



# Modeling the synergistic elimination of bacteria by phage and the innate immune system



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## ABSTRACT

Phage therapy has been viewed as a potential treatment for bacterial infections for over a century. Yet, the year 2016 marks one of the first phase I/II human trials of a phage therapeutic - to treat **burn wound patients in Europe**. The slow progress in realizing clinical therapeutics is matched by a similar dearth in principled understanding of phage therapy. Theoretical models and *in vitro* experiments find that combining phage and bacteria often leads to **coexistence of both phage and bacteria or phage elimination altogether**. Both outcomes stand in contrast to the stated goals of phage therapy. A potential resolution to the gap between models, experiments, and therapeutic use of phage is the hypothesis that the **combined effect of phage and host immune system can synergistically eliminate bacterial pathogens**. Here, we propose a phage therapy model that considers the **nonlinear dynamics arising from interactions between bacteria, phage and the host innate immune system**. The model builds upon earlier efforts by incorporating a maximum capacity of the immune response and density-dependent immune evasion by bacteria. We analytically identify a synergistic regime in this model in which phage and the innate immune response jointly contribute to the elimination of the target bacteria. Crucially, we find that in this synergistic regime, neither phage alone nor the innate immune system alone can eliminate the bacteria. We confirm these findings using numerical simulations in biologically plausible scenarios. We utilize our numerical simulations to explore the synergistic effect and its significance for guiding the use of phage therapy in clinically relevant applications.

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## 1. Introduction

Phage therapy denotes the use of bacteriophage, or viruses that exclusively infect bacteria, as therapeutic agents to treat infections by pathogenic bacteria. Phage therapy was applied in the 1920s and 1930s before the widespread use of antibiotics (Potera, 2013). Early applications of phage therapy were plagued by a number of problems, caused in part by poor understanding of phage biology (Carlton, 1999). These issues range from the lack of proper testing of the host range of phage to inappropriate preparation methods of phage stocks that inactivate the phage. In addition, interest in phage therapy declined after the discovery and mass production of antibiotics. However, the rise of pervasive antibiotic resistance has led to a renewal of interest in using phage to treat bacterial infections (Thiel, 2004).

One of the first international, single-blind clinical trials of phage therapy, Phagoburn, was launched in 2015 (Clark, 2015). The trial is designed to target 220 burn patients whose wounds are infected by *Escherichia coli* or *Pseudomonas aeruginosa* (Kingwell, 2015; Reardon, 2014). Other clinical trials are currently underway, including a phase I clinical trial by AmpliPhi Biosciences for treating infections of *Staphylococcus aureus* (Kingwell, 2015) and trials targeting respiratory tract infections such as pneumonia (François et al., 2016; Kingwell, 2015). Phage-based therapeutics have also been used for *in vitro* biocontrol of pathogenic or nuisance bacteria (Abedon, 2009; Hagens and Loessner, 2007), for example, in the reduction of populations of pathogens in produce (Leverentz et al., 2003), ready-to-eat foods (Guenther et al., 2009) and meat (Seo et al., 2016).

Phage therapy has a number of potential advantages over conventional drug therapy (Loc-Carrillo and Abedon, 2011). Phage can replicate inside bacterial cells and increase in number at the site of infection (Carlton, 1999). This self-amplification is in contrast to the fixed dose in conventional drug therapy (Carlton, 1999; Payne and Jansen, 2000; 2003). A consequence of the self-amplification is

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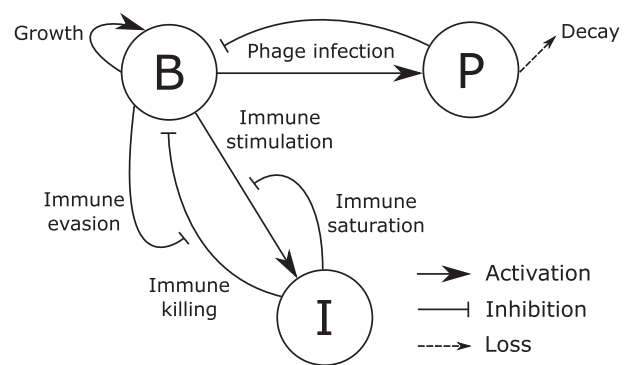
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that sufficiently high bacterial density is required for the proliferation of phage and the subsequent active control of bacteria (Cairns et al., 2009; Payne and Jansen, 2000, 2001). Phage are also more specific than broad spectrum antibiotics. This specificity reduces negative impacts on the normal flora of the human host (Skurnik et al., 2007). Some phage also have the ability to break down and clear biofilms which are resistant to antibiotics and recalcitrant to the host immune response (Alemayehu et al., 2012; Azeredo and Sutherland, 2008; Gutiérrez et al., 2015; Rodney, 2009; Timothy and Michael, 2011). Finally, innovations in genetic engineering provide a means to prototype and deploy combinations of phage targeted to individual infections (Campbell, 2003; Hermoso et al., 2007).

Despite reinvigorated interest in phage therapy, there remain many questions with respect to how, **when, why, and even if phage therapy works**. The elimination of a bacterial population by phage is not inevitable, even if phage can eliminate a targeted bacterial population given suitably chosen strains and initial conditions. Indeed, *in vitro* experiments (Chao et al., 1977; Dennehy, 2012; Lenski, 1984; Levin et al., 1977) and ecological models (Campbell, 1961; Levin et al., 1977; Weitz, 2015) of phage-bacteria systems predict broad regimes of coexistence among phage and bacteria populations. In many instances, co-culturing of phage and bacteria together leads to the emergence of resistant host strains and the elimination of the phage population (Dennehy, 2012; Meyer et al., 2012). Such outcomes are not desirable from a therapeutic perspective.

Unlike *in vitro* contexts, the host immune response is a key component of dynamics taking place in a bacterial infection inside animal hosts. Experimental studies have revealed that the host immune response influences the efficacy of phage in clearing pathogenic bacteria *in vivo* (Pincus et al., 2015; Tiwari et al., 2011; Trigo et al., 2013). The vertebrate immune system is composed of the innate and adaptive immune subsystems. The innate immune response reacts faster than the adaptive system but the latter is more specific and generally more effective. As animal studies of phage therapy have largely focused on acute infections, there is usually insufficient time for the adaptive immune response to fully activate. As such, innate immunity is expected to play a major role in these cases. In particular, neutrophils have been identified as an important player in determining the success of phage therapy for intraperitoneal infection of mice by *P. aeruginosa* (Tiwari et al., 2011). In addition, neutrophil dysfunction was found to exacerbate harmful inflammation response induced by excessive phage dosage in a mouse model of Methicillin-resistant *S. aureus* (MRSA) skin infection (Pincus et al., 2015). However, for infections by slow-growing bacterium such as *Mycobacterium ulcerans* which has a prolonged clinical course (>30 days), phage have been shown to stimulate the adaptive immune response by causing increased recruitment of effector T cells to lymph nodes and higher cytokine levels (Trigo et al., 2013).

These results highlight the need to understand the role of the immune response in concert with phage therapy. A small number of models have focused on the combined, nonlinear interactions of bacteria, phage, and the immune system (Levin and Bull, 1996; 2004). In such a combined system, phage-bacteria interactions are presumed to operate concurrently with that of the immune response. The immune response eliminates bacteria and the intensity of the immune response is stimulated by the presence of bacteria. Standard models of bacteria-phage-immune system share a few simplifying assumptions (Levin and Bull, 1996; 2004). First, these models do not distinguish between innate and adaptive immunity, which differ in both the time scale of activation and the effectiveness of its antimicrobial action. Second, they assume that the immune response can grow in strength without bounds. Finally, they assume that bacteria cannot evade the immune response. As a re-



**Fig. 1.** Schematic diagram of a phage therapy model with immune saturation at maximum capacity and immune evasion by bacteria.

sult of the latter two assumptions, these models presuppose that bacteria will be eliminated by the immune system when acting alone given sufficient time post-infection. In this framework, the added benefit of phage is to accelerate the time at which the bacteria are eliminated.

Here, **we extend earlier models to explore a clinically relevant regime in which bacteria elimination by the immune system is not inevitable**, neither in the short- nor long-term. In our model, we demonstrate that the **inclusion of immune saturation and bacterial immune evasion are sufficient to give rise to a robust mechanism of effective phage therapy**: synergistic elimination of a bacterial pathogen. This synergistic elimination is possible even when neither the innate immune response nor the phage can eliminate the bacterial pathogen, while acting alone. We discuss ways in which this synergistic mechanism can be leveraged in clinical settings.

## 2. Model

We propose a phage therapy model that includes interactions among bacteria *B*, phage *P*, and the innate immune response *I* (see Fig. 1). Here we focus on **acute infections and assume only the innate immune system contributes significantly to the killing of bacteria**. In this model, the bacterial population reproduces and can be infected and lysed by phage. **Phage particles can decay when outside of cells**. The presence of bacteria activates the innate immune response which in turn kills the bacteria. This phage therapy model leverages core components proposed in previous models (Levin and Bull, 2004). In so doing, we include two biological features not previously explored.

First, we include a **saturating innate immune response**. The capacity of the innate immune response is constrained by factors including the finite number of immune cells such as neutrophils that can be produced and tolerated (Summers et al., 2010). Experimental studies have shown that host innate immunity has a finite killing capacity that can be saturated (Drusano et al., 2010; 2011; Guo et al., 2011; Jubrail et al., 2016). For example, high bacterial burden can saturate granulocyte killing in a mouse thigh infection model of *P. aeruginosa* and *S. aureus* (Drusano et al., 2010). This saturation effect allows bacteria to multiply at high densities even under immune killing. The same phenomenon was observed in a murine model of *P. aeruginosa* pneumonia (Drusano et al., 2011). A related saturation effect was observed in a murine pneumonia model of *Acinetobacter baumannii* and *P. aeruginosa* (Guo et al., 2011) where increase in absolute neutrophil count leads to saturation in bacterial killing rate. In addition, *in vitro* experiments and a murine pneumonia model of *S. aureus* (Jubrail et al., 2016) demonstrated that macrophages have a finite capacity for intracellular killing. When this capacity is overwhelmed, bacteria persist intracellularly and are subsequently released through cell lysis. In

Fig. 1, this saturation effect is represented as an inhibition of the innate immune activation when the immune response is high, such that there is an upper bound on the magnitude of the host innate immune response.

Second, we include density-dependent immune evasion of bacteria. Experiments have shown that pathogenic bacteria utilize immune evasion strategies such as biofilm formation (Costerton et al., 1999) and production of virulence factors (Gellatly and Hancock, 2013) to evade the innate and adaptive immune responses. Coordinated by quorum sensing, bacteria activate these mechanisms at high population density to evade the immune killing action of their host (de Kievit and Iglewski, 2000; Sully et al., 2014). As a result, the efficiency of immune killing would decrease with bacterial population density. This is represented as inhibition of the immune killing by bacteria in Fig. 1.

The interactions shown in Fig. 1 are modeled by the following set of differential equations that govern the temporal evolution of bacteria, phage, and the innate immune response:

$$\dot{B} = \overbrace{rB \left(1 - \frac{B}{K_C}\right)}^{\text{Growth}} - \overbrace{\phi BP}^{\text{Lysis}} - \underbrace{\epsilon IB \left(1 + \frac{B}{K_D}\right)}_{\text{Immune killing}}, \quad (1)$$

$$\dot{P} = \overbrace{\beta \phi BP}^{\text{Replication}} - \overbrace{\omega P}^{\text{Decay}}, \quad (2)$$

$$\dot{I} = \underbrace{\alpha I \left(1 - \frac{I}{K_I}\right)}_{\text{Innate immune stimulation}} \frac{B}{B + K_N}. \quad (3)$$

In this model, the maximal bacterial growth rate is  $r$  and the carrying capacity is  $K_C$ . Phage attach to and infect bacteria at an adsorption rate of  $\phi$ , and release new viral particles with a net burst size of  $\beta$ . The phage particles decay or get washed out at a rate of  $\omega$ .

In the absence of immune evasion by bacteria, the immune killing rate in a well-mixed environment is expected to follow the mass action form  $\epsilon IB$  where  $\epsilon$  is a killing parameter. To model the effect of immune evasion by bacteria at high densities, we use Michaelis-Menten kinetics where the mass action killing term is scaled by the denominator  $(1 + B/K_D)$ . The saturation results in less efficient innate immune killing at high bacterial density with  $K_D$  being the bacterial density at which the host innate immunity is half as effective. This type of kinetics has been used to model immune saturation at high bacterial burden and was found to be in agreement with experimental measurements of *in vivo* bacterial burden (Drusano et al., 2010; 2011). The innate immune response is activated by the presence of bacteria with a maximum growth rate of  $\alpha$ . To model immune saturation, the factor  $(1 - I/K_I)$  is included to ensure the innate immune response saturates at the immune carrying capacity  $K_I$ . Finally,  $K_N$  is the bacterial population density at which the innate immune response growth rate is half its maximum. The estimation of model parameters and simulation procedures are described in the Methods section.

### 3. Results

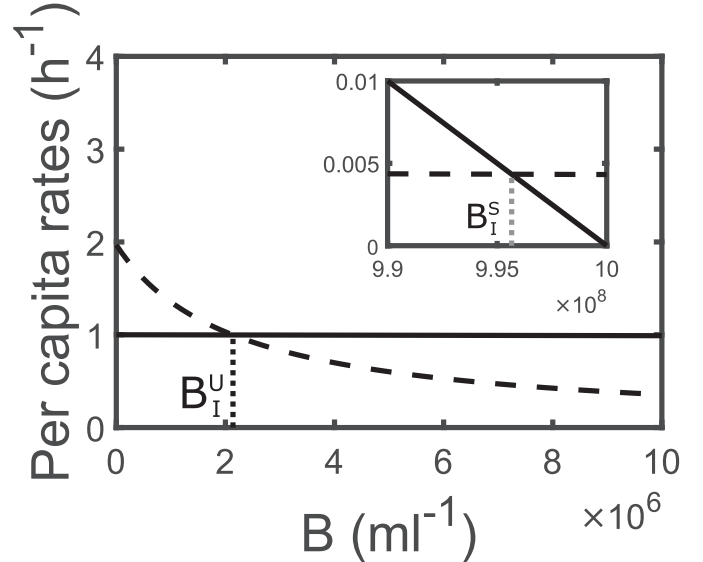
#### 3.1. Fixed points of the system and possible infection outcomes

We analyze the fixed points of the system to understand possible outcomes of infection. The fixed points of the system for the

**Table 1**

The different classes of fixed points of the system and the corresponding infection outcome.

Class	$B^*$	$P^*$	$I^*$	Outcome
I	0	0	$0 < I^* \leq K_I$	Bacteria elimination
II	$0 < B_I < K_C$	0	$K_I$	Bacteria persistence
III	$0 < B_{PI} < K_C$	$P_{BI} > 0$	$K_I$	Coexistence



**Fig. 2.** Per capita rates of bacterial growth  $G(B) \equiv r(1 - B/K_C)$  (solid line) and bacteria death  $D(B) \equiv \frac{\epsilon K_I}{1 + B/K_D}$  (dashed line) caused by the maximum innate immune response  $K_I$  as functions of bacterial density. The inset shows the rates at high bacterial density close to  $K_C$ . The black and grey dotted lines mark the positions of  $B_I^U$  and  $B_I^S$  respectively. The model parameters are given in Table 3.

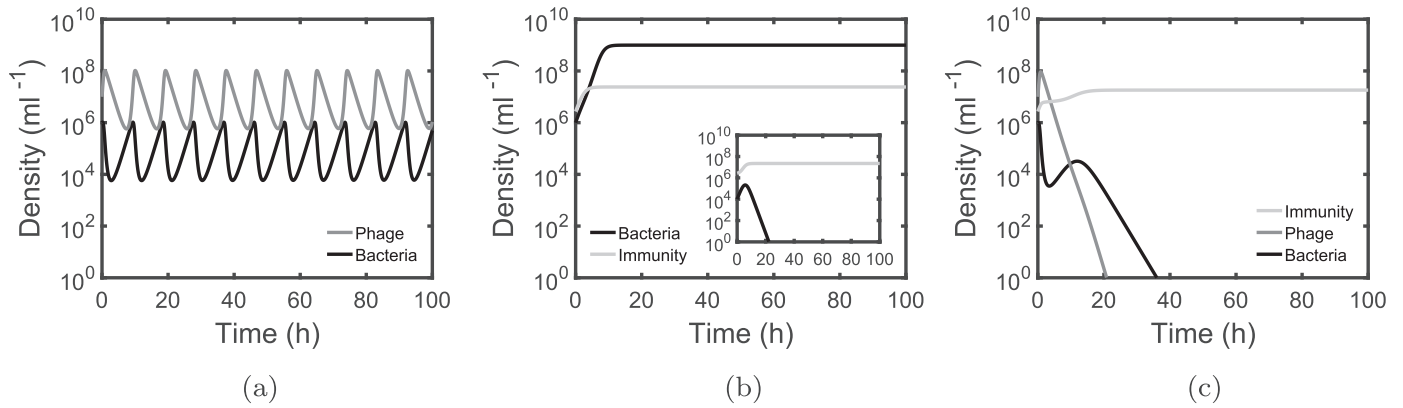
non-trivial case of  $I \neq 0$  can be categorized into three different classes (Table 1). The first class has no bacteria but has a finite innate immune response, corresponding to a state in which the innate immune response has eliminated the bacteria. There is also no phage population as phage require bacteria to replicate and persist. In this class, the innate immune response can take on any value less than the maximum,  $K_I$ .

The second class of phage-free fixed points contain a nonzero population of bacteria. Here the innate immune response is insufficient to eliminate the bacteria even when it reaches its maximum level,  $I^* = K_I$ . The equilibrium bacterial density for this class of fixed points depends on the relative magnitude of the bacterial logistic growth rate  $G(B) \equiv r(1 - B/K_C)$  and the bacterial death rate caused by the maximum innate immune response  $D(B) \equiv \frac{\epsilon K_I}{1 + B/K_D}$ . Fig. 2 compares the bacterial growth rate with the maximum innate immune killing rate as functions of bacterial density. There is an unstable fixed point  $B_I^U$  at low bacterial density (main figure) and a stable fixed point  $B_I^S$  at high bacterial density (inset figure).  $B_I^U$  and  $B_I^S$  can be obtained by considering  $G(B) = D(B)$  and solving the resulting quadratic equation, giving

$$B_I^U = \frac{K_C - K_D}{2} - \Delta \quad \text{and} \quad B_I^S = \frac{K_C - K_D}{2} + \Delta \quad (4)$$

where  $\Delta \equiv \sqrt{(K_C + K_D)^2/4 - K_C K_D \epsilon K_I/r}$ .

When the bacterial concentration is above  $B_I^U$ , the system will reach the stable fixed point  $\{B^* = B_I^S, P^* = 0, I^* = K_I\}$  such that the bacterial population persists. This fixed point is reached when there is no phage and the innate immune response alone is insufficient in wiping out the bacteria. On the other hand, when the bacterial density is below  $B_I^U$ , the innate immune killing rate is greater than the bacterial growth rate so the innate immune



**Fig. 3.** Time series of bacterial density  $B$  (black curve), phage density  $P$  (grey curve) and innate immune response  $I$  (light grey curve) in our model with (a) bacteria and phage only, (b) bacteria and innate immune response only, with the inset showing a lower bacterial inoculum leads to bacterial elimination, and (c) bacteria, phage and innate immune response combined. The model parameters are given in Table 3. The inset in (b) has a lower initial bacterial density of  $10^4 \text{ ml}^{-1}$ .

response can eventually eliminate the bacteria and drive the system to a bacteria-free class I fixed point. Therefore  $B_I^U$  gives the threshold of bacterial density above which the maximum innate immune response fail to eliminate the bacteria. This threshold phenomenon is consistent with experimental observations of the existence of an infective dose required for a bacterial infection to be established (Leggett et al., 2012; Smith and Smith, 2016).

Both saturation effects in the model are necessary to produce this threshold phenomenon, i.e., the innate immune intensity must have an upper bound and the efficiency of immune killing must decrease with bacterial burden. Without the first saturation effect ( $K_I \rightarrow \infty$ ), the immune response would invariably eliminate the bacteria in the long-term as any fixed point with  $B > 0$  and  $I > 0$  is impossible (see Eq. (3)). Without the second saturation effect ( $K_D \rightarrow \infty$ ), the dynamics would be solely determined by the maximum bacterial growth rate  $r$  and maximum per capita immune killing rate  $\epsilon K_I$ . In such a case, the bacterial population is either always eliminated ( $r \leq \epsilon K_I$ ) or never eliminated ( $r > \epsilon K_I$ ) by the immune response alone, both of which are inconsistent with the experimentally observed threshold phenomenon.

The third class of fixed points exhibits coexistence of bacteria, phage and innate immune response. In this case, the phage persist by infecting and lysing the bacterial population, but the combined effect of phage predation and innate immune response is insufficient to reduce the bacterial population to zero. By Eqs. (1) and (2) the equilibrium bacteria and phage densities are given respectively by

$$B_{PI} = B_P \equiv \frac{\omega}{\beta \phi}, \quad (5)$$

$$P_{BI} = \frac{1}{\phi} \left[ r \left( 1 - \frac{B_{PI}}{K_C} \right) - \frac{\epsilon K_I}{1 + B_{PI}/K_D} \right]. \quad (6)$$

The equilibrium level of bacteria  $B_{PI}$  in the coexistence state depends on the phage parameters and is identical to the equilibrium density  $B_P$  when controlled by phage alone. For the coexistence fixed point to be feasible, the phage population density must be positive. A positive phage population occurs when the bacteria growth rate exceeds that of the innate immune killing rate given by  $B = B_P$ . This condition is satisfied when  $B_I^U < B_P < B_I^S$ .

In summary, the bacteria can only be eliminated if the system reaches a class I bacteria-free fixed point. In a class II fixed point, the bacteria persist in the absence of phage. This can happen either when no phage is administered or when the phage administered cannot sustain its population and is eliminated. Finally, the combined killing action of phage and innate immune response is insufficient in eradicating the bacteria in a class III fixed point.

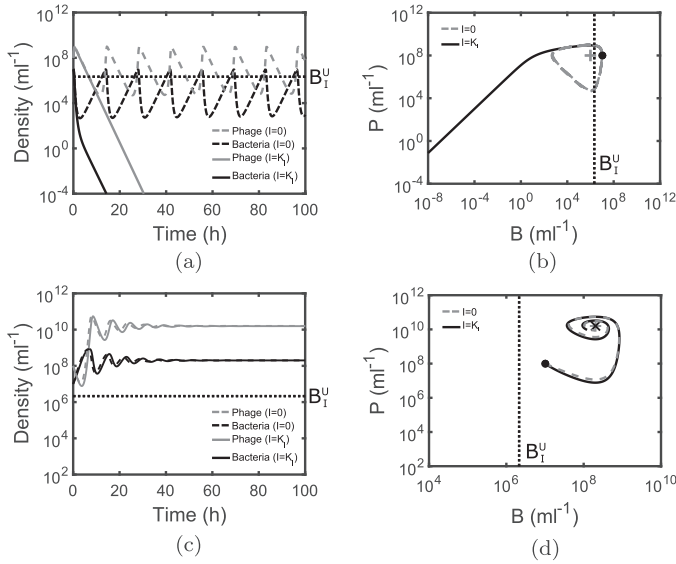
### 3.2. Demonstration of a possible synergistic effect between phage and innate immune response

Here we demonstrate that a synergistic effect can be realized in this phage therapy model. In Fig. 3, we compare the dynamics of bacteria, phage, and the innate immune response in three different cases. In the first case (Fig. 3(a)), the bacteria solely interact with phage. The bacteria and phage populations exhibit predator-prey oscillations. These oscillations would eventually be dampened so that populations reach an equilibrium point in the long term (see Eqs. (5) and (6) with  $\epsilon = 0$ ) (Weitz, 2015). In this case, the phage alone are unable to eliminate the bacteria. In the second case (Fig. 3(b)), the bacteria interact with the innate immune response in the absence of phage. Initially, there is rapid reproduction of the bacteria and the innate immune response grows as it is stimulated by the presence of bacteria. However, the bacteria persists by reaching a population that is sufficient to evade the maximum innate immune response  $K_I$ . This is an example of the system converging to a class II fixed point. In this case innate immune response alone is insufficient in eliminating the bacteria. In addition, we show in the inset of Fig. 3(b) that a lower bacterial inoculum can be cleared by the immune response, which is consistent with the existence of an infectious dose required to establish an infection. Finally, in Fig. 3(c) phage and innate immune response act together on the bacterial population initialized above the infectious dose. In this case, oscillations are observed initially for one cycle, but as the innate immune response grows, the phage drive the system to a bacteria-free class I fixed point where the bacteria is eventually eliminated. The phage and innate immune response thus works in synergy to eliminate the bacteria. This synergistic effect is caused by a reduction of the bacterial population by phage below a level of  $B_I^U$ . At this level the bacteria are controlled by the innate immune response. With the elimination of the bacterial population, the phage are also eliminated.

### 3.3. Conditions for bacteria elimination through static phage-immune synergy

Next, we simplify the system by applying a quasistatic approximation with the innate immune response treated as a constant. This simplification is justified given that bacteria and phage populations are expected to change more rapidly than the innate immune response. We apply this approximation in the case when the innate immune response has reached its maximum  $K_I$ . This corresponds to a scenario in which the innate immune response has not controlled a bacterial pathogen. Then phage are added as an





**Fig. 4.** Comparison of time series and phase portraits with and without innate immune response for two different adsorption rates. (a) Time series of bacteria (black curves) and phage densities (grey curves) with adsorption rate  $\phi = 10^{-8}$  ml h $^{-1}$ . Solid lines are for the case of  $I = K_I$  while dashed lines are for the case without innate immune response ( $I = 0$ ). The horizontal dotted line marks the position of  $B = B_I^U$ , the bacterial density below which the maximum innate immune response alone can eliminate the bacteria. (b) shows the phase portrait for the time series in (a). Black solid line is the phase trajectory when  $I = K_I$  while grey dashed line is the trajectory when  $I = 0$ . The vertical dotted line mark the position of  $B = B_I^U$  as in (a). The initial conditions ( $B_0 = 10^7$  ml $^{-1}$ ,  $P_0 = 10^8$  ml $^{-1}$ ) of the trajectory are marked by a filled circle and the fixed point  $\{B^* = B_p, P^* = \frac{r}{\phi} (1 - \frac{B_p}{K_C})\}$  without innate immunity ( $I = 0$ ) is denoted by a plus sign. (c) and (d) are the same as (a) and (b) but with a lower adsorption rate  $\phi = 5 \times 10^{-11}$  ml h $^{-1}$ . The coexistence fixed point  $\{B^* = B_{pI}, P^* = P_{pI}, I^* = K_I\}$  is marked by a cross in (d).

additional therapeutic. In this event, the model equations in Eqs. (1)–(3) reduce to

$$\dot{B} = rB \left(1 - \frac{B}{K_C}\right) - \phi BP - \frac{\epsilon K_I B}{1 + B/K_D}, \quad (7)$$

$$\dot{P} = \beta \phi BP - \omega P. \quad (8)$$

In this approximation, we identify the synergistic effect to mean that phage drive the system originally destined to reach the class II fixed point  $\{B^* = B_I^S, P^* = 0, I^* = K_I\}$  to the class I fixed point  $\{B^* = 0, P^* = 0, I^* = K_I\}$  instead. This transition corresponds to the scenario in which phage drive a system from one uncontrolled by the innate immune response to one in which both bacteria and phage are eliminated. This synergistic effect depends on the relative strength of phage and innate immune control of bacteria. The phage-controlled bacterial density is denoted as  $B_p$ . The bacterial density can reach a maximum of  $B_I^S$  when the innate immune response alone cannot eliminate the bacteria. Synergistic elimination occurs when the phage drive the bacterial population to a level below  $B_I^U$  where the maximum innate immune response alone can eliminate the bacteria. This is guaranteed to happen if  $B_p$  is below  $B_I^U$ , i.e.

$$B_p \equiv \frac{\omega}{\beta \phi} < B_I^U. \quad (9)$$

This synergistic effect only relies on the behavior of the system at equilibrium and is independent of the transient dynamics. We therefore denote Eq. (9) as the condition for bacteria elimination through “static synergy”.

In Fig. 4(a) and (b) we show the dynamics of the system with an initial bacterial density  $B_0 = 10^7$  ml $^{-1}$  and phage dose  $P_0 =$

$10^8$  ml $^{-1}$  for a multiplicity of infection (MOI) of 10. The administered phage has an adsorption rate  $\phi = 10^{-8}$  ml h $^{-1}$  chosen such that  $B_p$  is below  $B_I^U$ . In the absence of innate immune response ( $I = 0$ ), the bacteria and phage populations would oscillate around the fixed point  $\{B^* = B_p, P^* = \frac{r}{\phi} (1 - \frac{B_p}{K_C})\}$  such that part of the trajectory corresponds to states with a bacterial level below  $B_I^U$ . For the set of parameters we consider,  $B_I^U \approx 2.14 \times 10^6$  ml $^{-1}$  and the condition for static synergy is given by  $\phi \gtrsim 4.67 \times 10^{-9}$  ml h $^{-1}$ . As a result, the bacteria are eliminated given the maximum innate immune response  $I = K_I$ .

It is also important to consider the failure of the synergistic effect. In particular, when  $B_I^U < B_p < B_I^S$ , the coexistence steady state given by Eqs. (5) and (6) is feasible. In this event the phage drive the bacterial density to the level  $B_p$ . The innate immune response has a marginal effect on the dynamics of the system (Fig. 4(c) and (d)) and no synergistic effect between phage and innate immune response is observed. Finally, when  $B_p > B_I^S$  the innate immune response would bring the bacterial density down to  $B_I^S$  which is insufficient to support the phage population. The phage decay at a faster rate than its replication and eventually die out while the bacterial infection persists.

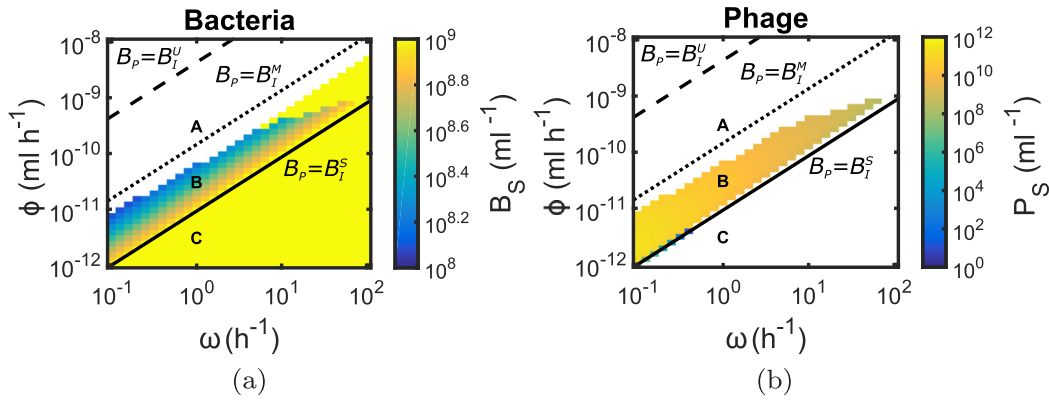
### 3.4. Conditions for bacteria elimination through dynamic phage-immune synergy

Here, we consider conditions in which the innate immune response alone cannot eliminate the bacteria. We initialize the system in a Class II fixed point. We then consider the effect of adding phage. In Fig. 5 we show simulation results for the steady state bacteria and phage density as functions of the phage decay rate  $\omega$  and adsorption rate  $\phi$ . When the phage decay at a slow rate and infects at a high rate which corresponds to a low  $B_p$ , it acts synergistically with the innate immune response to eliminate the bacteria. The thresholds  $B_p = B_I^U$  and  $B_p = B_I^S$  are compared to the simulation results and as expected when  $B_p < B_I^U$  the synergistic effect is always able to exterminate the bacteria. In addition, when  $B_p > B_I^S$  the bacteria persist but phage go extinct. The fixed point analysis predicted a feasible coexistence state of bacteria, phage and innate immune response when  $B_I^U < B_p < B_I^S$ , but in the simulation this is only observed for a subset of the region with  $B_p$  above an intermediate value. This implies that phage-immune synergy is more robust than expected solely from the feasibility of the coexistence state. This discrepancy can be explained by the stability of the coexistence state. Specifically, bacteria may be eliminated if the coexistence state is unstable. The stability of a dynamical system near a fixed point can be analyzed by considering its Jacobian matrix evaluated at the fixed point (Strogatz, 2014). In Appendix A we show that the condition for stability is:

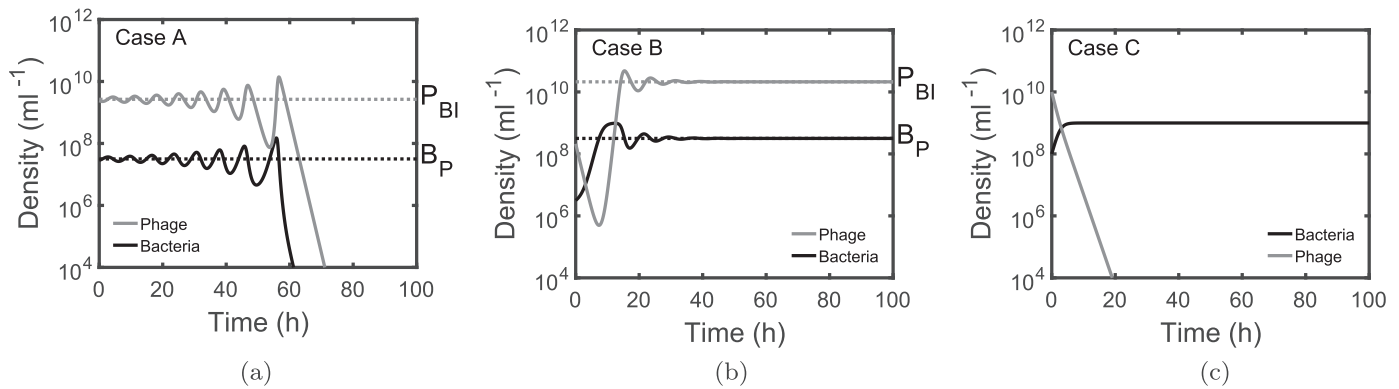
$$B_p > K_D \left( \sqrt{\frac{\epsilon K_I K_C}{r K_D}} - 1 \right) = B_I^M. \quad (10)$$

In Fig. 5 we plot the threshold  $B_p = B_I^M$  and verify that for  $B_p < B_I^M$  (unstable coexistence state) the bacteria is always driven to extinction.

To show the effect of stability on dynamics, in Fig. 6 we compare the time series of bacteria and phage densities at the three sample points A, B and C from Fig. 5. Case A satisfies  $B_I^U < B_p < B_I^M$  while case B satisfies  $B_I^M < B_p < B_I^S$ . Although coexistence is feasible in both cases, it is unstable in case A and the escalating oscillations caused by any initial deviation from the coexistence state eventually result in extinction of the bacteria. We note that the conditions we derive for instability are sufficient for elimination, and under-estimate the extent to which transient dynamics can enhance the robustness of the synergistic effect. In case B, bacteria persist as the system quickly converges to the coexistence state



**Fig. 5.** Heat maps showing the dependence of (a) steady state bacterial density  $B_S$  and (b) steady state phage density  $P_S$  on the phage decay rate  $\omega$  and adsorption rate  $\phi$ . The white region represents the parameter space with (a) elimination of bacteria and (b) phage extinction. The solid line is  $B_p = B_I^S$ , the dashed line is  $B_p = B_I^U$  and the dotted line is  $B_p = B_I^M$ . The points labeled by A, B and C are sample points of the different regimes with time series shown in Fig. 6(a), (b) and (c) respectively. The initial conditions are given by  $B_0 = B_I^S$ ,  $P_0 = 10 \times B_I^S$  and  $I_0 = K_I$ .



**Fig. 6.** Time series of bacteria (black curve) and phage densities (grey curve) at the three sample points A, B and C in Fig. 5: (a)  $\phi = 10^{-9.5} \approx 3.16 \times 10^{-10} \text{ ml h}^{-1}$  ( $B_I^U < B_P < B_I^M$ ), (b)  $\phi = 3.16 \times 10^{-11} \text{ ml h}^{-1}$  ( $B_I^M < B_P < B_I^S$ ) and (c)  $\phi = 3.16 \times 10^{-12} \text{ ml h}^{-1}$  ( $B_P > B_I^S$ ). The phage decay rate  $\omega = 1 \text{ h}^{-1}$  for all three cases. The initial conditions for (a) and (b) are chosen by perturbing from the coexistence state, i.e. ( $B_0 = 0.9 \times B_P(\phi)$ ,  $P_0 = 0.9 \times P_{BI}(\phi)$ ) and ( $B_0 = 0.01 \times B_P(\phi)$ ,  $P_0 = 0.01 \times P_{BI}(\phi)$ ) for (a) and (b) respectively. For (c) where the coexistence state is infeasible, the initial conditions are  $B_0 = 10^8 \text{ ml}^{-1}$  and  $P_0 = 10^{10} \text{ ml}^{-1}$ .

**Table 2**

Different regimes of the effect of phage therapy, the corresponding conditions and examples of time series in each regime.

Condition	Effect of adding phage	Example
$B_P < B_I^U$	Phage-immune synergy (static)	Fig. 4(a)
$B_I^U < B_P < B_I^M$	Phage-immune synergy (dynamic)	Fig. 6(a)
$B_I^M < B_P < B_I^S$	Stable coexistence	Fig. 6(b)
$B_P > B_I^S$	Phage extinction	Fig. 6(c)

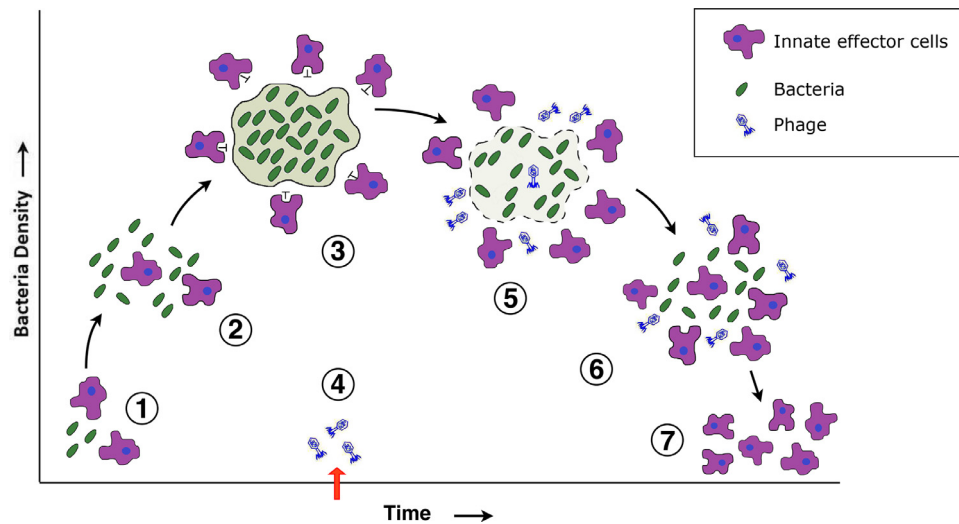
even from initial conditions far away from it. For case C,  $B_P > B_I^S$  and the coexistence state is infeasible as it has negative phage density. In this case the phage is unable to sustain its population through replication, leading to premature phage extinction.

We summarize the results of the analysis in Table 2. When  $B_P < B_I^U$  the phage drive the bacterial population below a level that can be controlled by the innate immune response which leads to bacteria elimination by static phage-immune synergy. When  $B_I^U < B_P < B_I^S$ , the phage can coexist with the bacteria in the presence of innate immune response, but when  $B_P < B_I^M$  the coexistence is unstable and the oscillations can still drive the bacteria to extinction via a dynamic synergistic effect. Finally, when  $B_P > B_I^S$  the phage become extinct rapidly as the bacteria persist at a level which cannot support phage growth. We conclude that the synergistic effect is enhanced when taking into account the stability of the coupled, nonlinear dynamical system. In Appendix B we show that the gen-

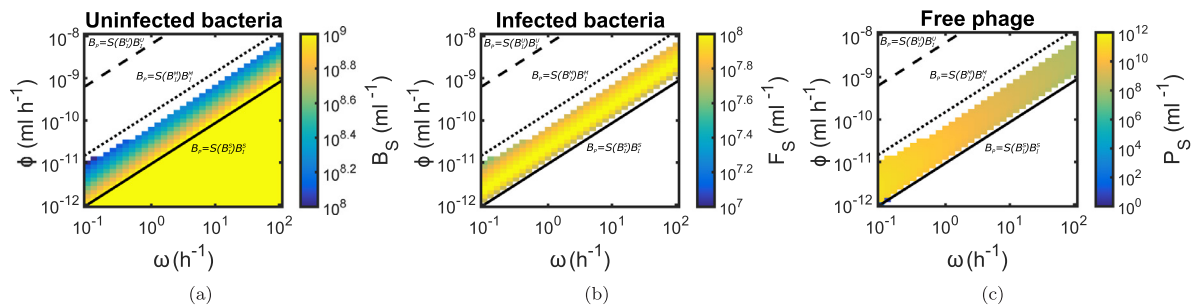
eral results of the analysis and the enhanced synergy domain are robust to model formulations. We do so by extending the model to include an explicitly infected class of bacteria. In this scenario, we still find the same qualitative results as in the model where infection is modeled implicitly (see Fig. B.1). In addition, we investigate the effect of initial conditions on the success of phage therapy in Appendix C. We show that phage-immune synergy is robust to initial bacterial inoculum and phage dose.

#### 4. Discussion

The science of phage therapy remains controversial despite renewed interest in translational and clinical applications. In particular, the interactions between bacteria, phage and the host immune response has yet to be fully characterized. Building on existing model of phage-bacteria-immune system (Levin and Bull, 2004), we developed a model of phage therapy that takes into account the finite capacity of host innate immune response and immune evasion of bacteria at high population densities. In this model, we identified a potential mechanism of phage therapy that relies on a synergistic effect between phage and the host innate immune response instead of through direct elimination of bacteria by phage. We show that the synergistic effect is robust to model formulation, bacterial inoculum, and phage dosage. Our results are qualitatively consistent with the experimental observation that phage treatment is effective in protecting normal mice from bacterial infection but



**Fig. 7.** Schematic of the mechanism of phage-immune synergy. Various stages of the infection and therapy: 1. Invasion of human host by bacteria, 2. Reproduction of bacteria, 3. Bacteria form a biofilm while innate immune response gets activated via production and recruitment of innate effector cells, 4. Administration of phage, 5. phage break down biofilm and reduce bacterial population, 6. Innate effector cells gain access to bacteria, and 7. Elimination of bacteria by innate effector cells and phage. Phage are eventually eliminated due to the absence of bacteria.



**Fig. B.1.** Heat maps showing the dependence of (a) steady state uninfected bacterial density  $B_S$ , (b) steady state infected bacterial density  $F_S$  and (c) log steady state free phage density  $P_S$  on the phage decay rate  $\omega$  and adsorption rate  $\phi$ . The white region represents the parameter space with elimination of (a) uninfected bacteria, (b) infected bacteria and (c) free phage. The solid, dotted and dashed lines are the scaled threshold relations in Eqs. (B.6), (B.7) and (B.8) respectively. The initial conditions are given by  $B_0 = B_I^S$ ,  $F_0 = 0$ ,  $P_0 = 10 \times B_I^S$  and  $I_0 = K_I$ . The lysis rate  $\eta = 2 \text{ h}^{-1}$ .

ineffective for neutropenic mice with a suppressed innate immune response (Tiwari et al., 2011).

The synergistic effect of phage therapy can be understood intuitively via the schematic in Fig. 7. In the initial phase of the infection, a small population of bacteria invade and reproduce within the human host. The bacterial population can become large enough to utilize immune evasion strategies such as biofilm formation if its growth is sufficiently fast compared to the activation of the innate immune response, for example, via production and recruitment of innate effector cells such as neutrophils. In such a case, the biofilm protects the bacteria from phagocytosis by the innate effector cells (Costerton et al., 1999), thus the innate immune response cannot eliminate the bacteria.

Addition of phage can reduce densities, e.g., by breaking down density-dependent defenses like biofilms (Alemayehu et al., 2012; Azeredo and Sutherland, 2008; Gutiérrez et al., 2015; Rodney, 2009; Timothy and Michael, 2011). The resulting reduced bacterial population exposes the bacteria to the action of the innate immune response which eventually eliminates the harmful bacteria. The phage population is eventually eliminated as its target hosts are eliminated. The model formulation is relevant to density-dependent bacterial inhibition of immune clearance, whether via biofilm formation or other means.

We have derived the conditions that predict the outcome of phage therapy in this model. The conditions for effective therapy depend on the relative strength of the phage and immune control of bacteria. Phage with a sufficiently high effectiveness act synergistically with the innate immune response in either a static or dynamic manner. In a static phage-immune synergy, phage lower the bacterial population to a point where the innate immune response can then eliminate it. In a dynamic phage-immune synergy, the introduction of phage destabilizes the system and the subsequent oscillations drive the bacterial densities sufficiently low to be eliminated by the immune response. Phage with intermediate effectiveness can stably coexist with the innate immune response without clearing the bacterial infection. Phage with low effectiveness will become extinct prematurely. The analytical conditions for phage therapy success also provide insights on the type of phage that would be effective. Our results indicate that phage with a low value of  $B_p = \omega/(\beta\phi)$  would be more effective as a therapeutic agent, i.e., a low decay rate, high adsorption rate and large burst size. Importantly, the condition suggests that multiple factors have to be considered when evaluating the suitability of a phage strain for therapeutic use. For example, a phage strain with relatively low adsorption rate may still be effective if it has a long biological half-life *in vivo*.

The proposed model enables analytical solutions for the conditions under which the synergistic effect can eliminate the bacteria. These conditions facilitate the identification of general principles of the synergism. However, the simplification also results in certain limitations which will have to be addressed in future developments of the model. For example, our simulation results indicate that the time scale of the immune response is important in determining the outcome of infection and phage administration. In our model we have focused on the innate immune system, which has a faster time scale than the adaptive immune system but is also generally less effective in comparison. As a result, the adaptive immune response may be more critical in determining the efficacy of phage therapy in chronic infections. Future modeling efforts should explore the existence of multiple time scales and immune response strengths on the outcome of phage therapy.

Another complication that may arise in the application of phage therapy is the development of phage resistance in bacteria. Bacteria employs a wide range of strategies to evade phage infection ranging from modification of surface receptors to degradation of exogenous genetic elements by mechanisms such as the CRISPR-Cas system (Labrie et al., 2010). Phage can also evolve counter-resistance and restore infectivity against resistant strains of bacteria, resulting in coevolution between the phage and bacteria (Buckling and Rainey, 2002; Hyman and Abedon, 2010; Weitz et al., 2005). Experiments have revealed that the coevolutionary dynamics can be categorized into at least two contrasting types: arms race dynamics where the bacteria become increasingly resistant while the phage become more infective, and fluctuating selection dynamics where there is no directional change in the bacterial resistance range and phage host range (Betts et al., 2014; Hall et al., 2011). Development of phage resistance in bacteria also alters the way they interact with the immune system and in many cases will lead to reduced virulence (Filippov et al., 2011; Seed et al., 2014). The effects of the coevolutionary dynamics between bacteria, phage and immune response on the efficacy of phage therapy still remains unclear. Generalizing phage therapy models to include multiple evolved strains of bacteria and phage will be essential.

Finally, it has been recently suggested that phage may be removed or degraded by both the innate and adaptive arms of the host immune system (Hodyra-Stefaniak et al., 2015). Such removal may affect the clinical outcome of phage therapy. This effect is assumed to be constant in our model and incorporated into the decay rate  $\omega$ . However, the immune suppression of phage may increase as the bacteria activate the innate immune response. This can be modeled as a phage decay rate  $\omega(I)$  that depends on the immune response. In such a case the outcome of phage administration is likely to depend on the relative strength between this direct immune inhibition of phage and the phage-immune synergistic effect.

How can we translate model findings into a therapeutic context? One finding of our model is that phage that are only partially effective in killing bacteria *in vitro* may still be effective *in vivo* due to the synergistic effect with the host innate immune response. Current screening of phage strains for phage therapy relies on *in vitro* killing (Gill and Hyman, 2010; Khan Mirzaei and Nilsson, 2015). As a consequence, phage strains of therapeutic value may be overlooked. The synergistic effect observed in our model highlights the need to measure the interactions between bacteria, phage and components of the immune system both *in vitro* and *in vivo*. Such experiments complement prior studies involving phage and bacteria (Brockhurst and Koskella, 2013; Buckling and Rainey, 2002; Levin et al., 1977) and between bacterial pathogens and innate effector cells such as neutrophils (Li et al., 2002) and macrophages (Ensminger et al., 2012; Nau et al., 2002). Information collected from such tripartite experiments would be important to

understand the effects of phage on microbes in animal hosts and within clinical studies.

## 5. Methods

### 5.1. Model simulation

We simulate the model in Eqs. (1)–(3) and obtain the time series of the bacterial density, phage density and innate immune response intensity. The numerical integration is carried out using ode45 in MATLAB. A threshold for the population densities is implemented such that when the bacteria or phage densities fall below a set value  $p_{th} = 1 \text{ ml}^{-1}$ , it is assumed to be extinct and the population density is set to 0. The steady state bacterial level  $B_S$  is estimated by running the simulation for a sufficiently long time ( $T = 10000 \text{ h}$ ) before averaging over a duration of  $T_{av} = 1000 \text{ h}$ . The code for our simulations is available online<sup>1</sup>.

### 5.2. Parameter estimation

In Table 3 we show estimated values of the parameters in the model which are used in the simulations unless otherwise specified. The life history traits of the bacteria and phage are obtained from well-established empirical values for common bacterial pathogens and their phage in the literature (Capparelli et al., 2010; De Paepe and Taddei, 2006; Guo et al., 2011; Shao and Wang, 2008). The decay rate  $\omega$  of phage is estimated from measured clearance of phage from the blood of mice (Hodyra-Stefaniak et al., 2015) and is higher than typical decay rates of phage *in vitro* (De Paepe and Taddei, 2006).

The maximum growth rate of the innate immune response  $\alpha$ , the initial (baseline) innate immune intensity  $I_0$ , and the maximum innate immune response are estimated from measurements of neutrophil recruitment in LPS-induced acute lung injury (Reutershan et al., 2005). Since LPS is highly immunogenic, we assume that it saturates the antigen dose response of the immune activation ( $B \gg K_N$ ). Under this limit, Eq. (3) yields

$$I = \frac{I_0 K_I}{I_0 + (K_I - I_0)e^{-\alpha t}}. \quad (11)$$

We normalize the measured interstitial neutrophil count (Reutershan et al., 2005) of the whole lung by the estimated lung tissue volume of 0.135 ml to obtain the time series of neutrophil concentration. We then perform a nonlinear fitting of Eq. (11) to the time series data using the damped least-squares method computed with the Grace graphing package and obtain the parameter values.

The killing rate parameter of the innate immune response  $\epsilon$  is estimated by setting it such that  $\epsilon K_I$  gives the fitted maximum killing rate of neutrophils in a murine model of pneumonia caused by *P. aeruginosa* (Drusano et al., 2011). We utilize the same dataset to obtain the bacterial concentration  $K_D$  at which innate immune response is half saturated (Drusano et al., 2011). The bacterial density  $K_N$  at which innate immune growth rate is half its maximum is estimated from the effect of bacterial burden on macrophage recruitment rate in *Mycobacterium tuberculosis* infection (Sadek et al., 1998; Wigginton and Kirschner, 2001). Initial bacterial load is set by typical values of bacterial inoculum for *P. aeruginosa* and *S. aureus* (Drusano et al., 2010; 2011). The initial phage dose is selected to give a multiplicity of infection (MOI) of 10 which was determined by experiments to provide optimal effectiveness for respiratory infections by *P. aeruginosa* (Debarbieux et al., 2010) and *Burkholderia cepacia* complex (Semler et al., 2014).

<sup>1</sup> <https://github.com/WeitzGroup/immune-phage-synergy>.



**Table 3**  
Estimated values of parameters in the model.

Symbol and parameter	Value	Estimated from
$r$ , growth rate of bacteria at low density	$1 \text{ h}^{-1}$	<i>A. baumannii</i> and <i>P. aeruginosa</i> (Guo et al., 2011)
$K_C$ , carrying capacity of bacteria	$10^9 \text{ ml}^{-1}$	Bacterial load of <i>P. aeruginosa</i> in lung tissue of immunosuppressed mice (Guo et al., 2011)
$\beta$ , burst size of phage	100	$\phi$ , adsorption rate of phage
$\phi$ , adsorption rate of phage	$5 \times 10^{-8} \text{ ml h}^{-1}$	Within the range for Lambda phage (Shao and Wang, 2008) and other coliphage (De Paepe and Taddei, 2006)
$\omega$ , decay rate of phage	$1 \text{ h}^{-1}$	Clearance of phage from blood of mice (Hodyra-Stefaniak et al., 2015)
$\alpha$ , maximum growth rate of innate immune response	$0.97 \text{ h}^{-1}$	Fitting of interstitial neutrophil recruitment data in LPS-induced acute lung injury (Reutershan et al., 2005)
$I_0$ , initial innate immune intensity	$2.7 \times 10^6 \text{ ml}^{-1}$	Fitting of neutrophil recruitment data in acute lung injury (Reutershan et al., 2005)
$K_I$ , maximum capacity of innate immune response	$2.4 \times 10^7 \text{ ml}^{-1}$	Fitting of neutrophil recruitment data in acute lung injury (Reutershan et al., 2005)
$\epsilon$ , killing rate parameter of innate immune response	$8.2 \times 10^{-8} \text{ ml h}^{-1}$	Set such that $\epsilon K_I$ gives $1.97 \text{ h}^{-1}$ , the fitted maximum killing rate of neutrophils in a murine model of pneumonia (Drusano et al., 2011)
$K_D$ , bacterial concentration at which innate immune response is half saturated	$2.2 \times 10^6 \text{ ml}^{-1}$	Fitted parameter in a murine model of pneumonia by <i>P. aeruginosa</i> (Drusano et al., 2011)
$K_N$ , bacterial concentration when innate immune response growth rate is half its maximum	$10^5 \text{ ml}^{-1}$	Effect of bacterial burden on macrophage recruitment rate in <i>Mycobacterium tuberculosis</i> infection (Sadek et al., 1998; Wigginton and Kirschner, 2001)
$B_0$ , initial bacterial density	$10^6 \text{ ml}^{-1}$	Typical bacterial inoculum used for in vivo growth experiments of <i>P. aeruginosa</i> and <i>S. aureus</i> (Drusano et al., 2010; 2011)
$P_0$ , initial phage dose	$10^7 \text{ ml}^{-1}$	Set to give a multiplicity of infection (MOI) of 10 required to ensure effective phage therapy (Debarbieux et al., 2010; Semler et al., 2014)

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## Appendix A. Derivation of the stability condition for the coexistence state

Here we derive the condition for the coexistence state  $\{B^*, P^*, I^*\} = \{B_{BI}, P_{BI}, I_{BI}\}$  to be stable. The type and stability of a fixed point can be characterized by the determinant  $\det(\mathbf{J})$  and trace  $\text{tr}(\mathbf{J})$  of the Jacobian matrix  $\mathbf{J}$  evaluated at the fixed point (Strogatz, 2014). In particular, the stability of the system is determined by the signs of  $\det(\mathbf{J})$  and  $\text{tr}(\mathbf{J})$ .

Rewriting Eqs. (7) and (8) into  $\dot{B} = f_B(B, P)$  and  $\dot{P} = f_P(B, P)$  respectively, the Jacobian matrix of the system is defined as

$$\mathbf{J} \equiv \begin{bmatrix} \frac{\partial f_B}{\partial B} & \frac{\partial f_B}{\partial P} \\ \frac{\partial f_P}{\partial B} & \frac{\partial f_P}{\partial P} \end{bmatrix} \quad (\text{A.1})$$

We compute the Jacobian matrix by calculating the partial derivatives:

$$\begin{aligned} \frac{\partial f_B}{\partial B} &= r \left( 1 - \frac{B}{K_C} \right) - \frac{\epsilon K_I}{1 + B/K_D} - \phi P \\ &\quad - \frac{rB}{K_C} + \frac{\epsilon K_I B}{K_D(1 + B/K_D)^2}, \end{aligned} \quad (\text{A.2})$$

$$\frac{\partial f_B}{\partial P} = -\phi B, \quad (\text{A.3})$$

$$\frac{\partial f_P}{\partial B} = \beta \phi P, \quad (\text{A.4})$$

$$\frac{\partial f_P}{\partial P} = \beta \phi B - \omega. \quad (\text{A.5})$$

The Jacobian matrix of the system can therefore be written as

$$\mathbf{J} = \begin{bmatrix} \frac{\partial f_B}{\partial B} & -\phi B \\ \beta \phi P & \beta \phi B - \omega \end{bmatrix}. \quad (\text{A.6})$$

At the coexistence state, the first line on the right hand side of Eq. (A.2) vanishes as a result of Eq. (6). Together with  $\beta \phi B_{BI} - \omega = 0$ , it yields the Jacobian matrix at coexistence

$$\mathbf{J} = \begin{bmatrix} -\frac{rB_{BI}}{K_C} + \frac{\epsilon K_I B_{BI}}{K_D(1 + B_{BI}/K_D)^2} & -\phi B_{BI} \\ \beta \phi P_{BI} & 0 \end{bmatrix}. \quad (\text{A.7})$$

Equation (A.7) gives the following determinant and trace:

$$\det(\mathbf{J}) = \beta \phi^2 B_{BI} P_{BI} = \omega \phi P_{BI} > 0, \quad (\text{A.8})$$

$$\text{tr}(\mathbf{J}) = \left[ -\frac{r}{K_C} + \frac{\epsilon K_I}{K_D(1 + B_{BI}/K_D)^2} \right] B_{BI}. \quad (\text{A.9})$$

Since the determinant is always positive, the condition for stability is given by  $\text{tr}(\mathbf{J}) < 0$  (Strogatz, 2014). By Eq. (A.9) this is satisfied when

$$B_{BI} > K_D \left( \sqrt{\frac{\epsilon K_I K_C}{r K_D}} - 1 \right) = B_I^M, \quad (\text{A.10})$$

which is the criterion in Eq. (10).

## Appendix B. Bacteria-phage-immune model with an infected bacterial class

In this appendix we show that the general results of our model is robust to variations in model formalism. In our model, the time between adsorption of a phage particle to lysis of the bacterial cell, or the latent period, is assumed to be sufficiently small such that the replication and release of new phage particles can be treated as instantaneous. Here we extend the model to account for the latent period by introducing an infected bacterial class  $F$  explicitly in which individuals are lysed at a rate  $\eta$  (Weitz, 2015). The generalized model is given by

$$\dot{B} = \overbrace{rB\left(1 - \frac{B+F}{K_C}\right)}^{\text{Growth}} - \overbrace{\phi BP}^{\text{Infection}} - \overbrace{\frac{\epsilon IB}{1 + (B+F)/K_D}}^{\text{Innate immune killing}}, \quad (\text{B.1})$$

$$\dot{F} = \overbrace{\phi BP}^{\text{Infection}} - \overbrace{\eta F}^{\text{Lysis}} - \overbrace{\frac{\epsilon IF}{1 + (B+F)/K_D}}^{\text{Innate immune killing}}, \quad (\text{B.2})$$

$$\dot{P} = \overbrace{\beta \eta F}^{\text{Release of phage}} - \overbrace{\phi BP}^{\text{Adsorption}} - \overbrace{\omega P}^{\text{Decay}}, \quad (\text{B.3})$$

$$\dot{I} = \overbrace{\alpha I \left(1 - \frac{I}{K_I}\right) \frac{B+F}{B+F+K_N}}^{\text{Innate immune stimulation}}, \quad (\text{B.4})$$

where  $F$  is the population density of the bacteria infected by phage,  $\eta$  is the rate at which the infected bacteria lyse, and the rest of the parameters are defined in the original model in Eqs. (1)–(3).

We simulate this model by fixing  $I = K_I$  as in Fig. 5 and show the steady state populations of uninfected bacteria, infected bacteria and phage in Fig. B.1. The results show all the same qualitative features as in Fig. 5 including regimes of phage-immune synergism, phage-bacteria-immune coexistence and phage extinction. This indicates that the results of our analysis is robust to the model formulation. The results differ from the model without an infected class only by a scaling of the thresholds  $B_P = B_I^S$ ,  $B_P = B_I^M$  and  $B_P = B_I^U$ . The scaling is caused by a reduction of the effective burst size that results from infected bacteria being killed by the innate immune response before the phage particles are released. As a result, for the phage infection to successfully produce viral progeny, the lysis must be completed before the bacterial cell is killed by the innate immune response. Assuming the innate immune response is at its maximum  $K_I$ , this gives the effective burst

size at equilibrium

$$\tilde{\beta} = \frac{\eta}{\eta + D(B^* + F^*)} \beta \quad (\text{B.5})$$

where the function  $D(x) \equiv \frac{\epsilon K_I}{1+x/K_D}$  is the per capita killing rate by the maximum innate immune response when the total (uninfected and infected) bacterial density is  $x$ .  $B^*$  and  $F^*$  are the equilibrium densities of the uninfected and infected bacteria respectively. Assuming that lysis happens at a sufficiently fast rate compared to the phage infection, the total bacterial density  $B^* + F^*$  at equilibrium can be estimated by the equilibrium bacterial density in the limit  $\eta \rightarrow \infty$ , i.e. the equilibrium value for the model without an infected class. The value of  $B^* + F^*$  is thus approximated by the value of  $B_P$  at each threshold from the original model in Eqs. (1)–(3). This results in the following scaled thresholds:

$$B_P = S(B_I^S) B_I^S, \quad (\text{B.6})$$

$$B_P = S(B_I^M) B_I^M, \quad (\text{B.7})$$

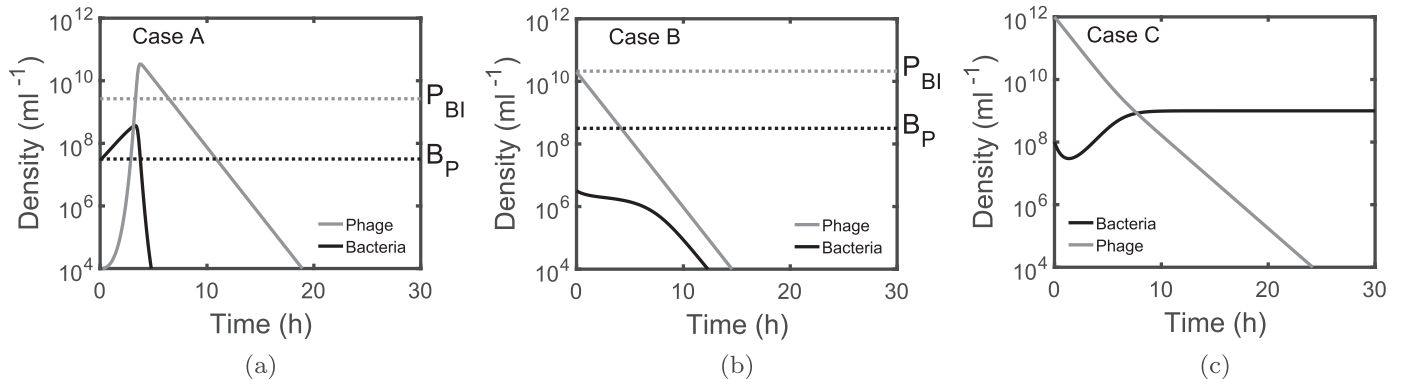
$$B_P = S(B_I^U) B_I^U \quad (\text{B.8})$$

where the scaling function  $S(B) \equiv (1 + D(B)/\eta)$ . The scaled thresholds are shown in Fig. B.1 and give satisfactory approximation of the transitions between regimes of phage-immune synergism, coexistence and phage extinction. The results of the analysis confirm that the same mechanism for the synergistic effect between phage and immune response applies after accounting for a reduced effective burst size.

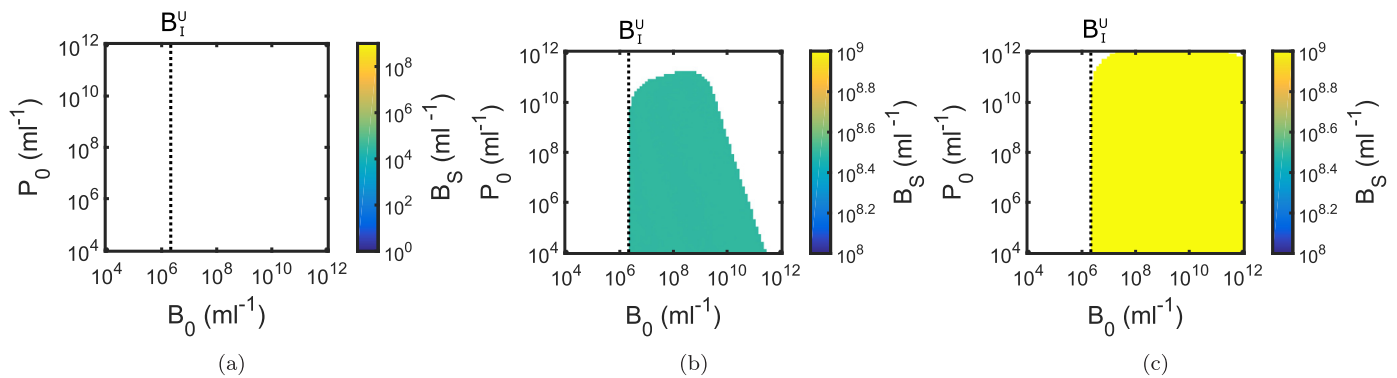
## Appendix C. Effects of initial conditions on outcome of phage therapy

In this appendix we investigate the effects of initial bacterial inoculum  $B_0$  and phage dose  $P_0$  on the efficacy of phage therapy. In Fig. 6, we showed the dynamics of our model in the regimes of dynamic phage-immune synergy ( $B_I^U < B_P < B_I^M$ ), stable coexistence ( $B_I^M < B_P < B_I^S$ ) and phage extinction ( $B_P > B_I^S$ ). We study the robustness of these regimes to perturbations in initial conditions by modifying the initial phage dose (Fig. C.1). We find that phage-immune synergy is highly robust to variations in initial conditions, as evident by bacteria elimination even after the phage dose is reduced by five orders of magnitude (compare Fig. 6(a) with Fig. C.1(a)). In this case, the ability of phage to replicate can quickly compensate for the lower phage dose.

For phage therapy failure caused by stable coexistence between bacteria, phage and host innate immunity, our simulation shows



**Fig. C.1.** Time series of bacteria (black curve) and phage densities (grey curve) with the parameters at the three sample points A ( $B_I^U < B_P < B_I^M$ ), B ( $B_I^M < B_P < B_I^S$ ) and C ( $B_P > B_I^S$ ) in Fig. 5. This figure is same as Fig. 6 but with different initial phage dose  $P_0$  given by (a)  $10^4 \text{ ml}^{-1}$ , (b)  $2 \times 10^{10} \text{ ml}^{-1}$  and (c)  $10^{12} \text{ ml}^{-1}$ .



**Fig. C.2.** Heat maps showing effects of initial bacterial inoculum and phage dose on steady-state bacterial concentration  $B_S$ . The parameters in (a), (b) and (c) are given by the three sample points A ( $B_I^U < B_P < B_I^M$ ), B ( $B_I^M < B_P < B_I^S$ ) and C ( $B_P > B_I^S$ ) in Fig. 5 respectively. The white region represents the parameter space with elimination of bacteria. The vertical dotted line marks the value of  $B_I^U$ .

that therapeutic efficacy may be restored by a substantial increase in phage dose (Fig. C.1(b)). This suggests that phage therapy may still be effective under limited circumstances in the stable coexistence regime, provided that a sufficiently high phage dose is used to compensate for the lack of phage-immune synergy. However, such high dosage may not be practical in clinical applications as excessive phage dosage has been linked to harmful inflammatory responses in the host (Pincus et al., 2015). Finally, in the phage extinction regime, even a significant increase in phage dose would not eliminate the bacteria (Fig. C.1(c)). The low phage adsorption rate in this case leads to rapid elimination of phage from the system that can negate the effect of a higher initial dose.

To verify the generality of these results, we compute the steady state bacterial density for a range of values of  $B_0$  and  $P_0$  under the three different regimes (Fig. C.2). Our results confirm the robustness of phage-immune synergy, with bacteria elimination observed over a wide range of initial conditions (Fig. C.2(a)). In the stable coexistence regime shown in Fig. C.2(b), bacteria can persist when the immune response alone is insufficient to eliminate the bacteria ( $B_0 > B_I^U$ ). Bacteria elimination can be restored by either having a very high phage dose ( $>10^{10} \text{ ml}^{-1}$ ) or a high initial bacteria density ( $>10^9 \text{ ml}^{-1}$ ). The paradoxical requirement of a high bacterial inoculum for subsequent bacteria elimination stems from the rapid replication of phage in the presence of high bacterial density. In such a case, phage population reaches a high level and eventually eliminate the bacteria. However, in practice the high bacterial burden may cause extensive inflammation and tissue damage, leading to host death before the phage population can reach sufficiently high densities. In the regime of phage extinction, increase in phage dose only has a marginal effect on the fate of the bacteria as the phage population cannot sustain itself (Fig. C.2(c)).

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