

# Machine Learning Algorithms

# Common ML Algorithms

Linear Regression

Logistic Regression

Support Vector Machine

Decision Tree

K-Nearest Neighbor

Neural Network

$$\hat{f}(X)$$

## The Prediction

$$\hat{y} = \hat{f}(X)$$

output                              input

**Regression**

continuous

$$\hat{y} = 66.5$$

## **Classification**

probability

$$\hat{y} = .85$$

# **Classification**

prediction

$$\hat{y} = 1$$

# **Classification**

prediction

$$\hat{y} = 0$$

# Linear Regression

equation of a line

$$y = mx + b$$

equation of a line

$$y = mx + b$$

linear regression

$$y = \beta_0 + \beta_1 x$$

# Simple Linear Regression

Input

$x_1$

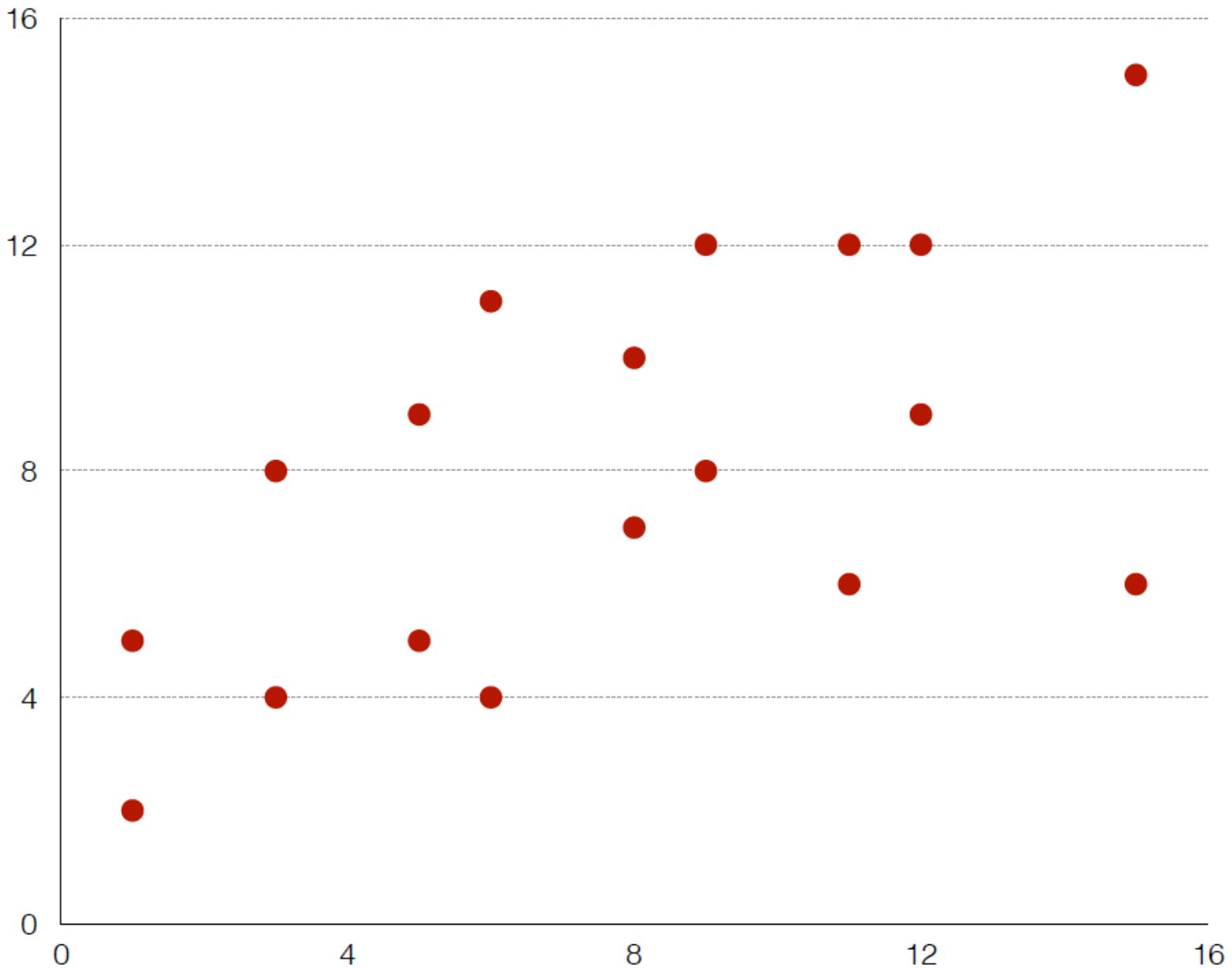
learned coefficients  
(weights)

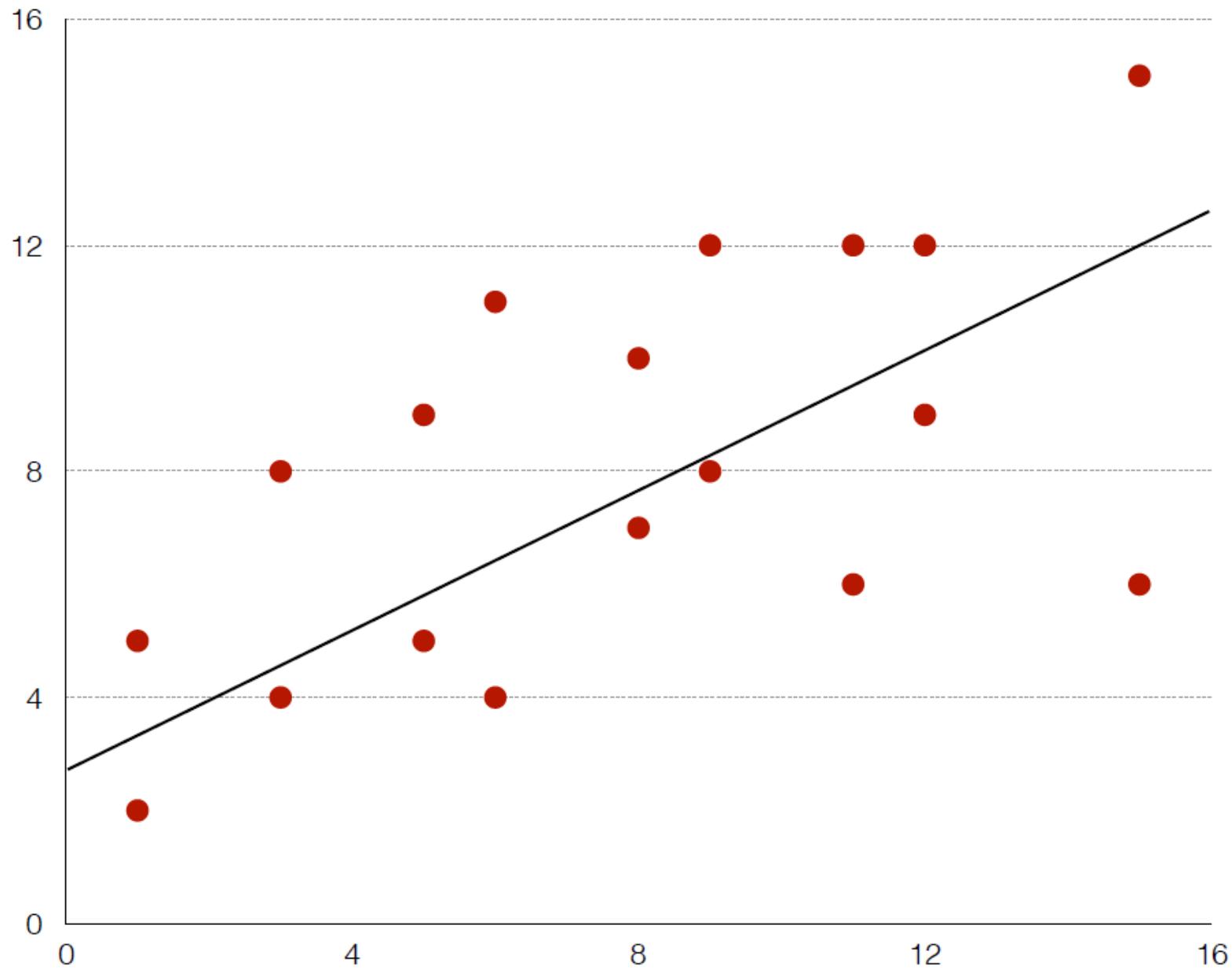
$\beta_0, \beta_1$

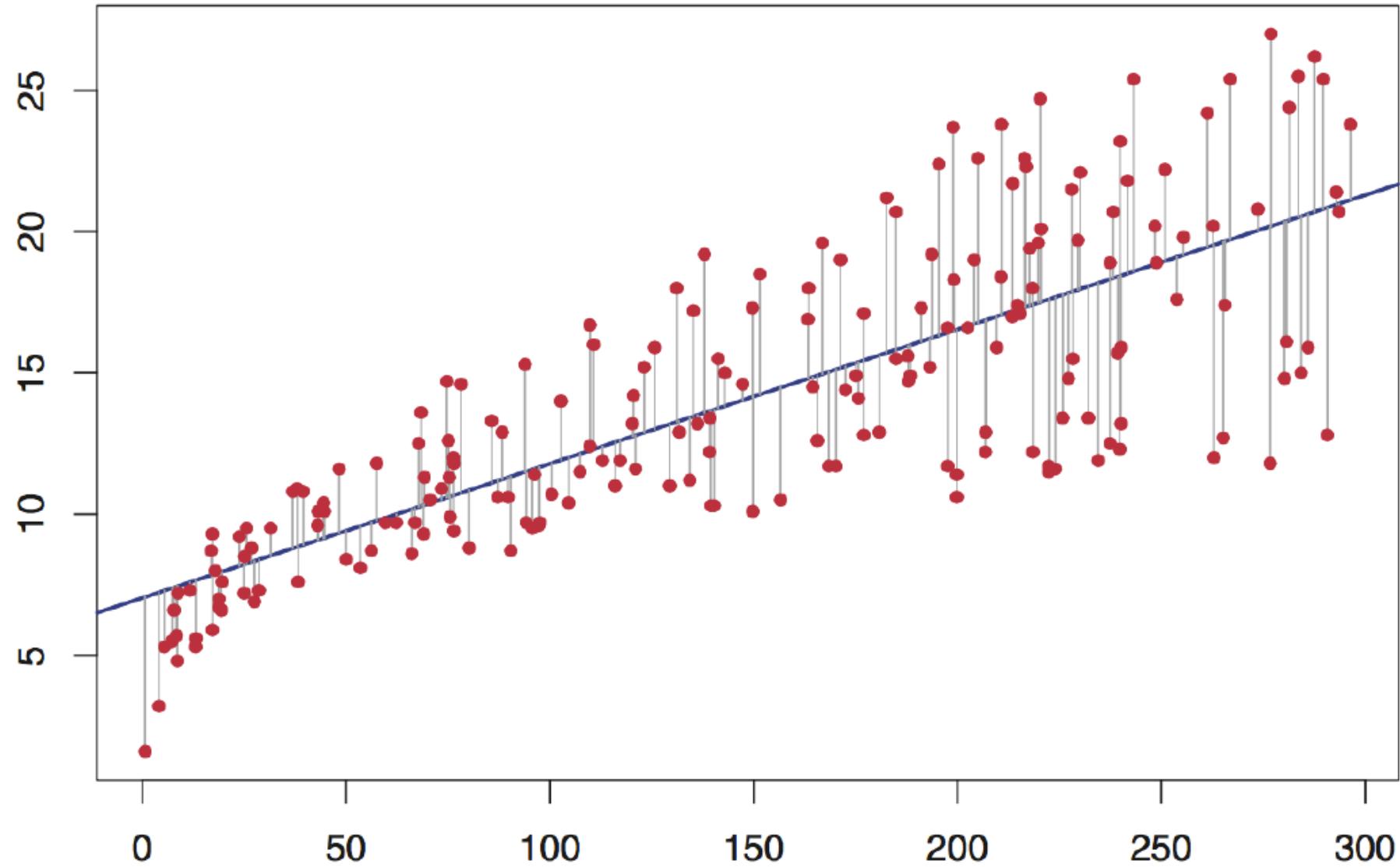
output

$y$

$$y = \beta_0 + \beta_1 x$$







# Weekly Hours Spent Studying

Gender	Number of Classes	Social Accounts	Hours Studying
Male	2	1	7.5
Male	4	3	12.25
Female	4	3	12.75
Female	3	4	7.75
Female	4	2	14
Male	2	3	5.75
Female	5	1	18.25

# Weekly Hours Spent Studying

Gender	Number of Classes	Social Accounts	Hours Studying
0	2	1	7.5
0	4	3	12.25
1	4	3	12.75
1	3	4	7.75
1	4	2	14
0	2	3	5.75
0	5	1	18.25

# Weekly Hours Spent Studying

Features →

Gender	Number of Classes	Social Accounts	Hours Studying
0	2	1	7.5
0	4	3	12.25
1	4	3	12.75
1	3	4	7.75
1	4	2	14
0	2	3	5.75
0	5	1	18.25

# Weekly Hours Spent Studying

Gender	Number of Classes	Social Accounts	Hours Studying	← Target (y)
0	2	1	7.5	
0	4	3	12.25	
1	4	3	12.75	
1	3	4	7.75	
1	4	2	14	
0	2	3	5.75	
0	5	1	18.25	

# Weekly Hours Spent Studying

Gender	Number of Classes	Social Accounts	Hours Studying
0	2	1	7.5
0	4	3	12.25
1	4	3	12.75
1	3	4	7.75
1	4	2	14
0	2	3	5.75
0	5	1	18.25

# Weekly Hours Spent Studying

Gender	Number of Classes	Social Accounts	Hours Studying
0	2	1	7.5
0	4	3	12.25
1	4	3	12.75
1	3	4	7.75
1	4	2	14
0	2	3	5.75
0	5	1	18.25

# Weekly Hours Spent Studying

0	2	1	7.5
0	4	3	12.25
1	4	3	12.75
1	3	4	7.75
1	4	2	14
0	2	3	5.75
0	5	1	18.25

# Weekly Hours Spent Studying

0	2	1	7.5
0	4	3	12.25
1	4	3	12.75
<b>X =</b>	1	3	<b>y = 7.75</b>
1	4	2	14
0	2	3	5.75
0	5	1	18.25

## Multiple Linear Regression

$$\text{Hrs. Studying} = 1.63 + 3.51\mathbf{x_1} + .25\mathbf{x_2} - 1.08\mathbf{x_3}$$

$\mathbf{x_1}$  = number of classes

$\mathbf{x_2}$  = gender (m=0, female=1)

$\mathbf{x_3}$  = number of social accounts

## Multiple Linear Regression

$$\text{Apps Sold} = 46.55 + 35.03\text{x}_1 + 7.11\text{x}_2 + 52.48\text{x}_3$$

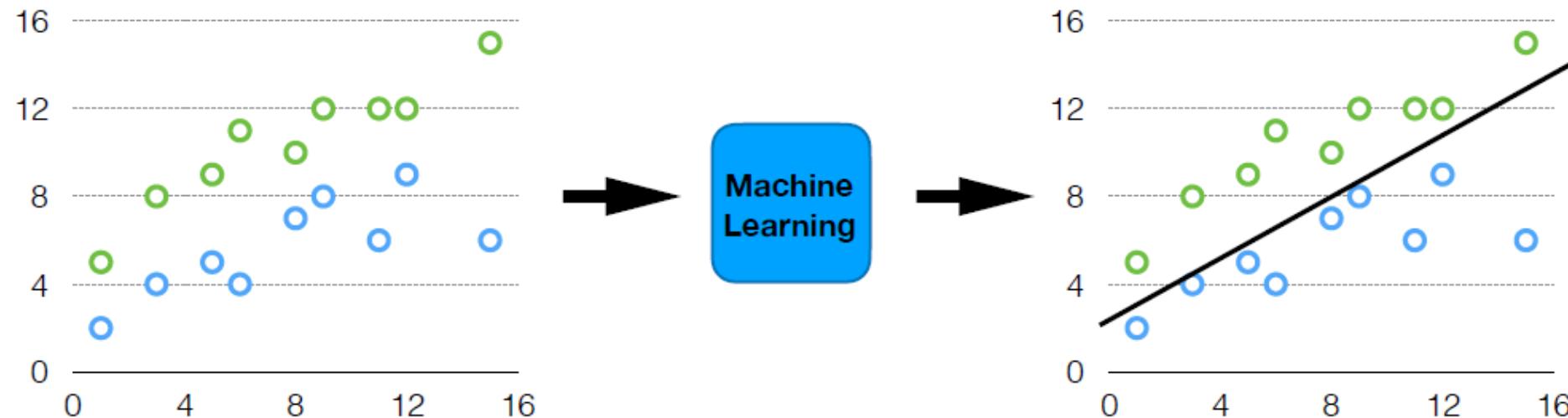
**x<sub>1</sub>** = per \$100 of advertising

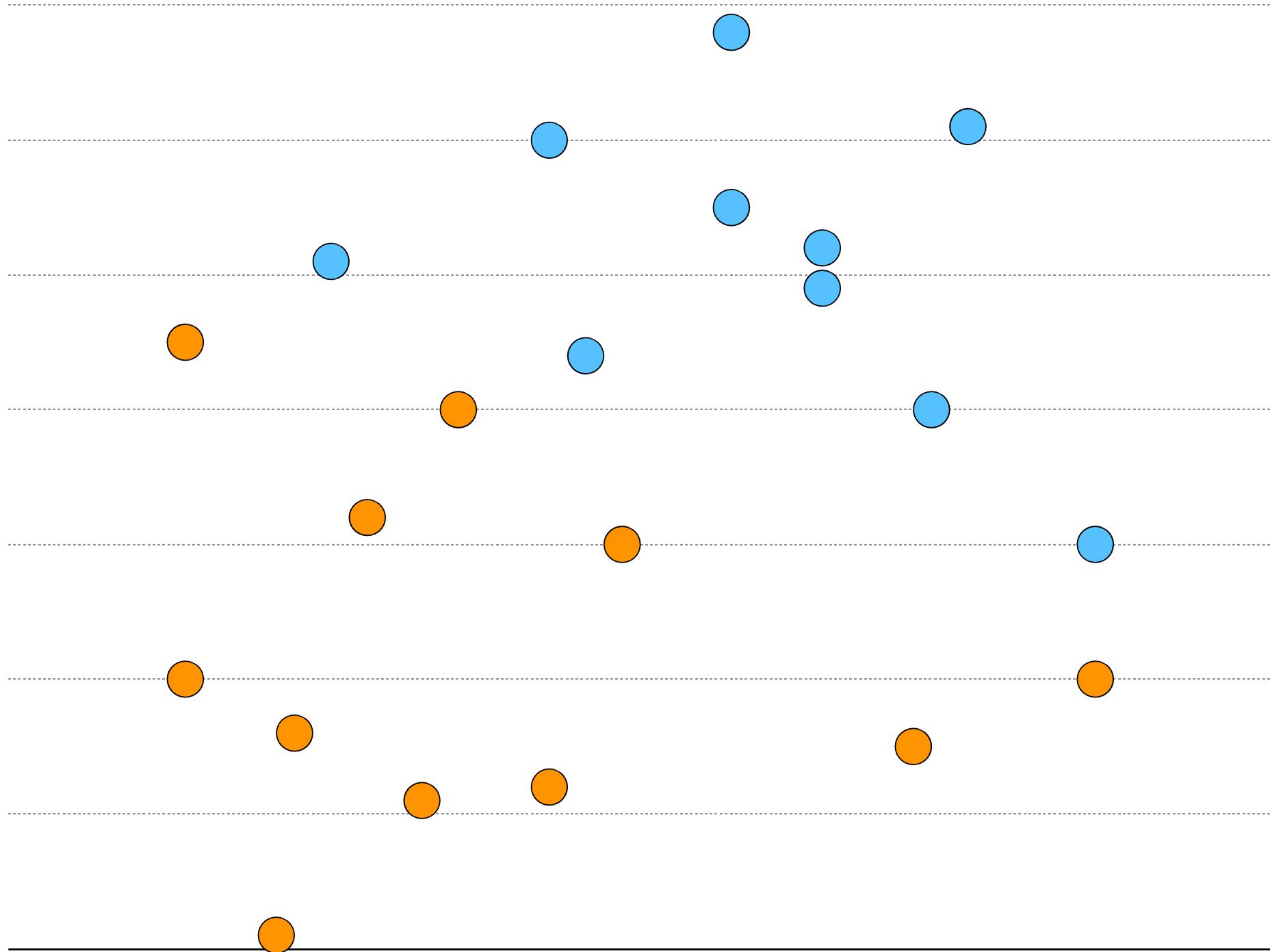
**x<sub>2</sub>** = public talks

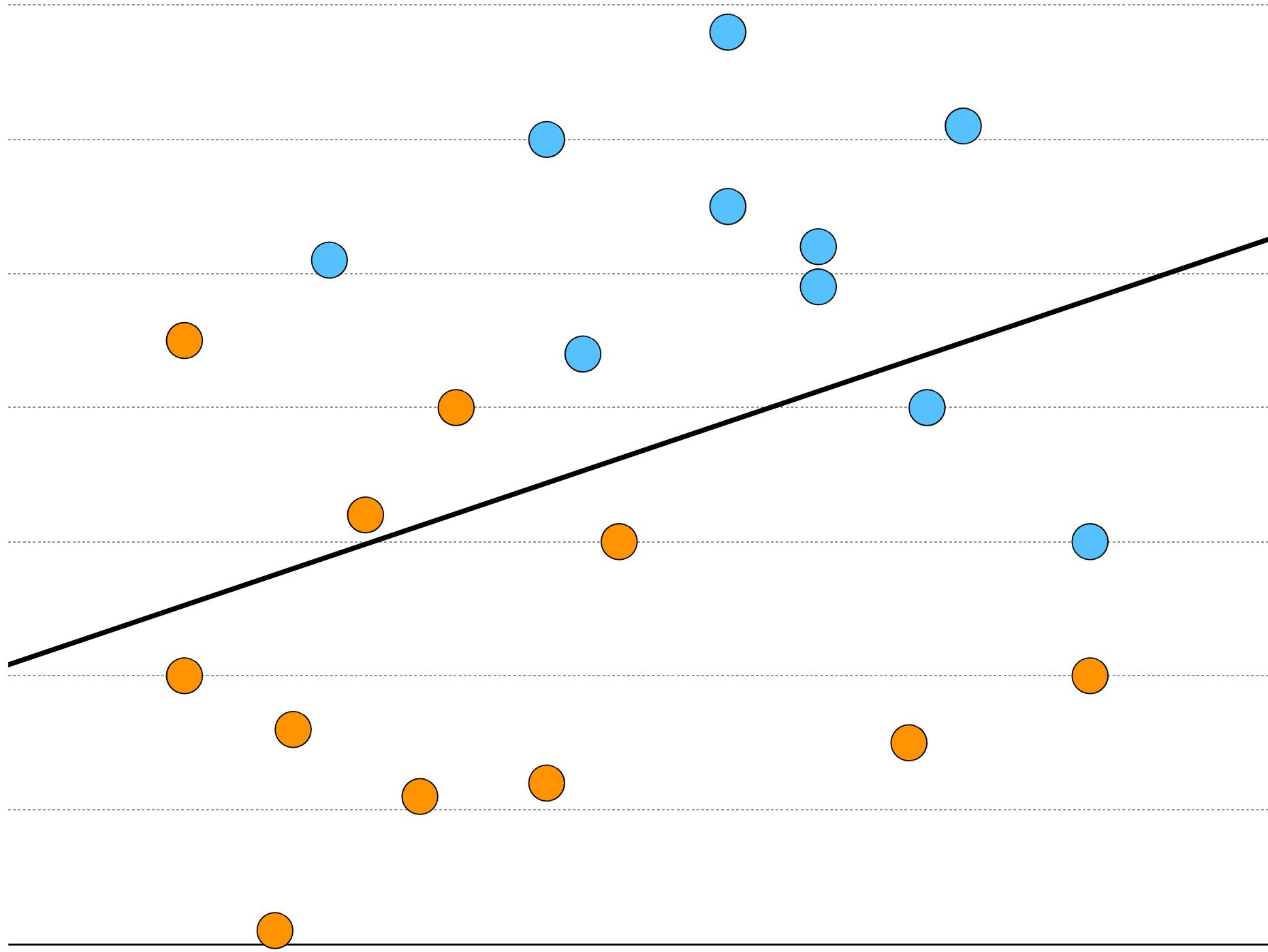
**x<sub>3</sub>** = targeted podcasts

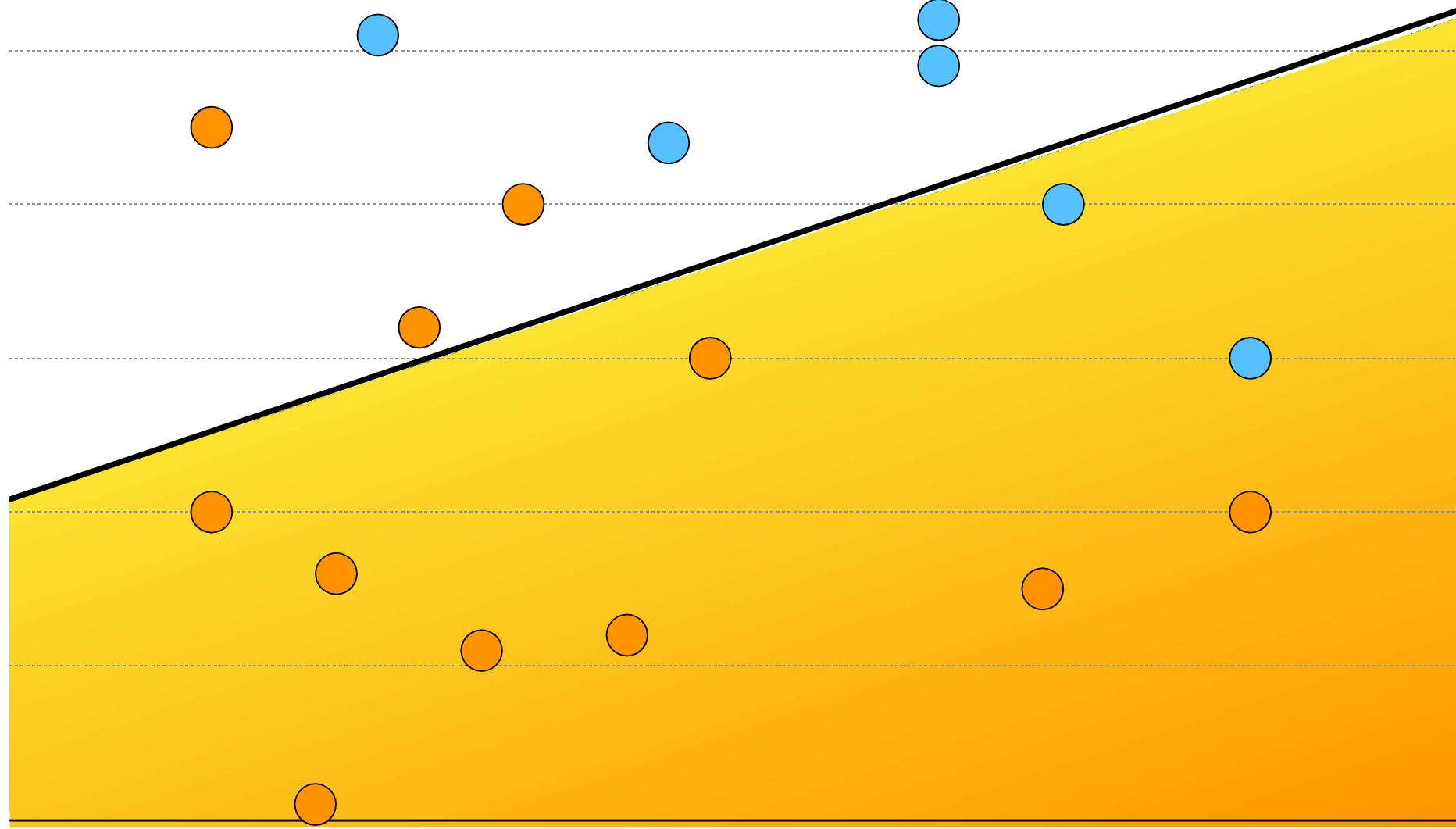
# Classification

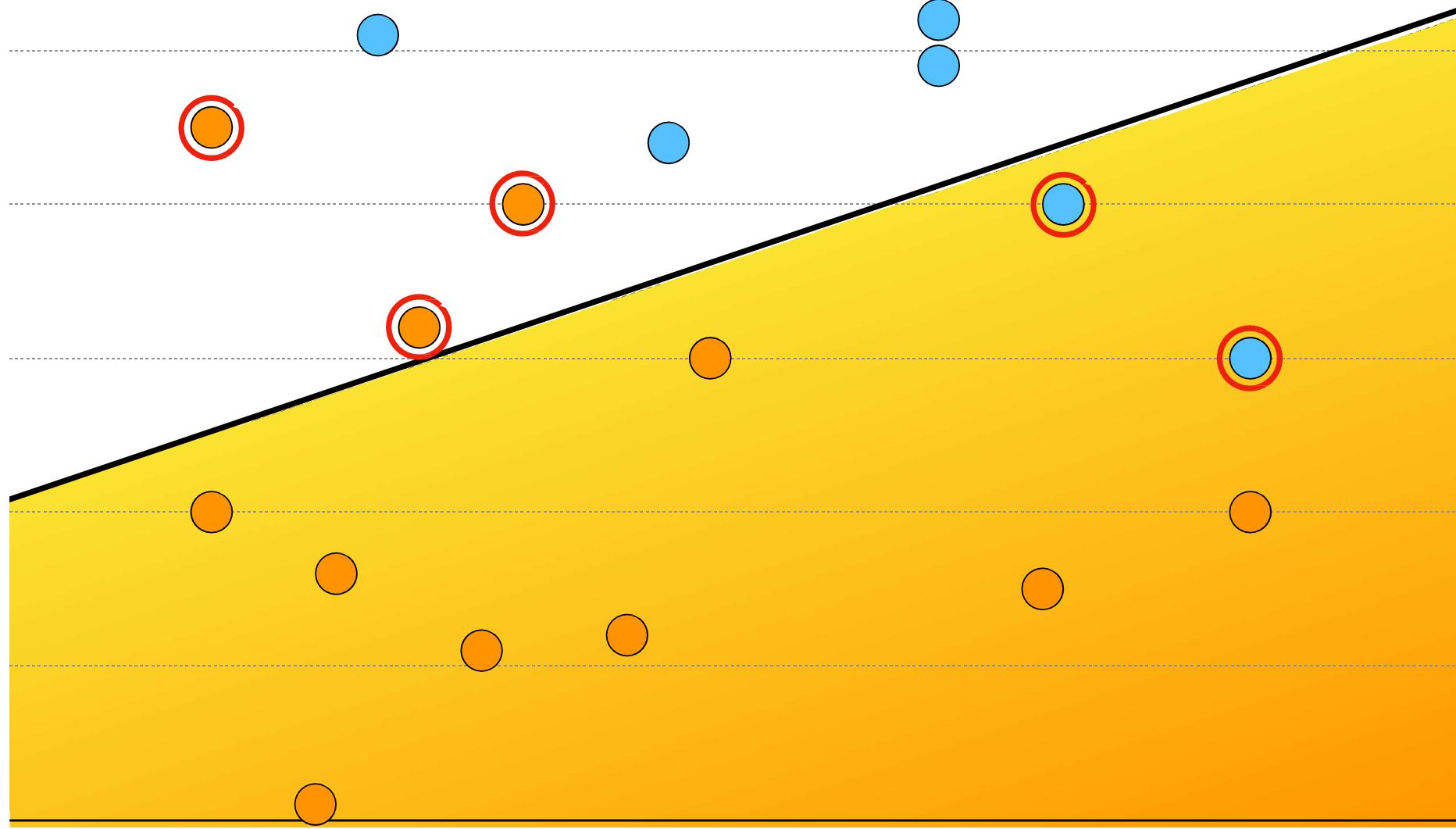
# What is a classifier?



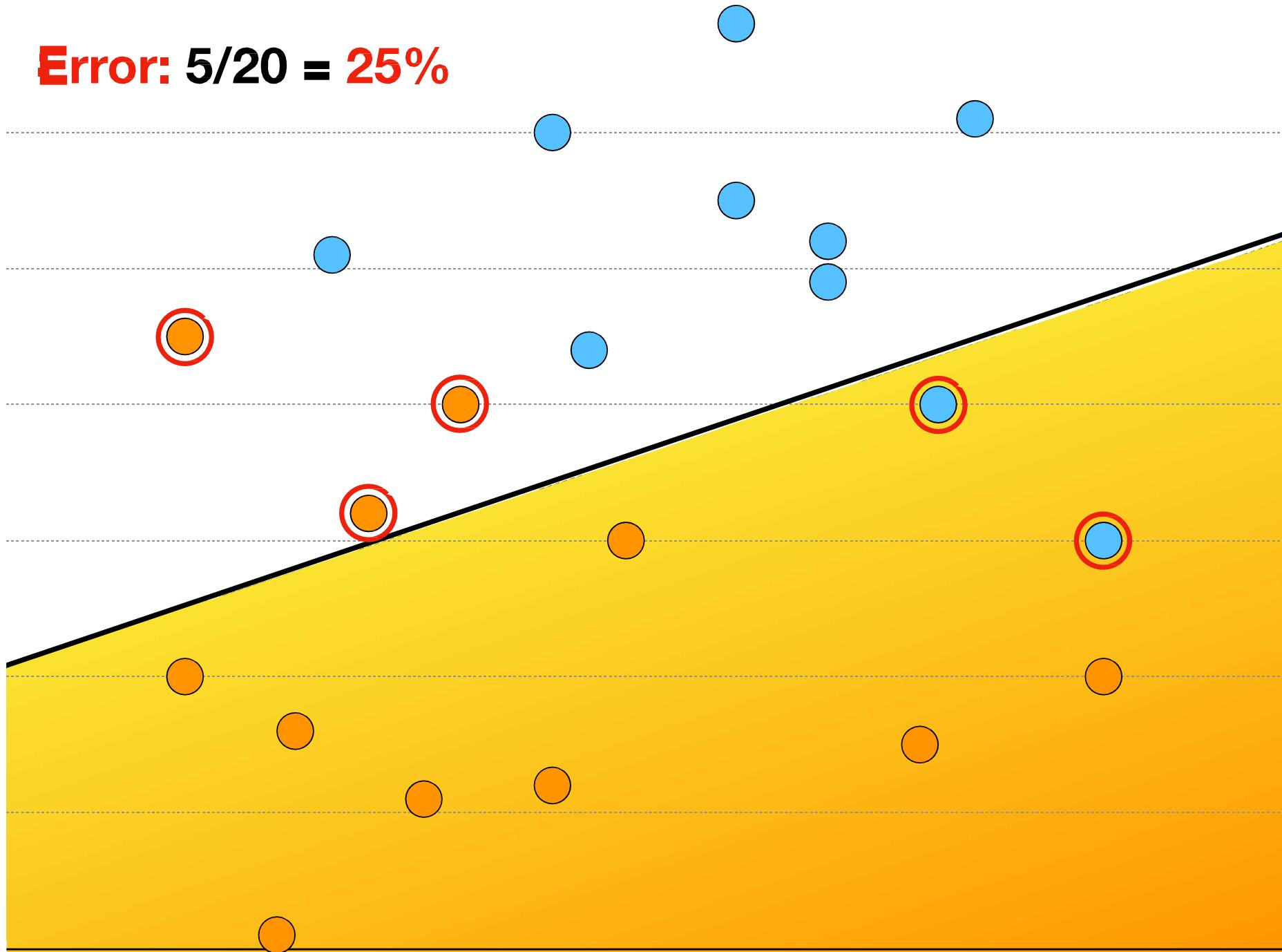


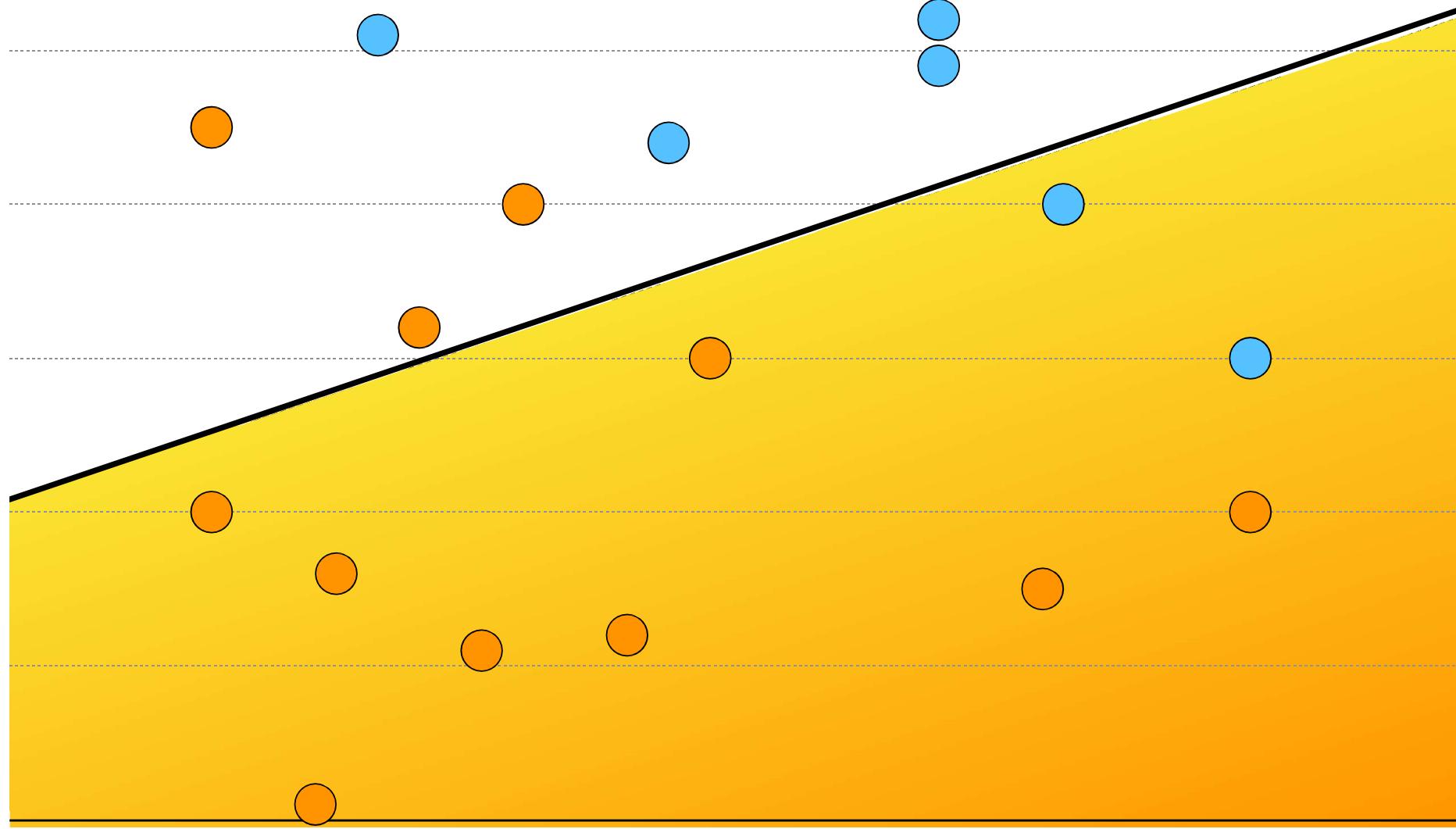


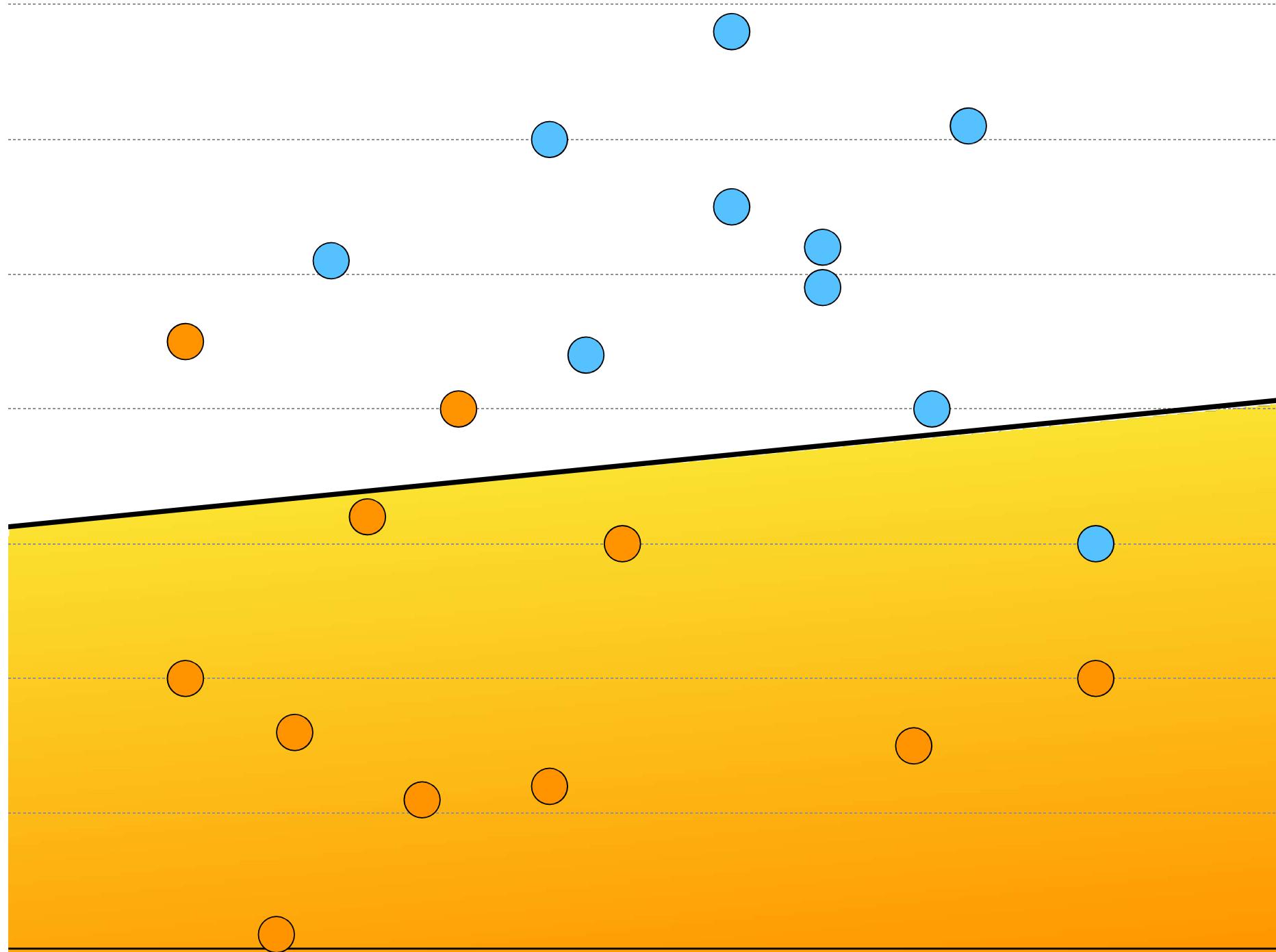


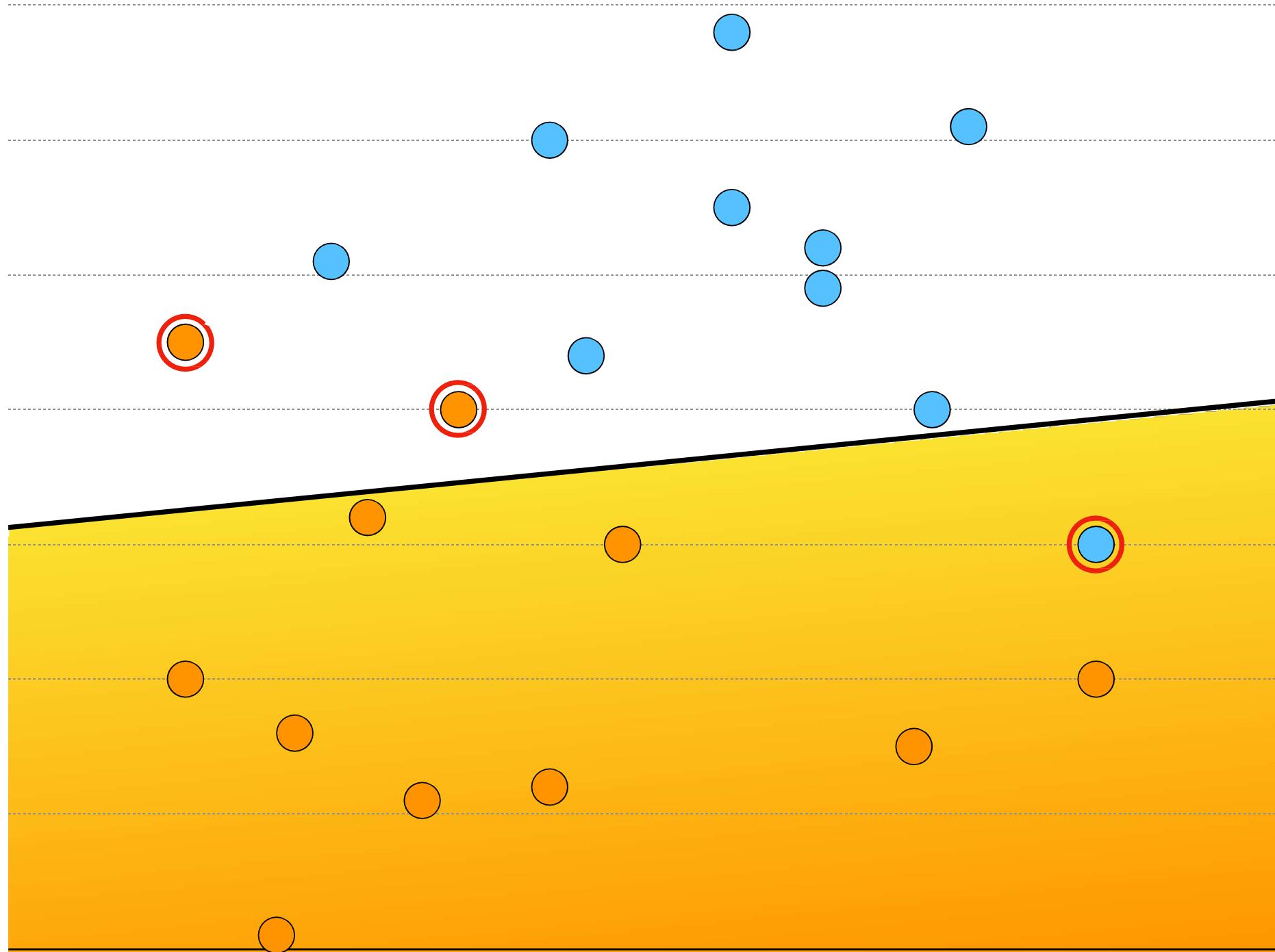


**Error: 5/20 = 25%**

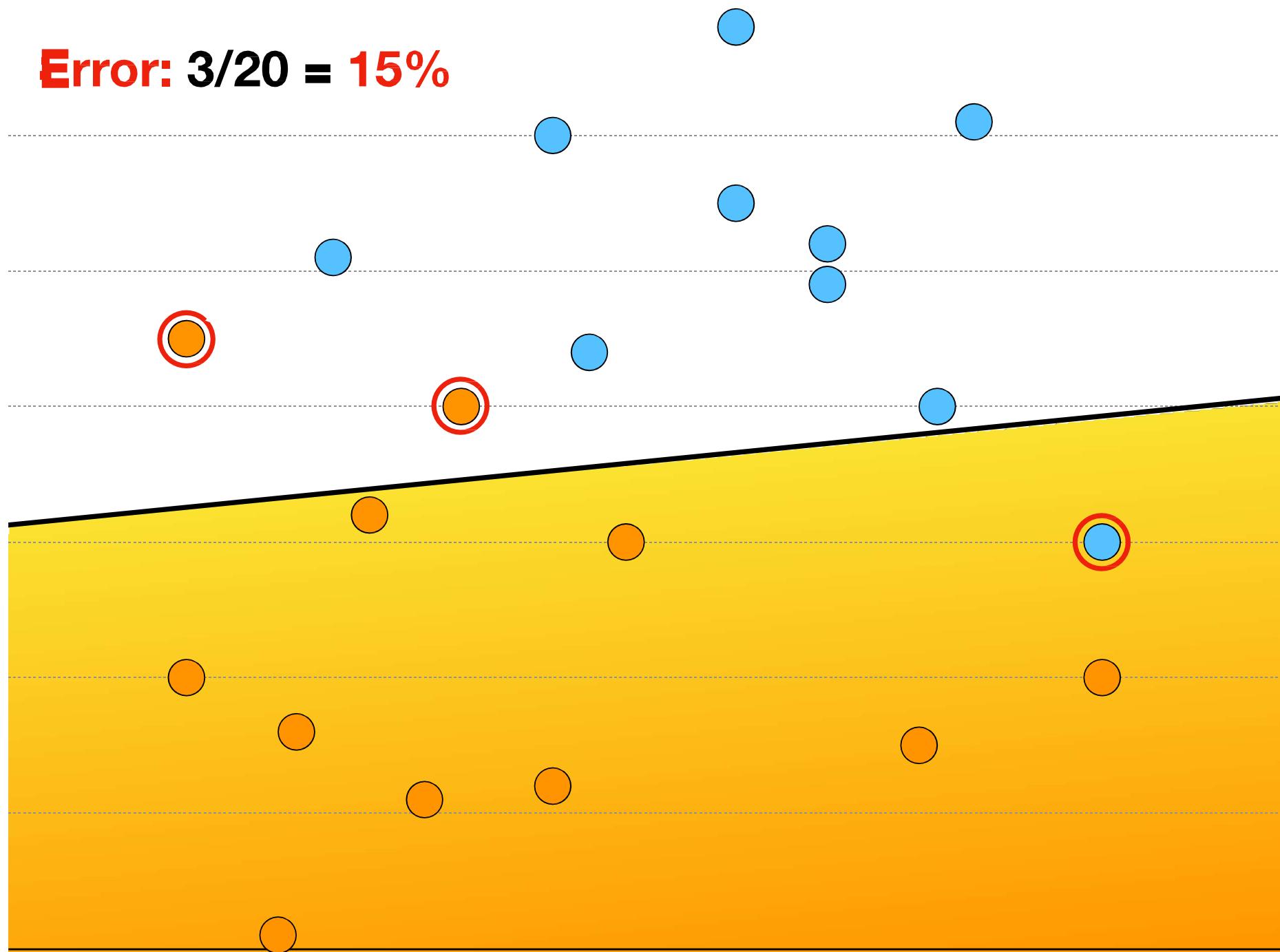


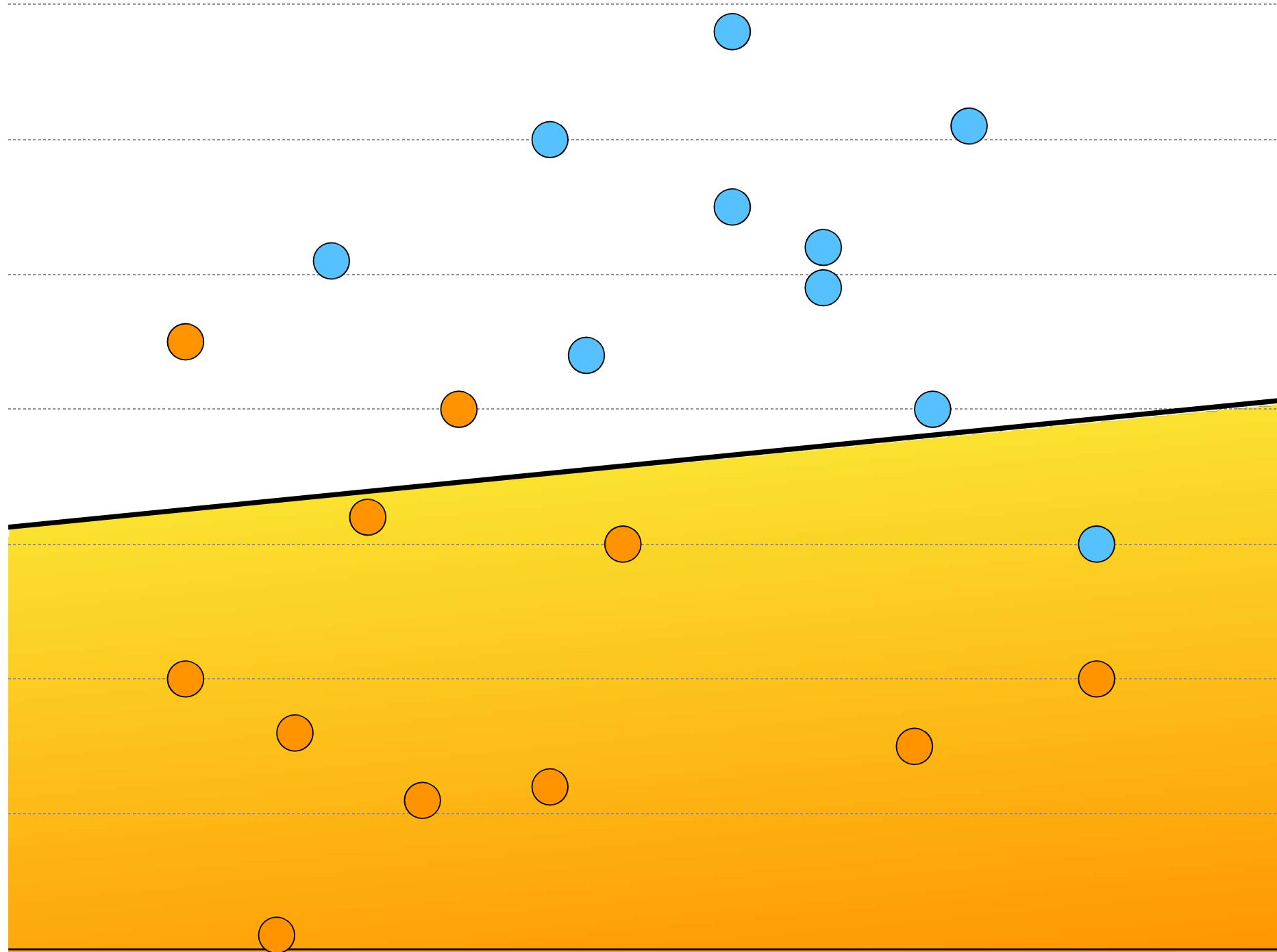


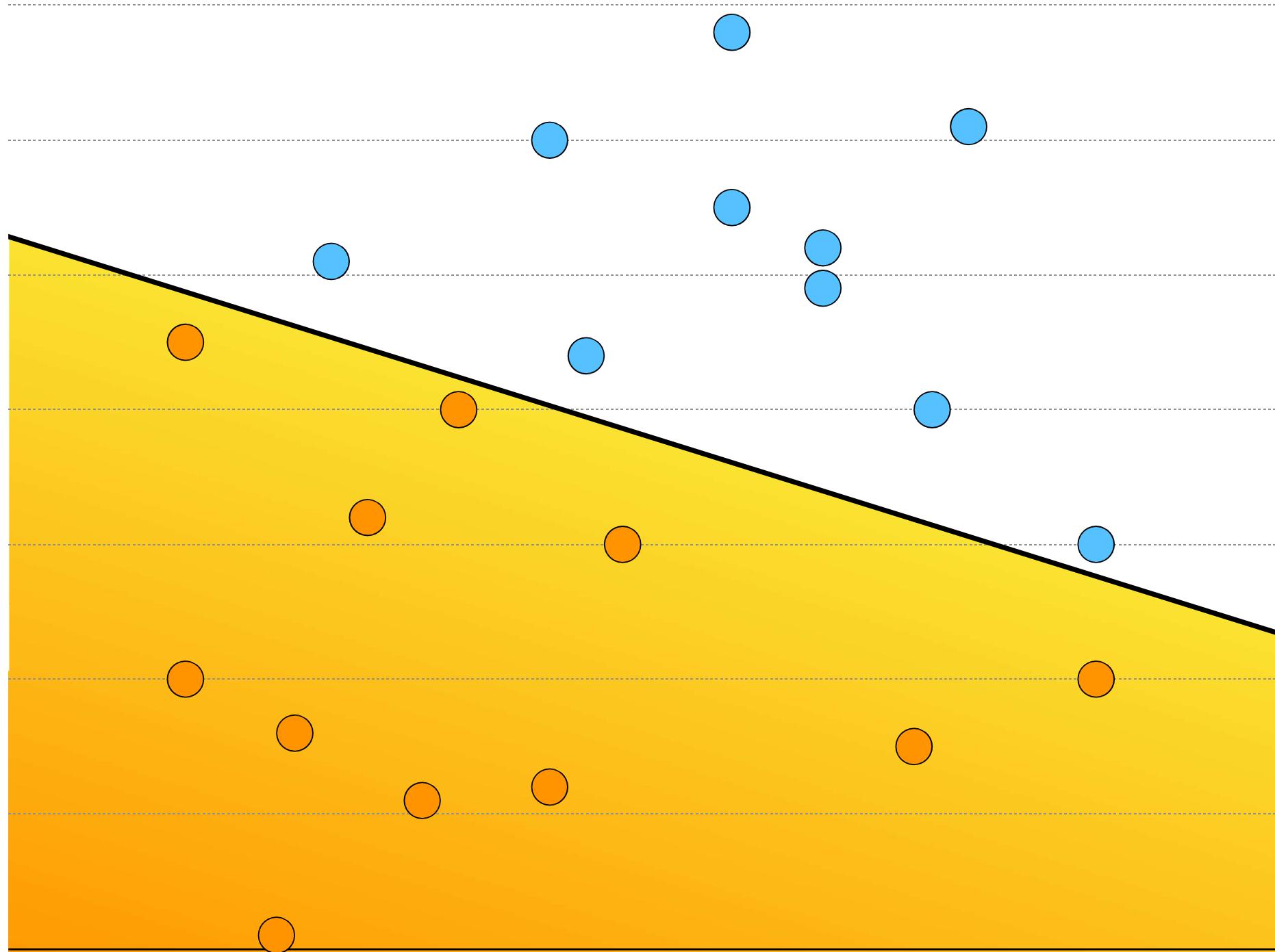




**Error:  $3/20 = 15\%$**

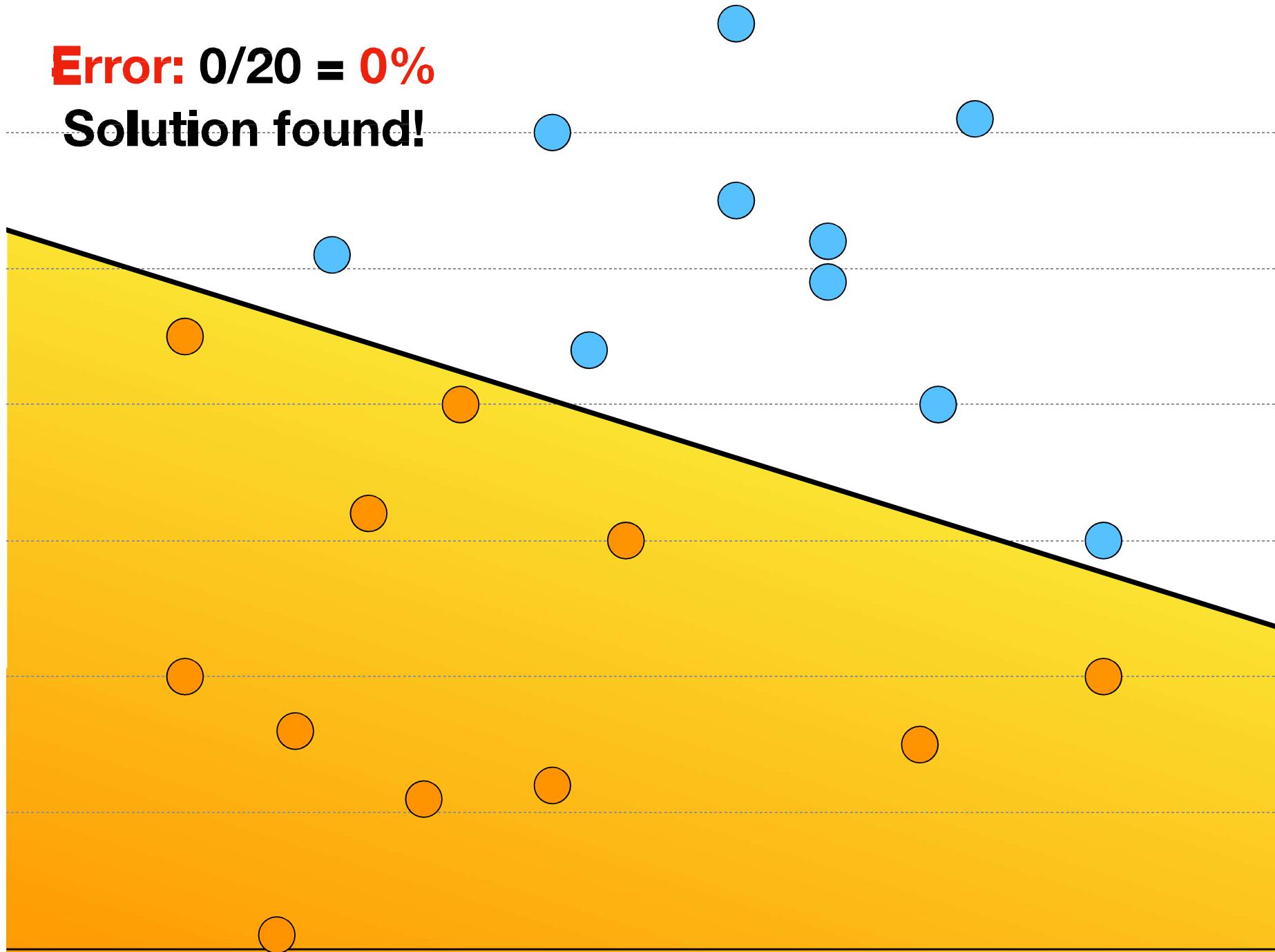






**Error: 0/20 = 0%**

**Solution found!**



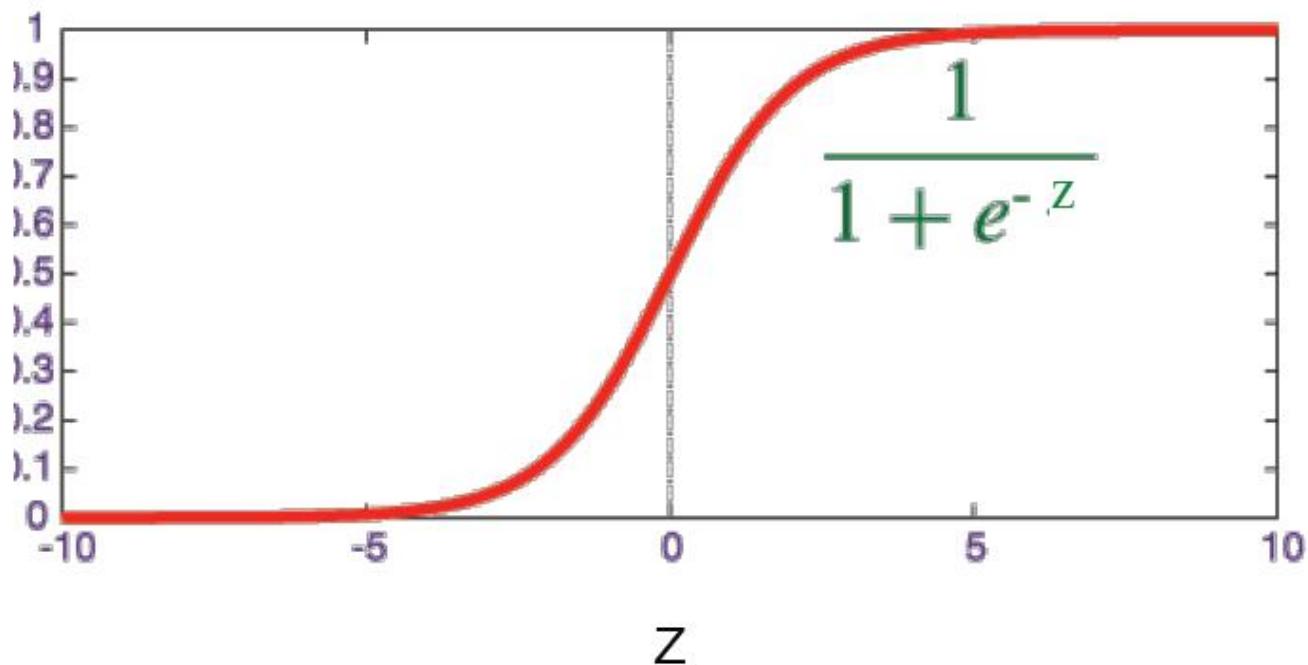
# Logistic Regression

# Logistic Regression

intermediate step

$$z = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3$$

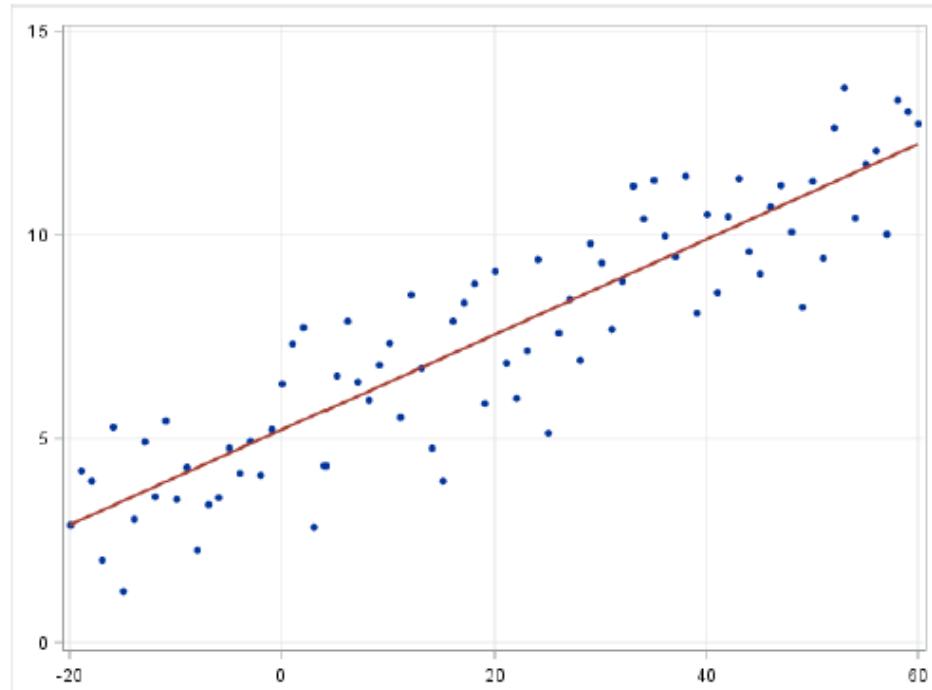
## Logistic (Sigmoid) Function



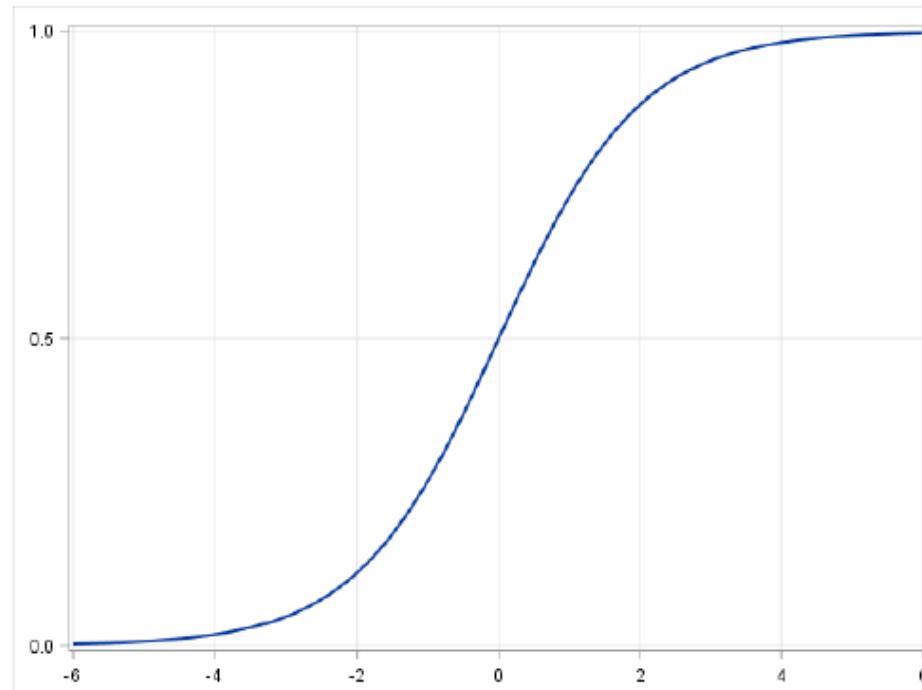
# Logistic Regression

$$\hat{f}(X) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 X_1 + \beta_2 X_2)}}$$

## Linear Regression



## Logistic Regression



positive class = 1

negative class = 0

predict 1 when  $\beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 \geq 0$

predict 0 when  $\beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 < 0$

positive class = 1

negative class = 0

if probability  $\geq 0.5$ : predict 1

if probability  $< 0.5$ : predict 0

# U.S. Pay Gap



## U.S. pay gap: All full-time working men vs. women

\$1



82¢



# U.S. pay gap:

## All full-time working men and women



## The highest paid occupations for women

Chief executives

Pharmacists

Lawyers

Computer and information systems managers

Physicians and surgeons

Nurse practitioners

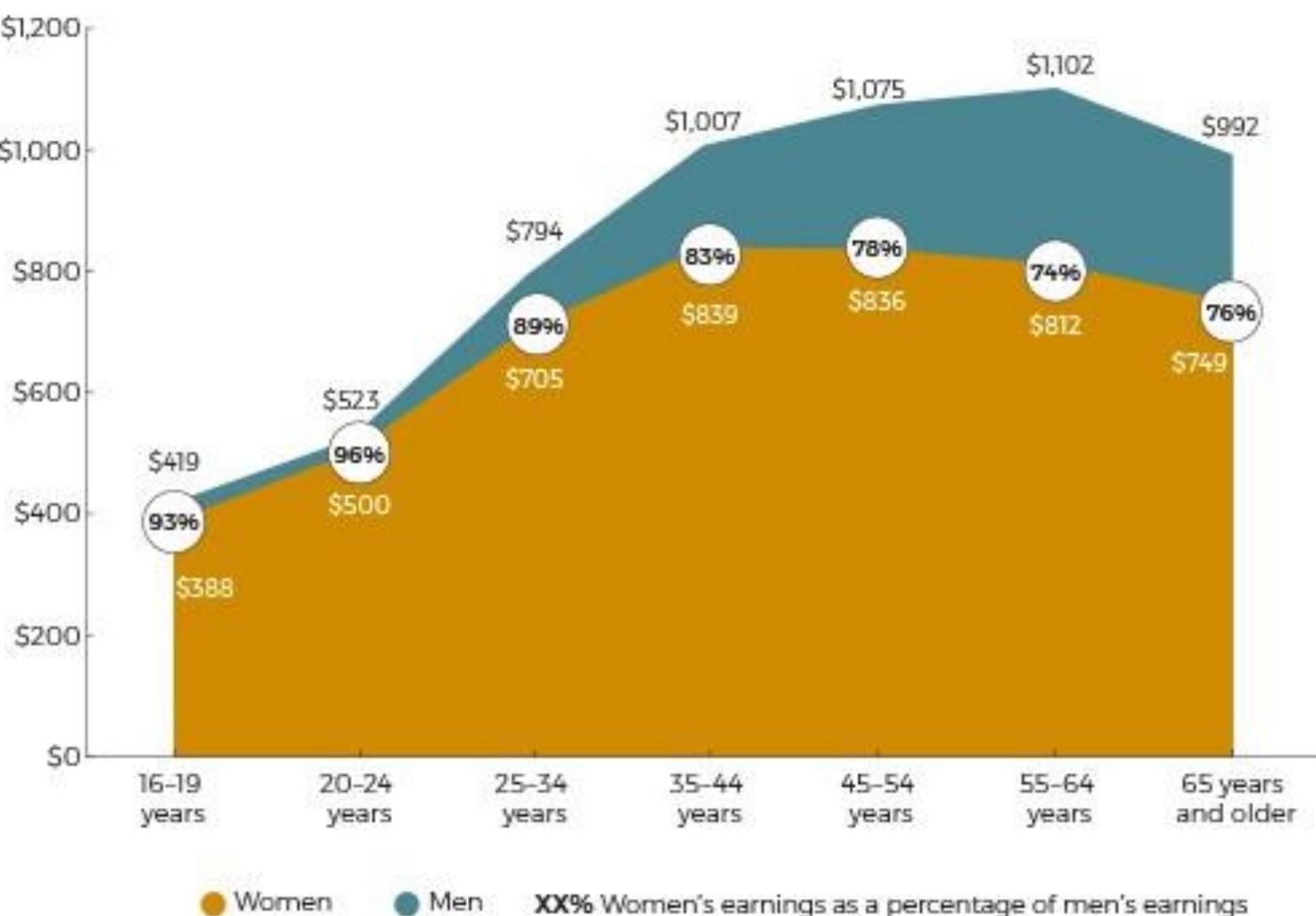
Engineers

Software developers

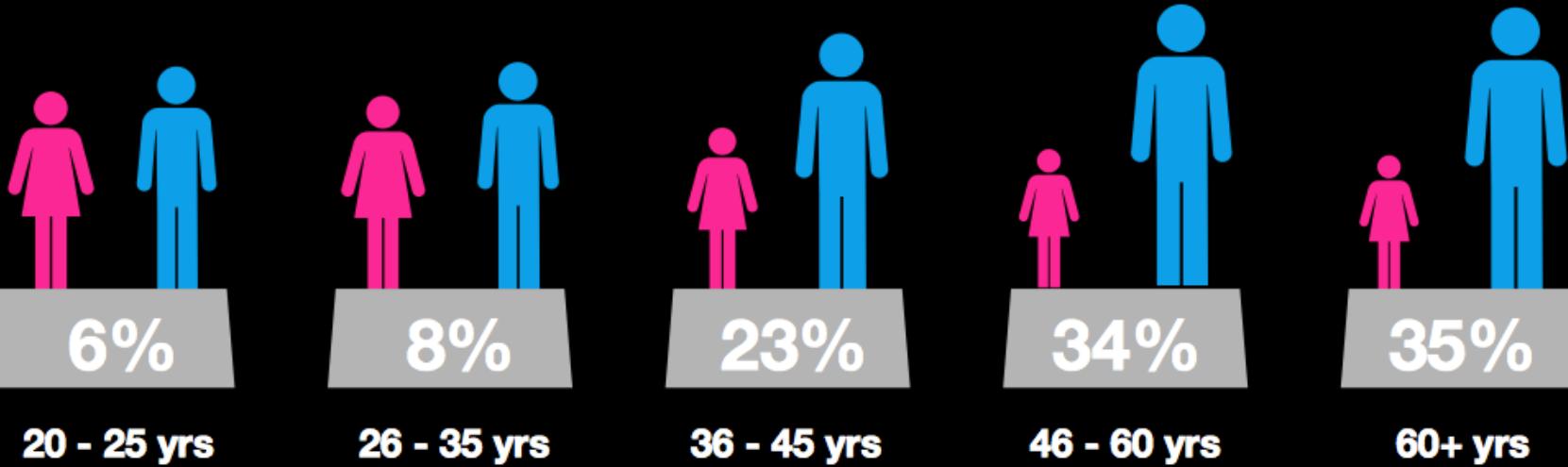
Management analysts

Operations research analysts

## Median Weekly Earnings, by Age and Gender, 2016

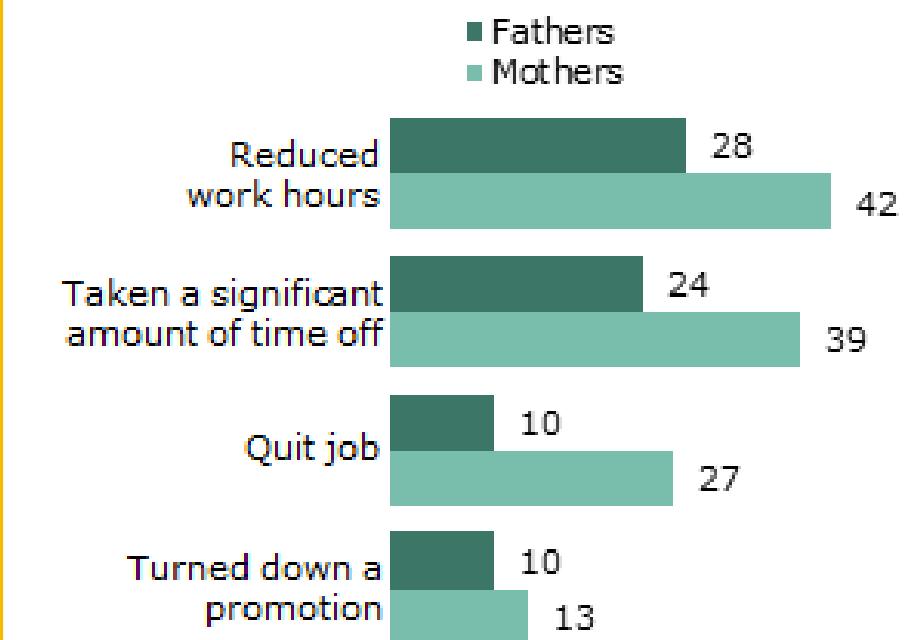


The gap pay gap increases with age.



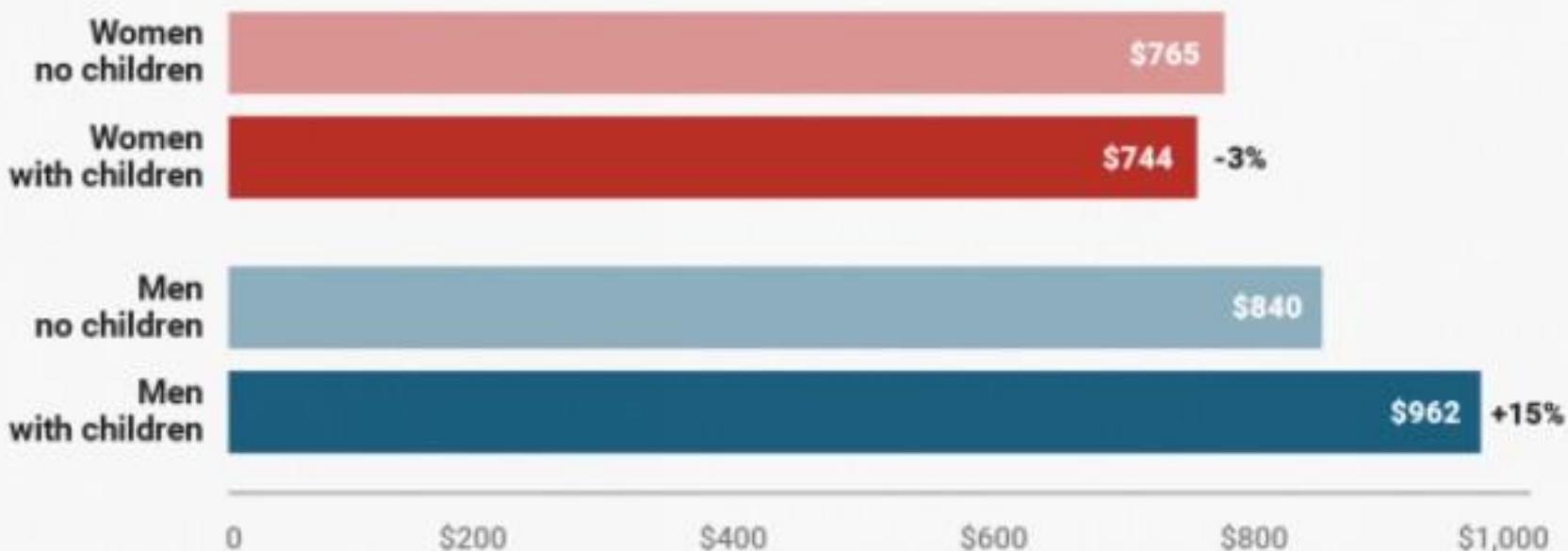
## Mothers, More than Fathers, Experience Career Interruptions

*% saying they have ... in order to care for a child or family member*



Notes: Based on those who have ever worked, "Fathers" and "mothers" include those with children of any age, including adult children (n=1,254).

## WEEKLY EARNINGS FOR WOMEN WITH/WITHOUT CHILDREN



Data

Race 1	Race 2	Race 3	Race 4	Top Paying	Age	Children	Pay Gap
1	0	0	0	0	49	1	1
0	0	0	0	1	43	0	0
0	0	1	0	0	37	0	0
0	1	0	0	0	28	1	1
0	1	0	0	0	25	1	0
0	0	0	1	0	23	0	0
0	0	1	0	0	48	0	1
0	0	0	0	1	33	0	1
1	0	0	0	0	39	1	1
0	0	0	1	0	47	1	0

# **Pay Gap Decision Boundary**

**predict 1 when:**

$$\beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 + \beta_4x_4 + \beta_5x_5 + \beta_6x_6 + \beta_7x_7 + \beta_8x_8 >= 0$$

**predict 0 when:**

$$\beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 + \beta_4x_4 + \beta_5x_5 + \beta_6x_6 + \beta_7x_7 + \beta_8x_8 < 0$$

# **Decision Boundary**

$$\text{Pay Gap} = \beta_0 + \beta_1 x_1 + \beta_2 x_2$$

# **Decision Boundary**

$$\text{Pay Gap} = -6 + 1x_1 + 1x_2$$

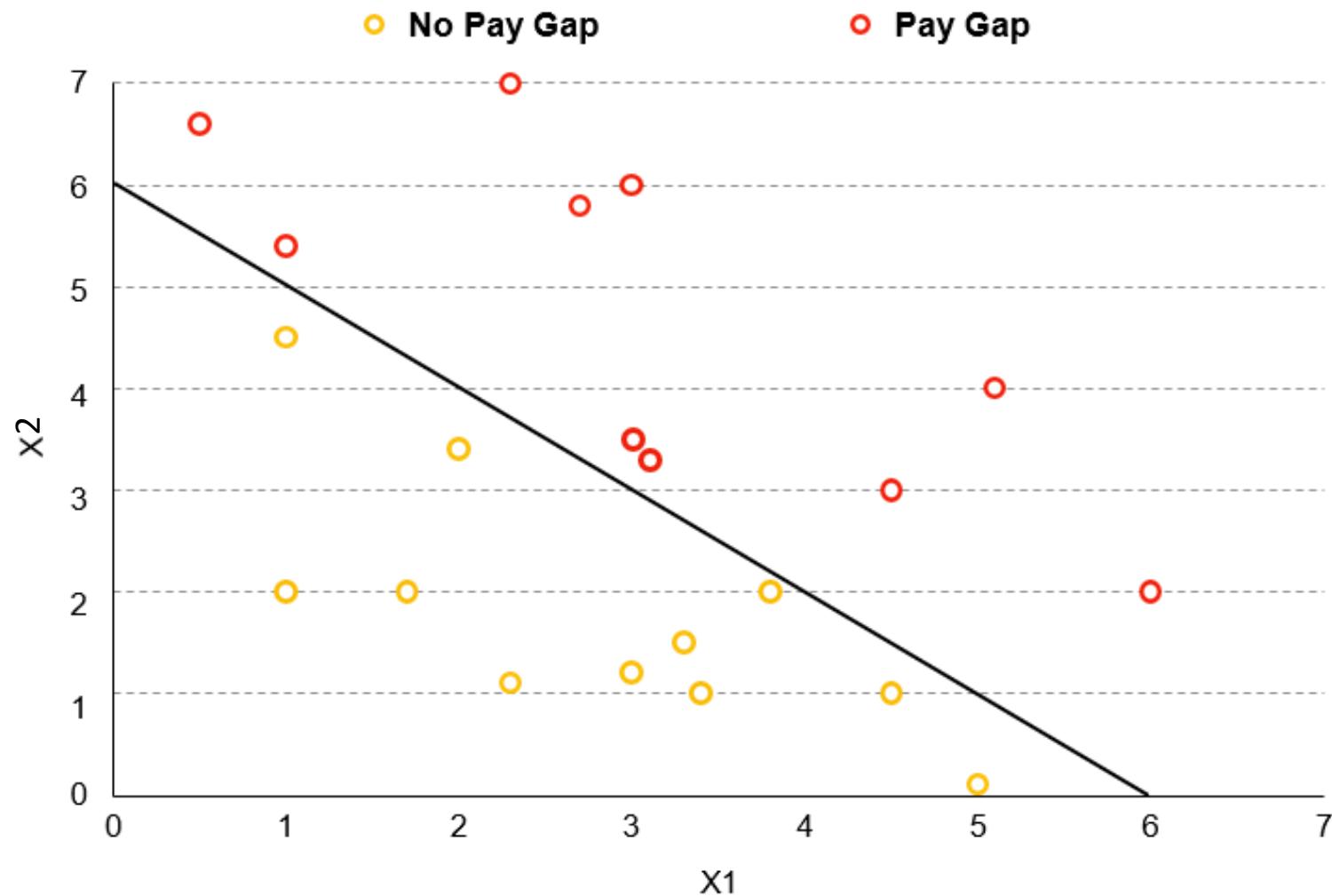
## Decision Boundary

$$\text{Pay Gap} = -6 + 1x_1 + 1x_2$$

predict 1 when  $-6 + 1x_1 + 1x_2 \geq 0$

predict 0 when  $-6 + 1x_1 + 1x_2 < 0$

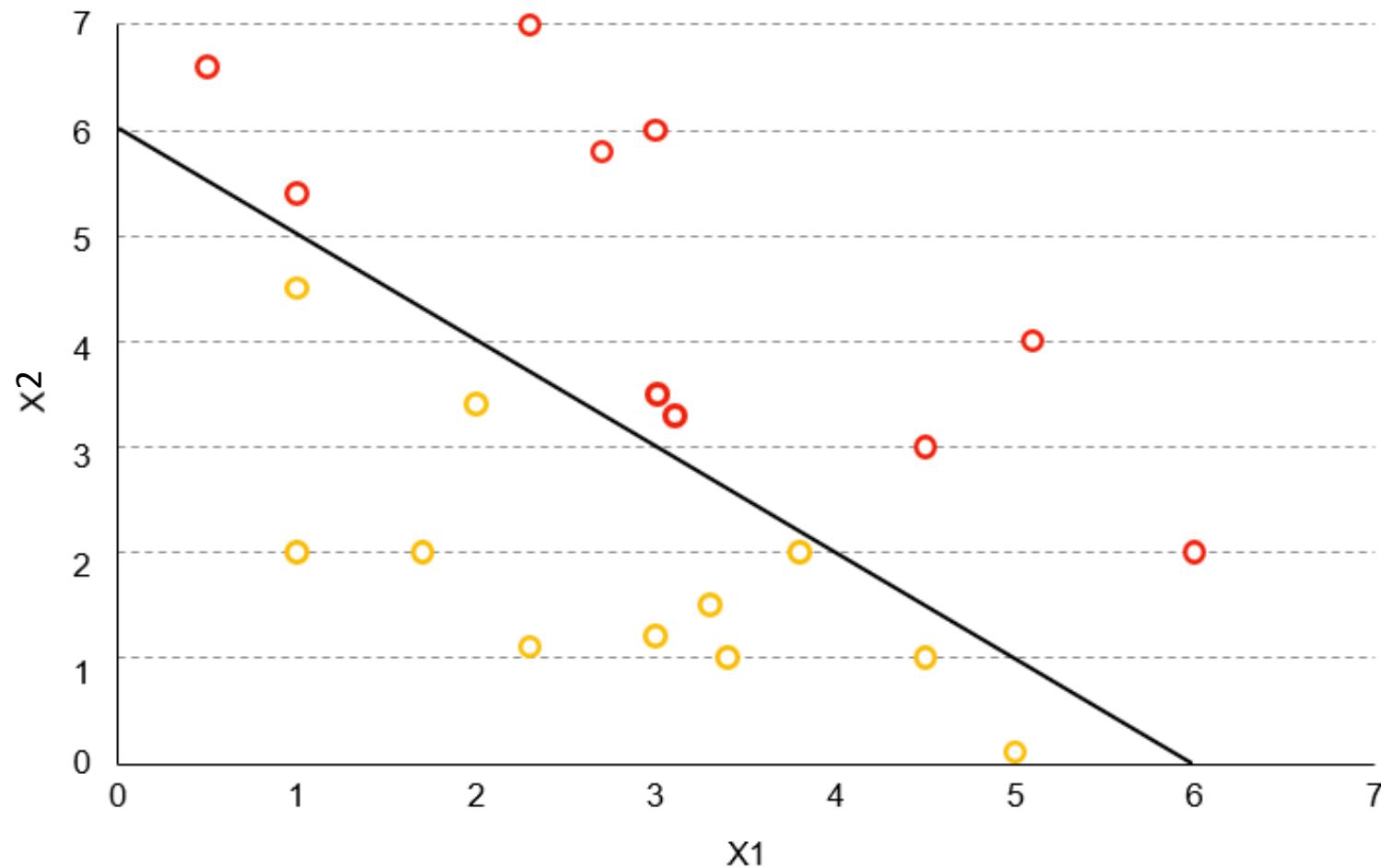
# Pay Gap Decision Boundary



$$\hat{f}(X) = \frac{1}{1 + e^{(-6 + 1x_1 + 1x_2)}}$$

○ No Pay Gap

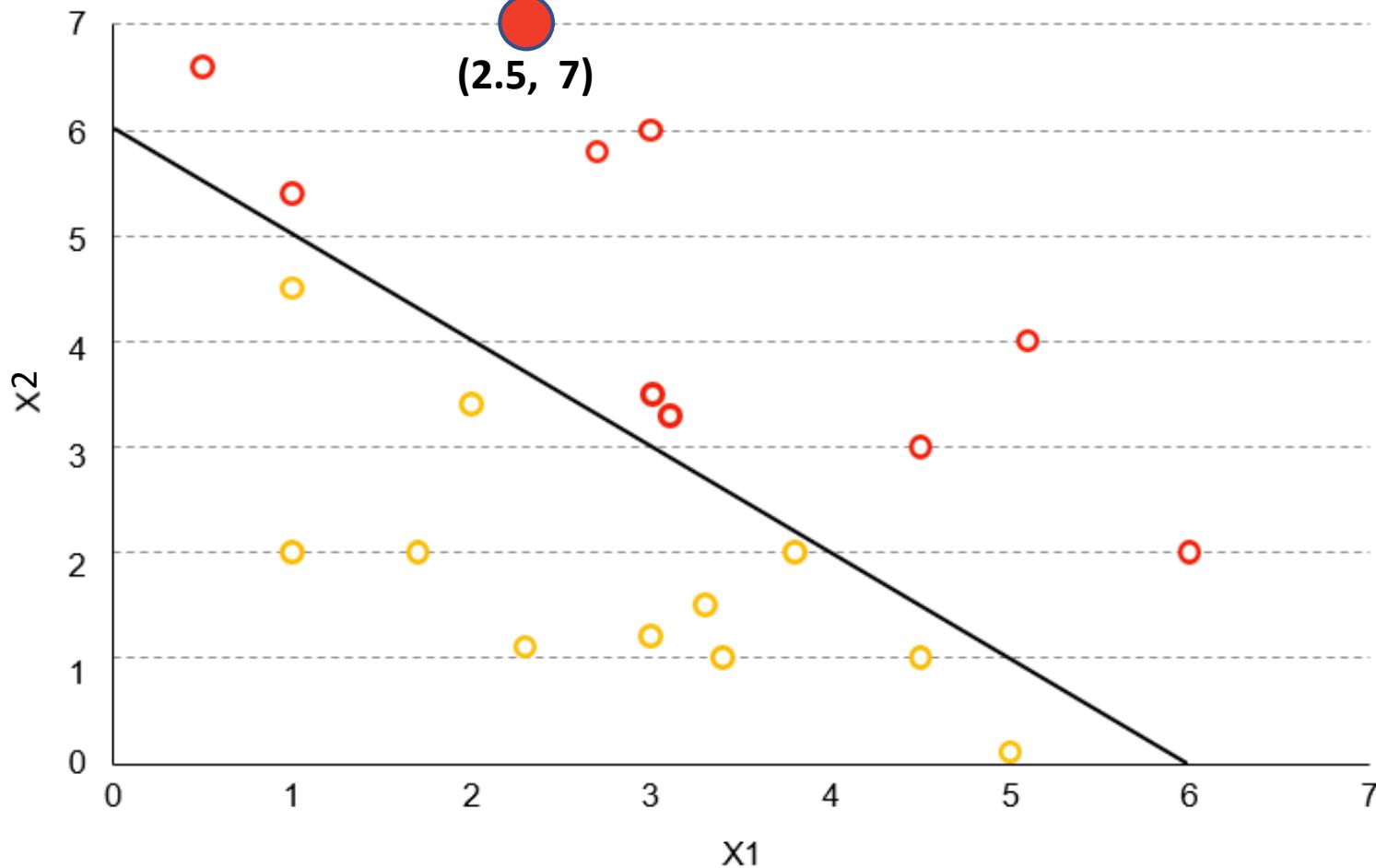
○ Pay Gap



$$\hat{f}(X) = \frac{1}{1 + e^{(-6 + 1x_1 + 1x_2)}}$$

○ No Pay Gap

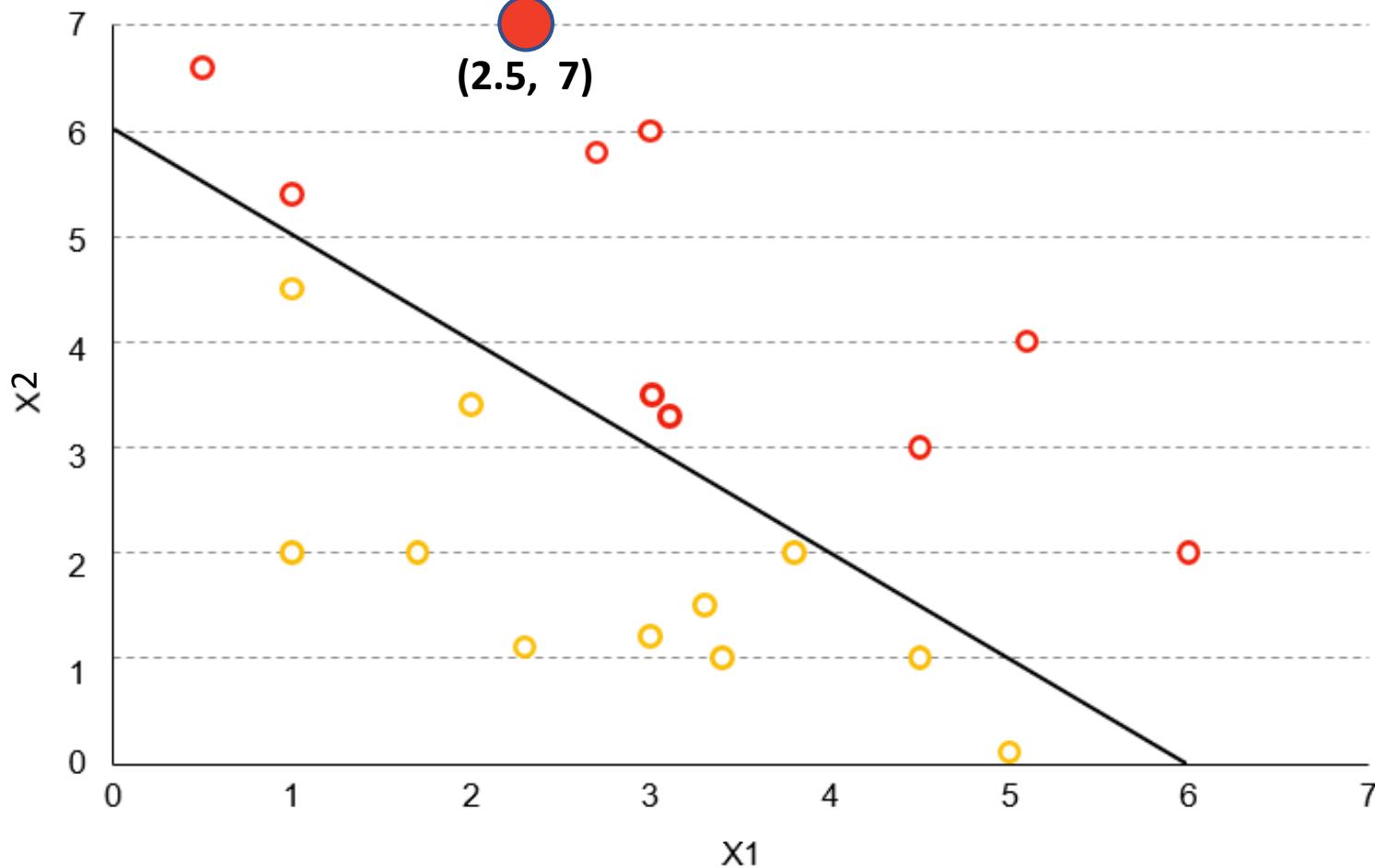
○ Pay Gap



$$\hat{f}(X) = \frac{1}{1 + e^{(-6 + 2.5 + 7)}}$$

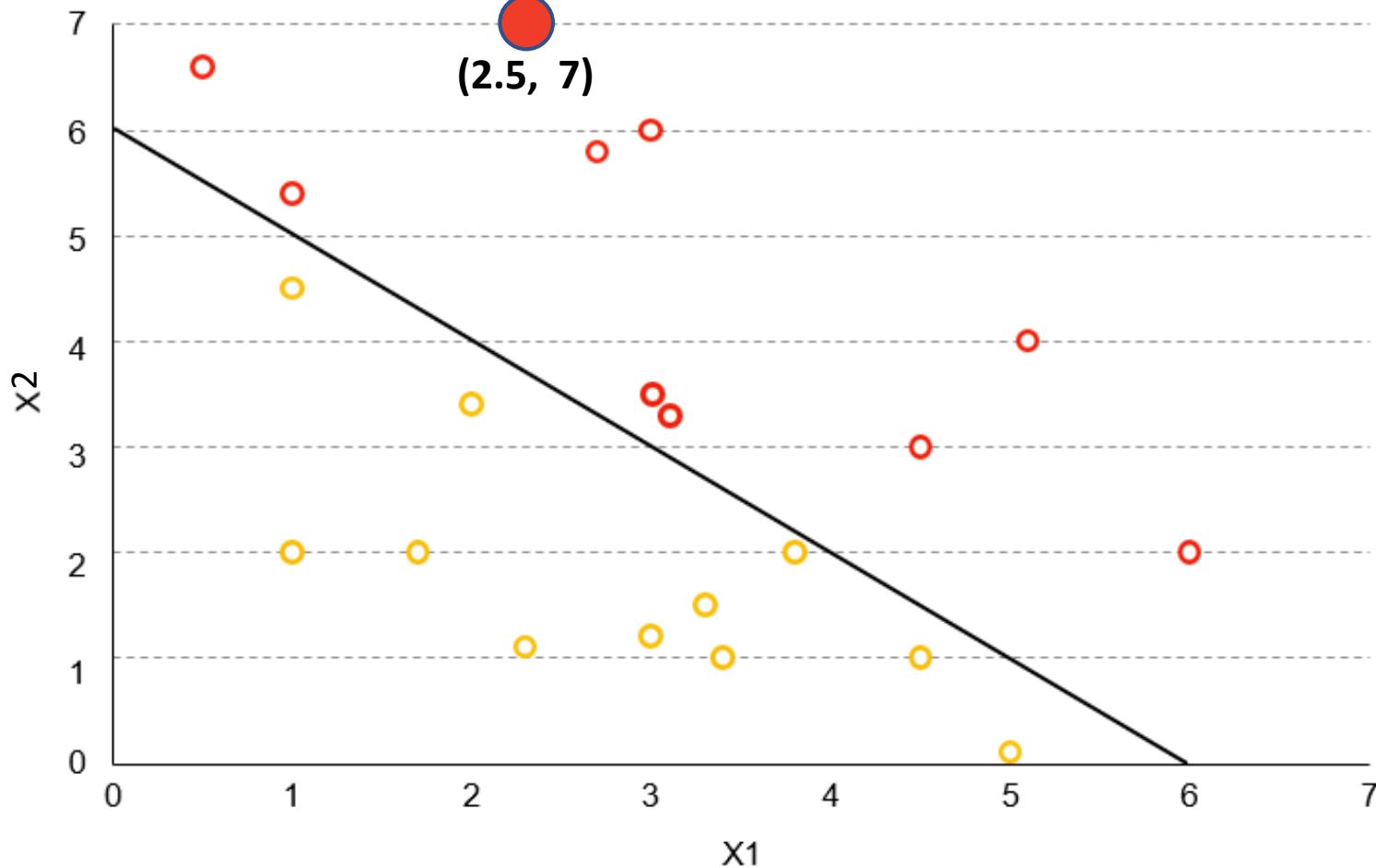
○ No Pay Gap

○ Pay Gap



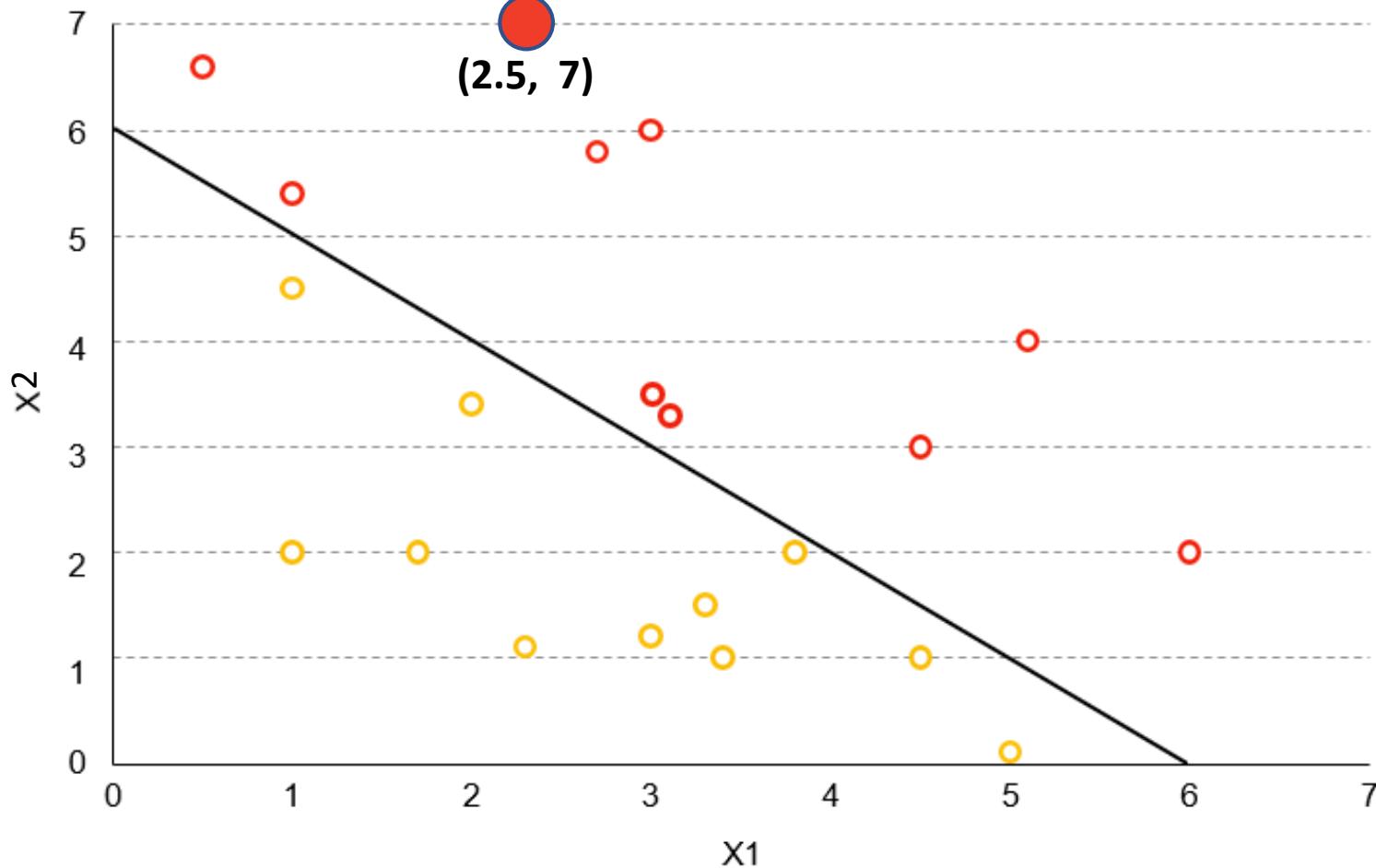
$$\hat{f}(X) = \frac{1}{1 + e^{(-6 + 9.5)}}$$

○ No Pay Gap      ○ Pay Gap

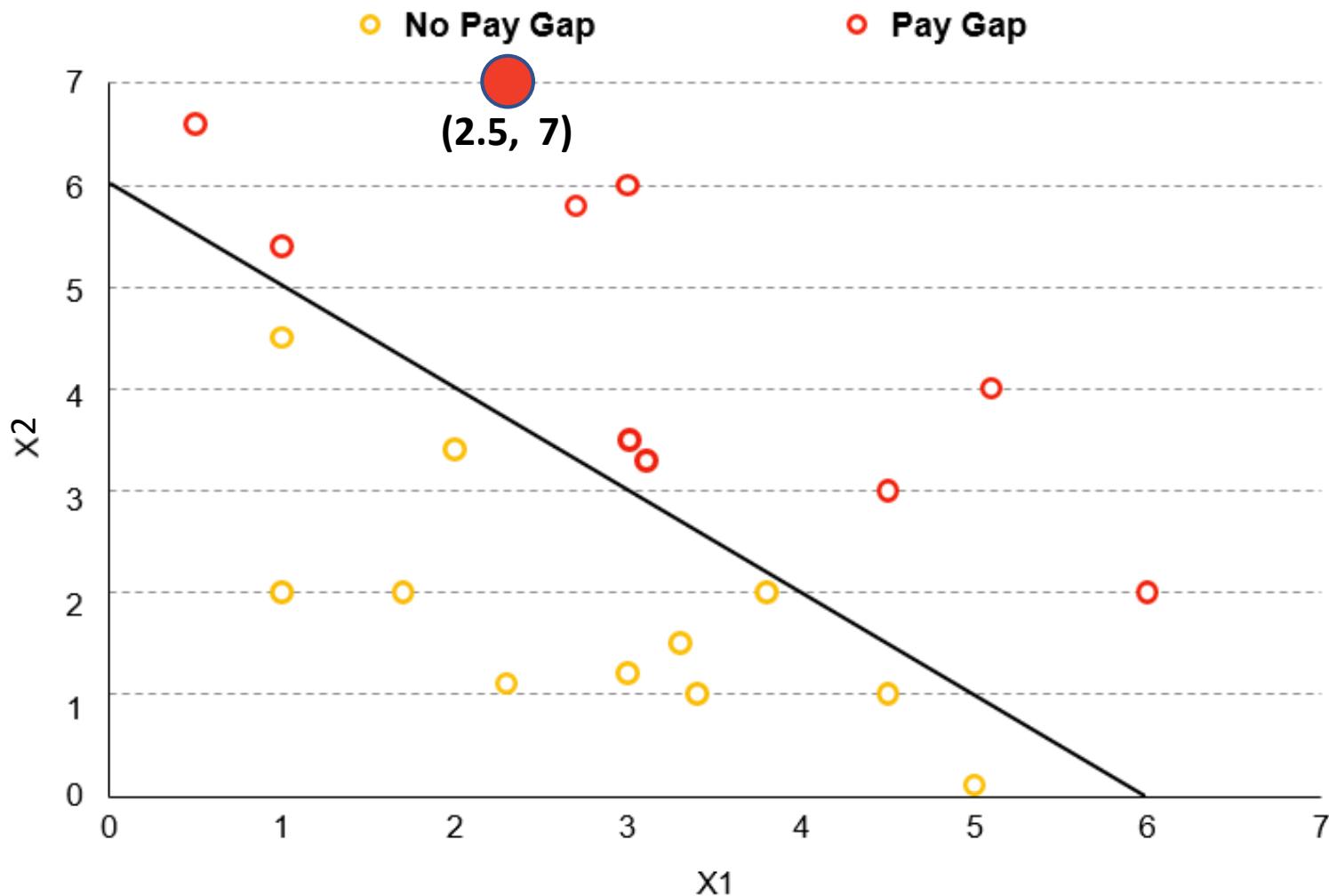


$$\hat{f}(X) = \frac{1}{1 + e^{-(3.5)}}$$

○ No Pay Gap      ○ Pay Gap

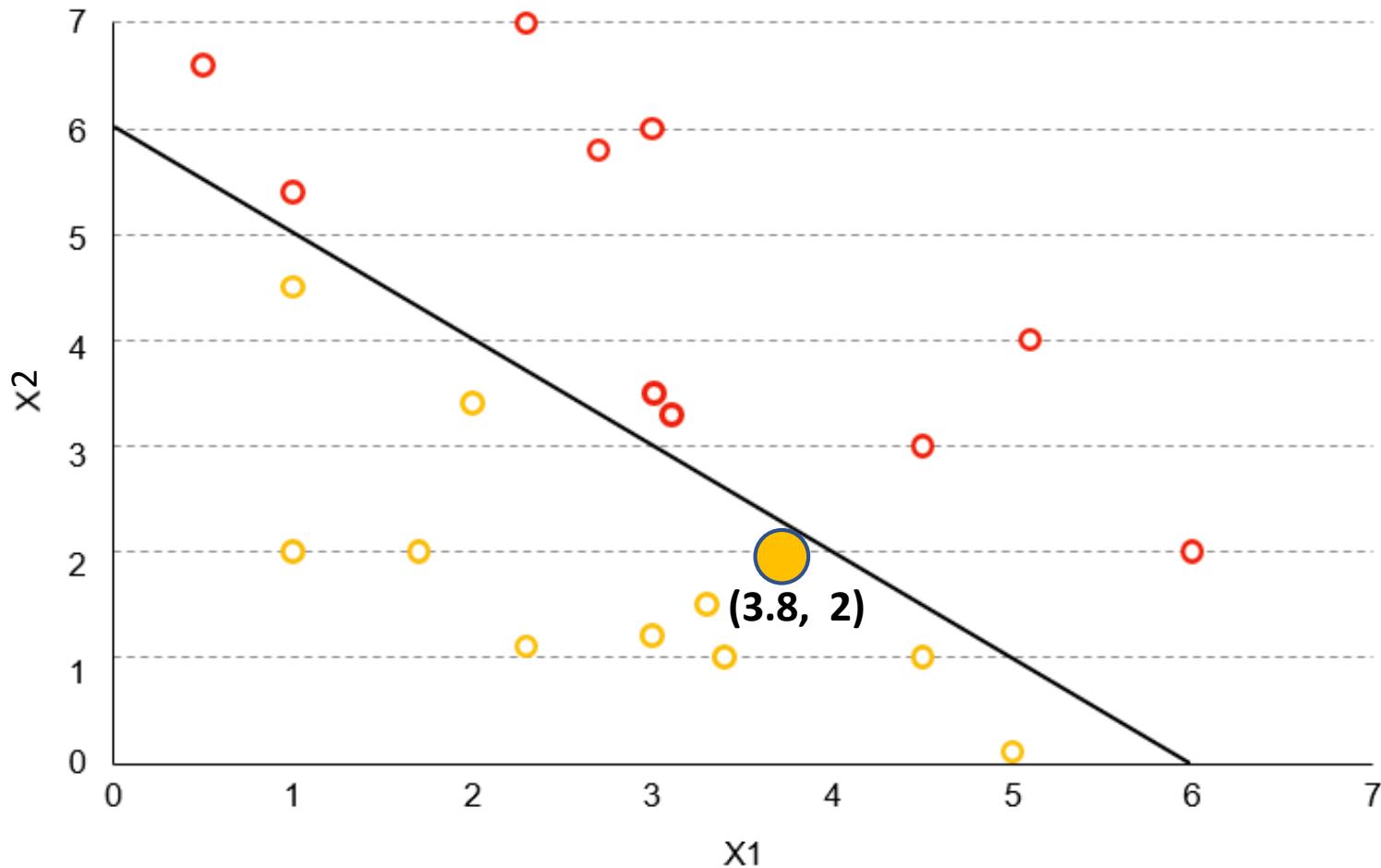


$$\hat{f}(X) = \frac{1}{1 + e^{-(3.5)}} = .97 \text{ (probability)}$$



$$\hat{f}(X) = \frac{1}{1 + e^{(-6 + 1x_1 + 1x_2)}}$$

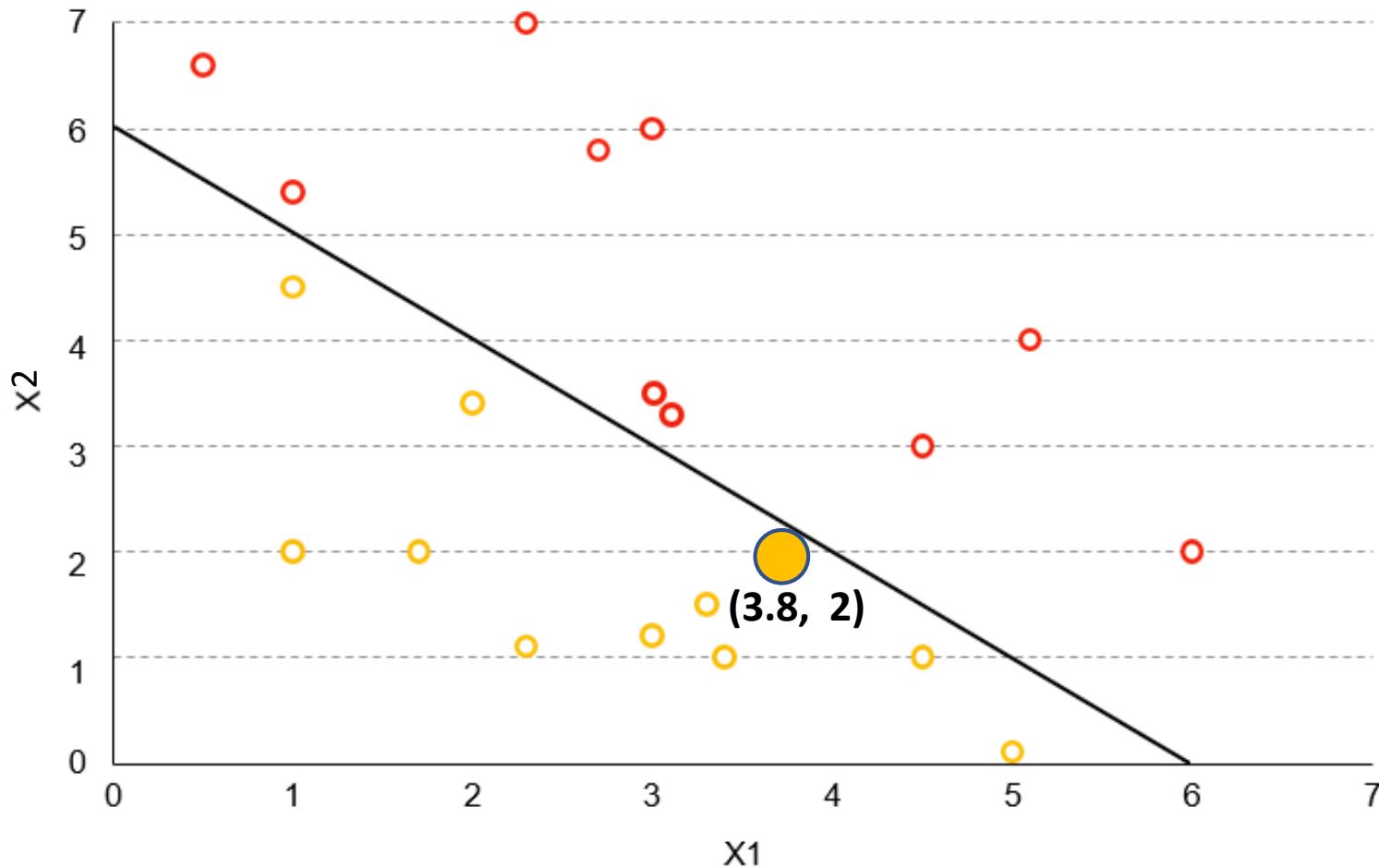
○ No Pay Gap      ○ Pay Gap



$$\hat{f}(X) = \frac{1}{1 + e^{(-6 + 3.8 + 2)}}$$

○ No Pay Gap

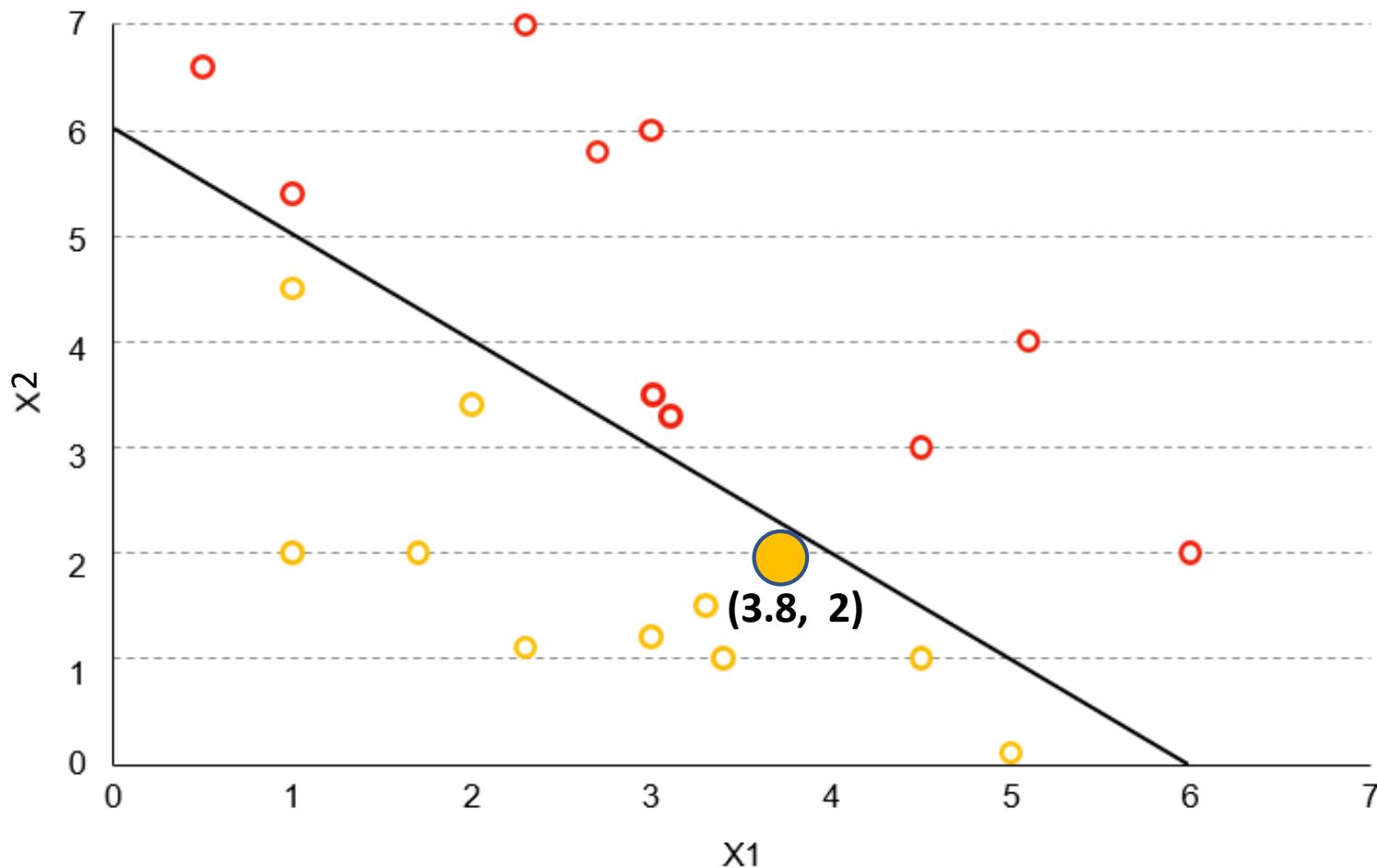
○ Pay Gap



$$\hat{f}(X) = \frac{1}{1 + e^{(-6 + 5.8)}}$$

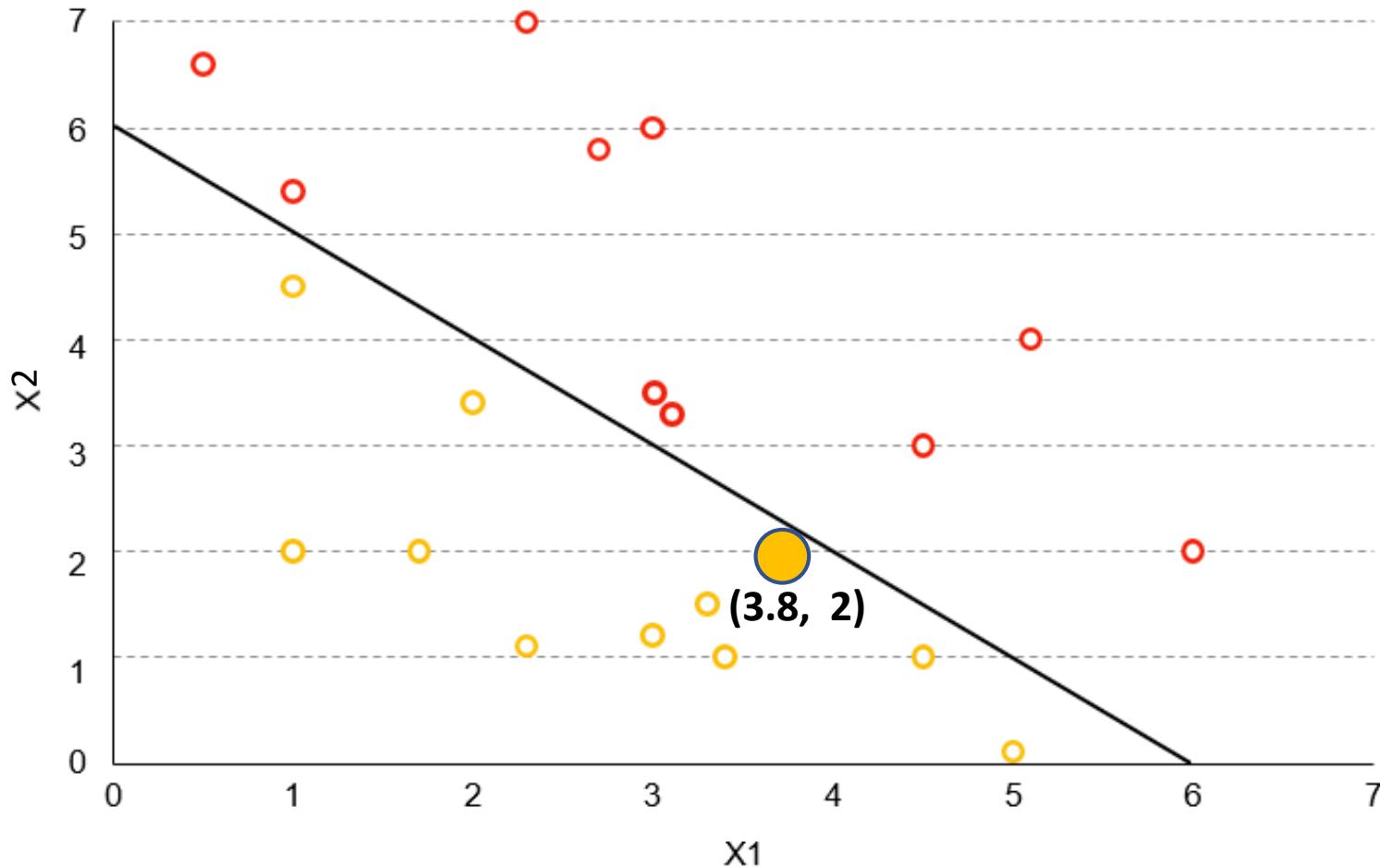
○ No Pay Gap

○ Pay Gap

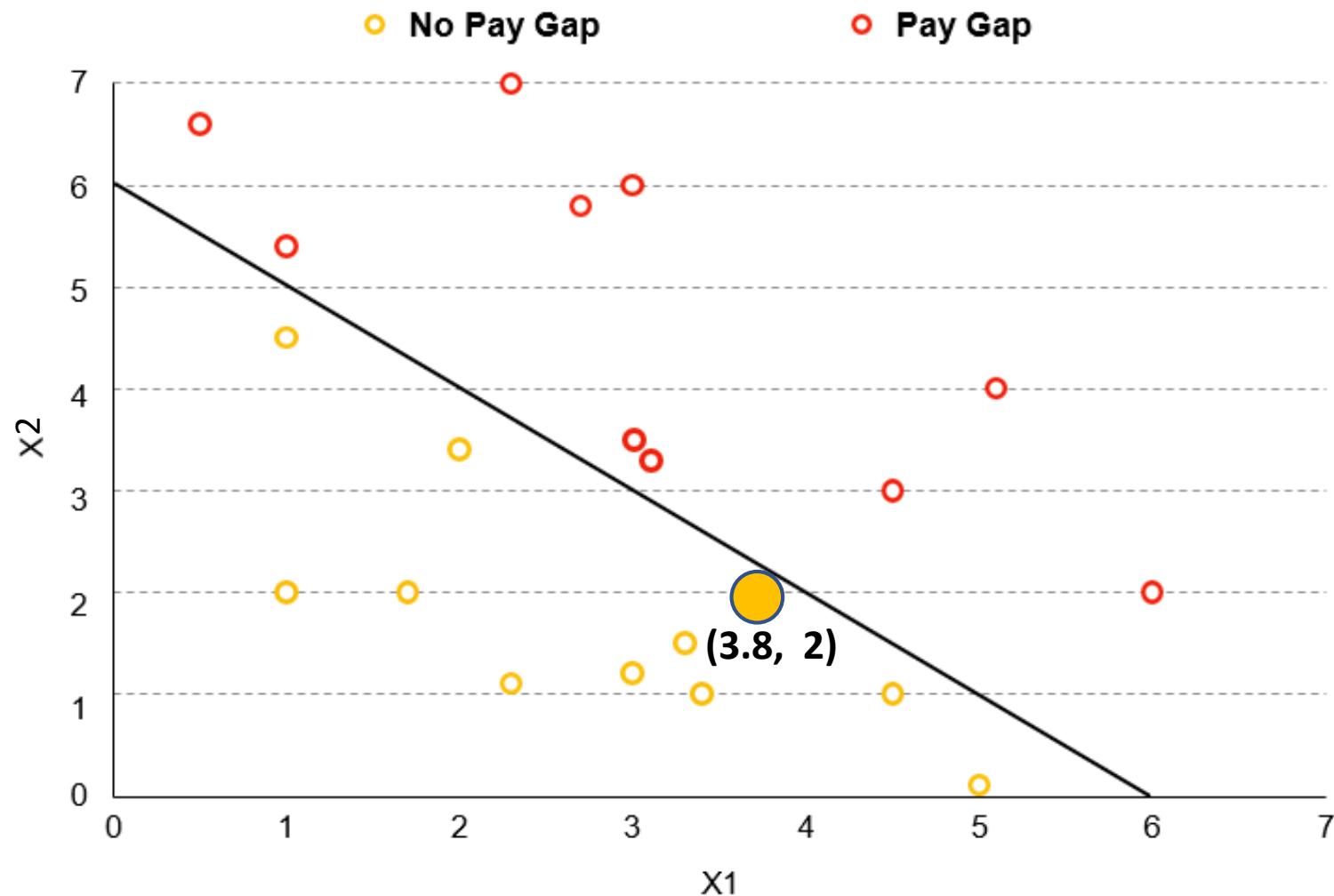


$$\hat{f}(X) = \frac{1}{1 + e^{-(-0.2)}}$$

○ No Pay Gap      ○ Pay Gap



$$\hat{f}(X) = \frac{1}{1 + e^{-(-0.2)}} = .45 \text{ (probability)}$$



# Support Vector Machine

# Support Vector Machine

$$\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3$$

**predict 1** when

$$\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 \geq 0$$

**predict 0** when

$$\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 < 0$$

# Support Vector Machine

predict 1 when  $\beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 \geq 1$

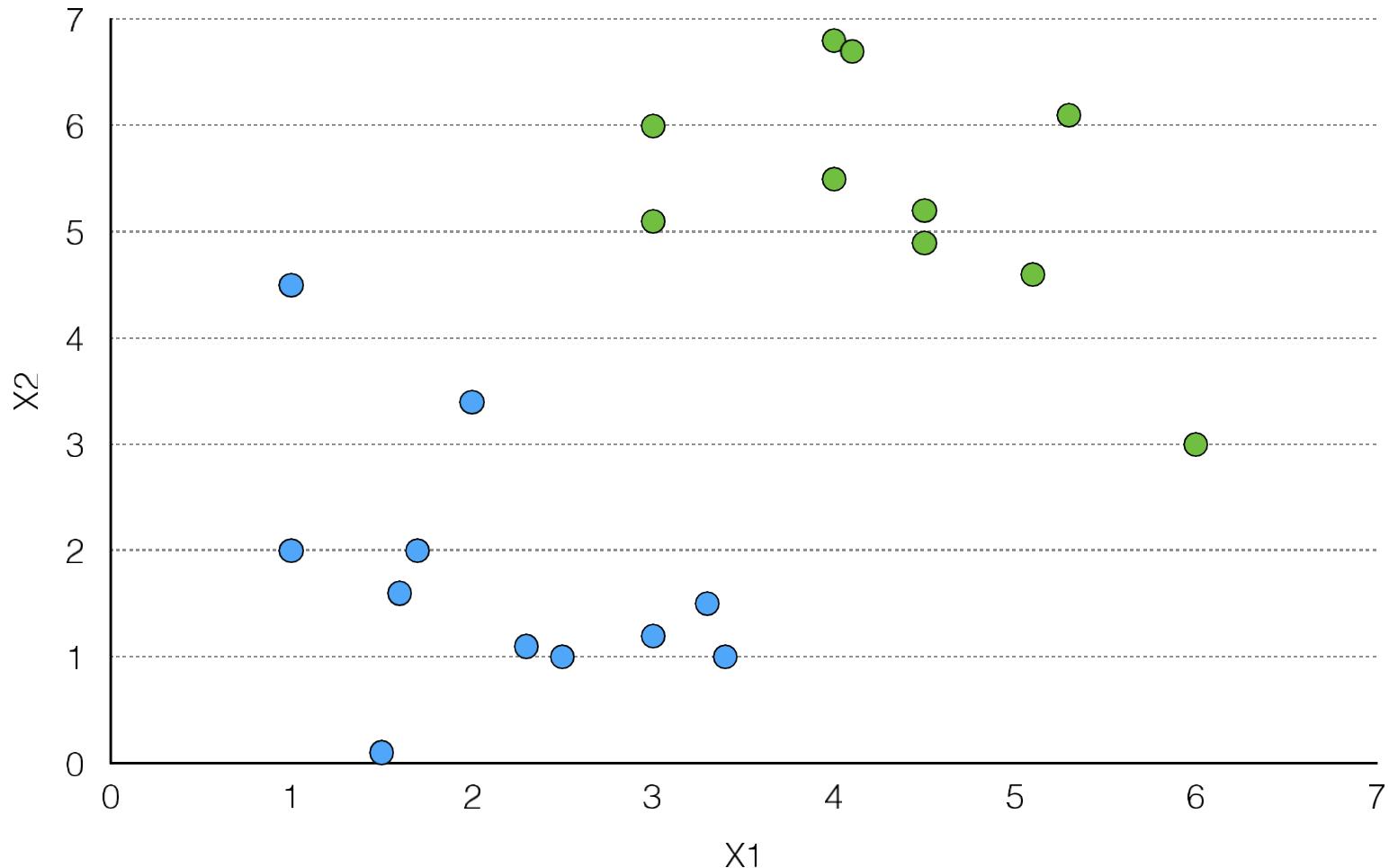
predict 0 when  $\beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 < -1$

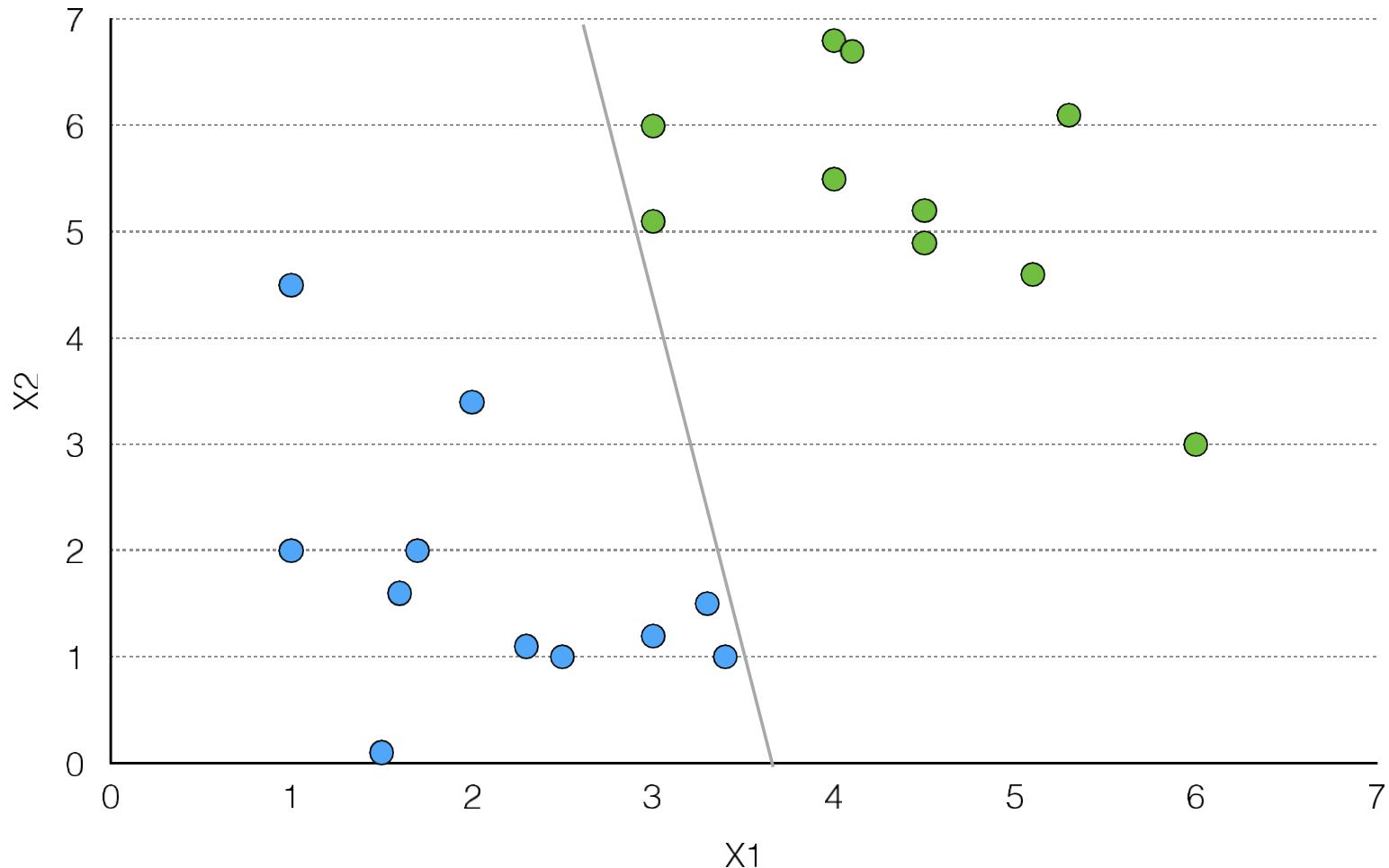
# Support Vector Machine

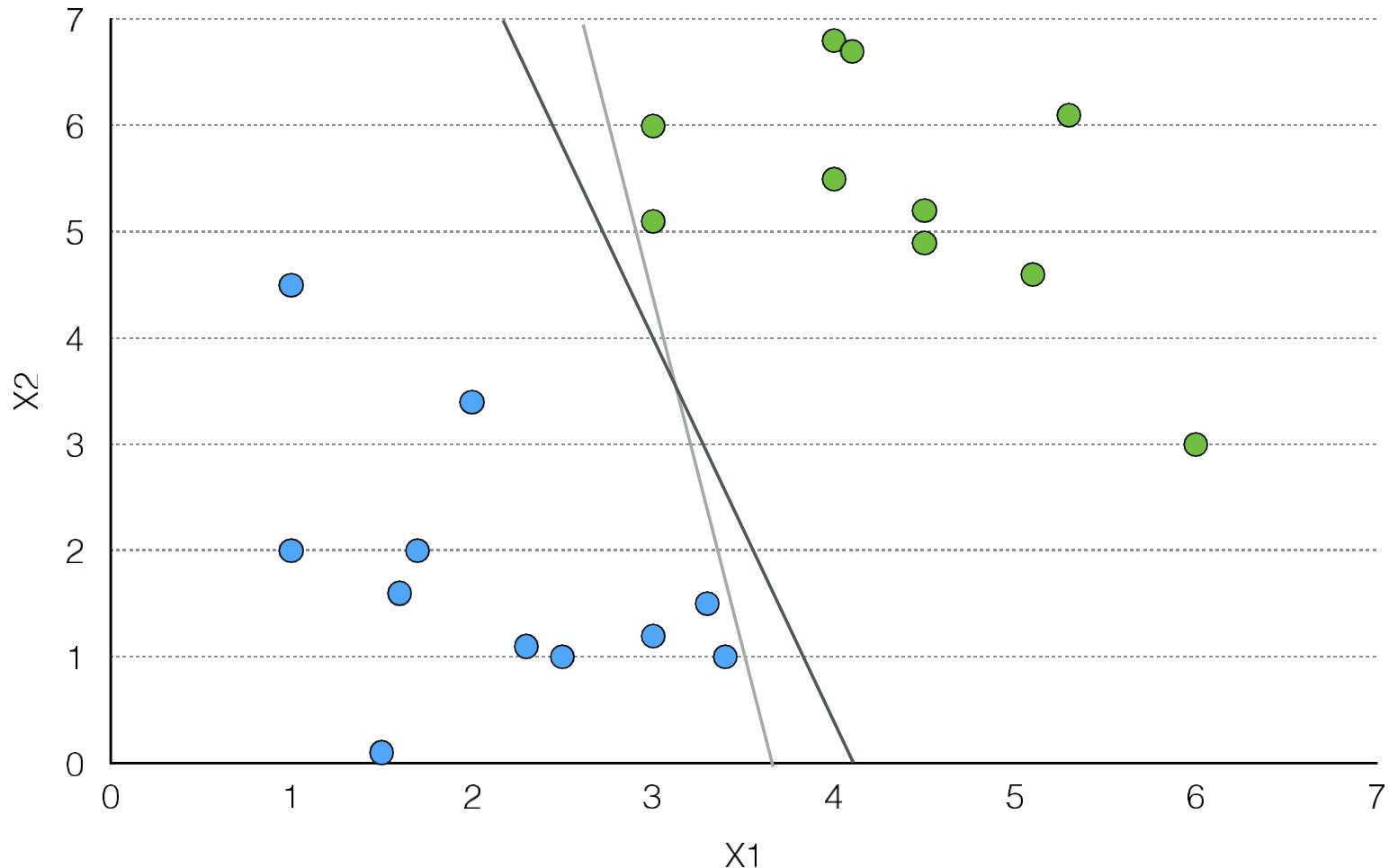
## Large Margin Classifier

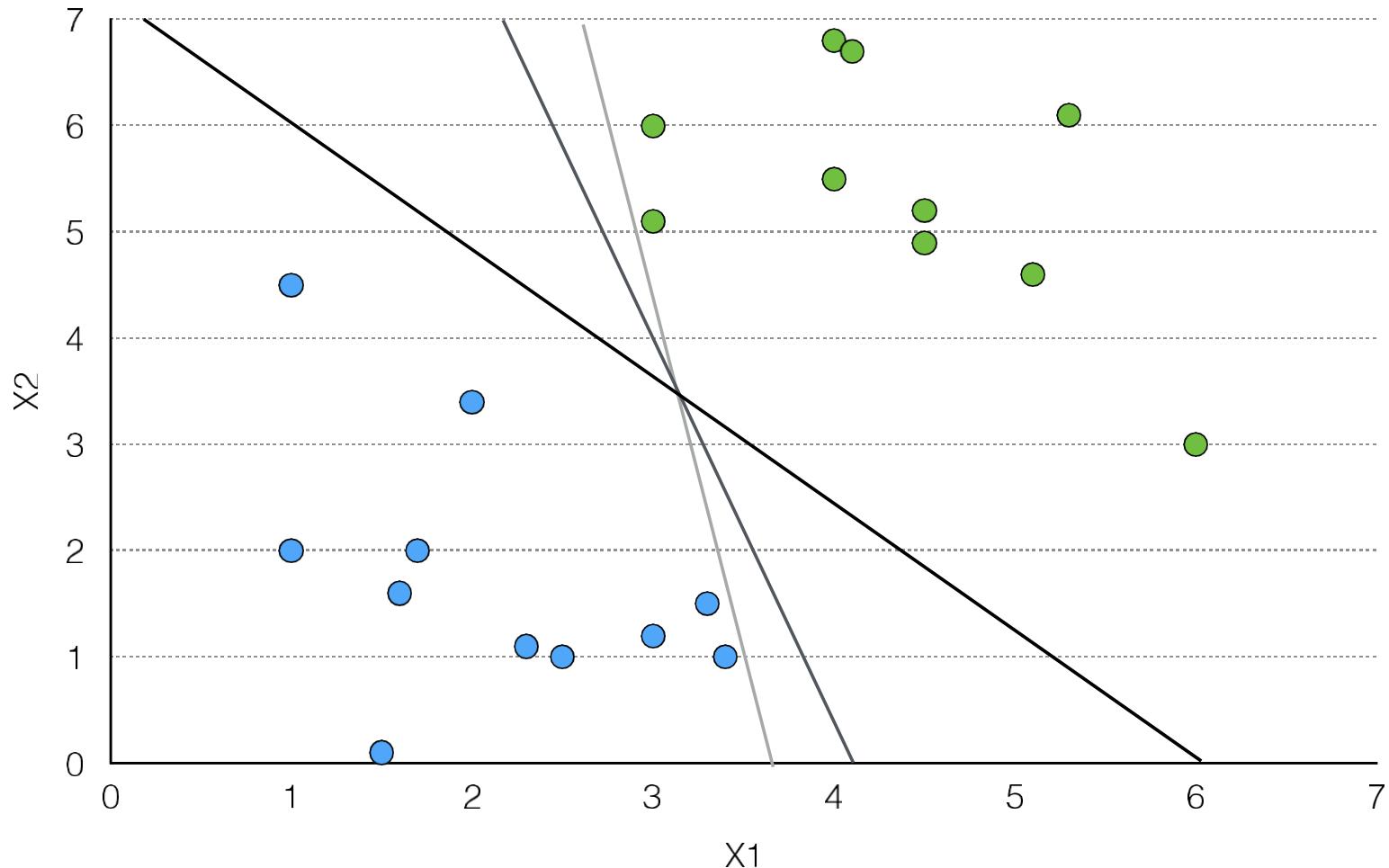
predict 1 when  $\beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 \geq 1$

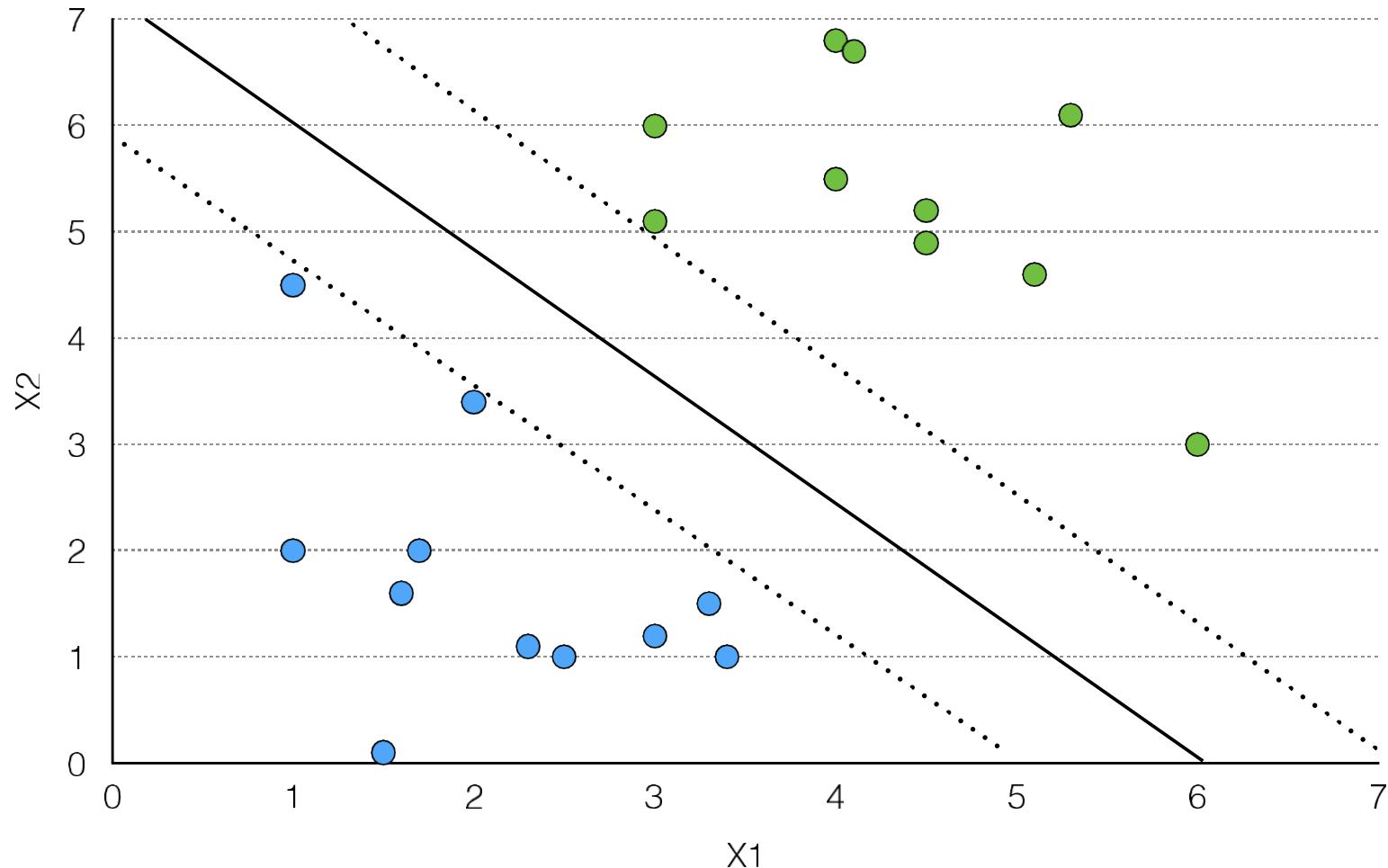
predict 0 when  $\beta_0 + \beta_1x_1 + \beta_2x_2 + \beta_3x_3 < -1$





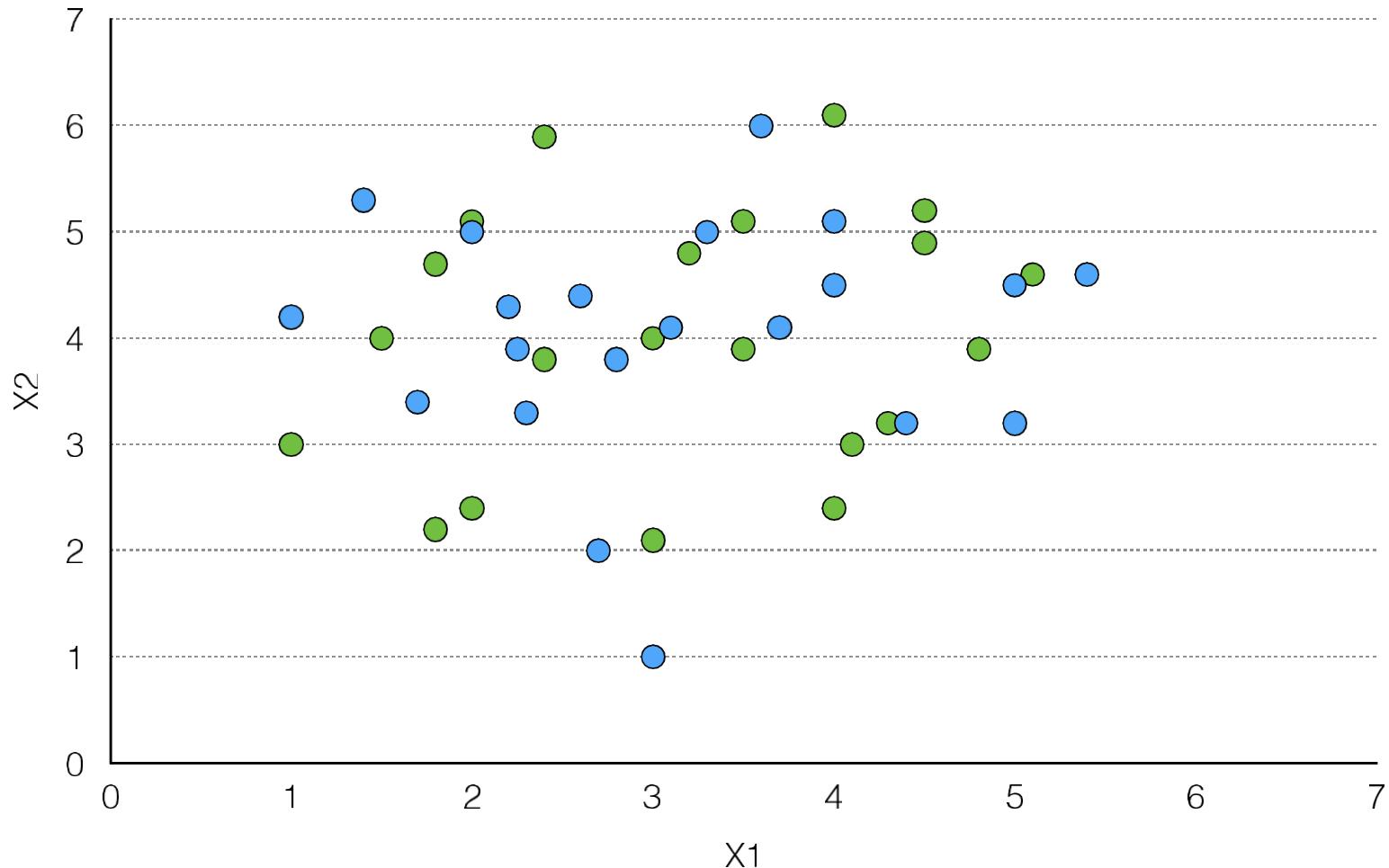








40-yard dash	Weight	Height	Drafted
5.10	290	74	1
4.92	275	75.5	1
4.43	178	69	0
4.62	221	74.5	1
4.91	248	75	0
5.53	303	77	0
4.47	189	71	1
4.56	205	71	1
4.75	267	73	0
4.84	261	74	1



40-yard dash	Weight	Height	Drafted
5.10	290	74	1
4.92	275	75.5	1
4.43	178	69	0
4.62	221	74.5	1
4.91	248	75	0
5.53	303	77	0
4.47	189	71	1
4.56	205	71	1
4.75	267	73	0
4.84	261	74	1

# Feature Engineering

40-yard dash	BMI (wt/ht <sup>2</sup> )	Drafted
5.10	37.2	1
4.92	33.9	1
4.43	26.3	0
4.62	28	1
4.91	31	0
5.53	35.9	0
4.47	26.4	1
4.56	28.6	1
4.75	35.2	0
4.84	33.5	1

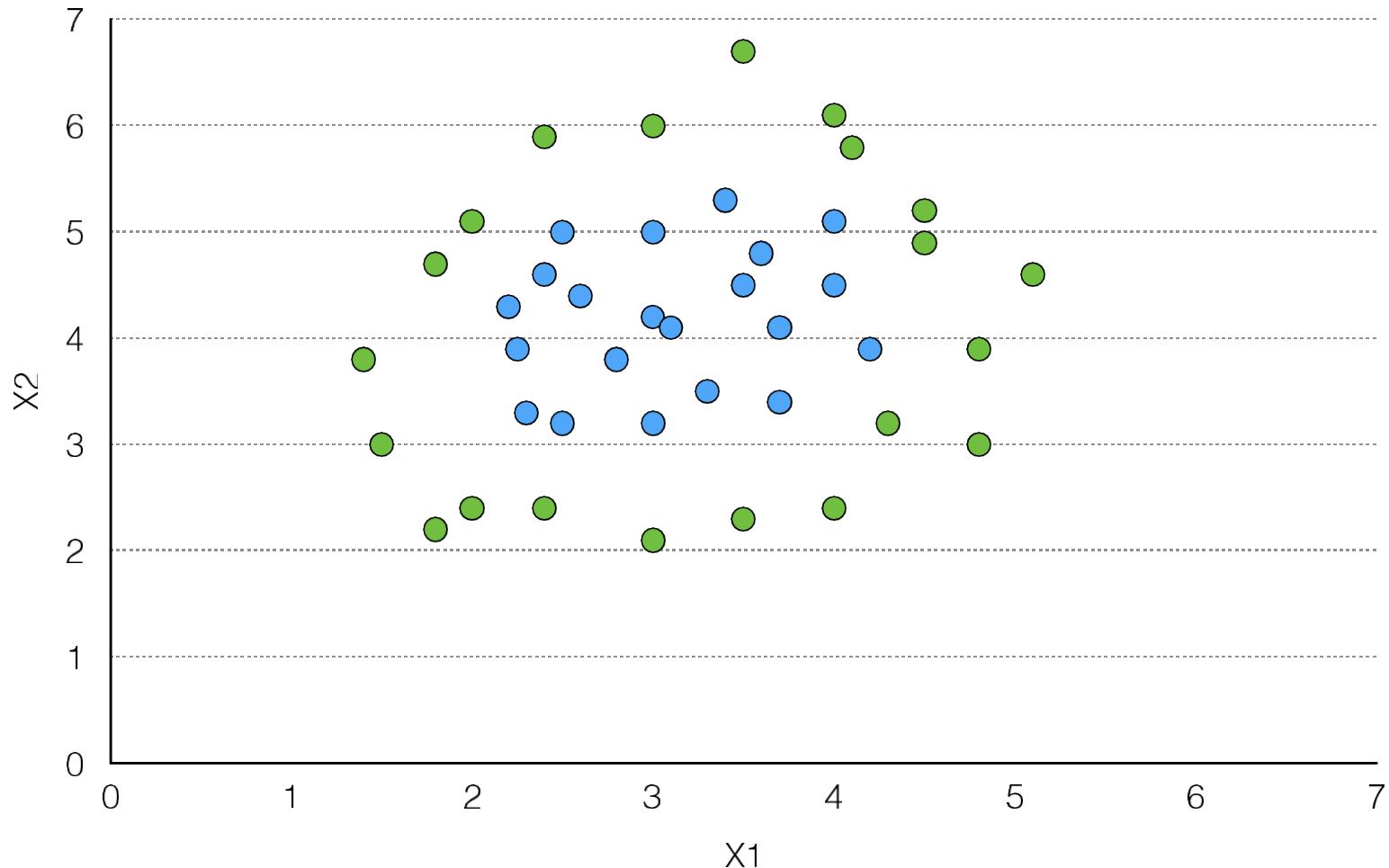


# Feature Engineering

40-yard dash	BMI (wt/ht <sup>2</sup> )	Drafted
5.10	37.2	1
4.92	33.9	1
4.43	26.3	0
4.62	28	1
4.91	31	0
5.53	35.9	0
4.47	26.4	1
4.56	28.6	1
4.75	35.2	0
4.84	33.5	1

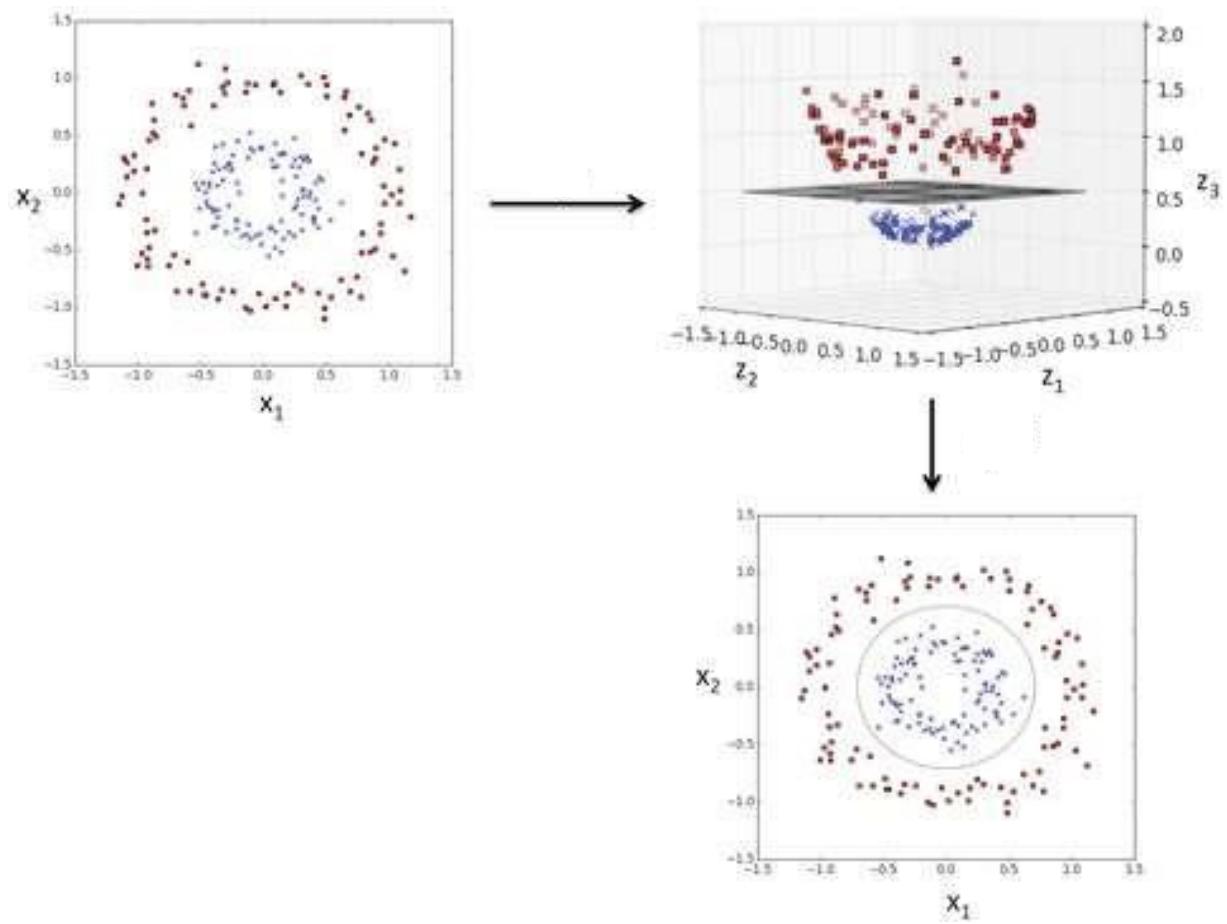
# Feature Engineering

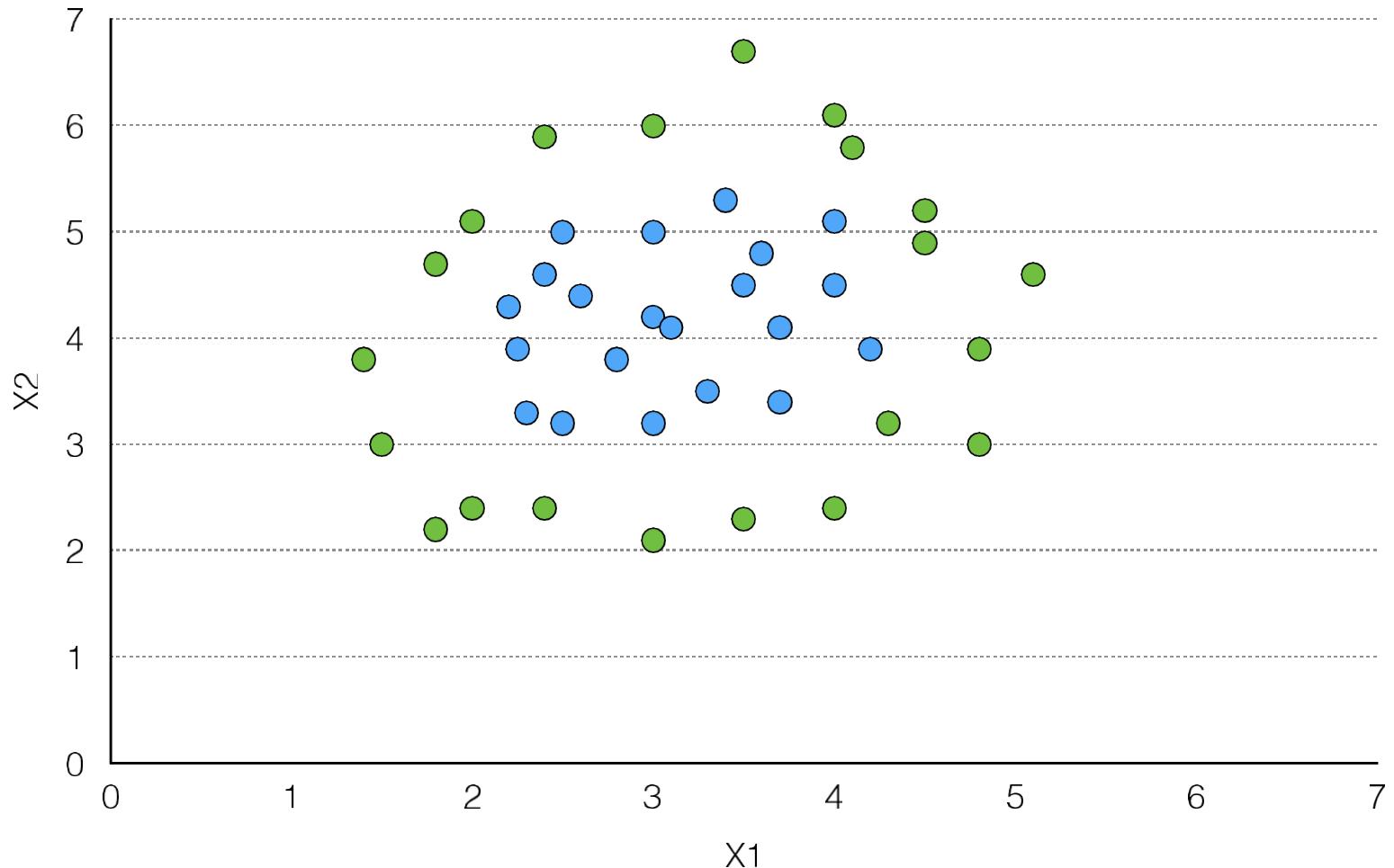
Speed-to-Size (40-yd/bsa)	BMI (wt/ht <sup>2</sup> )	Drafted
2.16	37.2	1
2.06	33.9	1
2.02	26.3	0
1.97	28	1
2.23	31	0
2.00	35.9	0
2.03	26.4	1
1.99	28.6	1
1.85	35.2	0
2.03	33.5	1

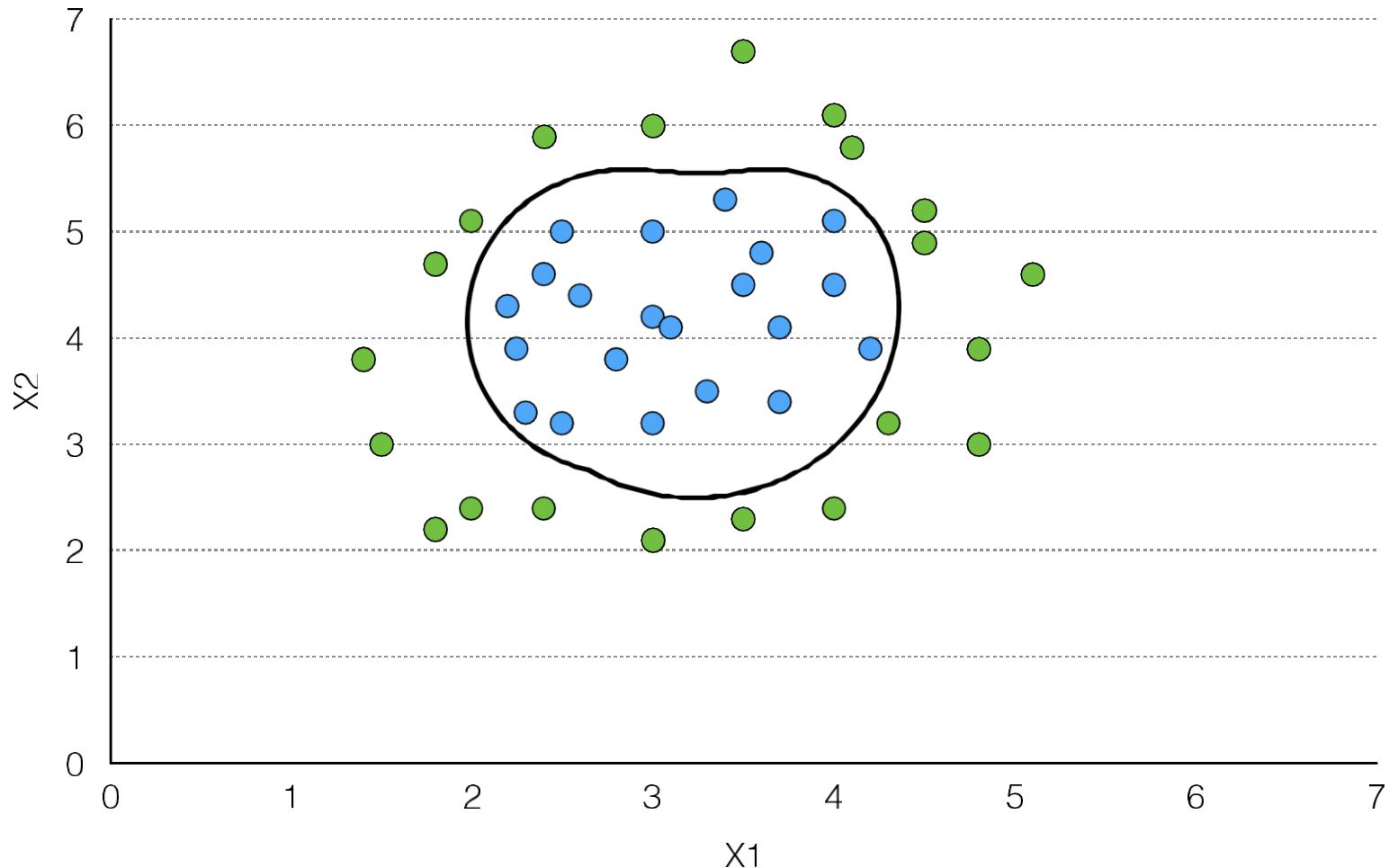


# Kernel

## Non-linear Classification

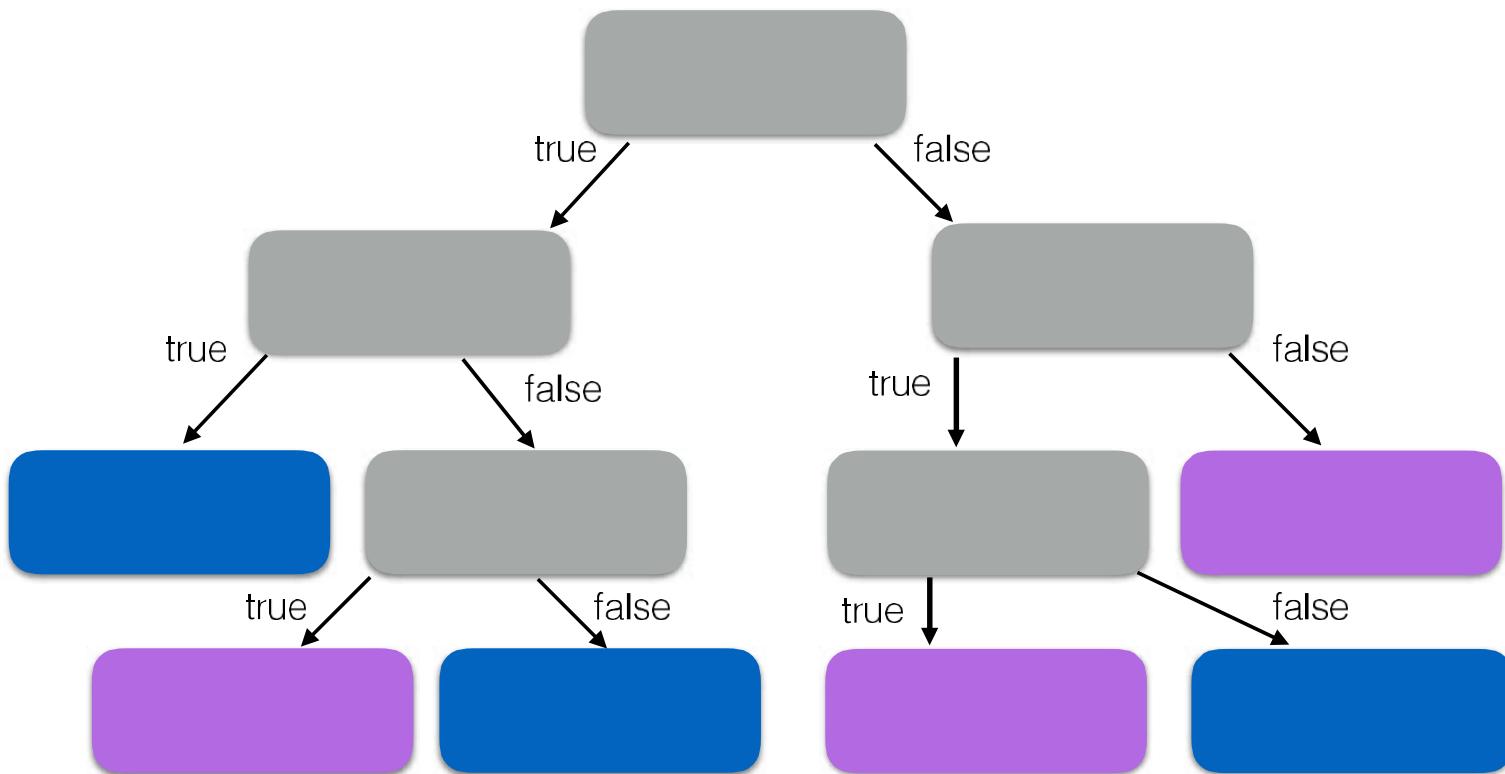






# Decision Tree

# Decision Tree

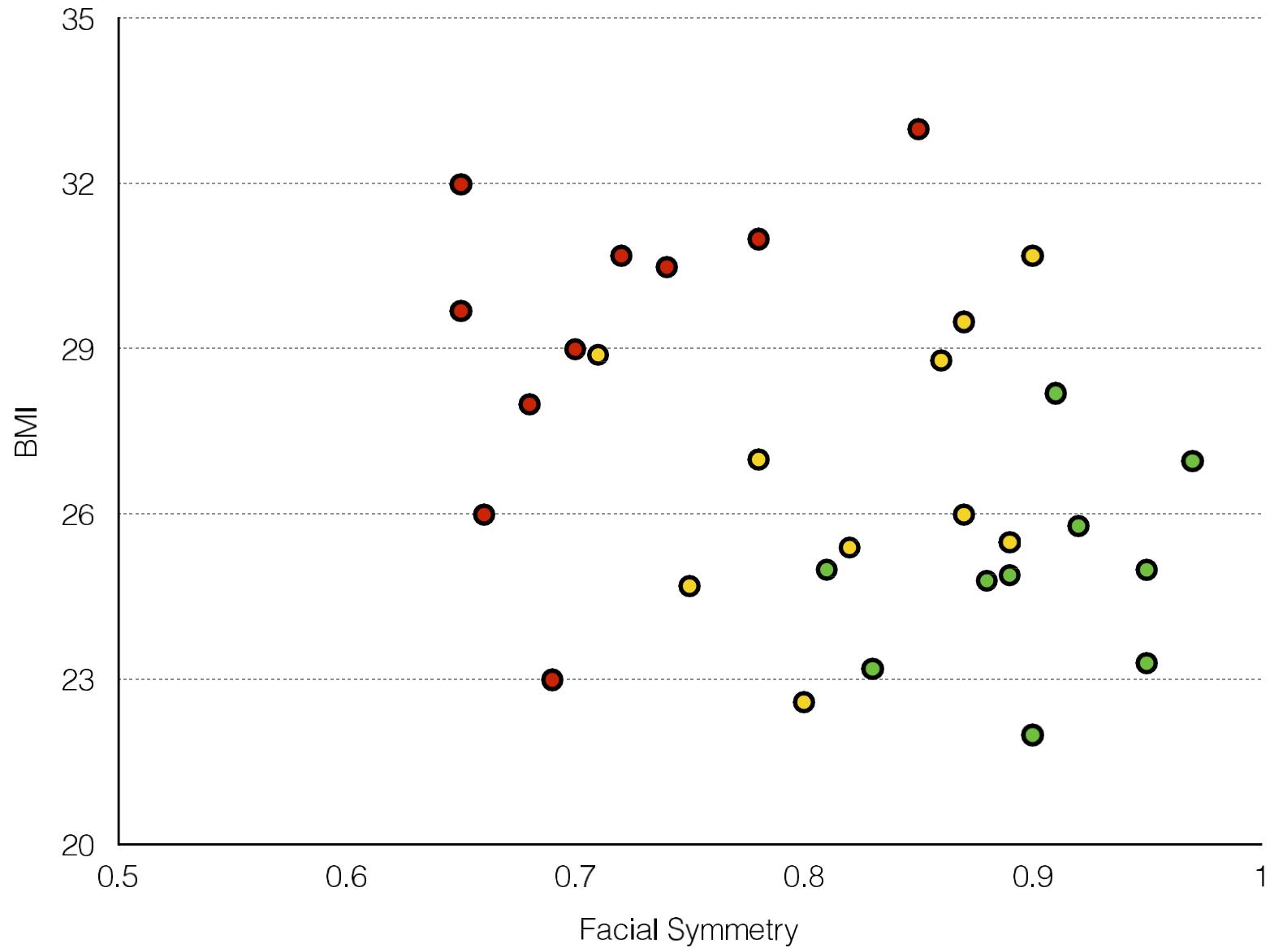


# Short-term Attractiveness



# Short-term Attractiveness

Facial Symmetry	BMI	Waist-to-Hip	Well-Groomed
0.9	23.4	0.93	1
0.85	27.9	0.87	0
0.65	27.1	0.79	1
0.85	22.6	0.91	1
0.9	30.3	0.82	0
0.75	29.0	0.82	0
0.85	22.3	0.89	1
0.7	37.6	0.73	0
0.85	24.2	0.85	0

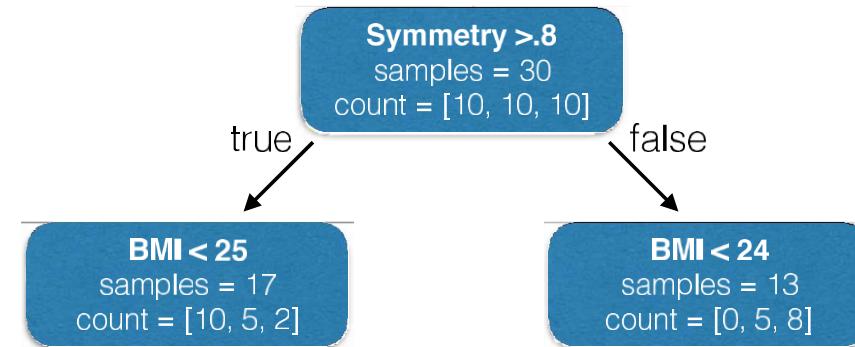


**Symmetry >.8**

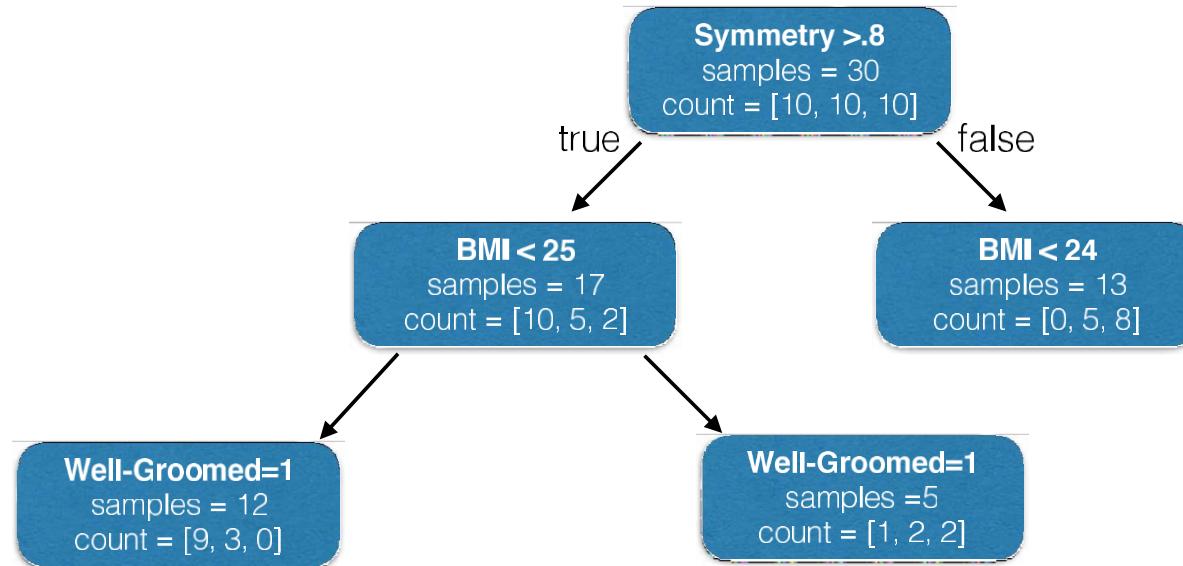
samples = 30

count = [10, 10, 10]

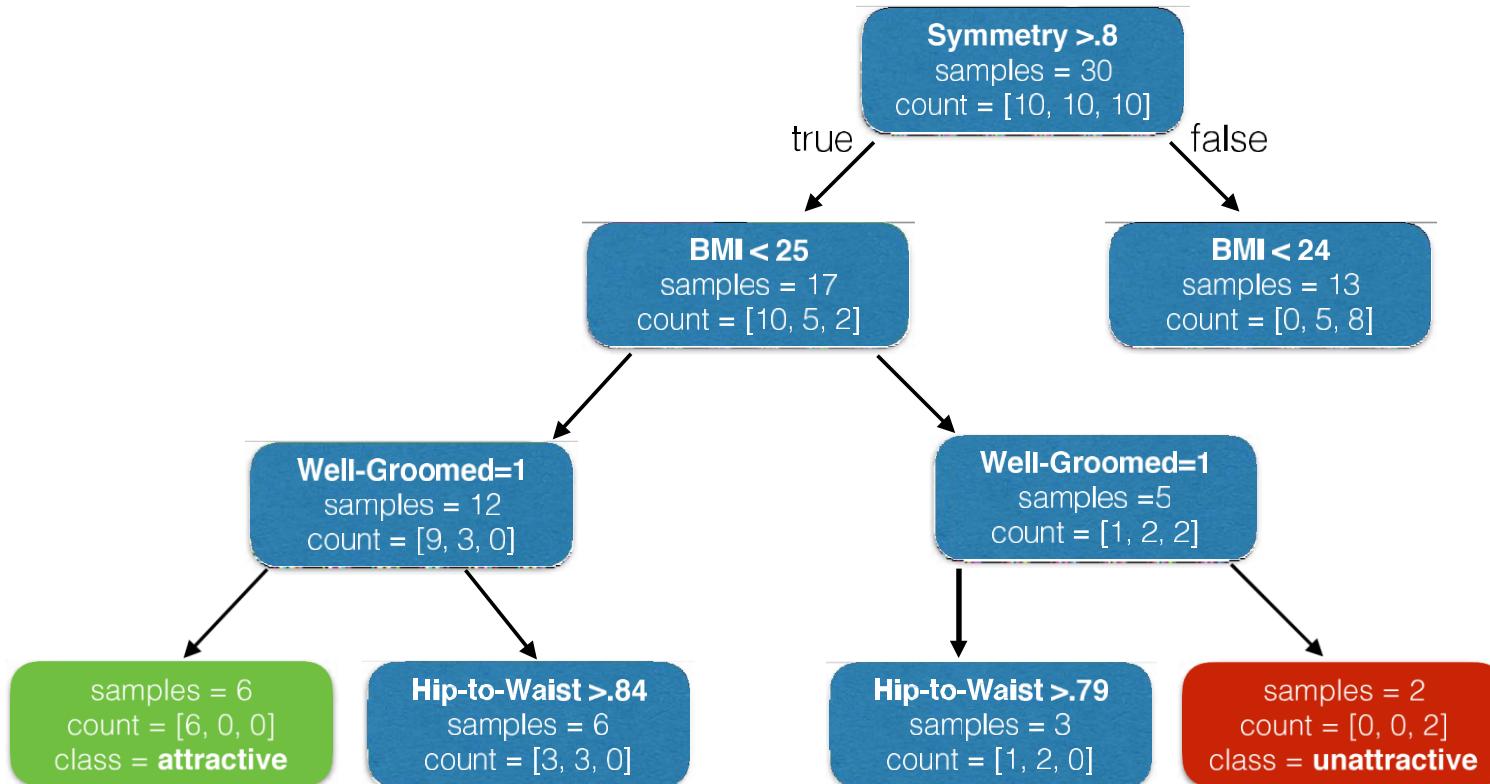
[att, ave, un]



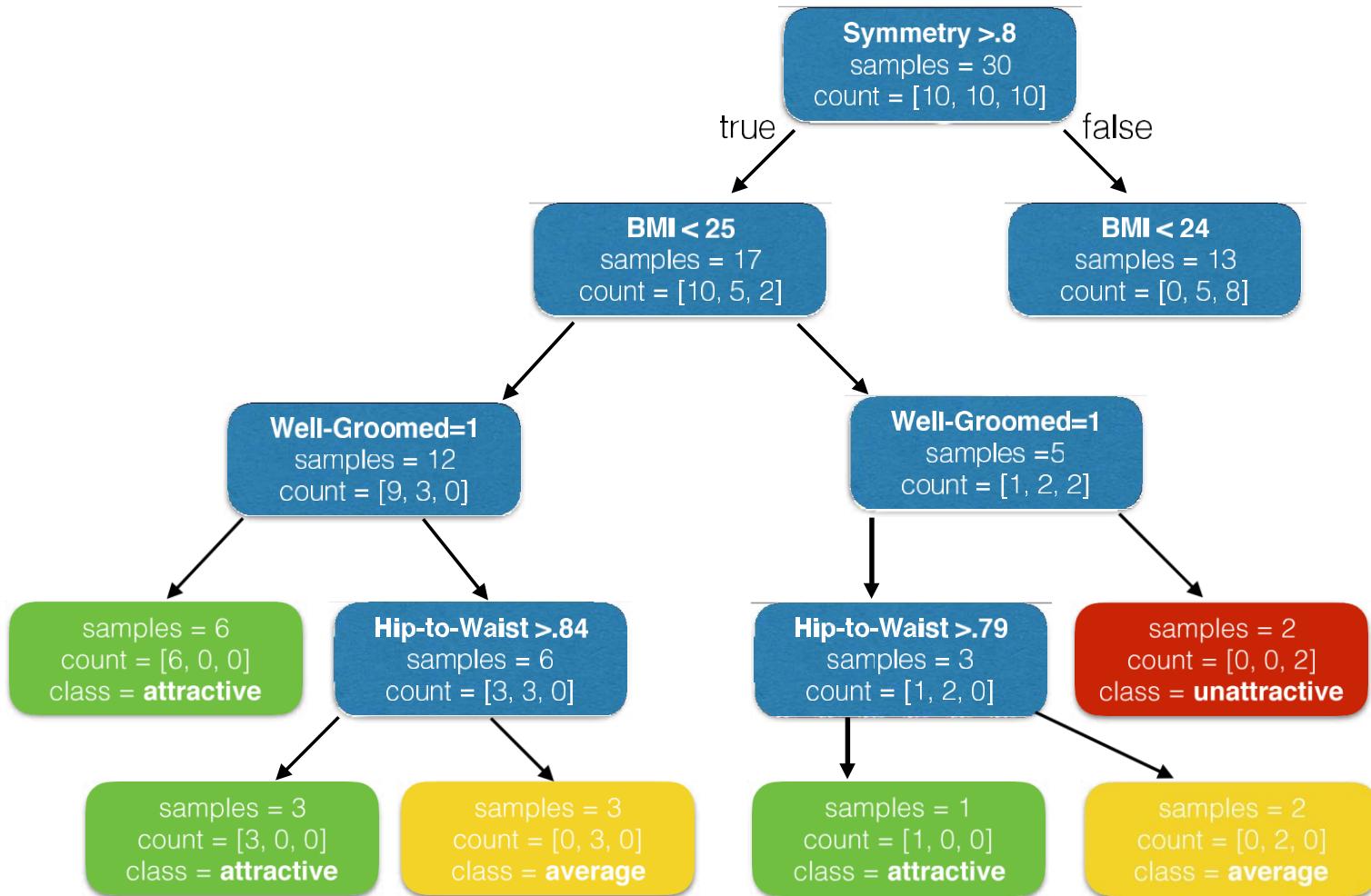
[att, ave, un]



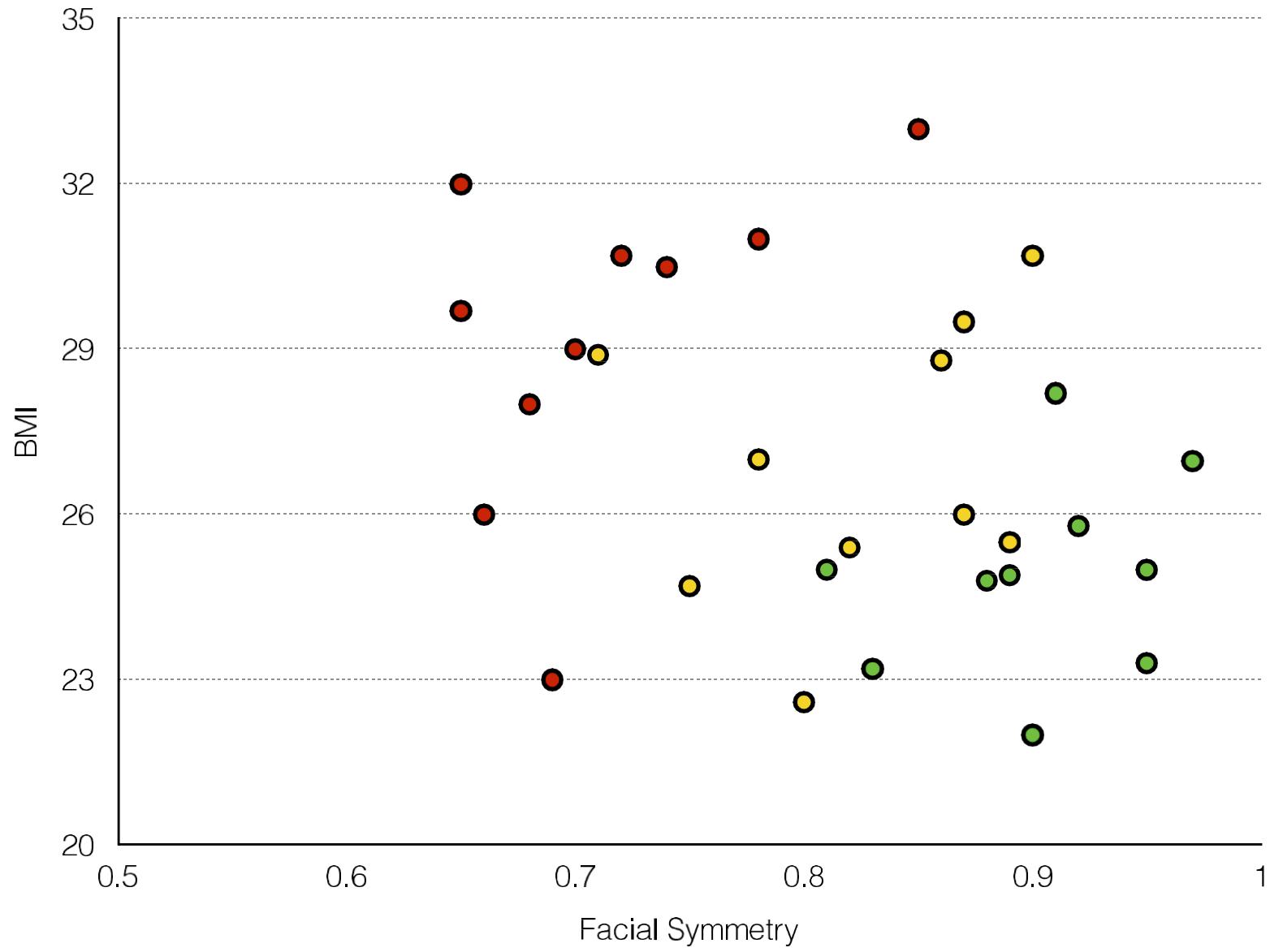
[att, ave, un]

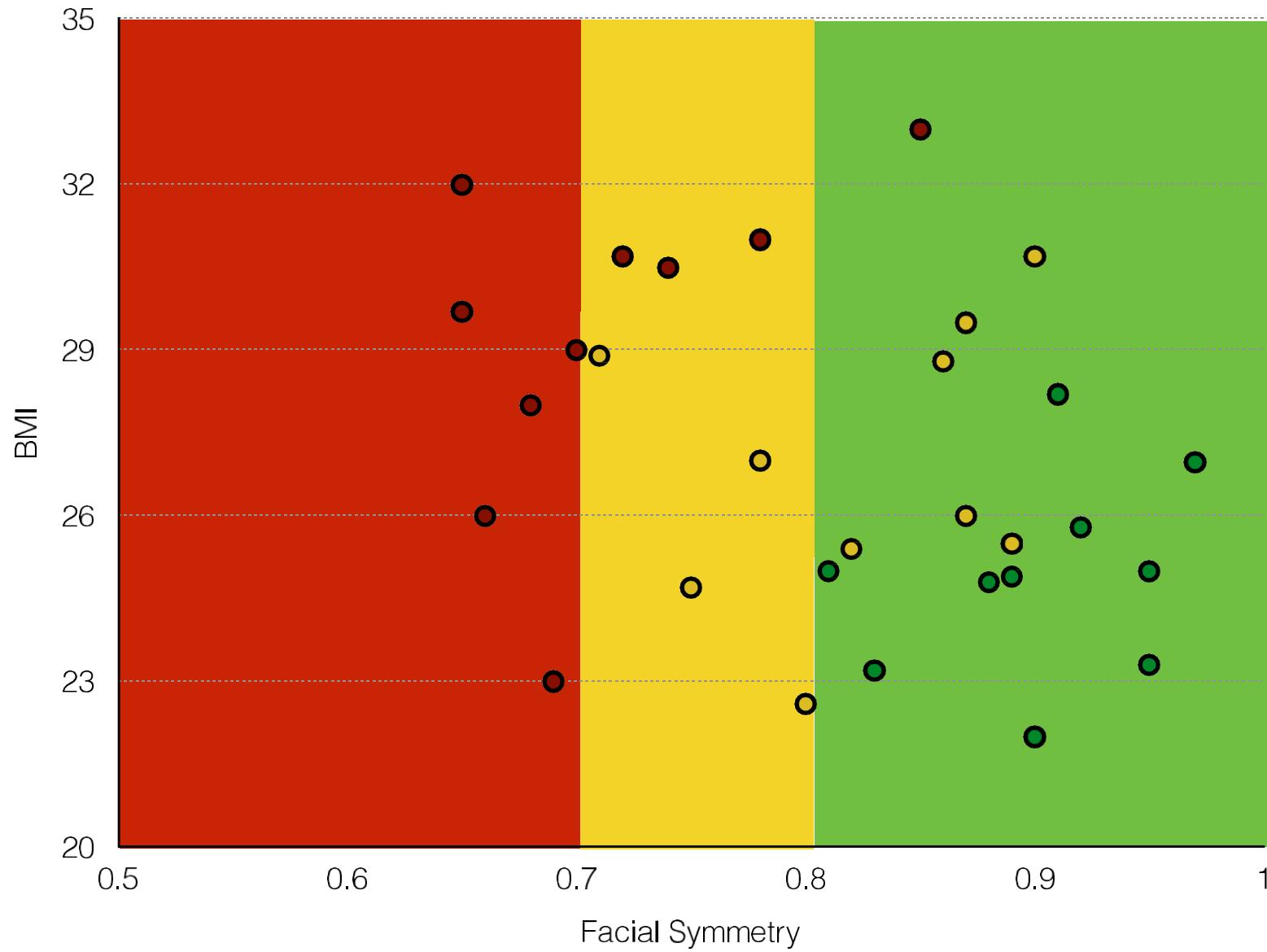


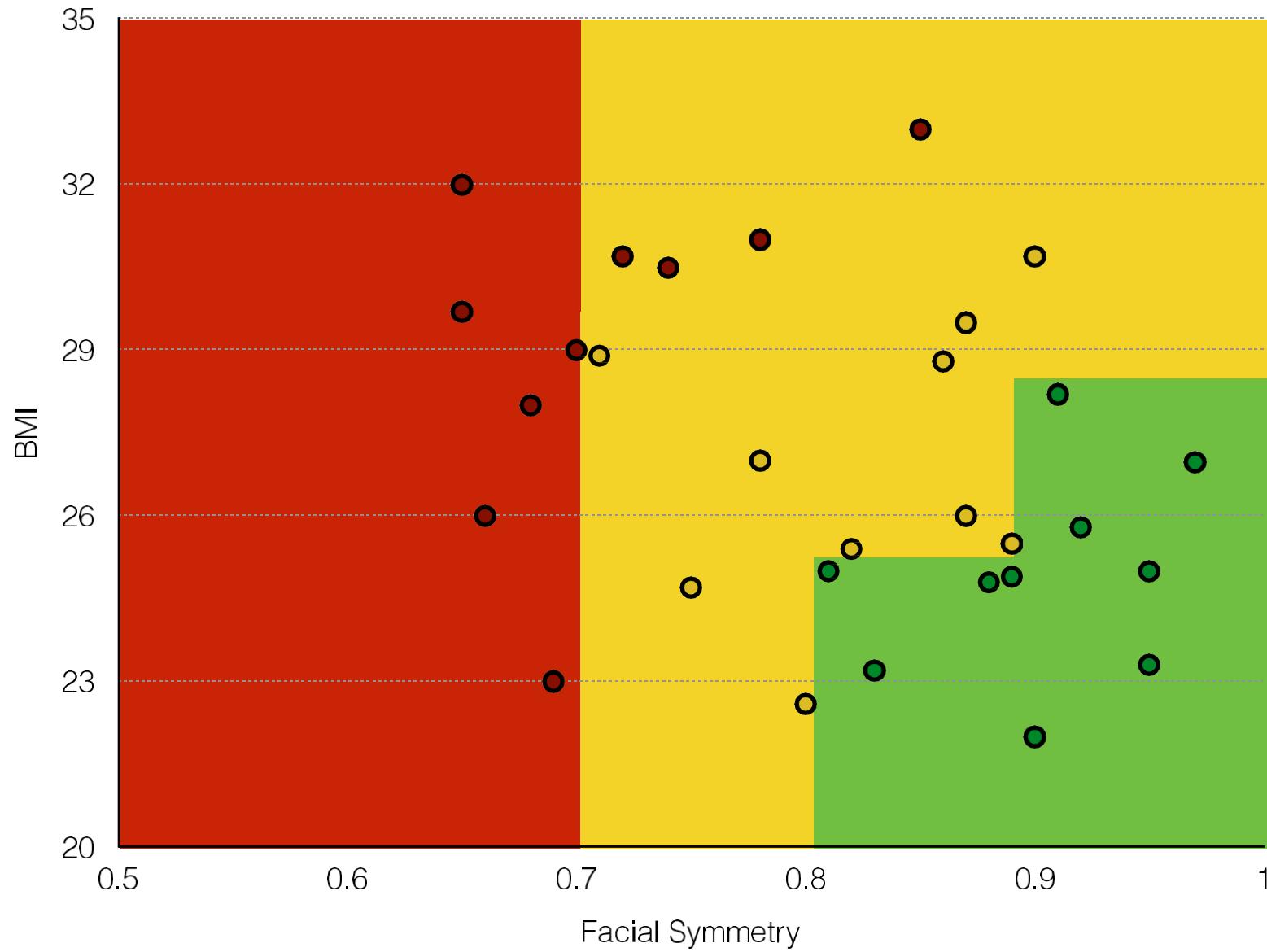
[att, ave, un]

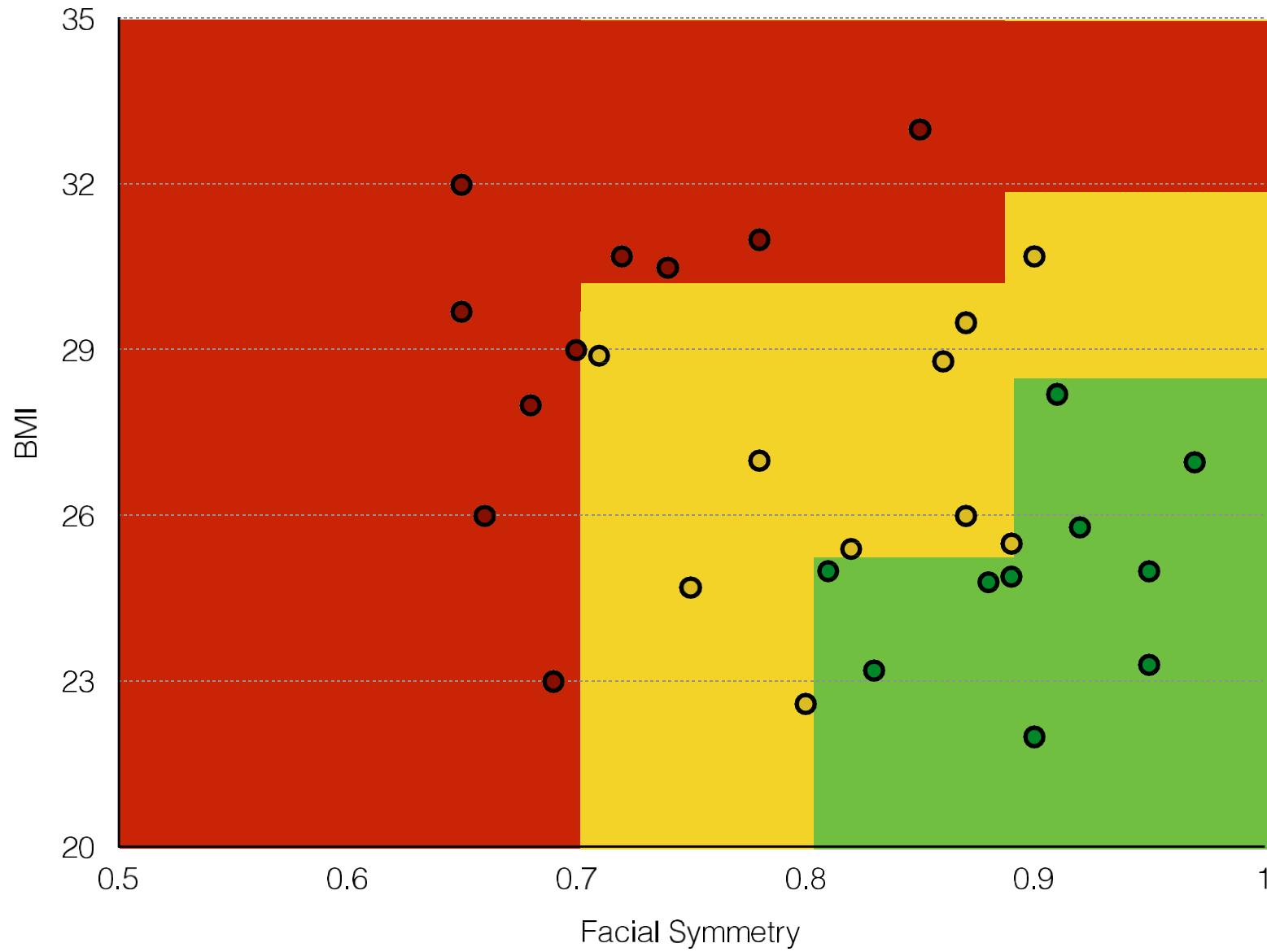


[att, ave, un]









# K-nearest Neighbor







	<b>Number of Relationships</b>	<b>Grade of First Relationship</b>
sample a	3	7
sample b	6	11
sample c	3	9
sample d	5	10

# **Euclidean Distance**

point a = [a<sub>1</sub>, a<sub>2</sub>]

point b = [b<sub>1</sub>, b<sub>2</sub>]

# **Euclidean Distance**

point a = [a<sub>1</sub>, a<sub>2</sub>]

point b = [b<sub>1</sub>, b<sub>2</sub>]

Two dimensions (features)

$$\sqrt{(a_1 - b_1)^2 + (a_2 - b_2)^2}$$

# **Euclidean Distance**

Feature Vector

$$a = [3, 7]$$

$$b = [6, 11]$$

## **Euclidean Distance**

$$\sqrt{(3-6)^2 + (7-11)^2}$$

Feature Vector

$$a = [3, 7]$$

$$b = [6, 11]$$

## **Euclidean Distance**

$$\sqrt{(3-6)^2 + (7-11)^2}$$

Feature Vector

$$a = [3, 7]$$

$$b = [6, 11]$$

$$\sqrt{(-3)^2 + (-4)^2}$$

## **Euclidean Distance**

$$\sqrt{(3-6)^2 + (7-11)^2}$$

Feature Vector

$$a = [3, 7]$$

$$b = [6, 11]$$

$$\sqrt{(-3)^2 + (-4)^2}$$

$$\sqrt{9+16}$$

## **Euclidean Distance**

$$\sqrt{(3-6)^2 + (7-11)^2}$$

Feature Vector

$$a = [3, 7]$$

$$b = [6, 11]$$

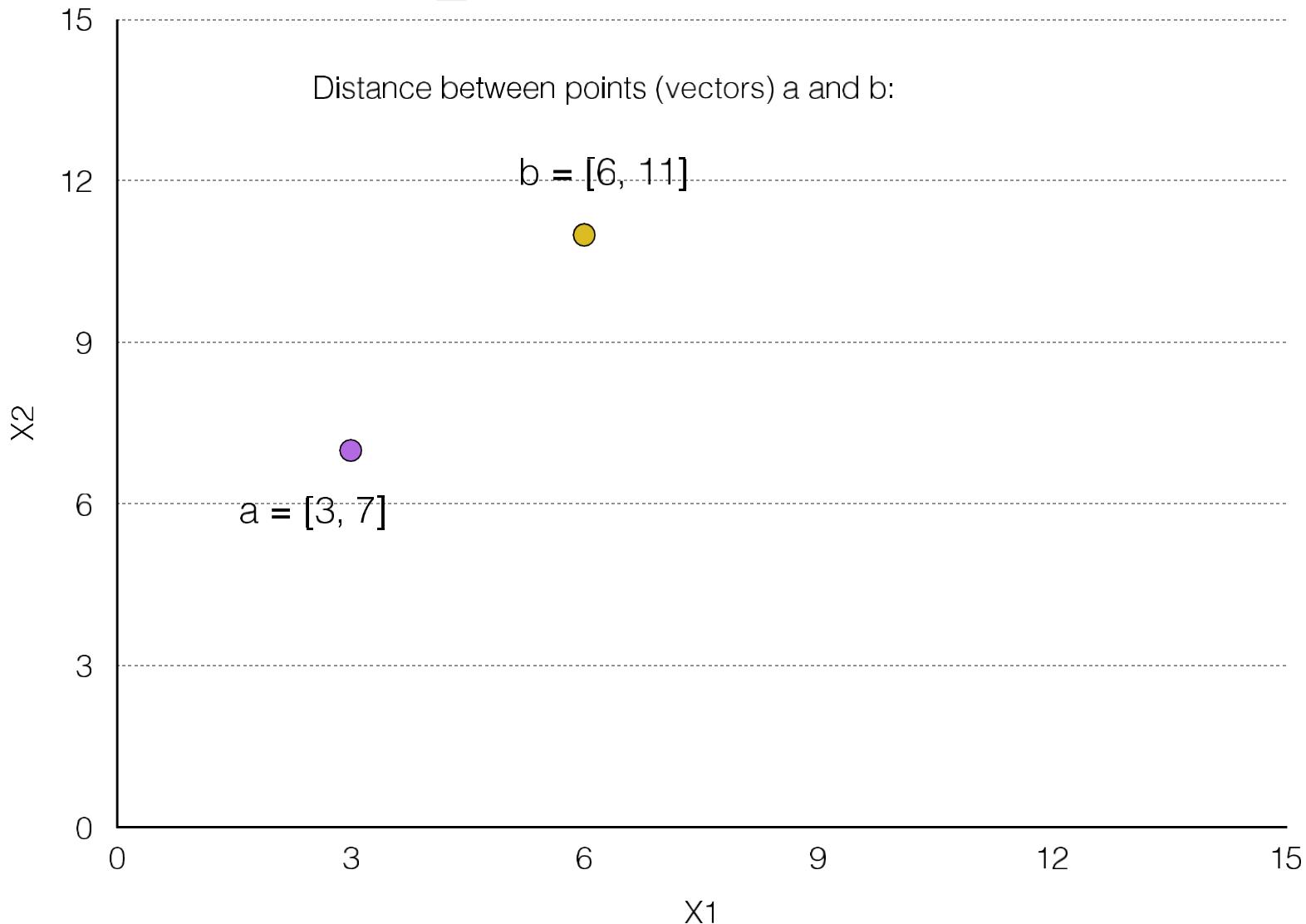
$$\sqrt{(-3)^2 + (-4)^2}$$

$$\sqrt{9+16}$$

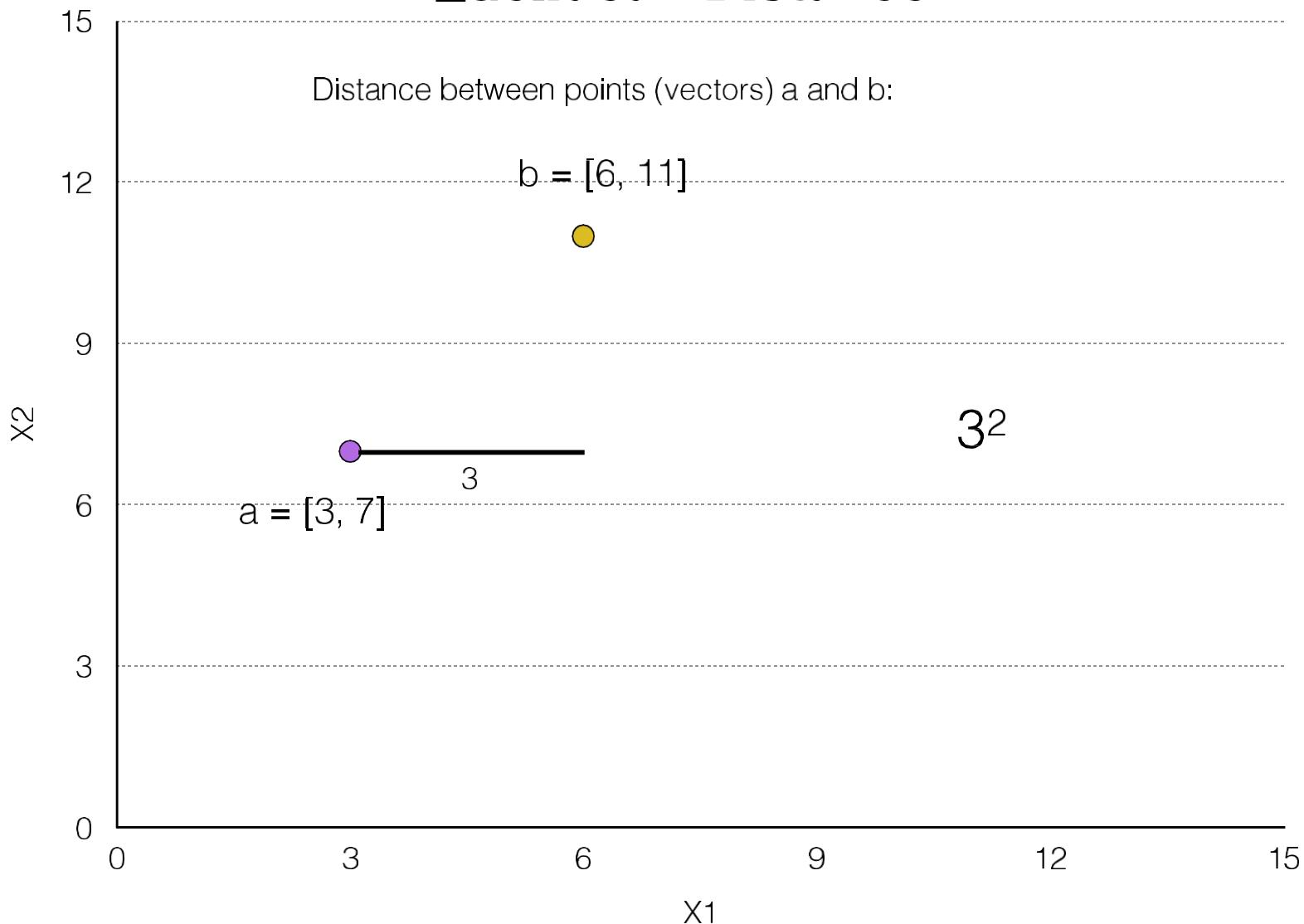
Distance between points (vectors) a and b:

$$\sqrt{25} = 5$$

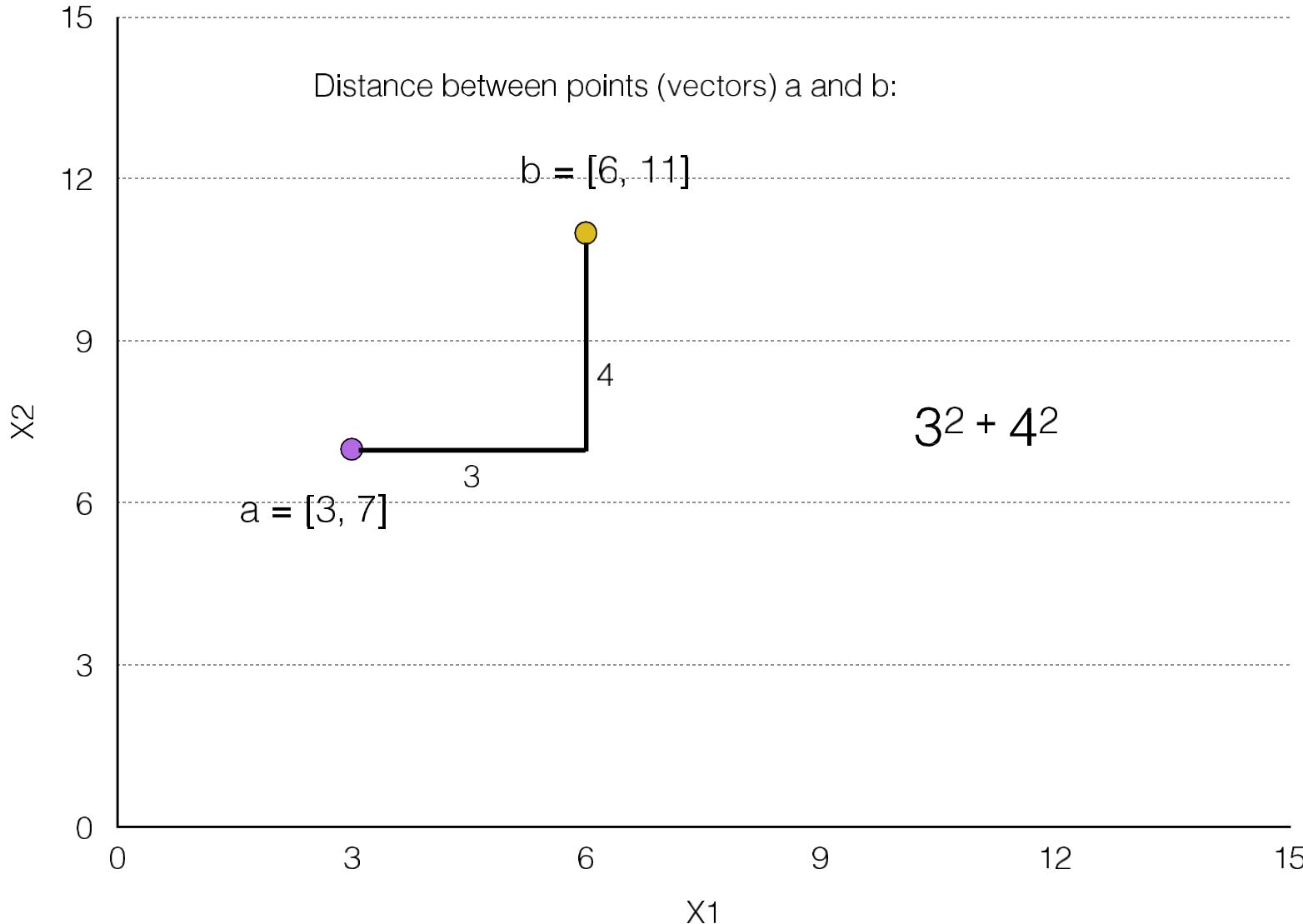
# Euclidean Distance



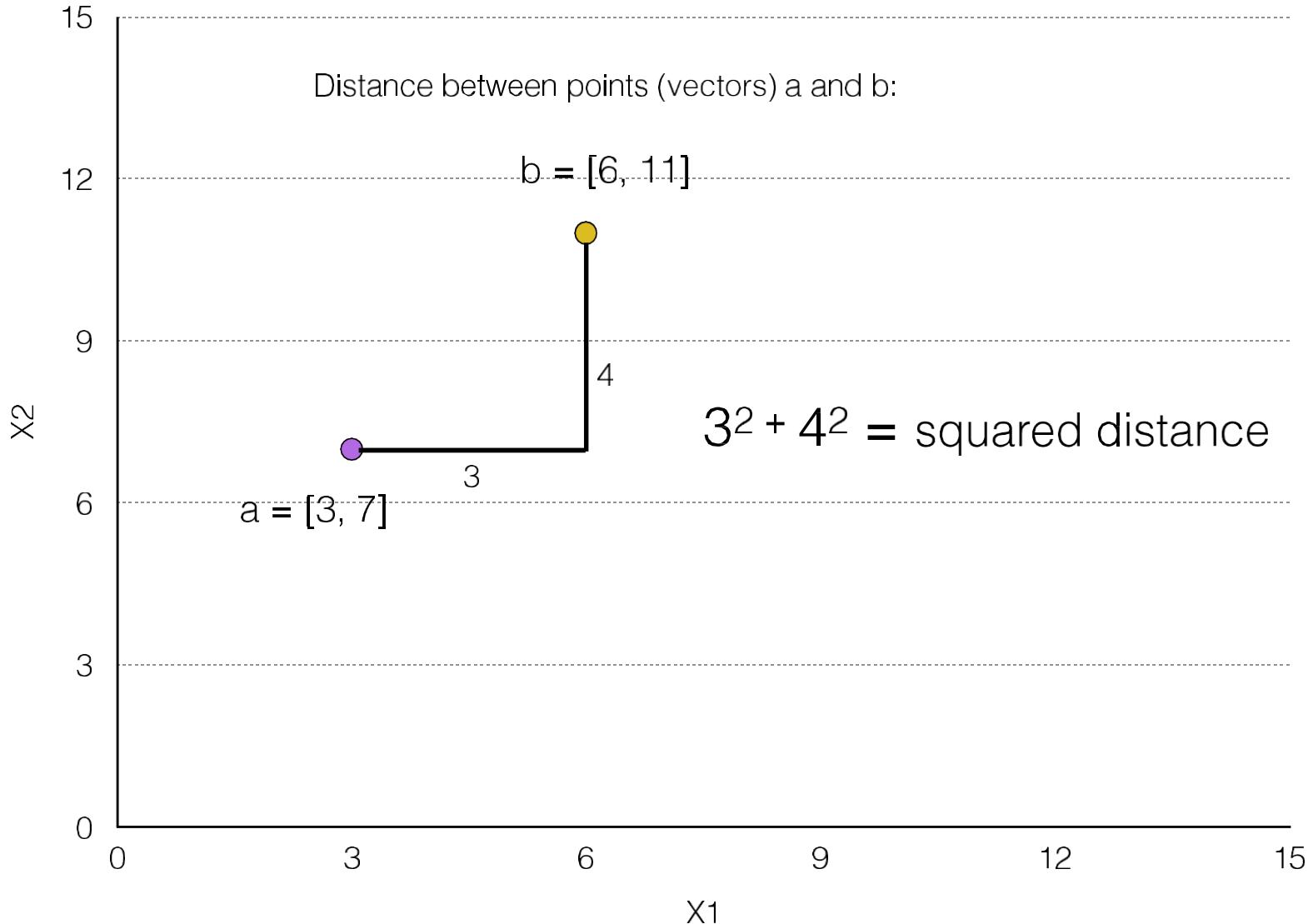
# Euclidean Distance



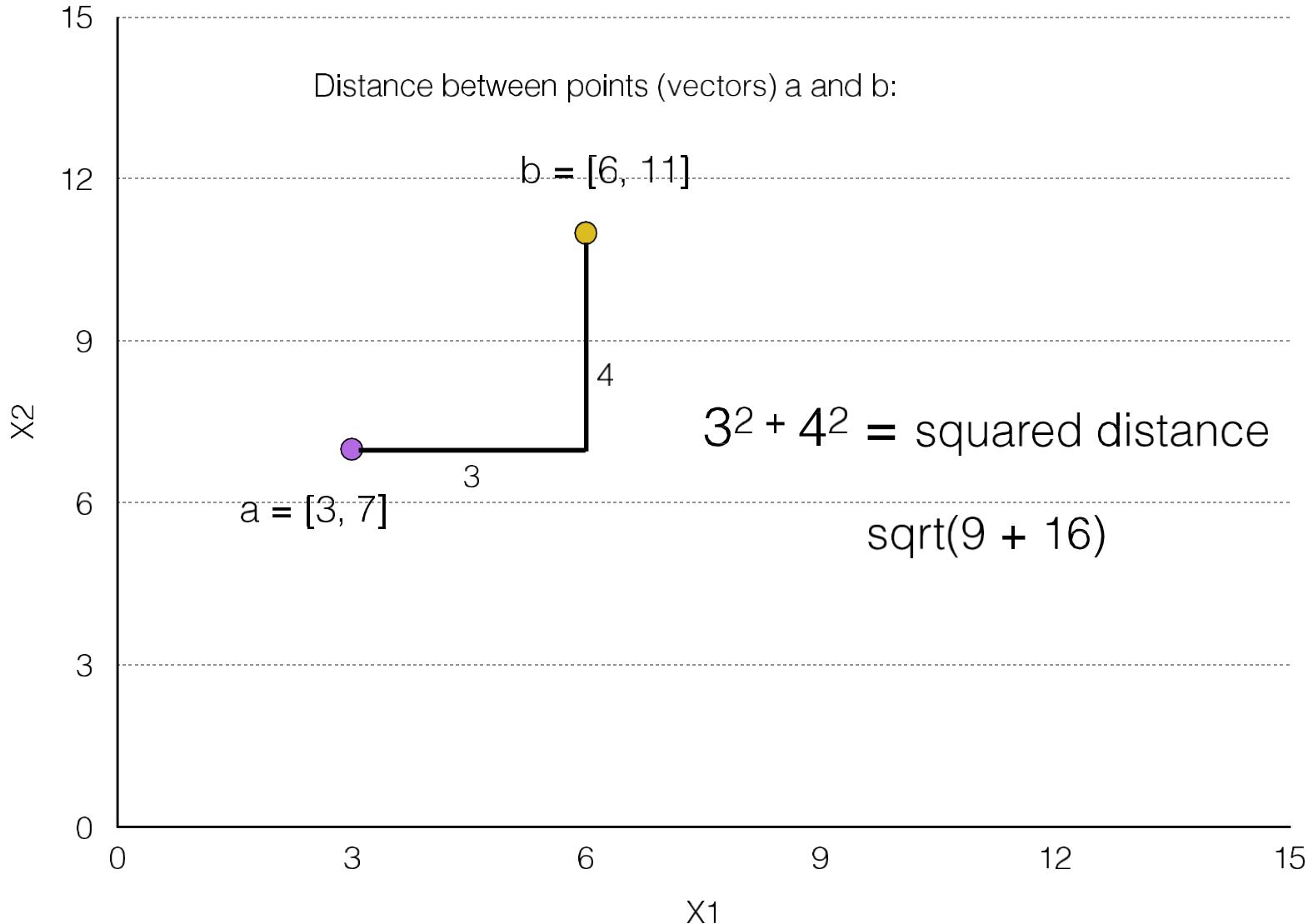
# Euclidean Distance



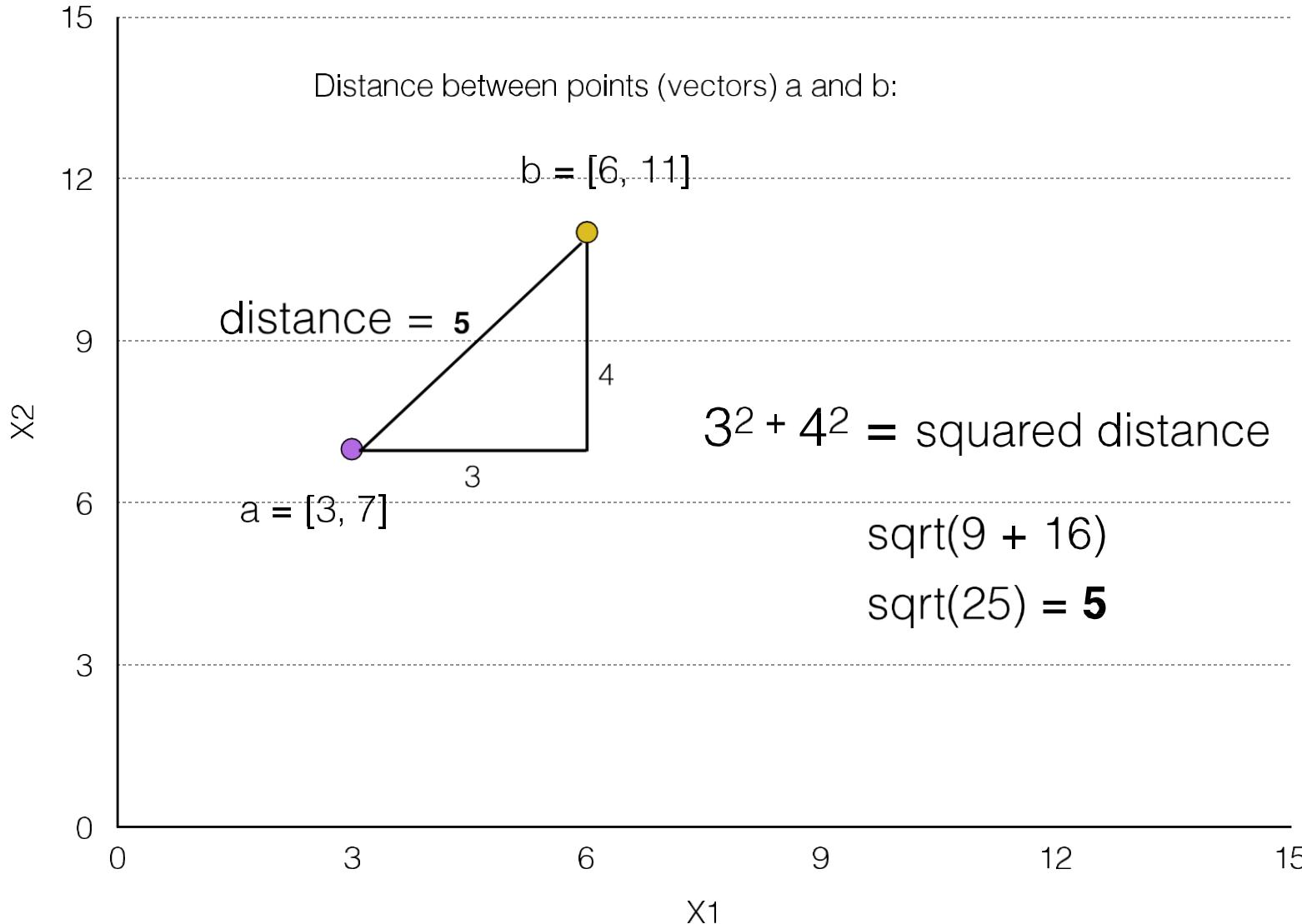
# Euclidean Distance



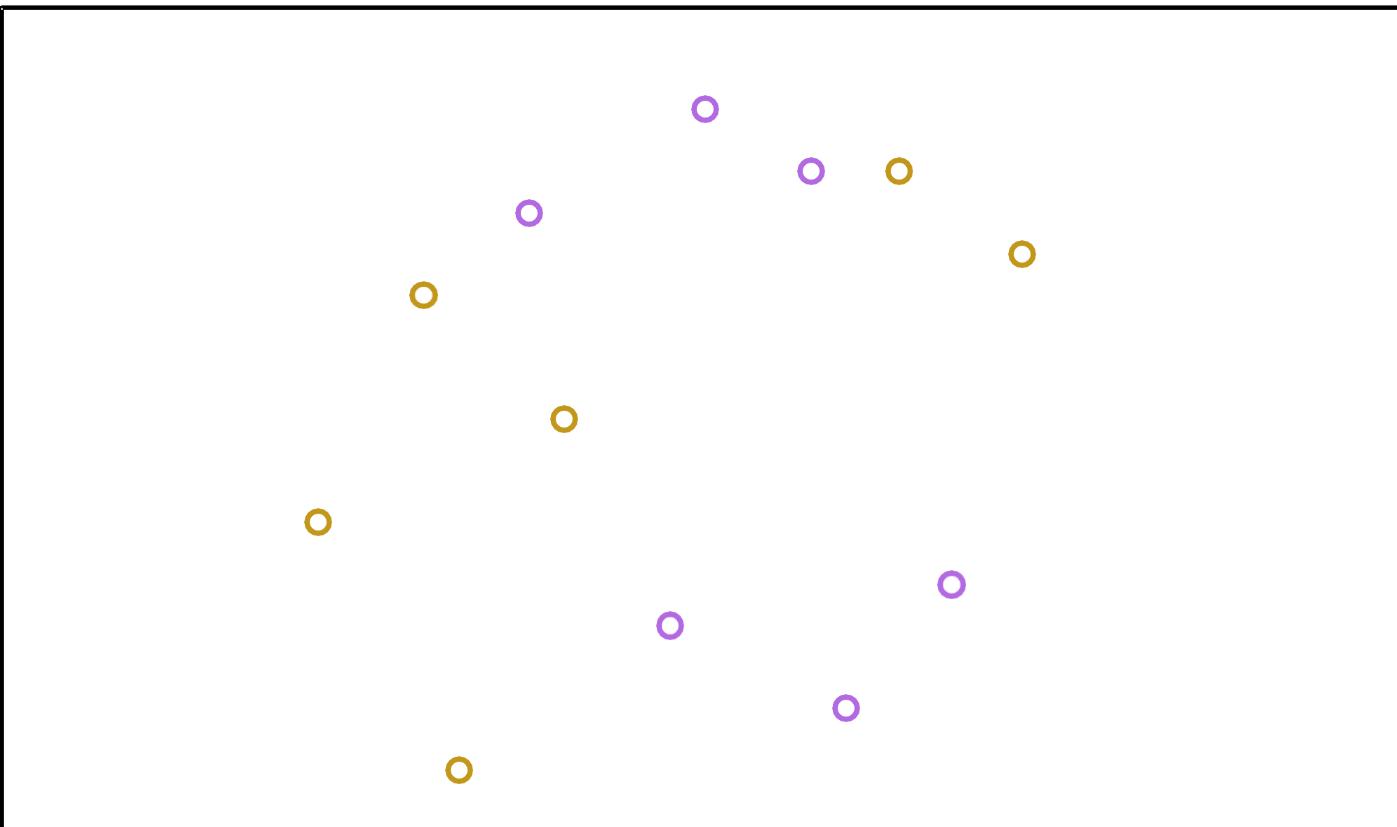
# Euclidean Distance



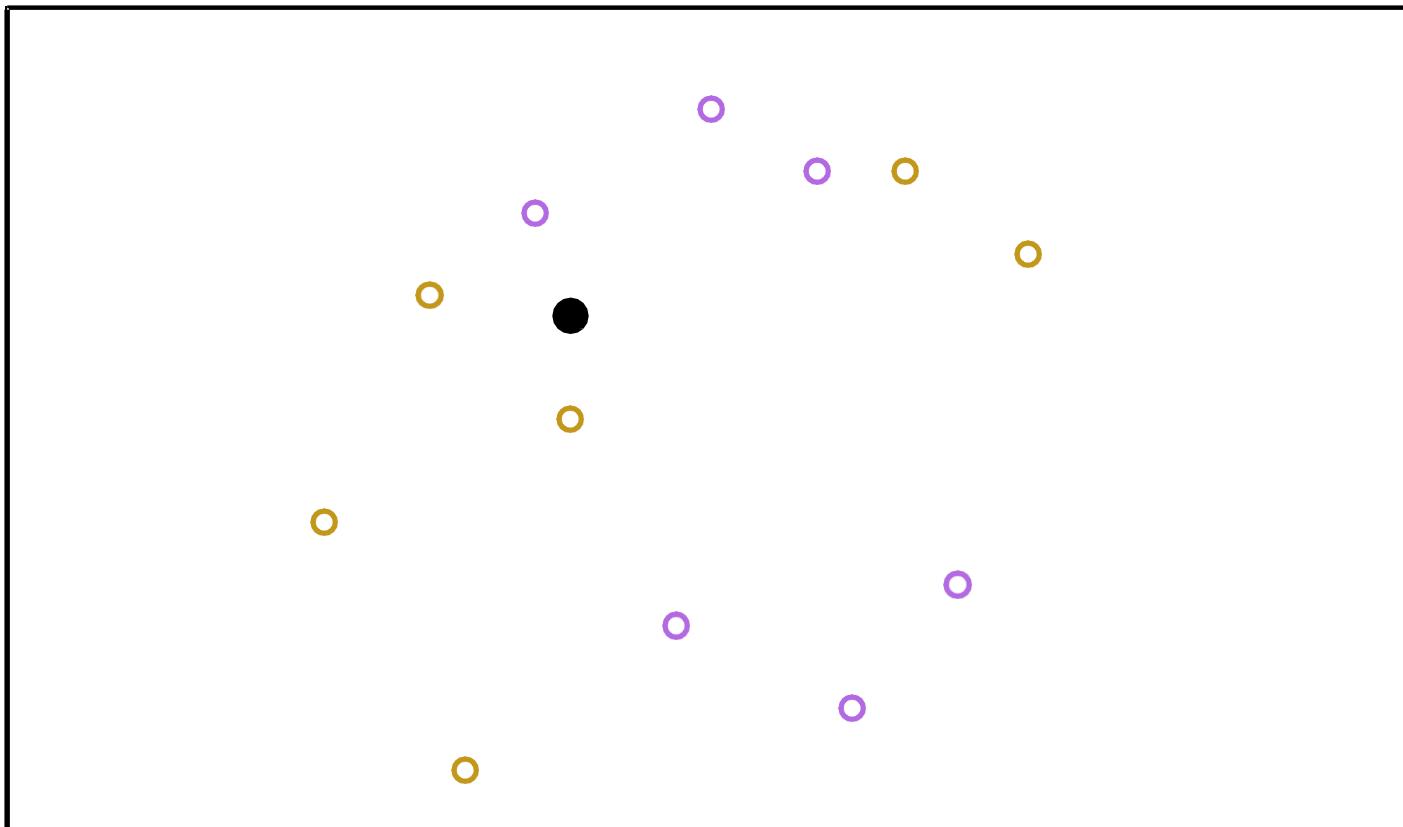
# Euclidean Distance



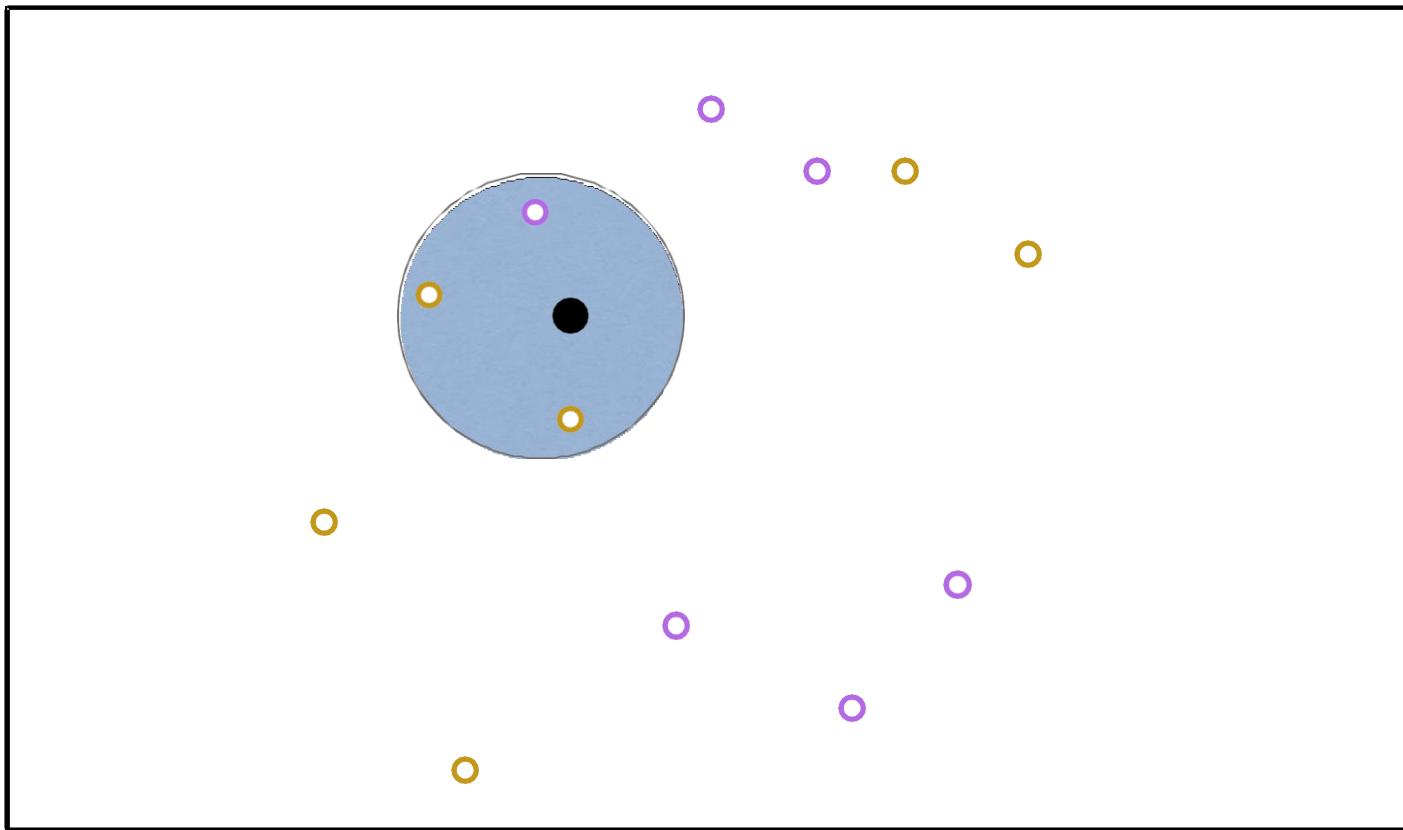
# K-nearest Neighbor



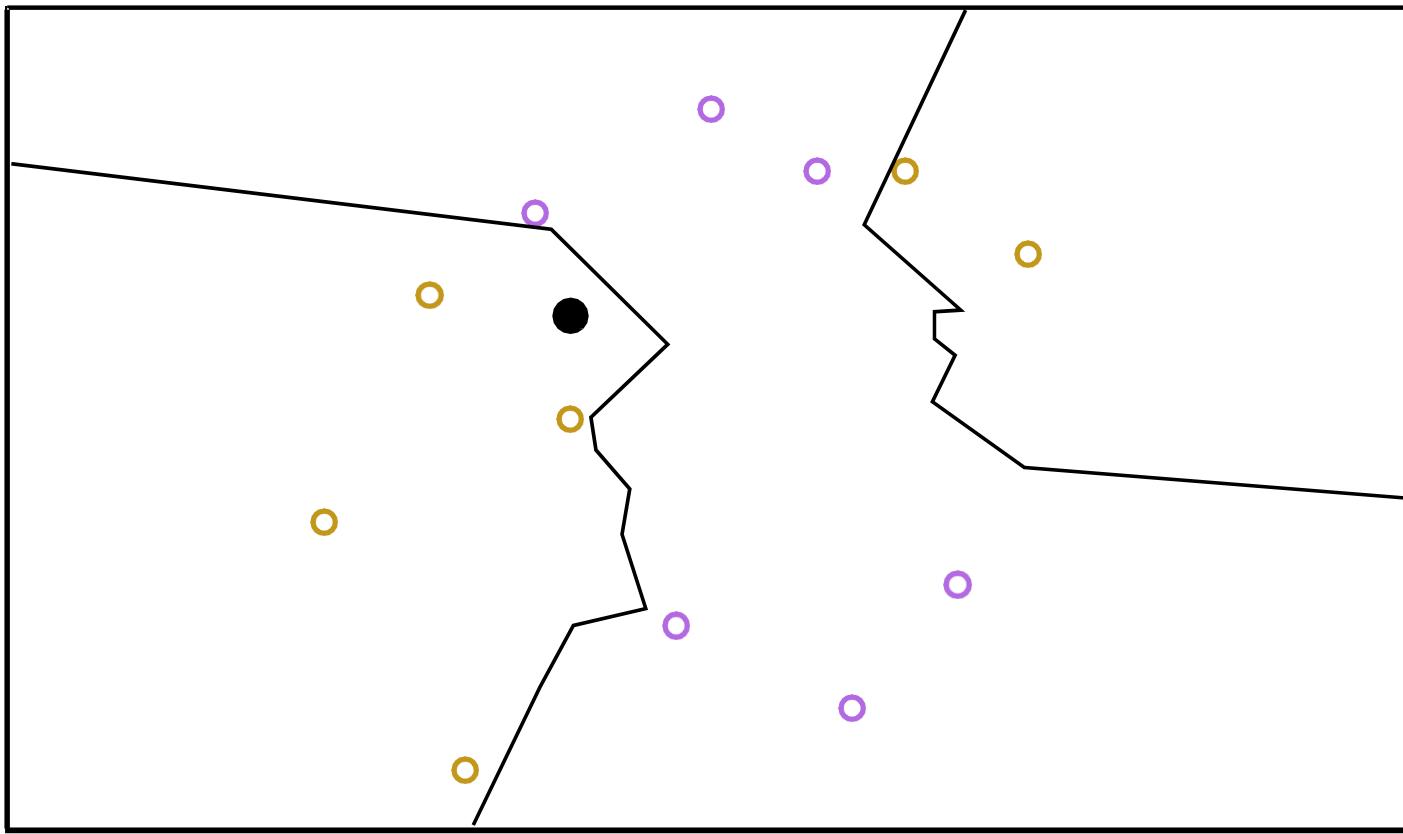
# K-nearest Neighbor



**K = 3**



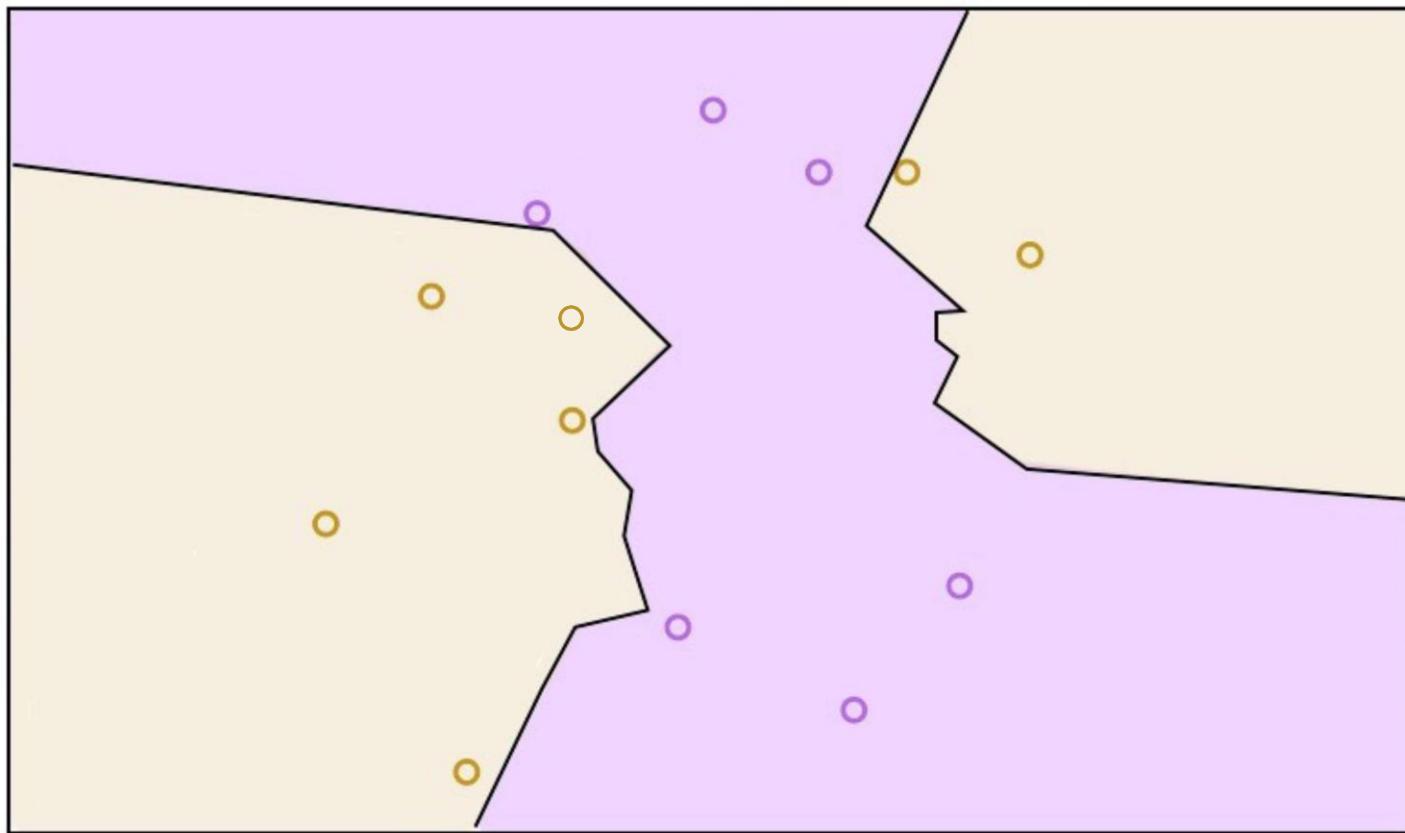
**K = 3**



● Stays together

○ Breaks up

**K = 3**



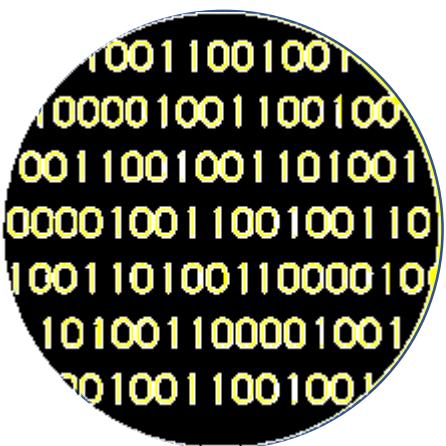
# Scikit-learn

Model.**fit(X\_train,y\_train)**

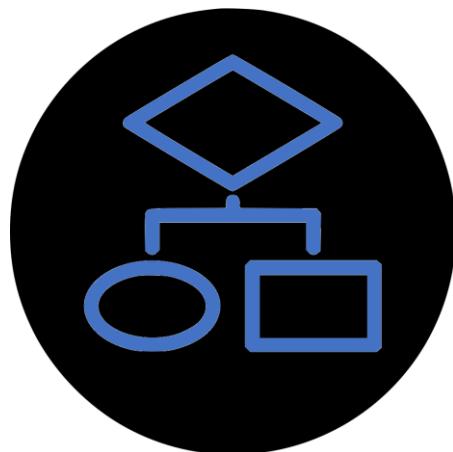
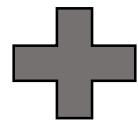
Model.**predict(X\_test)**

Model.**score(X\_test,y\_test)**

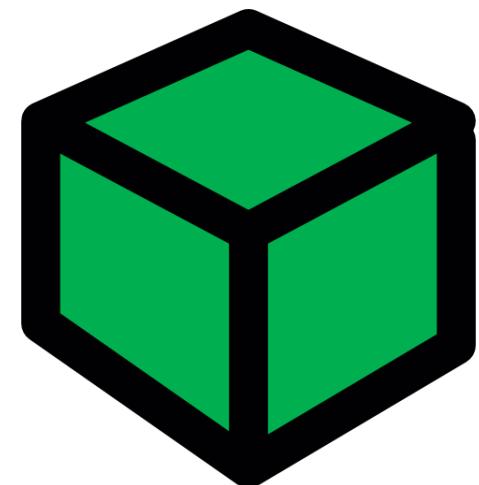
`Model.fit(X_train,y_train)`



**TRAIN DATA**

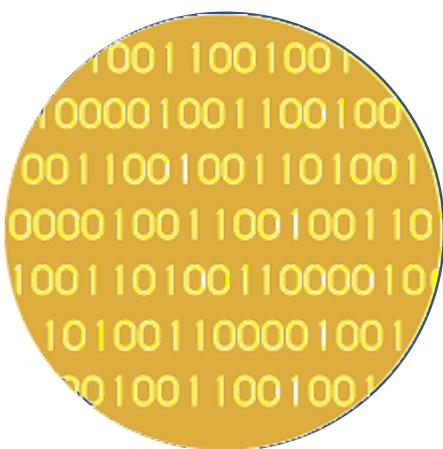


**ALGORITHM**



**MODEL**

# Model. predict(x\_test)

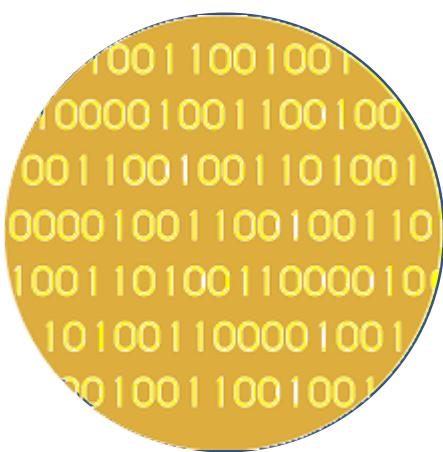


**TEST DATA**

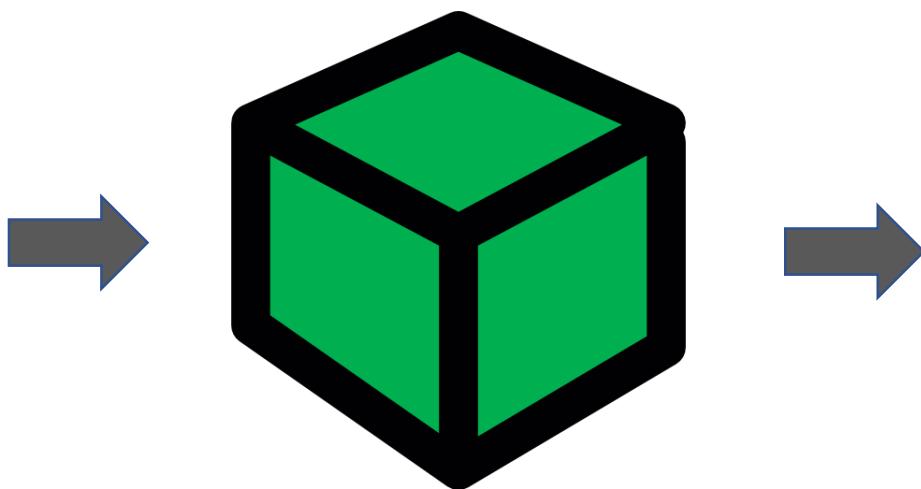


Prediction
0
1
0
0
1
0

# Model. score(X\_test)



TEST DATA



MODEL

Prediction	Label
0	1
1	1
0	0
0	1
1	0
0	0