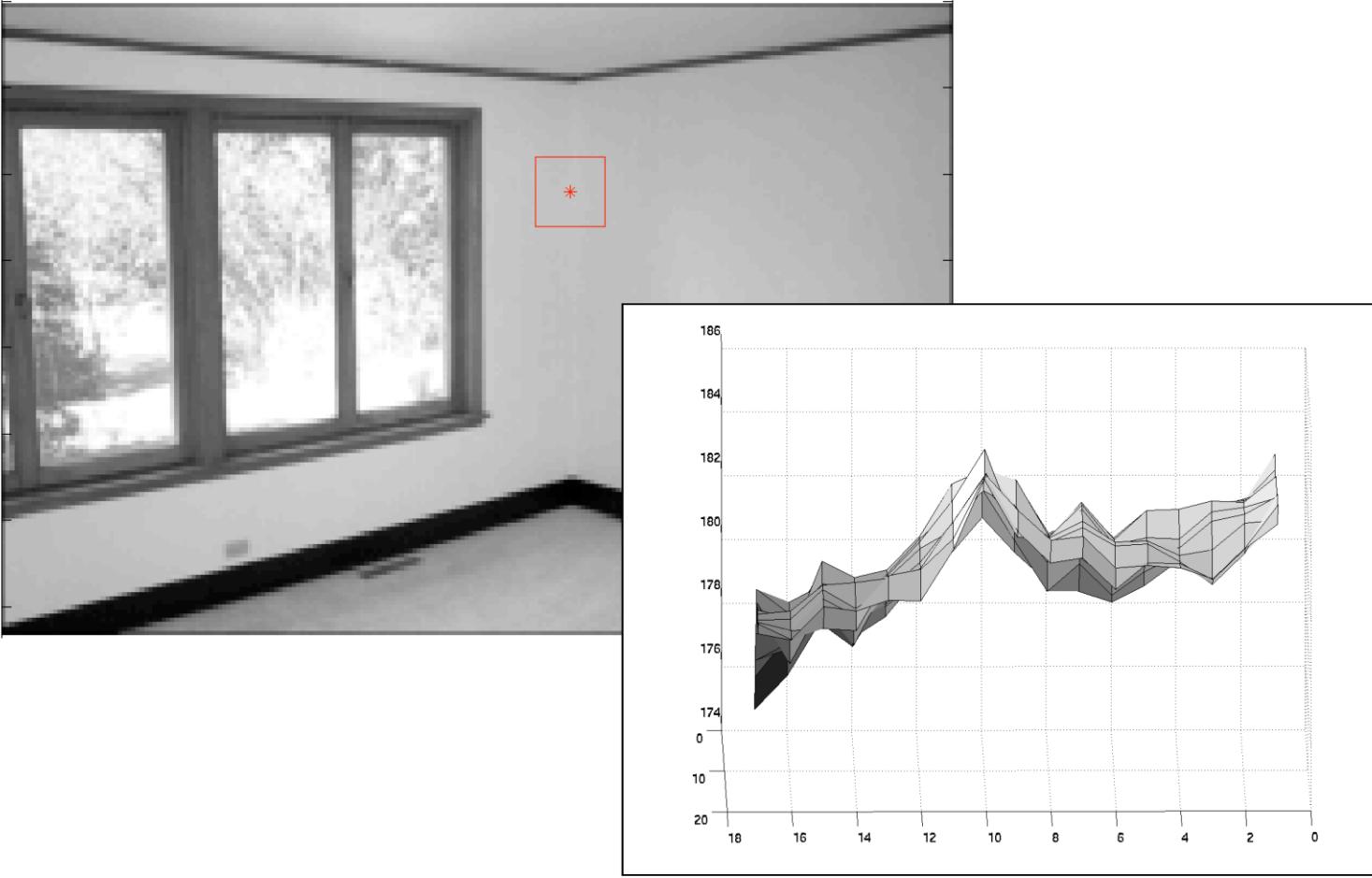
# Ridge Edge



# Ridge Edge



# Roof Edge



Roof Edge

# Image Gradients

- Use image gradients

Central difference

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x + 0.5h) - f(x - 0.5h)}{h}$$

-1	0	1
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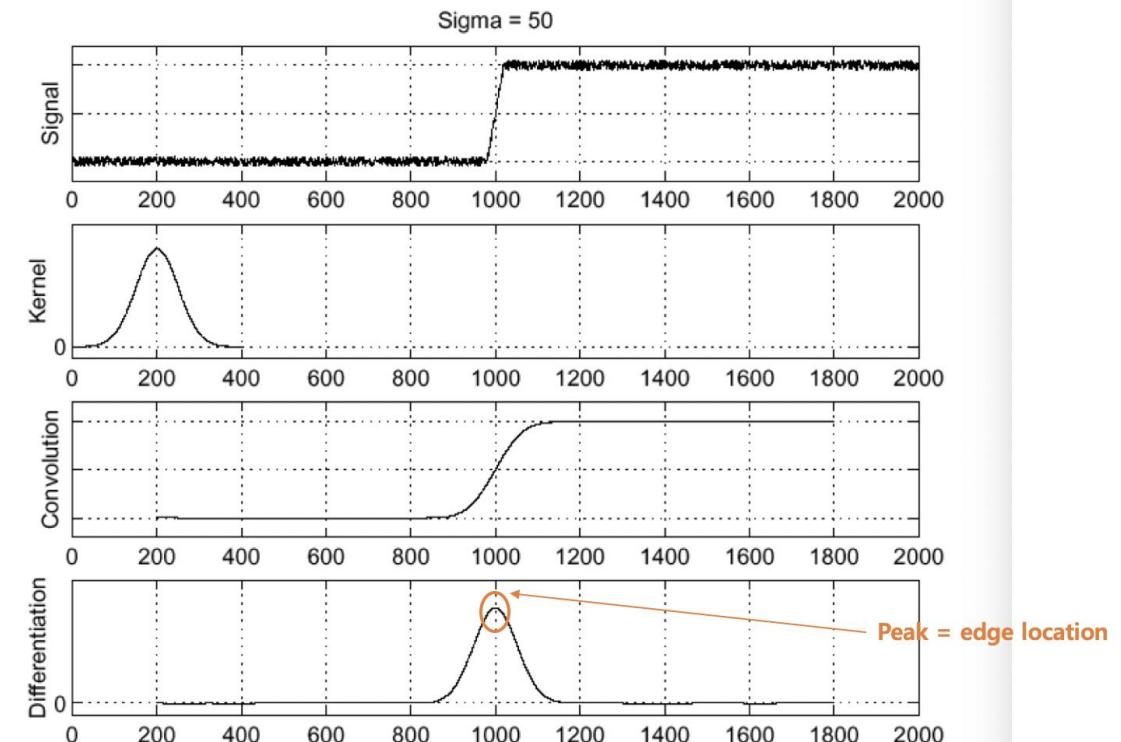
X derivative

Image  $f$

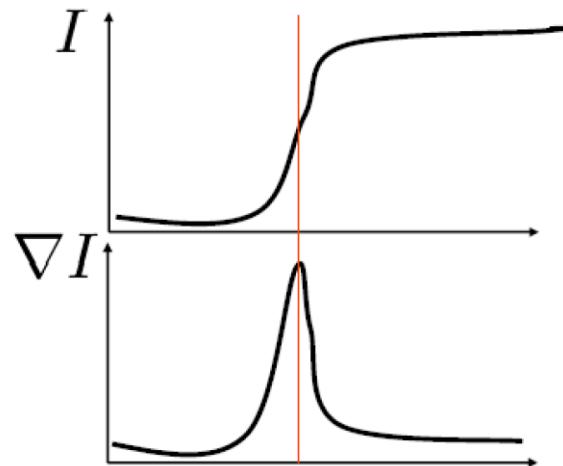
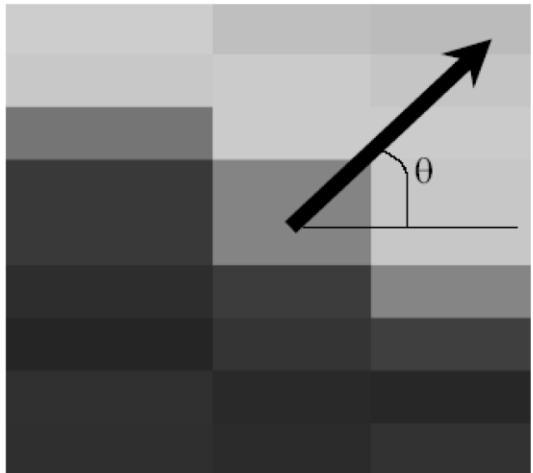
Gaussian Filter  $h$

Convolution  $h \star f$

Derivative  $\frac{\partial}{\partial x}(h \star f)$



# Image Gradients



Gradient Vector:  $\nabla I = \left[ \frac{\partial I}{\partial x}, \frac{\partial I}{\partial y} \right]^T$

$$|\nabla I| = \sqrt{\left(\frac{\partial I}{\partial x}\right)^2 + \left(\frac{\partial I}{\partial y}\right)^2}$$

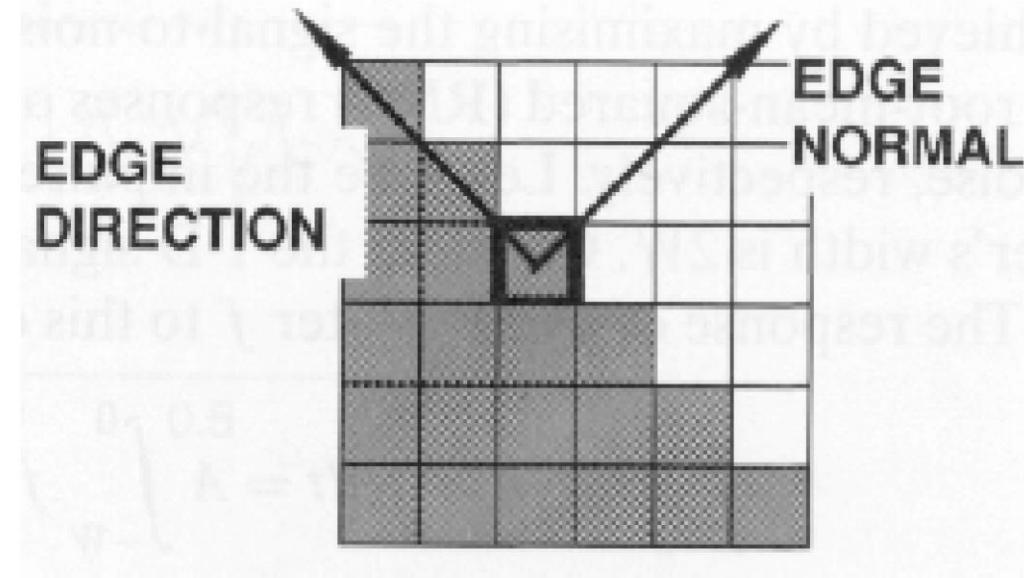
Magnitude:

$$\theta = \text{atan}2\left(\frac{\partial I}{\partial y}, \frac{\partial I}{\partial x}\right)$$

Orientation

# Edge Normal and Edge Direction

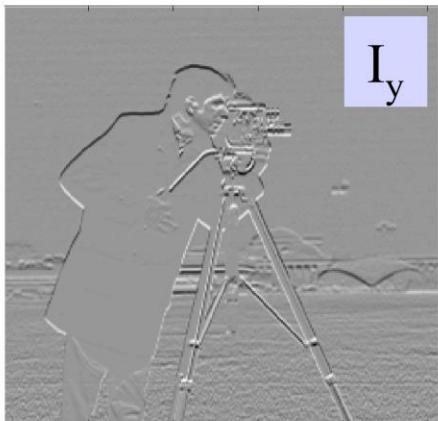
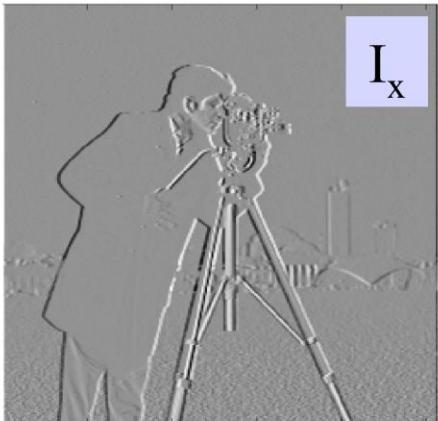
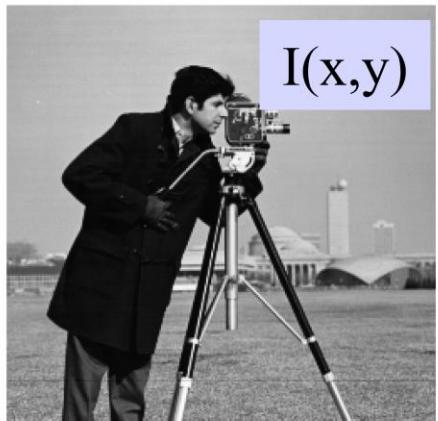
- Edge normal
  - Unit vector in the direction of maximum intensity change
  - Gradient direction
- Edge direction
  - Unit vector along edge (perpendicular to edge normal)



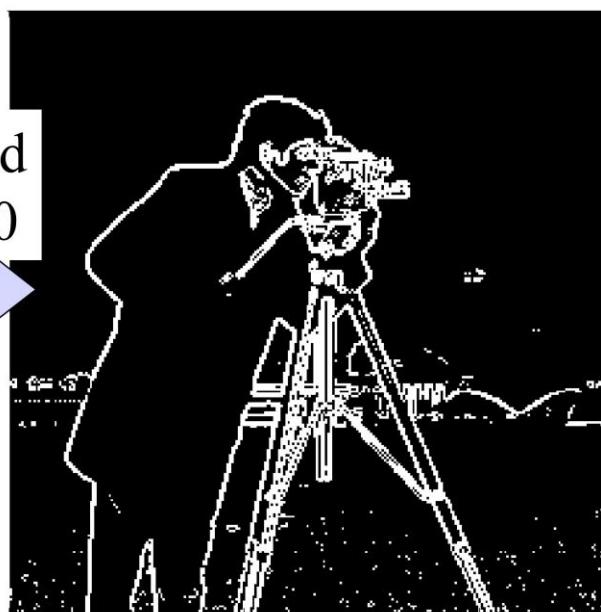
# Edge Detection

- A simple edge detector using gradient magnitude
  1. Compute gradient vector at each pixel by convolving image with horizontal and vertical derivative filters
  2. Compute gradient magnitude at each pixel
  3. If magnitude at a pixel exceeds a threshold, report a possible edge point

# Edge Detection



Magnitude of gradients



# Edge Detection

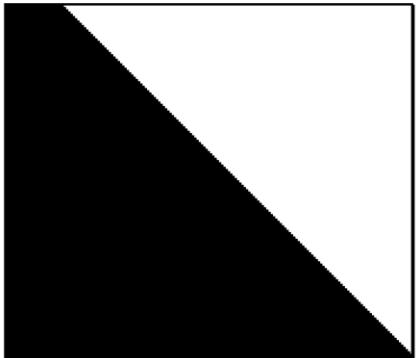
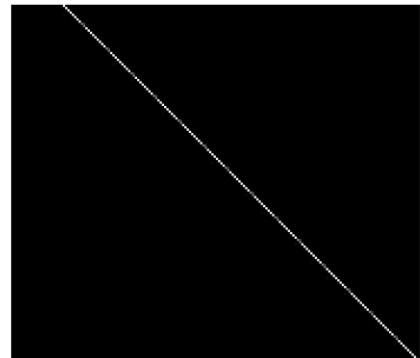


Image with Edge



Edge Location

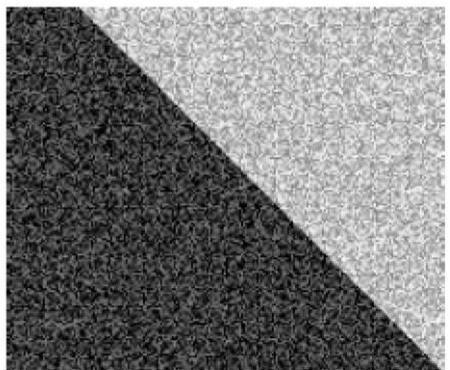
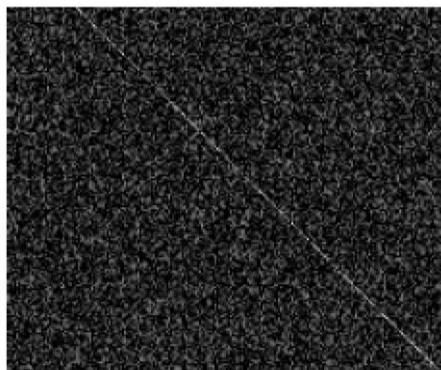


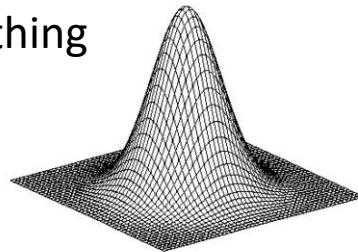
Image + Noise



Derivatives detect  
edge and noise

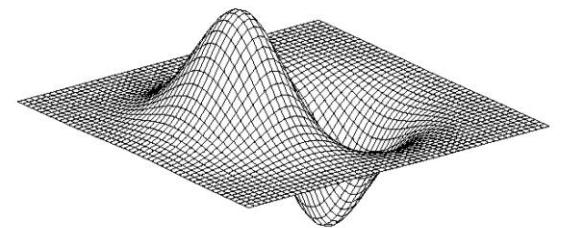
$$\frac{\partial}{\partial x}(h \star f) = (\frac{\partial}{\partial x}h) \star f$$

Smoothing



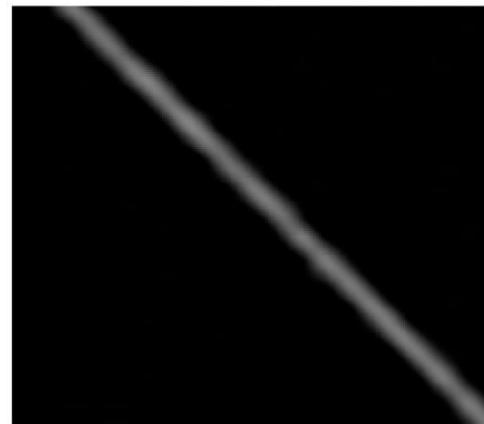
Gaussian

$$h_\sigma(u, v) = \frac{1}{2\pi\sigma^2} e^{-\frac{u^2+v^2}{2\sigma^2}}$$



derivative of Gaussian (x)

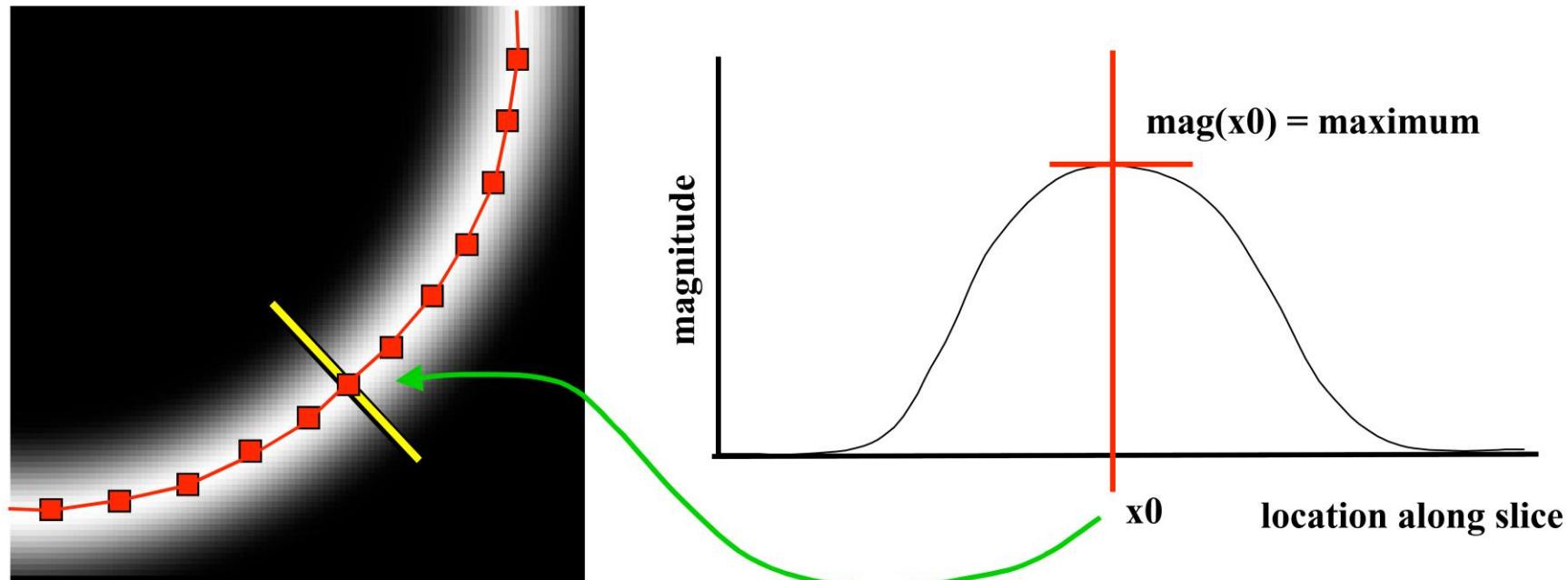
$$\frac{\partial}{\partial x} h_\sigma(u, v)$$



Smoothed derivative removes  
noise, but blurs edge

# Edge Detection

- Thinning

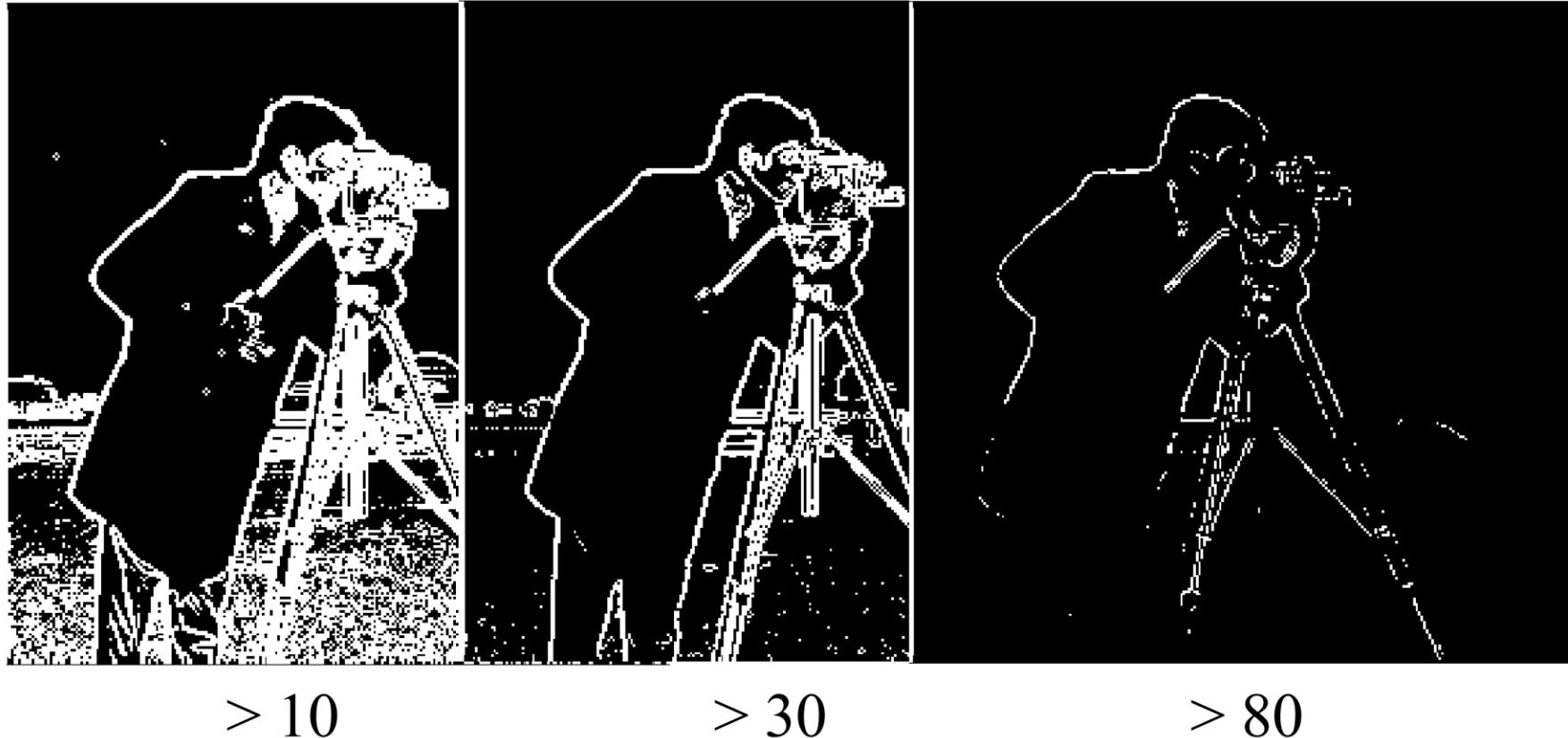


Along a 1D intensity slice normal to the curve (non-maximum suppression)

- Direction of gradient

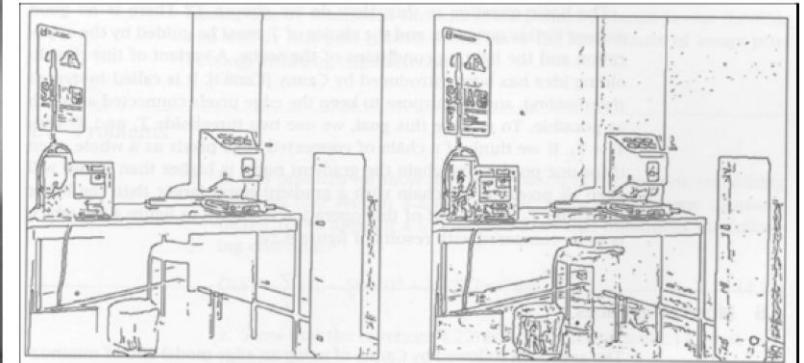
# Edge Detection

- How to chose the threshold?



# Edge Detection

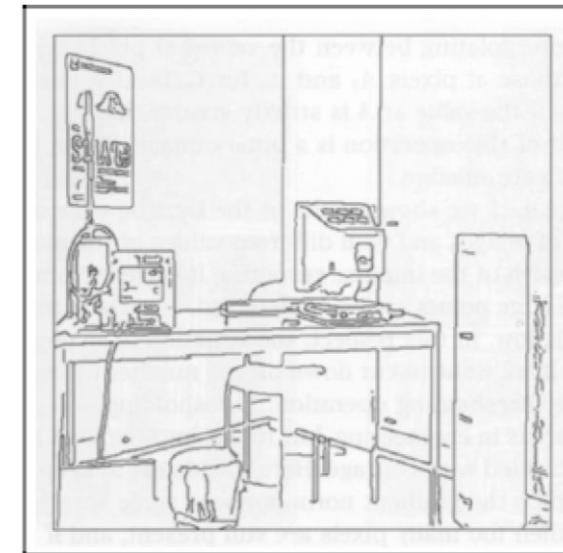
- How to chose the threshold?



Two thresholds applied to gradient magnitude  
 $T = 15$        $T = 5$

- Hysteresis thresholding

- Keep a high threshed  $H$  and a low threshold  $L$
- Any edge with strength  $< L$  is discarded
- Any edge with strength  $> H$  is kept
- An edge  $P$  with strength between  $L$  and  $H$  is kept only if there is a path of edges with strength  $> L$  connecting  $P$  to an edge of strength  $> H$



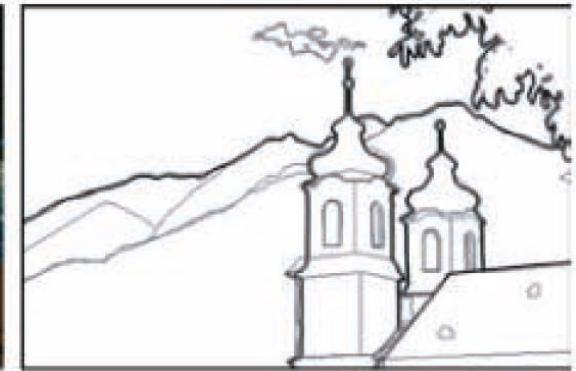
Hysteresis  
 $T_h=15$   $T_l = 5$

Canny Edge Detector

J. Canny A Computational Approach to Edge Detection, IEEE Transactions on Pattern Analysis and Machine Intelligence, Vol 8, No. 6, Nov 1986

# Contour Detection

- Link edge points into contours
  - Check neighboring pixels
- How to store contours?
  - A list of edgels (edge points)
  - (x, y) coordinates

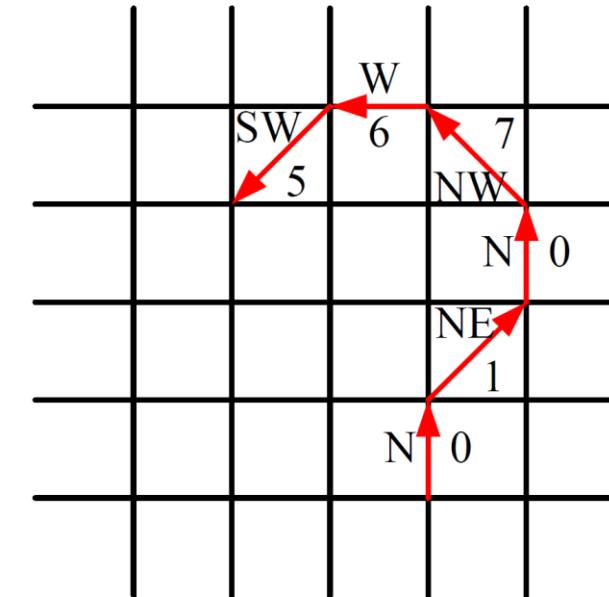
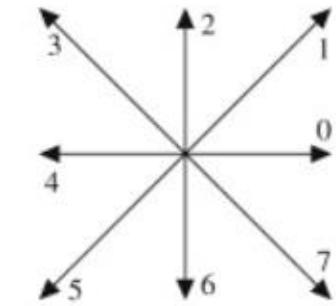
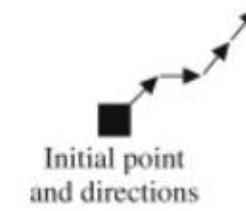


# Contour Detection

- How to store contours?
- Chain code
  - Initial coordinates
  - 8 directions (N, NE, E, SE, S, SW, W, NW)

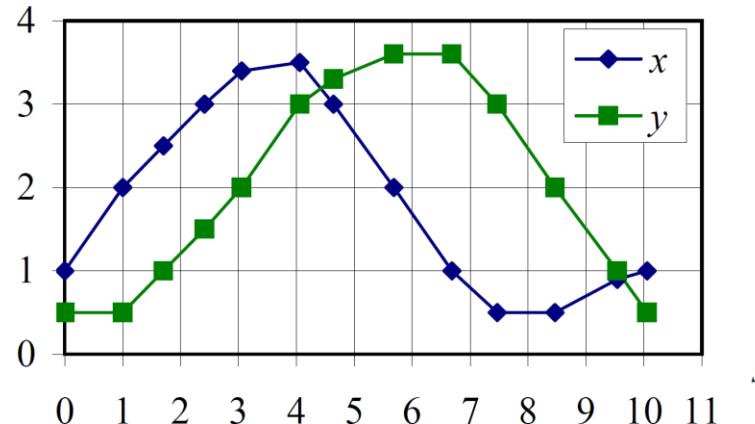
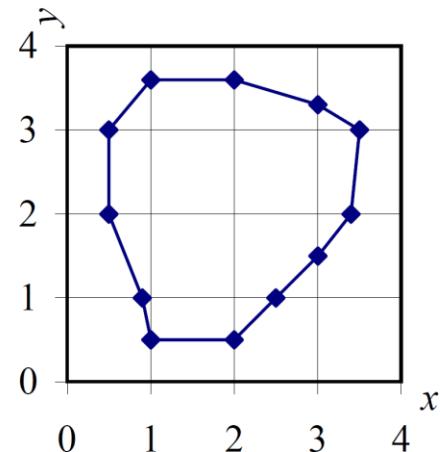
0 1 0 7 6 5

- Not suitable for further processing



# Contour Detection

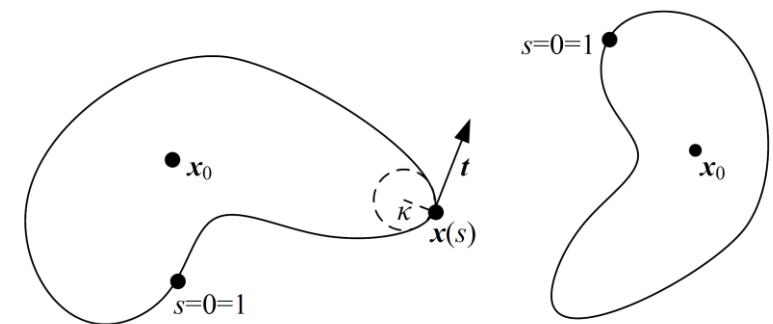
- How to store contours?
- Arc-length parameterization  $\mathbf{x}(s)$



- Can be resampled
- Fourier transform by treating  $(x, y)$  as a complex number (contour matching)

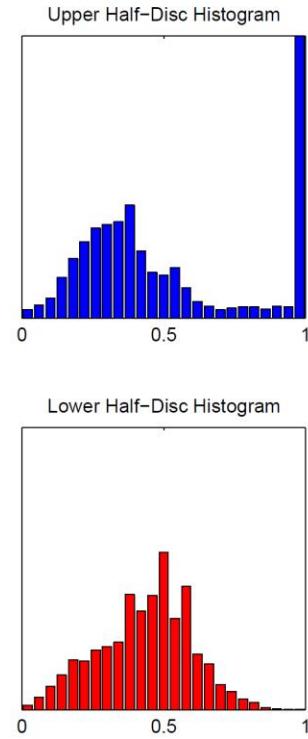
- Start point  $(1.0, 0.5)$ ,  $s = 0$
- Next point  $(2.0, 0.5)$ ,  $s = 1$
- Next point  $(2.5, 1.0)$ ,  $s = 1.7071$

...

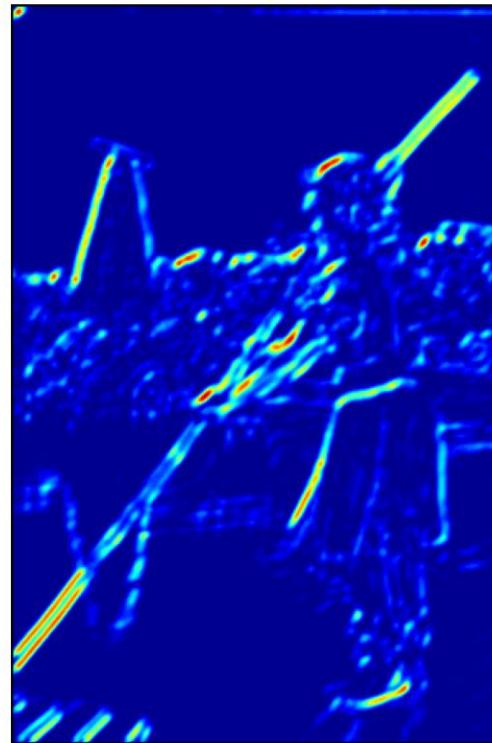


# mPb Contour Detector

- Oriented gradient of histograms  $G(x, y, \theta)$



Histogram of intensity



Radius: 5 pixels  $\theta = \frac{\pi}{4}$

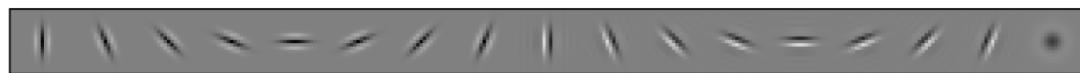
Gradient magnitude:

$\chi^2$  distance between  
the two histograms

$$\chi^2(g, h) = \frac{1}{2} \sum_i \frac{(g(i) - h(i))^2}{g(i) + h(i)}$$

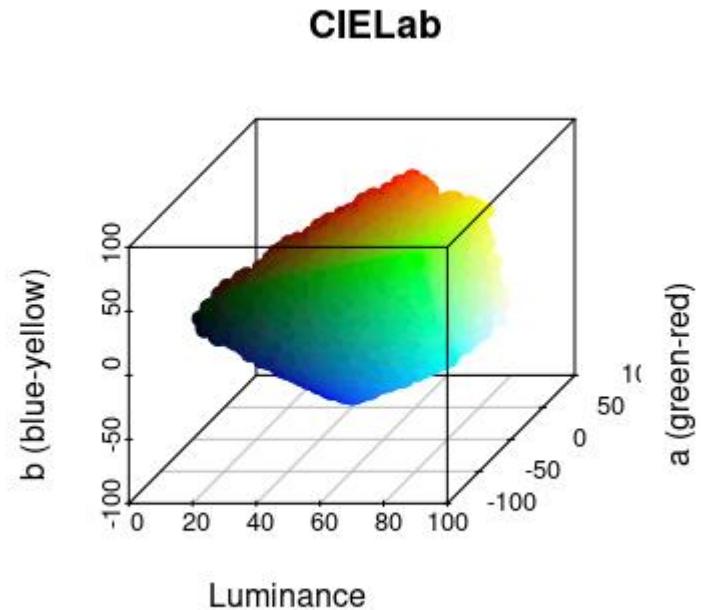
# mPb Contour Detector

- Brightness, color, texture gradients
  - L\*a\*b color space: brightness, color a and color b
  - Texture: assign a pixel to a texton id



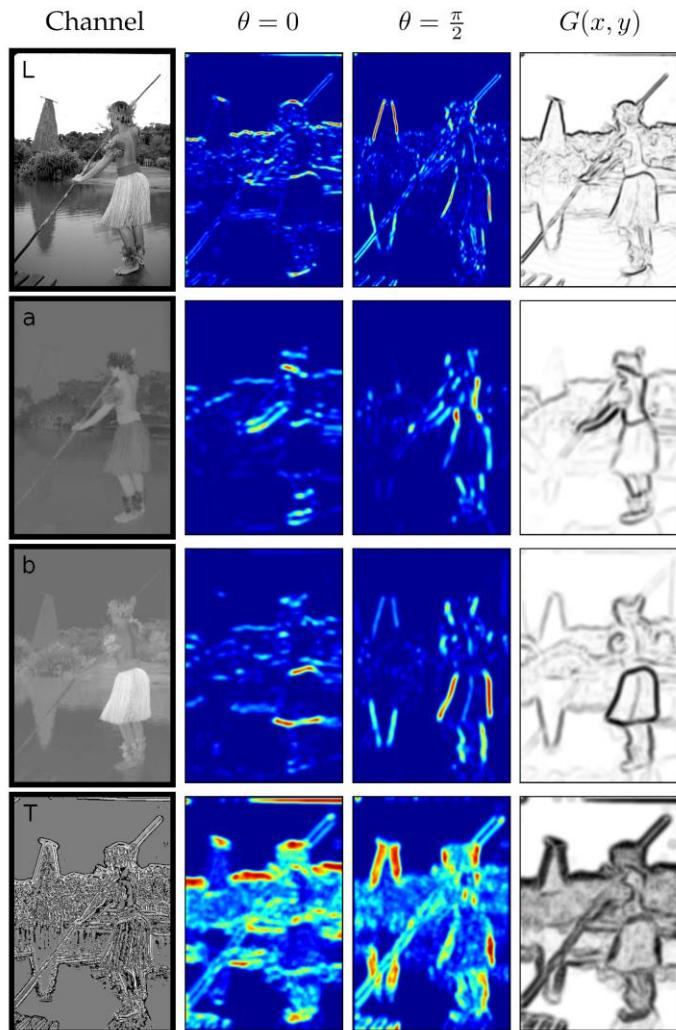
- 17 Gaussian derivative filters
- 17D feature vector for each pixel

- K-means clustering, K = 32, textons
- Texture image: pixels with integer [1, K]



<https://cran.r-project.org/web/packages/colordistance/vignettes/color-spaces.html>

# mPb Contour Detector



maximum response over eight orientations in  $[0; \pi]$

- Consider multiple scales  $[\frac{\sigma}{2}, \sigma, 2\sigma]$

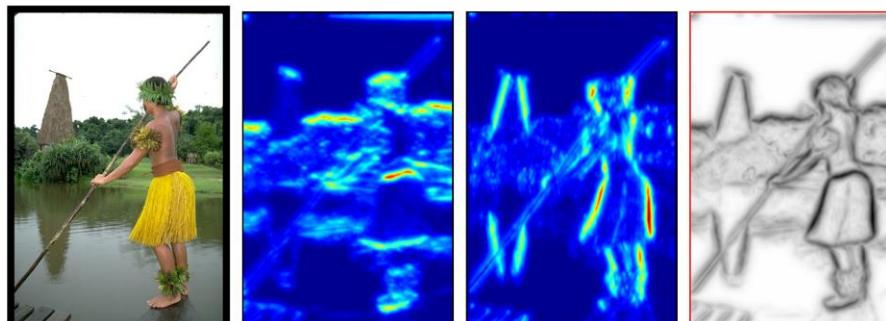
$\sigma = 5$  pixels for brightness

$\sigma = 10$  pixels for color and texture

$$mPb(x, y, \theta) = \sum_s \sum_i \alpha_{i,s} G_{i,\sigma(i,s)}(x, y, \theta)$$

Scale Channel (brightness, color a, color b, texture)

$$mPb(x, y) = \max_{\theta} \{mPb(x, y, \theta)\}$$



$mPb(x, y)$

# Lines

- Lines are common in the human-made world

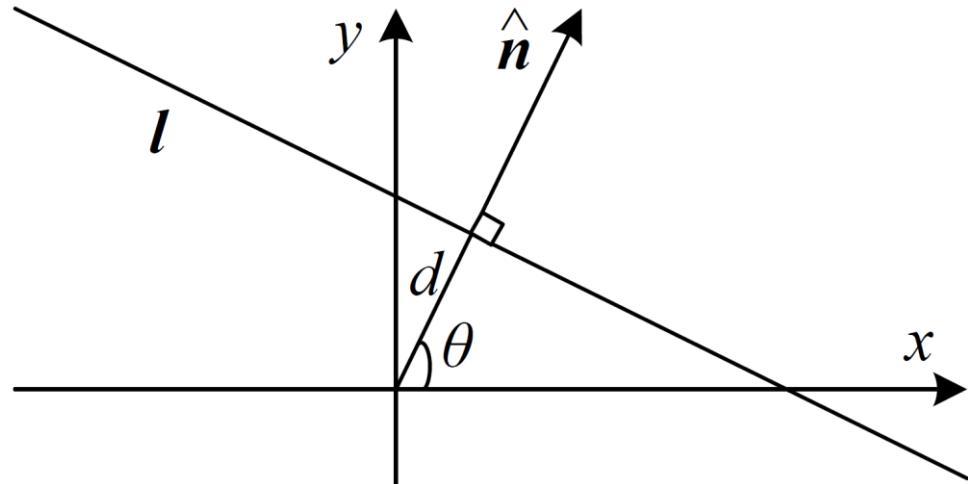


Manhattan World  
Assumption

Srikumar Ramalingam and Matthew Brand. Lifting 3D Manhattan Lines from a Single Image. ICCV'13.

# Lines

- 2D lines



$$ax + by + c = 0$$

$$\mathbf{l} = (a, b, c)$$

Normalize by  $\sqrt{a^2 + b^2}$

$$\mathbf{l} = (\hat{n}_x, \hat{n}_y, d) = (\hat{\mathbf{n}}, d)$$

$$\hat{\mathbf{n}} = (\hat{n}_x, \hat{n}_y) = (\cos \theta, \sin \theta)$$

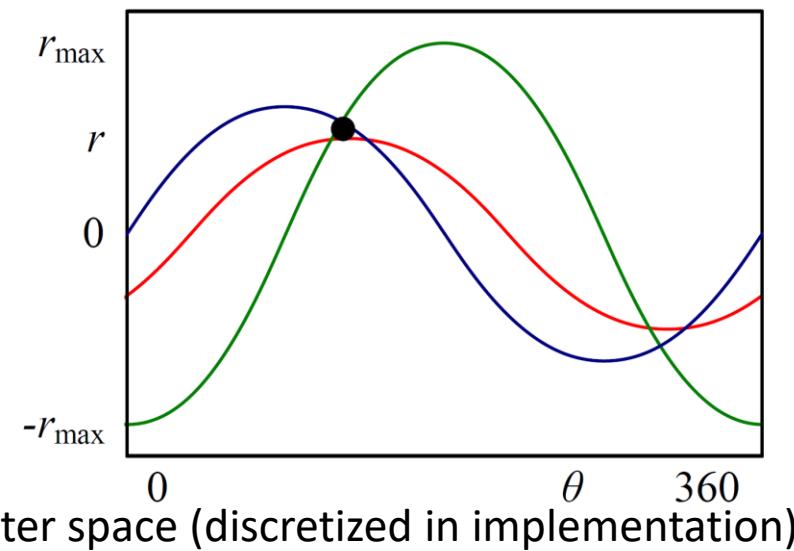
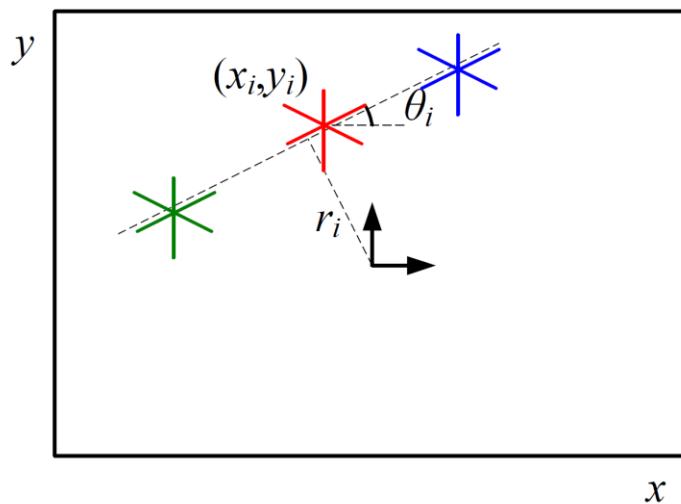
polar coordinates  $(\theta, d)$

$$x \cos \theta + y \sin \theta + d = 0$$

# Line Detection

- Hough transform
  - Observations vote for model parameters
  - Observations?  $(x_i, y_i)$  Edge points
  - Model parameters?  $(r, \theta)$

$$r_i(\theta) = x_i \cos \theta + y_i \sin \theta$$



$$a \cos x + b \sin x = c \cos(x + \varphi)$$

where  $c$  and  $\varphi$  are defined as so:

$$c = \operatorname{sgn}(a) \sqrt{a^2 + b^2},$$

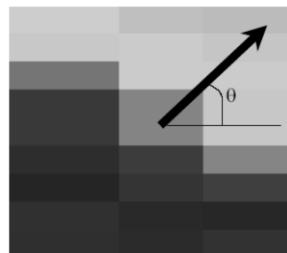
$$\varphi = \arctan\left(-\frac{b}{a}\right),$$

given that  $a \neq 0$ .

[https://en.wikipedia.org/wiki/List\\_of\\_trigonometric\\_identities](https://en.wikipedia.org/wiki/List_of_trigonometric_identities)

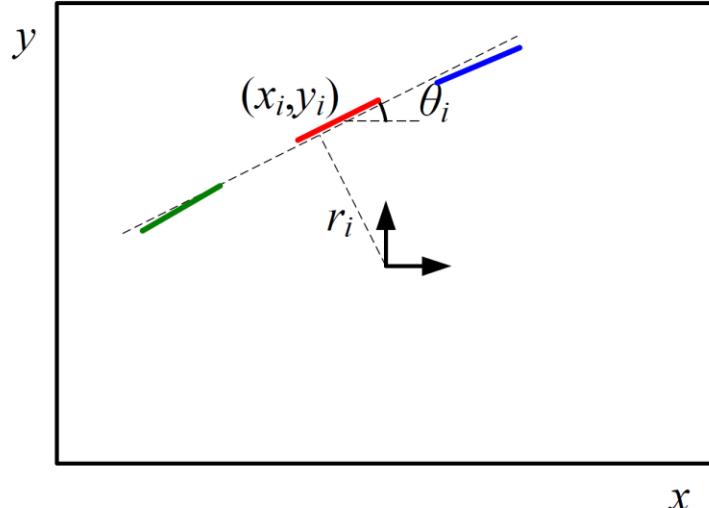
# Line Detection

- Oriented Hough Transform
  - Use gradient orientation as theta

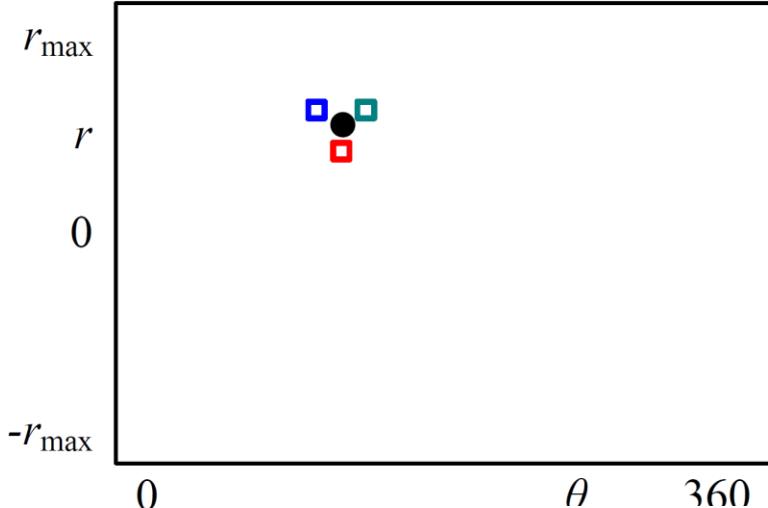


$$\theta = \text{atan}2\left(\frac{\partial I}{\partial y}, \frac{\partial I}{\partial x}\right)$$

Orientation



$$r_i(\theta) = x_i \cos \theta + y_i \sin \theta$$



$$\hat{\mathbf{n}}_i = (\cos \theta_i, \sin \theta_i)$$

$$r_i = \hat{\mathbf{n}}_i \cdot \mathbf{x}_i$$

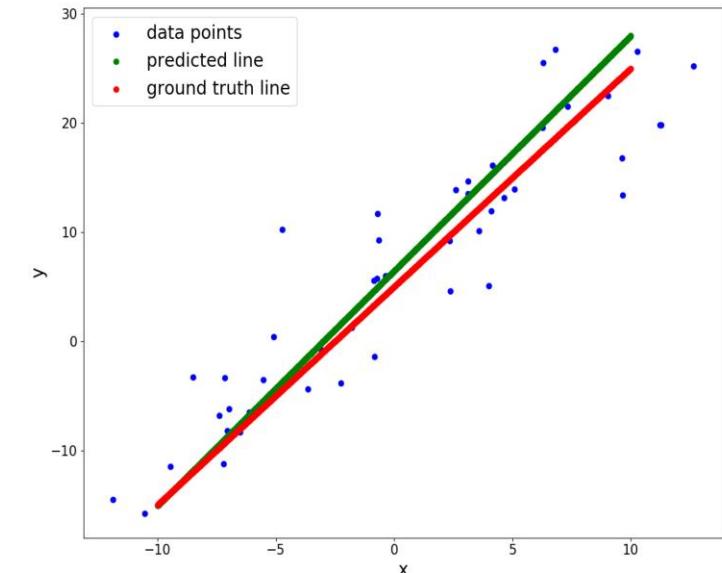
# Line Detection

- Random Sample Consensus (RANSAC)

RANSAC Algorithm {

1. Selects  $N$  data items as random
2. Estimates parameter  $\vec{x}$
3. Finds how many data items (of  $M$ ) fit the model with parameter vector  $\vec{x}$  within a user given tolerance. Call this  $K$ .
4. If  $K$  is big enough, accept fit and exit with success.
5. Repeat step 1 until 4 (as  $L$ times)
6. Algorithm will be exit with fail

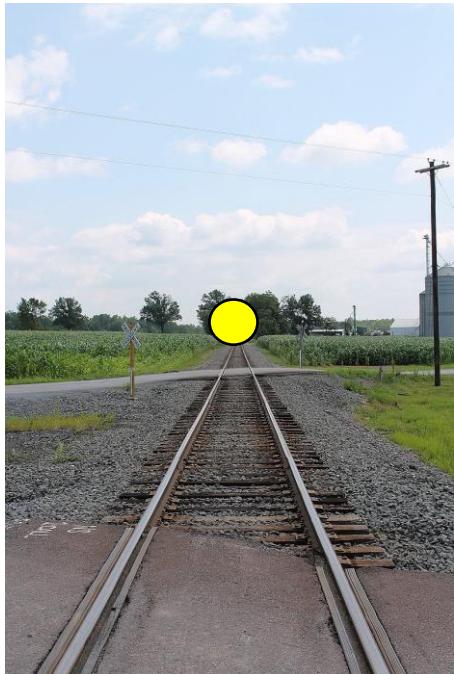
}



- Sample two edge points
- Estimate the line parameter  $(\theta, d)$   
$$x \cos \theta + y \sin \theta + d = 0$$
- Find how many edgels obey it

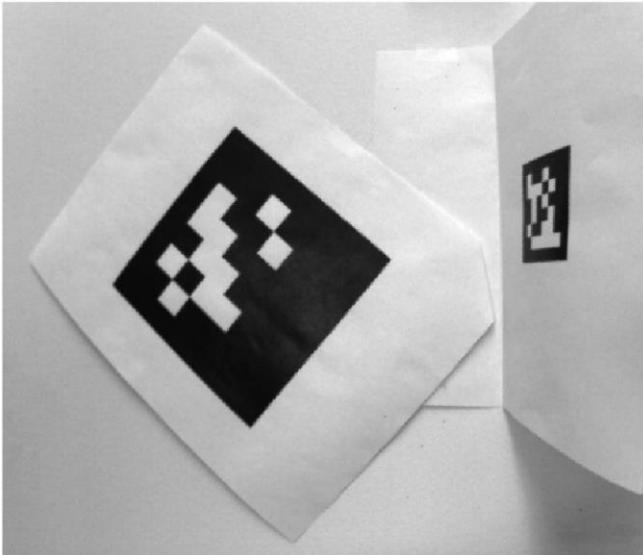
# Vanishing Points

- Parallel lines in 3D converge in 2D images due to perspective projection

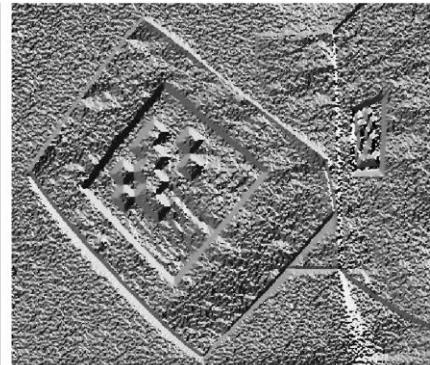


Recovering the Spatial Layout of Cluttered Rooms. Hedau et al., ICCV'09

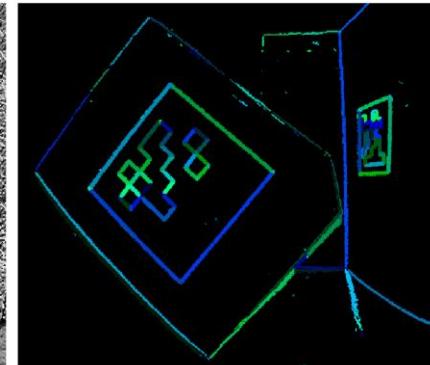
# Application: AprilTag Detection



Gradient magnitudes



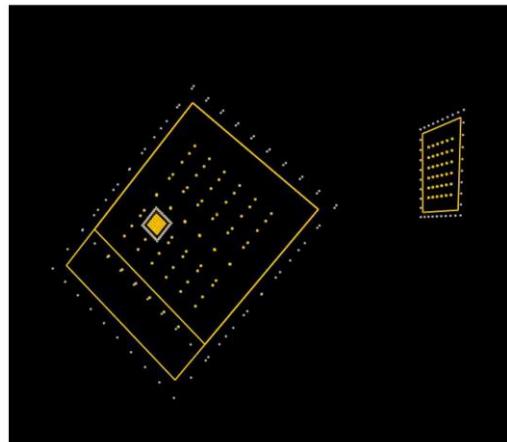
Gradient directions



Clustering



Line segments for cluster components



Quad detection



AprilTag: A robust and flexible visual fiducial system. Edwin Olson. ICRA, 2011

# Further Reading

- Section 7.2, 7.4, Computer Vision, Richard Szeliski
- J. Canny. A Computational Approach to Edge Detection, IEEE Transactions on Pattern Analysis and Machine Intelligence, Vol 8, No. 6, Nov 1986.
- Pablo Arbelaez, Charless Fowlkes, Jitendra Malik. Contour Detection and Hierarchical Image Segmentation. TPAMI'10