### Homework

### My Name

### 1 Model Building

### 1.1 Data Preprocessing

**Multicollinearity Analysis**: Generate a correlation diagram of the covariates to investigate the relationship between variables. As shown in Figure 1a and Table 1, ...

*Transformation and Residual Analysis*: The next step is to check model assumptions and transformation.

### 1.2 Model Summary

The estimated model is shown as below. The residual standard error is 0.3 and the AIC value is -67. The detail of the summary is shown in Output 1.

$$\tilde{y} = 12 + 0.2 * V5$$
$$-0.01 * V15 : V12$$
$$y = (75\tilde{y} + 1)^{2/3} - 20$$

## 2 Important Variables and Reliability Assessment

Combing the result of model comparison, the final model  $\dots$ 

## 3 Model Comparison

Compare the proposed model  $\mathbf{m1}$  with candidate models: regression tree, random forest, bagging [Faraway(2016)], ... The optimal lo and gam model are as follows:

#### References

[Faraway(2016)] J. J. Faraway, Extending the linear model with R: generalized linear, mixed effects and nonparametric regression models. Chapman and Hall/CRC, 2016.

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# Appendices

# Appendix A: Figures

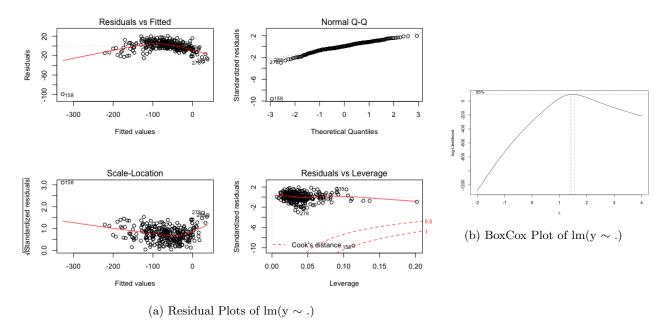


Figure 1: Diagnostics Plots of  $lm(y \sim .)$ 

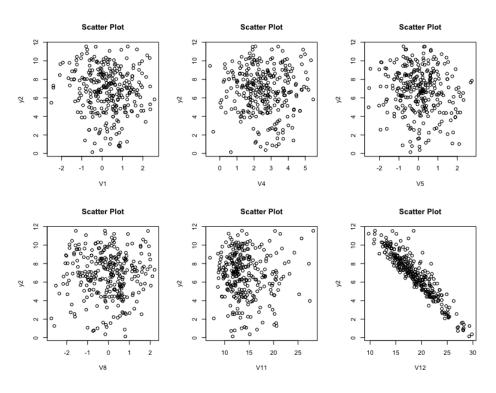


Figure 2: Scatter plot between response and variables

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## Appendix B: Tables

Table 1: Grouping of Variables

| $\overline{G0}$ | 1 | 2 | 3 | 4 |
|-----------------|---|---|---|---|
| G1              | 5 | 6 | 7 |   |

Table 2: Variables selected and VSD values

| mothod                | nethod Variables |     | ARM       |               |     | BIC       |          |  |
|-----------------------|------------------|-----|-----------|---------------|-----|-----------|----------|--|
| тетоа                 | v arrabies       | VSD | VSD_minus | $VSD_{-}plus$ | VSD | VSD_minus | VSD_plus |  |
| LASSO                 | {1 2 3 4}        | 0   | 0         | 0             | 0   | 0         | 0        |  |
| $\operatorname{SCAD}$ | {1 2 3}          | 0   | 0         | 0             | 0   | 0         | 0        |  |
| MCP                   | {1 2}            | 0   | 0         | 0             | 0   | 0         | 0        |  |

Table 3: Variable Importance

| Metric        | Importance Order                 |  |  |
|---------------|----------------------------------|--|--|
| IncMSE        | 1 2 3 4                          |  |  |
| IncNodePurity | 1 2 3 4                          |  |  |
| SOIL          | 1 2 3 4                          |  |  |
|               | (leftmost is the most important) |  |  |

Table 4: Uncertainty Assessment

| Method      |               | $S=\{1, 2, 3, 4\}$ |  |
|-------------|---------------|--------------------|--|
|             | Sequential    | 0                  |  |
| Instability | Bootstrap     | 0                  |  |
|             | Perturbation  | 0                  |  |
| ARM         | VSD           | 0                  |  |
|             | $VSD\_minus$  | 0                  |  |
|             | $VSD_{-}plus$ | 0                  |  |
|             | F-measure     | 0                  |  |
|             | G-measure     | 0                  |  |
| BIC         | VSD           | 0                  |  |
|             | $VSD\_minus$  | 0                  |  |
|             | $VSD_{-}plus$ | 0                  |  |
|             | F-measure     | 0                  |  |
|             | G-measure     | 0                  |  |

Table 5: Model Comparison

| Comparison             | Winner | Winning Fraction of m1 |
|------------------------|--------|------------------------|
| m1 vs. Regression Tree | m1     | 1                      |
| m1 vs. random forest   | m1     | 1                      |
| m1 vs. bagging         | m1     | 1                      |
| m1 vs. loess           | m1     | 1                      |
| m1 vs. gam             | gam    | 0                      |

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Table 6: Cross Validation MSE and Absolute Error

| Model            | CV MSE | CV Mean Absolute Error |
|------------------|--------|------------------------|
| m1               | 0      | 0                      |
| Regression Tree  | 0      | 0                      |
| random forest    | 0      | 0                      |
| bagging<br>loess | 0      | 0                      |
| loess            | 0      | 0                      |
| gam              | 0      | 0                      |

# Appendix C: R output

#### Output 1

> summary(m3.1)

#### Coefficients:

Estimate Std. Error t value Pr(>|t|) (Intercept) 12.915676 0.502463 25.705 < 2e-16 \*\*\* ۷5 0.287077 0.108717 2.641 0.00873 \*\* 8V -0.033139 0.020466 -1.619 0.10649 V11 0.402557 0.042078 9.567 < 2e-16 \*\*\*

Residual standard error: 0.3505 on 289 degrees of freedom

> extractAIC(m3.1)

[1] 10.0000 -617.0269