

Q1.

If Feature 5 \leq 0.5:

```
-----→Yes: If Feature 1  $\leq$  420000.0:
|      -----→Yes: If Feature 17  $\leq$  2506.0:
|      |      -----→Yes: If Feature 2  $\leq$  1.0:
.
.
.
-----→No: If Feature 5  $\leq$  1.0:
      -----→Yes: If Feature 6  $\leq$  2.0:
      |      -----→Yes: If Feature 10  $\leq$  2.0:
```

Q2.

Training and test error is: 42%.

The errors I detect is to compare the predict label and true label to decide if it is an error.

Q3.

After 1 round: 4%

After 2 round: 7%

Q4.

Age is the most salient and prominent feature.

```
/*
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 */

import java.io.BufferedReader;
import java.io.File;
import java.io.FileReader;
import java.io.IOException;
import java.util.ArrayList;
import java.util.LinkedList;
import java.util.ListIterator;
import java.util.PriorityQueue;

public class ID3DT {

    // set variables
    static LinkedList<double[]> trainList;
    static LinkedList<double[]> testList;
    static Node root;
    static String tabs;
    public static void main(String[] args) throws IOException {

        // open file and read data from pa2train.
        File trainFile = new File("/Users/Jason/Desktop/ID3/src/pa2train.txt");
        BufferedReader rtrain = new BufferedReader(new FileReader(trainFile));
        // call function to collect data from file
        trainList = collectData(rtrain);
        //System.out.print("Read from train file is: " + trainList);
```

```

// set a root for tree
root = new Node( -1, -1.0, -1.0, null, null);
/*
System.out.println("Now the list is: " );
for( int i = 0; i < trainList.size(); i++){
    for( int j = 0; j < trainList.get(i).length; j++){
        System.out.print(trainList.get(i)[j] + " ");
    }
    System.out.println(" ");
}
*/
// call function to build tree based on our list and root
tabs = " ";
//System.out.println("Start building tree");
root = buildTree(trainList, root);
//System.out.println("Build done");

File testFile = new File("/Users/Jason/Desktop/ID3/src/pa2test.txt");
BufferedReader rtest = new BufferedReader(new FileReader(testFile));
testList = collectData(rtest);
/*
for( int i = 0; i < testList.size(); i++){
    for(int j = 0; j < testList.get(i).length; j++){
        System.out.print(testList.get(i)[j] + " ");
    }
    System.out.println(" ");
}
*/
int errorCount = 0;
for (int i = 0; i < testList.size(); i++)
{
    double[] currentData = testList.get(i);
    double predict = Stats(root, currentData);
    if (predict != currentData[4])
    {
        errorCount++;
    }
}

System.out.println("Dataset Size: " + testList.size());
System.out.println("Error Count: " + errorCount);
System.out.println("Percent Error: " + 100*(errorCount/((float)testList.size())) + "%");
}

private static double Stats(Node node, double[] dataLine) {
    if (node.lchild == null && node.rchild == null) {
        return node.feature;
    }

    if (dataLine[node.feature] <= node.threshold) {
        return Stats(node.lchild, dataLine);
    } else {
        return Stats(node.rchild, dataLine);
    }
}

// function to build tree
public static Node buildTree( LinkedList<double[]> list, Node root ){

    // check if all node has same label (pure already)
    //int label_idx = 22;

    /*

```

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System.out.println("alist is: ");
for( int i = 0; i < alist.length; i ++ ){
    System.out.print(alist[i]);
}
*/
// use for loop to check if all label same
//System.out.println("In buildTree function");
boolean pure = true;
int label_idx = 22;
double[] alist = list.get(0);

for(int i = 1; i < list.size(); i++) {
    double[] reflat = list.get(i);
    if (alist[label_idx] != reflat[label_idx]) {
        pure = false;
    }
    alist = reflat;
}

// if result
//If it's pure, return
//System.out.println("Pure is: " + pure);
if (pure == true)
{
    System.out.println("Predict " + (int)alist[label_idx]);
    root.setLabel(alist[label_idx]);
    root.setFeature((int)alist[label_idx]);
    return root;
}

/*
System.out.println("Now the list is: ");
for( int i = 0; i < list.size(); i++ ){
    for( int j = 0; j < list.get(i).length; j++){
        System.out.print(list.get(i)[j] + " ");
    }
    System.out.println(" ");
}
*/
// Sort each feature ( 0 - 21 : 22) to get new list
//System.out.println("sort for 0");
LinkedList<double[]> f0 = sort_list(list, 0);
/*
System.out.println("After sorting f0, the list is: ");
for( int i = 0; i < f0.size(); i++ ){
    for( int j = 0; j < f0.get(i).length; j++){
        System.out.print(f0.get(i)[j] + " ");
    }
    System.out.println(" ");
}
*/

//System.out.println("sort for 1");
LinkedList<double[]> f1 = sort_list(list, 1);

/*
System.out.println("After sorting f1, the list is: ");
for( int i = 0; i < f1.size(); i++ ){
    for( int j = 0; j < f1.get(i).length; j++){
        System.out.print(f1.get(i)[j] + " ");
    }
    System.out.println(" ");
}
*/

//System.out.println("sort for 2");
LinkedList<double[]> f2 = sort_list(list, 2);
LinkedList<double[]> f3 = sort_list(list, 3);

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LinkedList<double[]> f4 = sort_list(list, 4);
LinkedList<double[]> f5 = sort_list(list, 5);
LinkedList<double[]> f6 = sort_list(list, 6);
LinkedList<double[]> f7 = sort_list(list, 7);
LinkedList<double[]> f8 = sort_list(list, 8);
LinkedList<double[]> f9 = sort_list(list, 9);
LinkedList<double[]> f10 = sort_list(list, 10);
LinkedList<double[]> f11 = sort_list(list, 11);
LinkedList<double[]> f12 = sort_list(list, 12);
LinkedList<double[]> f13 = sort_list(list, 13);
LinkedList<double[]> f14 = sort_list(list, 14);
LinkedList<double[]> f15 = sort_list(list, 15);
LinkedList<double[]> f16 = sort_list(list, 16);
LinkedList<double[]> f17 = sort_list(list, 17);
LinkedList<double[]> f18 = sort_list(list, 18);
LinkedList<double[]> f19 = sort_list(list, 19);
LinkedList<double[]> f20 = sort_list(list, 20);
LinkedList<double[]> f21 = sort_list(list, 21);

/*
System.out.println("After sorting f6, the list is: ");
for( int i = 0; i < f6.size(); i++) {
    for( int j = 0; j < f6.get(i).length; j++){
        System.out.print(f6.get(i)[j] + " ");
    }
    System.out.println(" ");
}
*/

// calculate the possible threshold list and decide the threshold
//  $IG(Z) = H(X) - H(X|Z)$ 
// get threshold and place
//System.out.println("Start threshold");
double[] igThres0 = target_ig(f0, 0);
/*
System.out.println("IG: " + igThres0[0]);
System.out.println("Place: " + igThres0[1]);
*/
double[] igThres1 = target_ig(f1, 1);
//System.out.println("IG1: " + igThres0[0]);
//System.out.println("Place1: " + igThres0[1]);
double[] igThres2 = target_ig(f2, 2);
double[] igThres3 = target_ig(f3, 3);
//System.out.println("IG3: " + igThres0[0]);
//System.out.println("Place3: " + igThres0[1]);
double[] igThres4 = target_ig(f4, 4);
double[] igThres5 = target_ig(f5, 5);
double[] igThres6 = target_ig(f6, 6);
double[] igThres7 = target_ig(f7, 7);
double[] igThres8 = target_ig(f8, 8);
double[] igThres9 = target_ig(f9, 9);
double[] igThres10 = target_ig(f10, 10);
double[] igThres11 = target_ig(f11, 11);
double[] igThres12 = target_ig(f12, 12);
double[] igThres13 = target_ig(f13, 13);
double[] igThres14 = target_ig(f14, 14);
double[] igThres15 = target_ig(f15, 15);
double[] igThres16 = target_ig(f16, 16);
double[] igThres17 = target_ig(f17, 17);
double[] igThres18 = target_ig(f18, 18);
double[] igThres19 = target_ig(f19, 19);
double[] igThres20 = target_ig(f20, 20);
double[] igThres21 = target_ig(f21, 21);

// compare each threshold and decide which one will be used first
LinkedList<double[]> threshlist = f0;
double threshold = igThres0[1];

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```
int axis = 0;
//System.out.println("ig0: " + igThres0[0]);
double IG = igThres0[0];

if (IG < igThres1[0])
{
    //System.out.println("in 1");
    axis = 1;
    IG = igThres1[0];
    threshlist = f1;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres1[1];
}

if (IG < igThres2[0])
{
    //System.out.println("in 2");
    axis = 2;
    IG = igThres2[0];
    threshlist = f2;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres2[1];
}

if (IG < igThres3[0])
{
    //System.out.println("in 3");
    axis = 3;
    IG = igThres3[0];
    threshlist = f3;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres3[1];
}

if (IG < igThres4[0])
{
    //System.out.println("in 4");
    axis = 4;
    IG = igThres4[0];
    threshlist = f4;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres4[1];
}

if (IG < igThres5[0])
{
    //System.out.println("in 5");
    axis = 5;
    IG = igThres5[0];
    threshlist = f5;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres5[1];
}

if (IG < igThres6[0])
{
    //System.out.println("in 6");
    axis = 6;
    IG = igThres6[0];
    threshlist = f6;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres6[1];
}

if (IG < igThres7[0])
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{
    //System.out.println("in 7");
    axis = 7;
    IG = igThres7[0];
    threshlist = f7;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres7[1];
}

if (IG < igThres8[0])
{
    //System.out.println("in 8");
    axis = 8;
    IG = igThres8[0];
    threshlist = f8;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres8[1];
}

if (IG < igThres9[0])
{
    //System.out.println("in 9");
    axis = 9;
    IG = igThres9[0];
    threshlist = f9;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres9[1];
}

if (IG < igThres10[0])
{
    //System.out.println("in 10");
    axis = 10;
    IG = igThres10[0];
    threshlist = f10;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres10[1];
}

if (IG < igThres11[0])
{
    //System.out.println("in 11");
    axis = 11;
    IG = igThres11[0];
    threshlist = f11;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres11[1];
}

if (IG < igThres12[0])
{
    //System.out.println("in 12");
    axis = 12;
    IG = igThres12[0];
    threshlist = f12;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres12[1];
}

if (IG < igThres13[0])
{
    //System.out.println("in 13");
    axis = 13;
    IG = igThres13[0];
    threshlist = f13;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres13[1];
}

```

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}

if (IG < igThres14[0])
{
    //System.out.println("in 14");
    axis = 14;
    IG = igThres14[0];
    threshlist = f14;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres14[1];
}

if (IG < igThres15[0])
{
    //System.out.println("in 15");
    axis = 15;
    IG = igThres15[0];
    threshlist = f15;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres15[1];
}

if (IG < igThres16[0])
{
    //System.out.println("in 16");
    axis = 16;
    IG = igThres16[0];
    threshlist = f16;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres16[1];
}

if (IG < igThres17[0])
{
    //System.out.println("in 17");
    axis = 17;
    IG = igThres17[0];
    threshlist = f17;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres17[1];
}

if (IG < igThres18[0])
{
    //System.out.println("in 18");
    axis = 18;
    IG = igThres18[0];
    threshlist = f18;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres18[1];
}

if (IG < igThres19[0])
{
    //System.out.println("in 19");
    axis = 19;
    IG = igThres19[0];
    threshlist = f19;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres19[1];
}

if (IG < igThres20[0])
{
    //System.out.println("in 20");
    axis = 20;
    IG = igThres20[0];
    threshlist = f20;
    //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
    threshold = igThres20[1];
}

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    }
    if (IG < igThres21[0])
    {
        //System.out.println("in 21");
        axis = 21;
        IG = igThres21[0];
        threshlist = f21;
        //System.out.println("Now threshold is: " + threshlist.get((int)threshold)[axis]);
        threshold = igThres21[1];
    }

    // draw
    LinkedList left_half = new LinkedList(threshlist.subList(0, (int)threshold+1));
    LinkedList right_half = new LinkedList(threshlist.subList((int)threshold+1, threshlist.size()));

    //5. Load the threshold and axis into the node we were passed as an argument
    root.threshold = threshlist.get((int)threshold)[axis];
    root.feature = axis;

    //6. Create the two child nodes,
    root.lchild = new Node(-1, -1.0, -1.0, null, null);
    root.rchild = new Node(-1, -1.0, -1.0, null, null);

    //7. make the recursive calls, interlacing them with the prints
    System.out.println("If Feature " + (root.feature+1) + " <= " + root.threshold + ":");
    tabs = tabs + "\t";
    System.out.print(tabs + "-----> Yes: ");
    tabs = tabs + "|";
    root.lchild = buildTree(left_half, root.lchild); //one priority queue
    if (tabs.length() > 1) tabs = tabs.substring(0, tabs.length()-1);
    System.out.print(tabs + "-----> No: ");
    root.rchild = buildTree(right_half, root.rchild); //one priority queue
    if (tabs.length() > 1) tabs = tabs.substring(0, tabs.length()-1);
    //8. Return the node we were passed.
    return root;
}

// function to calculate threshold
private static double[] target_ig(LinkedList<double[]> dataList, int feature)
{
    //System.out.println("In threshold function");
    //System.out.println("The passed in list is: ");
    /*
    for(int i = 0; i < dataRange.size(); i++){
        for(int j = 0; j < dataRange.get(i).length; j++){
            System.out.print(dataRange.get(i)[j] + " ");
        }
        System.out.println(" ");
    }
    */
    // set variables for threshold
    double threshold = 0.0;
    double info_gain = -1.0;
    int idx = 0;

    // use loop to calculate the H
    for (int i = 0; i < dataList.size() - 2; i++)
    {
        int num0left = 0;
        int num1left = 0;

        int j;
        for (j = 0; j <= i; j++)
        {
            int curr_label = (int)dataList.get(j)[22];
            if (curr_label == 0)
            {

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        num0left++;
    }
    else
    {
        num1left++;
    }
}

int num0right = 0;
int num1right = 0;

for (; j < dataList.size() - 1; j++)
{
    int curr_label = (int)dataList.get(j)[22];
    if (curr_label == 0)
    {
        num0right++;
    }
    else
    {
        num1right++;
    }
}

//calculate conditional entropy
double PL = (num0left + num1left) / (double)(dataList.size());
double PR = (num0right + num1right) / (double)(dataList.size());

double P0L = (num0left / (double)(dataList.size())) / PL;
double P1L = (num1left / (double)(dataList.size())) / PL;

double P0R = (num0right / (double)(dataList.size())) / PR;
double P1R = (num1right / (double)(dataList.size())) / PR;

double log0, log1;
if (P0L == 0)
    log0 = 0;
else
    log0 = Math.log(P0L);
if (P1L == 0)
    log1 = 0;
else
    log1 = Math.log(P1L);

double entropyL = -(P0L * log0) - (P1L * log1);

if (P0R == 0)
    log0 = 0;
else
    log0 = Math.log(P0R);
if (P1R == 0)
    log1 = 0;
else
    log1 = Math.log(P1R);

double entropyR = -(P0R * log0) - (P1R * log1);

double condEntro = (PL * entropyL) + (PR * entropyR);

//get normal entropy
double pr0 = (num0left + num0right) / (double)(dataList.size());
double pr1 = (num1left + num1right) / (double)(dataList.size());

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        if (pr0 == 0)
            log0 = 0;
        else
            log0 = Math.log(pr0);
        if (pr1 == 0)
            log1 = 0;
        else
            log1 = Math.log(pr1);

        double origEntro = -(pr0 * log0) - (pr1 * log1);

        //get temporary information gain
        double tempInfoGain = origEntro - condEntro;

        //System.out.println("tempInfoGain: " + tempInfoGain);
        //System.out.println(" dataList.size(): " + dataList.size() + ", prR: " + prR);
        // check if need to update
        if (tempInfoGain > info_gain)
        {
            info_gain = tempInfoGain;
            threshold = dataList.get(i)[feature];
            idx = i;
        }
    }

    return (new double[] {(double) (info_gain), (double) (idx)});

}

// function to sort list as index of feature
public static LinkedList<double[]> sort_list( LinkedList<double[]> list, int index ){

    // at the ending of recursion, end
    if (list.size() <= 1)
        return list;

    // get the middle of index
    //System.out.println("In sort_list");
    //System.out.println("The size is: " + list.size());
    int mid_idx = list.size() / 2;
    //System.out.println("The middle index is: " + mid_idx);
    double[] middle = list.get(mid_idx);
    /*
    for( int i = 0; i < middle.length; i++ ){
        System.out.print(middle[i] + " ");
    }
    System.out.println(" ");
    */
    // add back to list later
    list.remove(mid_idx);

    // set two list to split list
    LinkedList<double[]> left = new LinkedList();
    LinkedList<double[]> right = new LinkedList();

    // for loop to sort list
    for(int i = 0; i < list.size(); i++)
    {
        // case add to left
        if (list.get(i)[index] <= middle[index])
        {
            left.add(list.get(i));
        }
        // case add to right
    }
}

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        else {
            right.add(list.get(i));
        }

    }

    // recursion to sort each half again
    left = sort_list(left, index);
    right = sort_list(right, index);

    // add middle back
    left.add(middle);

    // for loop to add right to left
    for(int j = 0; j < right.size(); j++)
    {
        left.add(right.get(j));
    }

    return left;
}

// class for root
public static class Node{

    // set variables
    private int feature;
    private double threshold;
    private double label;
    private Node lchild;
    private Node rchild;

    public Node(){

    }

    public Node( int feature, double threshold, double label, Node lchild, Node rchild){
        this.feature = feature;
        this.threshold = threshold;
        this.label = label;
        this.lchild = lchild;
        this.rchild = rchild;
    }

    public double getFeature() {
        return feature;
    }

    public void setFeature(int feature) {
        this.feature = feature;
    }

    public double getThreshold() {
        return threshold;
    }

    public void setThreshold(double threshold) {
        this.threshold = threshold;
    }

    public double getLabel() {
        return label;
    }

    public void setLabel(double label) {
        this.label = label;
    }
}

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    }

    public Node getLchild() {
        return lchild;
    }

    public void setLchild(Node lchild) {
        this.lchild = lchild;
    }

    public Node getRchild() {
        return rchild;
    }

    public void setRchild(Node rchild) {
        this.rchild = rchild;
    }
}

// function to read data from file
public static LinkedList<double[]> collectData(BufferedReader br) throws IOException{
    // set a return value
    LinkedList<double[]> dataList = new LinkedList<double[]>();

    // read one line each time
    String st;
    while( (st = br.readLine()) != null){

        // set a array to store each number in line splited by whitespace
        String readLine[] = st.split("\\s");
        // get length of readLine
        int nof = readLine.length;
        // set a array to store each element in integer
        double[] readVec = new double[nof];
        // transfer String to integer
        for( int i = 0; i < nof; i++){
            // transfer
            readVec[i] = Double.parseDouble(readLine[i]);
        }
        // this line is done, collect all integer data
        dataList.add(readVec);

    }
    // return dataList
    return dataList;
} // collectData done
}

```