

$$1.35 \quad \int_{-\infty}^{\infty} x p(x) dx = \mu \quad (1.106)$$

$$\int_{-\infty}^{\infty} (x-\mu)^2 p(x) dx = \sigma^2 \quad (1.107)$$

$$H[X] = - \int p(x) \ln p(x) dx$$

$$= - \int p(x) \left(-\frac{1}{2} \ln(2\pi\sigma^2) - \frac{(x-\mu)^2}{2\sigma^2} \right) dx$$

$$= \frac{1}{2} (\ln(2\pi\sigma^2)) + \frac{1}{\sigma^2} \int p(x) (x-\mu)^2 dx$$

$$= \frac{1}{2} (\ln(2\pi\sigma^2) + 1)$$