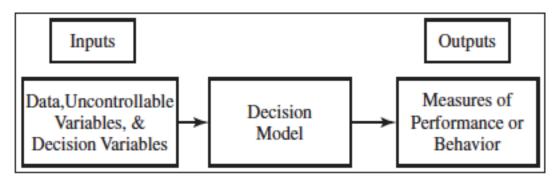


Statistics, Data Analysis, and Decision Modeling, Fifth Edition

James R. Evans



- A model is an abstraction or representation of a real system, idea, or object.
- Models could be pictures, spreadsheets, or mathematical relationships
- Models contain data, uncontrollable variables, and decision variables





Decision Models – Outsourcing Example

 Decision models are models that can be used to understand, analyze, or facilitate making a decision

	А	В
1	Outsourcing Decision Model	
2		
3	Data	
4		
5	Manufactured in-house	
6	Fixed cost	\$ 50,000
7	Unit variable cost	\$ 125
8		
9	Purchased from supplier	
10	Unit cost	\$ 175
11		
12	Model	
13		
14	Demand volume	1500
15		
16	Total manufacturing cost	\$ 237,500
17	Total purchased cost	\$ 262,500
18	Difference	\$ (25,000)
19		
20	Decision	Manufacture

	A	В
1	Outsourcing Decision Model	
2		
3	Data	
4		
5	Manufactured in-house	
6	Fixed cost	50000
7	Unit variable cost	125
8		
9	Purchased from supplier	
10	Unit cost	175
11		
12	Model	
13		
14	Demand volume	1500
15		
16	Total manufacturing cost	=B6+B7*B14
17	Total purchased cost	=B14*B10
18	Difference	=B16-B17
19		
20	Decision	=IF(B18<=0, "Manufacture", "Outsource")



Outsourcing Model

- Model components
 - F = fixed cost of in-house manufacturing
 - V = unit variable cost of in-house manufacturing
 - C = unit cost of outsourcing
 - D = demand volume
- Total Manufacturing Cost = TMC = F + V * D
- Total outsourcing cost = TOC = C * D.



Types of Decision Models

- Descriptive describe relationships and provide information for evaluation
- Prescriptive (optimization models) determine an optimal policy, that is, the
 best course of action that a decision
 maker should take to maximize or
 minimize some objective

Airline Pricing Model

	٨	
4	A	В
1	Airline Pricing Model	
2		
3	Data	
4	Airplane capacity	300
5	Fixed cost	\$ 90,000
6	Demand function	
7	slope	-2.33
8	intercept	1900
9	·	
10	Model	
11		
12	Revenue	
13	Unit price	\$ 500.00
14	Demand	733
15	Number of flights/day	3
16	Total Revenue	\$366,666.67
17	Cost	
18	Fixed Cost	\$270,000.00
19		
20	Profit	\$96,666.67

	A	В
1	Airline Pricing Model	В
2	Annie i neing moder	
3	Data	
4	Airplane capacity	300
	Fixed cost	90000
6	Demand function	
7	slope	=-7/3
8	intercept	1900
9	·	
10	Model	
11		
12	Revenue	
13	Unit price	
14	Demand	=B8+B7*B13
15		=ROUNDUP(B14/B4,0)
16	Total Revenue	=B13*B14
17	Cost	
18	Fixed Cost	=B5*B15
19		
20	Profit	=B16-B18



Model Analysis

- What-If Analysis evaluate how specific combinations of model inputs that reflect key model assumptions affect model outputs (often called sensitivity analysis).
- Excel tools
 - Data tables
 - Scenario manager
 - Goal seek



Data Tables

- Summarizes the impact of one or two inputs on a specified output
- Excel tools
 - One-way data tables
 - Two-way data tables

One Way Data Table

_					,		
	А	В	С	D	E	F	G
1	Outsourcing Decision Model						
2			Column		Fixed Costs	Difference	Decision
3	Data		input cell			\$(25,000)	Manufacture
4		/	mparcen		\$ 30,000	\$ (45,000)	Manufacture
5	Manufactured in-house	V			\$ 40,000	\$(35,000)	Manufacture
6	Fixed cost	\$ 50,000			\$ 50,000	\$ (25,000)	Manufacture
7	Unit variable cost	\$ 125			\$ 60,000	\$(15,000)	Manufacture
8					\$ 70,000	\$ (5,000)	Manufacture
9	Purchased from supplier				\$ 80,000	\$ 5,000	Outsource
10	Unit cost	\$ 175			\$ 90,000	\$ 15,000	Outsource
11					\$ 100,000	\$ 25,000	Outsource
12	Model						
13							
14	Demand volume	1500					
15							
16	Total manufacturing cost	\$ 237,500					
17	Total purchased cost	\$ 262,500					
18	Difference	\$ (25,000)					
19							
20	Decision	Manufacture					

Two Way Data Table

	А	В	С	D	Е	F	G	Н	I	J	К
1	Outsourcing Decision Model										
2			Column		Fixed Cost			Variable Cost			
3	Data		input cell		Manufacture	\$ 100	\$ 110	\$ 120	\$ 130	\$ 140	\$ 150
4		/			\$ 30,000	Manufacture	Manufacture	Manufacture	Manufacture	Manufacture	Manufacture
5	Manufactured in-house	K			\$ 40,000	Manufacture	Manufacture	Manufacture	Manufacture	Manufacture	Outsource
6	Fixed cost	\$ 50,000			\$ 50,000	Manufacture	Manufacture	Manufacture	Manufacture	Manufacture	Outsource
7	Unit variable cost	\$ 125			\$ 60,000	Manufacture	Manufacture	Manufacture	Manufacture	Outsource	Outsource
8		K	Row		\$ 70,000	Manufacture	Manufacture	Manufacture	Outsource	Outsource	Outsource
9	Purchased from supplier	`	input cell		\$ 80,000	Manufacture	Manufacture	Manufacture	Outsource	Outsource	Outsource
10	Unit cost	\$ 175	purce		\$ 90,000	Manufacture	Manufacture	Outsource	Outsource	Outsource	Outsource
11					\$ 100,000	Manufacture	Outsource	Outsource	Outsource	Outsource	Outsource
12	Model										
13											
14	Demand volume	1500									
15											
16	Total manufacturing cost	\$ 237,500									
17	Total purchased cost	\$ 262,500									
18	Difference	\$ (25,000)									
19											
20	Decision	Manufacture									

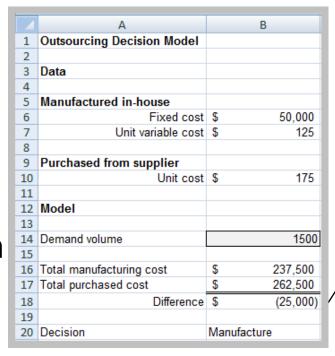
Scenario Manager

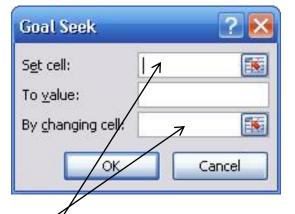
	Fixed Cost	Unit Variable Cost	Demand Volume
Best case	\$40,000	\$120	1,800
Worst case	\$60,000	\$140	1,000
Most likely case	\$55,000	\$125	1,500

_									
2	Scenario Summ	ary							
3		Cu	rrent Values:		Best case	Worst case	Мо	st likely case	
5	Changing Cells:								
6	\$B\$6	\$	50,000	\$	40,000	\$	60,000	\$	55,000
7	\$B\$7	\$	125	\$	120	\$	140	\$	125
8	\$B\$14		1500	0 180		1000			1500
9	Result Cells:								
10	\$B\$18	\$	(25,000)	\$	(59,000)	\$	25,000	\$	(20,000)
11	\$B\$20	Mai	nufacture	Ma	nufacture	Ou	tsource	Ma	nufacture
12	Notes: Current V	alue	es column re	pre	sents values	of	changing cel	ls a	t
13	time Scenario Sur	mm	ary Report v	/as	created. Cha	ngi	ng cells for e	each	
14	scenario are high	ligh	ted in gray.						



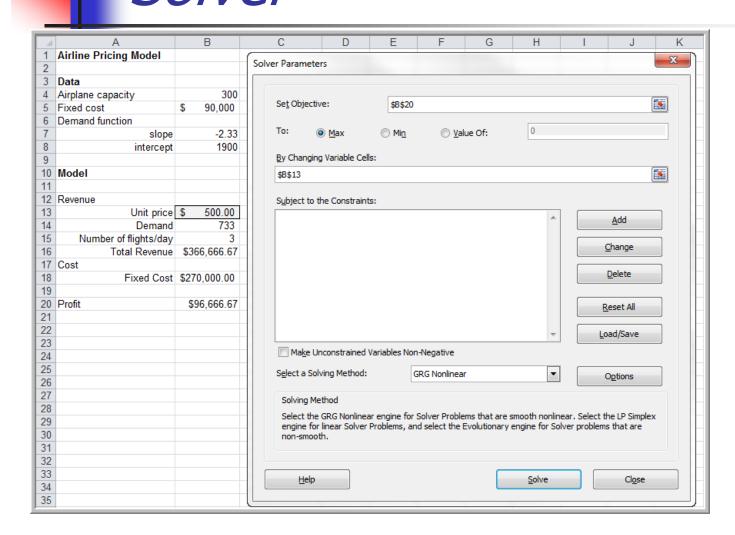
- Find the value of an input that produces a known result within a spreadsheet
- Example: find the breakeven point in the outsourcing decision model





Set cell is B18; To value = 0; By changing cell is B14

Optimization Models: Excel Solver



Solution: Price = \$428.57; profit = \$115,714.28



Tools for Model Building

- Logic and business principles
- Common mathematical functions
- Data fitting
- Spreadsheet engineering



Logic and Business Principles

- Profit = Revenue Cost
- Revenue = (Unit price)(Quantity sold)
- Cost = Fixed cost + Unit cost*Quantity produced
- Quantity sold = Min(Quantity produced, Demand)
- Profit = (Unit price)Min(Quantity produced, Demand)– [Fixed cost + (Unit cost)(Quantity produced)]



Modeling Example: Gasoline Consumption

- m = miles/day driven
- d = days/month
- f = miles/gallon
- Miles driven/month = md
- Gallons consumed/month = md/f



Net Present Value

- Measures the worth of a stream of cash flows, taking into account the time value of money.
- A cash flow of F dollars t time periods in the future is worth $F(1 + i)^t$ dollars today, where i is the discount rate. $NPV = \sum_{t=0}^{n} \frac{F_t}{(1+i)^t}$

 $\overline{t=0} (1+i)^{t}$

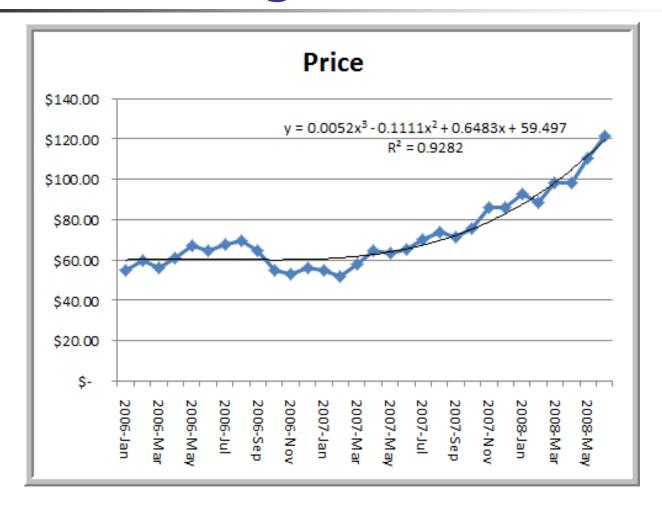
Excel function NPV(rate, value1, value2,...)



Common Mathematical Functions

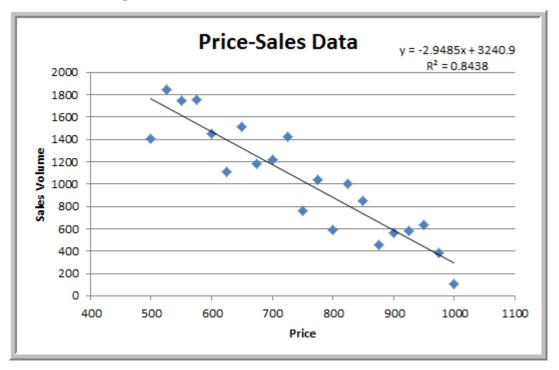
- *Linear: y* = *mx* + *b*
- Logarithmic: y = ln(x)
- Polynomial: $y = ax^2 + bx + c$ (quadratic)
- Power: $y = ax^b$
- Exponential: y = ab^x

Data Fitting



Revenue Model

Total revenue = Price*Sales = Price * (-2.794 * Price + 3149) = -2.794 * Price² + 3149 * Price





Spreadsheet Engineering

- Improve the design and format of the spreadsheet itself.
- Improve the process used to develop a spreadsheet.
- Inspect your results carefully and use appropriate tools available in Excel.
 - Use the Data Validation tool
 - Inspect and audit formulas

New Product Development Model

	Α	В	С	D	Е	F
1	Moore Pharmaceuticals					
2						
3	Data					
4						
5	Market size	2,000,000				
6	Unit (monthly Rx) revenue	\$ 130.00				
7	Unit (monthly Rx) cost	\$ 40.00				
8	Discount rate	9%				
9						
10	Project Costs					
11	R&D	\$ 700,000,000				
12	Clinical Trials	\$ 150,000,000				
13	Total Project Costs	\$ 850,000,000				
14	_					
15	Model					
16						
17	Year	1	2	3	4	
18	Market growth factor		3.00%	3.00%	3.00%	3.009
19	Market size	2,000,000	2,060,000	2,121,800	2,185,454	2,251,018
20	Market share growth rate		20.00%	20.00%	20.00%	20.009
21	Market share	8.00%	9.60%	11.52%	13.82%	16.599
22	Sales	160,000	197,760	244,431	302,117	373,417
23						
24	Annual Revenue	\$ 249,600,000	\$ 308,505,600	\$ 381,312,922	\$ 471,302,771	\$ 582,530,225
25	Annual Costs	\$ 76,800,000	\$ 94,924,800	\$ 117,327,053	\$ 145,016,237	\$ 179,240,069
26	Profit	\$ 172,800,000	\$ 213,580,800	\$ 263,985,869	\$ 326,286,534	\$ 403,290,156
27	Cumulative Net Profit	\$(677,200,000)	\$(463,619,200)	\$(199,633,331)	\$ 126,653,203	\$ 529,943,358
28						
29	Net Present Value	\$ 185,404,860				

New Product Development Model Formulas

	Α	В	С	D	E	F
1	Moore Pharmaceuticals					
2						
3	Data					
4						
5	Market size	2000000				
6	Unit (monthly Rx) revenue	130				
7	Unit (monthly Rx) cost	40				
8	Discount rate	0.09				
9						
10	Project Costs					
11	R&D	700000000				
12	Clinical Trials	150000000				
13	Total Project Costs	=B11+B12				
14	_					
15	Model					
16						
17	Year	1	2	3	4	5
18	Market growth factor		0.03	0.03	0.03	0.03
19	Market size	=B5	=B19*(1+C18)	=C19*(1+D18)	=D19*(1+E18)	=E19*(1+F18)
20	Market share growth rate		0.2	0.2	0.2	0.2
21	Market share	0.08	=B21*(1+C20)	=C21*(1+D20)	=D21*(1+E20)	=E21*(1+F20)
22	Sales	=B19*B21	=C19*C21	=D19*D21	=E19*E21	=F19*F21
23						
24	Annual Revenue	=B22*\$B\$6*12	=C22*\$B\$6*12	=D22*\$B\$6*12	=E22*\$B\$6*12	=F22*\$B\$6*12
25	Annual Costs	=B22*\$B\$7*12	=C22*\$B\$7*12	=D22*\$B\$7*12	=E22*\$B\$7*12	=F22*\$B\$7*12
26	Profit	=B24-B25	=C24-C25	=D24-D25	=E24-E25	=F24-F25
27	Cumulative Net Profit	=B26-B13	=B27+C26	=C27+D26	=D27+E26	=E27+F26
28						
29	Net Present Value	=NPV(B8,B26:F26)-B13				



Single Period Purchase Decisions (Newsvendor Model)

- C = purchase cost
- R = sale price
- S = salvage value
- D = demand during a single period
- Q = quantity purchased
- Net profit = R * Quantity Sold + S * Surplus Quantity - C * Q

Newsvendor Model Spreadsheet

	А	В
1	Newsvendor Model	
2		
3	Data	
4		
5	Selling price	18
6	Cost	12
7	Discount price	9
8		
9	Model	
10		
11	Demand	41
12	Purchase Quantity	44
13		
14	Quantity Sold	=MIN(B11,B12)
15	Surplus Quantity	=MAX(0,B12-B11)
16		
17	Profit	=B14*B5+B15*B7-B12*B6

	А		В	С	D	Е	F	G	Н		J	K	L	M	N
1	Newsvendor Model				Demand					Purchase	Quantity				
2					\$ 237.00	40	41	42	43	44	45	46	47	48	49
3	Data				40	\$ 240.00	\$ 237.00	\$ 234.00	\$ 231.00	\$ 228.00	\$ 225.00	\$ 222.00	\$ 219.00	\$ 216.00	\$ 213.00
4					41	\$ 240.00	\$ 246.00	\$ 243.00	\$ 240.00	\$ 237.00	\$ 234.00	\$ 231.00	\$ 228.00	\$ 225.00	\$ 222.00
5	Selling price	\$	18.00		42	\$ 240.00	\$ 246.00	\$ 252.00	\$ 249.00	\$ 246.00	\$ 243.00	\$ 240.00	\$ 237.00	\$ 234.00	\$ 231.00
6	Cost	\$	12.00		43	\$ 240.00	\$ 246.00	\$ 252.00	\$ 258.00	\$ 255.00	\$ 252.00	\$ 249.00	\$ 246.00	\$ 243.00	\$ 240.00
7	Discount price	\$	9.00		44	\$ 240.00	\$ 246.00	\$ 252.00	\$ 258.00	\$ 264.00	\$ 261.00	\$ 258.00	\$ 255.00	\$ 252.00	\$ 249.00
8					45	\$ 240.00	\$ 246.00	\$ 252.00	\$ 258.00	\$ 264.00	\$ 270.00	\$ 267.00	\$ 264.00	\$ 261.00	\$ 258.00
9	Model				46	\$ 240.00	\$ 246.00	\$ 252.00	\$ 258.00	\$ 264.00	\$ 270.00	\$ 276.00	\$ 273.00	\$ 270.00	\$ 267.00
10					47	\$ 240.00	\$ 246.00	\$ 252.00	\$ 258.00	\$ 264.00	\$ 270.00	\$ 276.00	\$ 282.00	\$ 279.00	\$ 276.00
11	Demand		41		48	\$ 240.00	\$ 246.00	\$ 252.00	\$ 258.00	\$ 264.00	\$ 270.00	\$ 276.00	\$ 282.00	\$ 288.00	\$ 285.00
12	Purchase Quantity		44		49	\$ 240.00	\$ 246.00	\$ 252.00	\$ 258.00	\$ 264.00	\$ 270.00	\$ 276.00	\$ 282.00	\$ 288.00	\$ 294.00
13															
14	Quantity Sold		41												
15	Surplus Quantity		3												
16															
17	Profit	\$ 2	237.00												



Monte Carlo Simulation

The process of generating random values for uncertain inputs in a model, computing the output variables of interest, and repeating this process for many trials in order to understand the distribution of the output results.

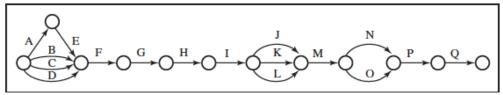
Overbooking Decisions

4	A	В
1	Hotel Overbooking Model	
2	_	
3	Data	
4		
5	Rooms available	300
6	Price	\$120
7	Overbooking cost	\$100
8		
9	Model	
10		
11	Reservation limit	300
12	Customer demand	290
13	Reservations made	290
14	Cancellations	15
15	Customer arrivals	275
16	Overbooked customers	0
17		
18	Net revenue	\$33,000

	A	В
1	Hotel Overbooking Model	
2		
3	Data	
4		
5	Rooms available	300
6	Price	120
7	Overbooking cost	100
8		
9	Model	
10		
11	Reservation limit	300
12	Customer demand	290
13	Reservations made	=MIN(B11,B12)
14	Cancellations	15
15	Customer arrivals	=B13-B14
16	Overbooked customers	=MAX(0,B15-B5)
17		
18	Net revenue	=MIN(B15,B5)*B6-B16*B7

Project Management

	Activity	Predecessors	Activity Time
Α	Select steering committee	_	15
В	Develop requirements list	_	50
C	Develop system size estimates	_	20
D	Determine prospective vendors	_	3
E	Form evaluation team	Α	7
F	Issue request for proposal	B,C,D,E	6
G	Bidders conference	F	1
Н	Review submissions	G	36
1	Select vendor short list	Н	6
J	Check vendor references	1	6
K	Vendor demonstrations	1	32
L	User site visit	I	4
M	Select vendor	J,K,L	3
N	Volume-sensitive test	M	15
0	Negotiate contracts	M	18
P	Cost-benefit analysis	N,O	2
Q	Obtain board of directors approval	Р	5



Spreadsheet Model

	A	В	С	D	E	F	G	Н
1			_	U		- 1	G	- 11
2	Becker Consulting Project Mana		ment woder					
3		A adicates	E-ulu	Caula	Latant	Latant		On Cuitinal
_	A -45-54-	Activity	Early	Early	Latest	Latest	ClI-	On Critical
4	Activity	Time	Start	Finish	Start	Finish	Slack	Path?
5	A	15.00	0.00	15.00	28.00	43.00	28.00	0
6	В	50.00	0.00	50.00	0.00	50.00	0.00	1
7	С	20.00	0.00	20.00	30.00	50.00	30.00	0
8	D	3.00	0.00	3.00	47.00	50.00	47.00	0
9	E	7.00	15.00	22.00	43.00	50.00	28.00	0
10	F	6.00	50.00	56.00	50.00	56.00	0.00	1
11	G	1.00	56.00	57.00	56.00	57.00	0.00	1
12	Н	36.00	57.00	93.00	57.00	93.00	0.00	1
13	I	6.00	93.00	99.00	93.00	99.00	0.00	1
14	J	6.00	99.00	105.00	125.00	131.00	26.00	0
15	K	32.00	99.00	131.00	99.00	131.00	0.00	1
16	L	4.00	99.00	103.00	127.00	131.00	28.00	0
17	M	3.00	131.00	134.00	131.00	134.00	0.00	1
18	N	15.00	134.00	149.00	137.00	152.00	3.00	0
19	0	18.00	134.00	152.00	134.00	152.00	0.00	1
20	Р	2.00	152.00	154.00	152.00	154.00	0.00	1
21	Q	5.00	154.00	159.00	154.00	159.00	0.00	1
22								
23		Project com	pletion time	159.00				

4

Model Formulas

	Α	В	С	D	Е	F	G	Н
1	Becker Consulting							
2								
3		Activity	Early	Early	Latest	Latest		On Critical
4	Activity	Time	Start	Finish	Start	Finish	Slack	Path?
5	Α	15	0	=C5+B5	=F5-B5	=E9	=F5-D5	=IF(G5<0.0001,1,0)
6	В	50	0	=C6+B6	=F6-B6	=E10	=F6-D6	=IF(G6<0.0001,1,0)
7	С	20	0	=C7+B7	=F7-B7	=E10	=F7-D7	=IF(G7<0.0001,1,0)
8	D	3	0	=C8+B8	=F8-B8	=E10	=F8-D8	=IF(G8<0.0001,1,0)
9	E	7	=D5	=C9+B9	=F9-B9	=E10	=F9-D9	=IF(G9<0.0001,1,0)
10	F	6	=MAX(D6,D7,D8,D9)	=C10+B10	=F10-B10	=E11	=F10-D10	=IF(G10<0.0001,1,0)
11	G	1	=D10	=C11+B11	=F11-B11	=E12	=F11-D11	=IF(G11<0.0001,1,0)
12	Н	36	=D11	=C12+B12	=F12-B12	=E13	=F12-D12	=IF(G12<0.0001,1,0)
13	I	6	=D12	=C13+B13	=F13-B13	=MIN(E14,E15,E16)	=F13-D13	=IF(G13<0.0001,1,0)
14	J	6	=D13	=C14+B14	=F14-B14	=E17	=F14-D14	=IF(G14<0.0001,1,0)
15	K	32	=D13	=C15+B15	=F15-B15	=E17	=F15-D15	=IF(G15<0.0001,1,0)
16	L	4	=D13	=C16+B16	=F16-B16	=E17	=F16-D16	=IF(G16<0.0001,1,0)
17	M	3	=MAX(D14,D15,D16)	=C17+B17	=F17-B17	=MIN(E18,E19)	=F17-D17	=IF(G17<0.0001,1,0)
18	N	15	=D17	=C18+B18	=F18-B18	=E20	=F18-D18	=IF(G18<0.0001,1,0)
19	0	18	=D17	=C19+B19	=F19-B19	=E20	=F19-D19	=IF(G19<0.0001,1,0)
20	Р	2	=MAX(D18,D19)	=C20+B20	=F20-B20	=E21	=F20-D20	=IF(G20<0.0001,1,0)
21	Q	5	=D20	=C21+B21	=F21-B21	=D21	=F21-D21	=IF(G21<0.0001,1,0)
22								·
23		Project completion time		=D21				



Model Assumptions, Complexity, and Realism

- All models reflect assumptions used by the modeler.
- Assumptions simplify models and make them easier to manipulate and solve
- Assumptions should be as realistic as necessary to make models useful but not overly complex
- Assumptions should be clearly stated and documented

Example: Retirement Planning

4	А		В	С	D	E
1	Retirement Plan Model					
2						
3	Data					
4	Retirement contribution (% of salary)		8%			
5	Employer match		35%			
6	Annual salary increase		4%			
7	Annual return on investment		8%			
8						
9	Model			Employee	Employer	
10	Age	Sal	ary	Contribution	Contribution	Balance
11	25		\$50,000	\$4,000	\$1,400	\$5,400
12	26		52,000	\$4,160	\$1,456	\$11,448
13	27		54,080	\$4,326	\$1,514	\$18,204
14	28	\$	56,243	\$4,499	\$1,575	\$25,735
15	29	\$	58,493	\$4,679	\$1,638	\$34,111
16	30	\$	60,833	\$4,867	\$1,703	\$43,410
17	31	\$	63,266	\$5,061	\$1,771	\$53,715
18	32	\$	65,797	\$5,264	\$1,842	\$65,119
19	33	\$	68,428	\$5,474	\$1,916	\$77,719
20	34	\$	71,166	\$5,693	\$1,993	\$91,622
21	35	\$	74,012	\$5,921	\$2,072	\$106,945
22	36		76,973	\$6,158	\$2,155	\$123,814
23	37		80,052	\$6,404	\$2,241	\$142,364
24	38		83,254	\$6,660	\$2,331	\$162,745
25	39	\$	86,584	\$6,927	\$2,424	\$185,115
26	40	,	90,047	\$7,204	\$2,521	\$209,650
27	41	-	93,649	\$7,492	\$2,622	\$236,536
28	42		97,395	\$7,792	\$2,727	\$265,977
29	43	-	101,291	\$8,103	\$2,836	\$298,195
30	44		105,342	\$8,427	\$2,950	\$333,428
31	45		109,556	\$8,764	\$3,068	\$371,934
32	46		113,938	\$9,115	\$3,190	\$413,994
33	47		118,496	\$9,480	\$3,318	\$459,911
34	48	\$	123,236	\$9,859	\$3,451	\$510,013
35	49	\$	128,165	\$10,253	\$3,589	\$564,656
36	50	\$	133,292	\$10,663	\$3,732	\$624,224

	А	В	С	D	E
1	Retirement Plan Model				
2					
3	Data				
4	Retirement contribution (% of salary)	0.08			
5	Employer match	0.35			
6	Annual salary increase	0.04			
7	Annual return on investment	0.08			
8					
9	Model		Employee	Employer	
10	Age	Salary	Contribution	Contribution	Balance
11	25	50000	=B11*\$B\$4	=\$B\$5*C11	=C11+D11
12	26	= B11*(1+\$B\$6)	=B12*\$B\$4	=\$B\$5*C12	=E11*(1+\$B\$7) + C12+D12
13	27	= B12*(1+\$B\$6)	=B13*\$B\$4	=\$B\$5*C13	=E12*(1+\$B\$7) + C13+D13
14	28	= B13*(1+\$B\$6)	=B14*\$B\$4	=\$B\$5*C14	=E13*(1+\$B\$7) + C14+D14