

1. Given the data as listed below

x	4.0	4.2	4.5	4.7	5.1	5.5	5.9	6.3
y	102.6	113.2	130.1	142.1	167.5	195.1	224.9	256.8

- Construct the least squares approximation of degree two and compute the error.
  - Construct the least squares approximation of the form  $be^{ax}$  and compute the error.
  - Construct the least squares approximation of the form  $bx^n$  and compute the error.
2. Find the least squares polynomial approximation of degree two on the interval  $[-1,1]$  for the function  $f(x) = \frac{1}{2}\cos x + \frac{1}{4}\sin 2x$
3. Determine the discrete least squares trigonometric polynomial  $S_4$

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using  $m=16$  for  $f(x) = x^2 \sin x$  on the interval  $[0,1]$ .

b. Compute  $\int_0^1 S_4(x) dx$

c. Compare the integral in part (b) to  $\int_0^1 x^2 \sin x dx$

d. Compute the error  $E(S_4)$

==== 第一題：資料擬合 ====

1.a 二次多項式係數 (c2, c1, c0): [ 6.69118439 -1.88374644 3.0863933 ]

1.a 擬合誤差: 0.0052456855825467295

1.b 指數函數擬合參數 (a, b): [ 0.38666401 22.82449552]

1.b 擬合誤差: 74.36078759754199

1.c 冪次函數擬合參數 (n, b): [2.02016212 6.23352099]

1.c 擬合誤差: 0.010270381747465208

==== 第二題：區間 [-1,1] 上的二次多項式擬合 ====

二次多項式擬合係數 a0, a1, a2: [ 0.49827931 0.32654833 -0.23263145]

==== 第三題：離散最小平方三角多項式 S4 ====

a係數: [ 0.39534439 -0.26547437 0.07282666 0.00205101 -0.02226183]

b係數: [ 0. 0.22673215 -0.23724918 0.16582793 -0.123859 ]

$\int_0^1 S_4(x) dx = 0.3772041437995669$

$\int_0^1 x^2 \sin(x) dx = 0.22324427548393272$

誤差  $E(S_4) = 1.0655169327253133$