

$$g-c = g-L * \frac{\partial Q}{\partial c} = g-L$$

$$g-d = g-L * \frac{\partial Q}{\partial d} = g-L$$

$$g-a = g-L * \frac{\partial Q}{\partial a} = g-L * b$$

$$g-b = g-L * \frac{\partial Q}{\partial b} = g-L * a$$

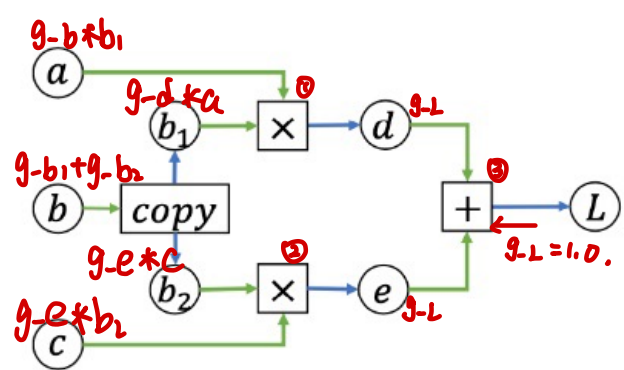
$$Q = c + d$$

$$\frac{\partial Q}{\partial c} = 1$$

$$Q = a \times b$$

$$\frac{\partial Q}{\partial a} = b$$

$$\frac{\partial Q}{\partial b} = a$$



$$Q = a \times b_1$$

$$\frac{\partial Q}{\partial a} = b_1, \quad \frac{\partial Q}{\partial b_1} = a$$

$$g-a = g-L * \frac{\partial Q}{\partial a} = g-L * b_1$$

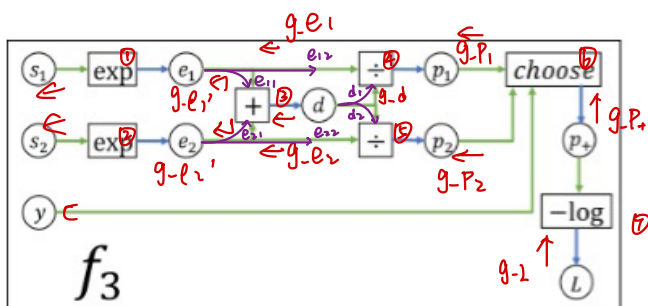
$$g-b_1 = g-L * \frac{\partial Q}{\partial b_1} = g-L * a$$

$$Q = b_2 \times c$$

$$\frac{\partial Q}{\partial b_2} = c, \quad \frac{\partial Q}{\partial c} = b_2$$

$$g-b_2 = \frac{\partial Q}{\partial b_2} * g-L = c * g-L$$

$$g-c = \frac{\partial Q}{\partial c} * g-L = b_2 * g-L$$



$$Q = -\log P_+$$

$$\frac{\partial Q}{\partial P_+} = -\frac{1}{P_+ \cdot \ln 10}$$

$$g-P_+ = \frac{\partial Q}{\partial P_+} * (g-L)$$

$$g-P_+ = \frac{-g-L}{P_+ \cdot \ln 10}$$

$$Q = P_1 (2-y) - P_2 (1-y)$$

$$= P_1 (2-y) + P_2 (y-1)$$

$$g-P_2 = g-P_+ * \frac{\partial Q}{\partial P_2}$$

$$= g-P_+ * (y-1)$$

$$g-P_1 = g-P_+ * \frac{\partial Q}{\partial P_1}$$

$$= g-P_+ * (2-y)$$

$$Q = e_1 / d$$

$$g-e_1 = g-P_1 * \frac{\partial Q}{\partial e_1}$$

$$= g-P_1 * \frac{1}{d}$$

$$g-d = g-P_1 * \frac{\partial Q}{\partial d}$$

$$= g-P_1 * e_1 * (-1) * (d^{-2})$$

$$Q = e_2 / d$$

$$g-e_2 = g-P_2 * \frac{\partial Q}{\partial e_2}$$

$$= g-P_2 * \frac{1}{d}$$

$$g-d = g-P_2 * \frac{\partial Q}{\partial d}$$

$$= g-P_2 * e_2 * (-1) * (d^{-2})$$

$$g-d = g-P_1 * e_1 + g-P_2 * e_2$$

$$Q = e^{s_1}$$

$$g-s_1 = \frac{\partial Q}{\partial s_1} * g-e_1 = e^{s_1} * g-e_1$$

f3 : (required - 10 points)

y is an integer equal to either 1 or 2. You don't need to compute a gradient for y.

The \div nodes compute $p_1 = e_1/d$ and $p_2 = e_2/d$.

The choose node outputs p_1 if $y = 1$, and outputs p_2 if $y = 2$.

$$\sigma = e^{S_2}$$

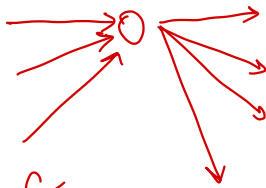
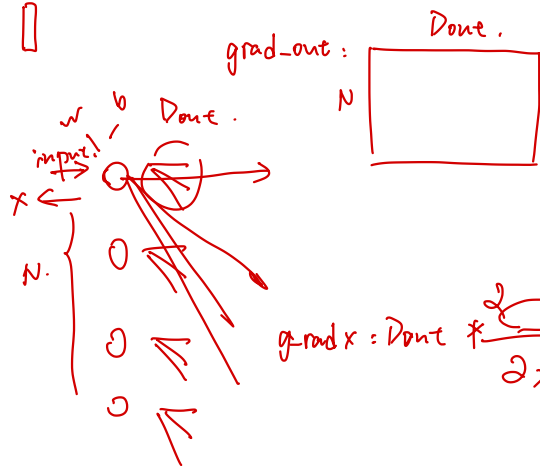
$$g_{-S_2} = \frac{\partial \sigma}{\partial S_2} * g_{-L_2} = e^{S_2} * g_{-L_2}$$

$$g_{-y} = g_{-P_+} * \frac{\partial \sigma}{\partial y}$$

$$= g_{-P_+} * (-P_1 + P_2)$$

$$\begin{matrix} \times \\ \text{Din} \end{matrix} \begin{matrix} \times \\ \text{Dout} \\ \text{Din} \end{matrix} = \begin{matrix} \times \\ \text{Dout} \end{matrix} \quad \Rightarrow \quad \begin{matrix} \square \\ \text{Din} \\ \times \end{matrix} \times \begin{matrix} \times \\ \text{Din} \end{matrix} = \square$$

$$b = \begin{matrix} \text{Dout.} \\ \text{Dout.} \\ \text{Dout.} \\ \text{Dout.} \end{matrix} \quad \left. \vphantom{\begin{matrix} \text{Dout.} \\ \text{Dout.} \\ \text{Dout.} \\ \text{Dout.} \end{matrix}} \right\} N.$$



$$\begin{matrix} 0.4 & 0.2 & 0.3 & 0.1 \\ \uparrow & \uparrow & \uparrow & \uparrow \\ \text{Din} & \text{Din} & \text{Din} & \text{Din} \end{matrix} \quad \text{non-linear} \quad \text{output} = X \cdot W + b.$$

$$\frac{\partial \text{output}}{\partial w} = x \quad \begin{matrix} \text{Din} \\ N \end{matrix}$$

$$g\text{-rad-}w = \text{grad-out} * \frac{\partial \sigma}{\partial w}$$

$$\frac{\partial \text{output}}{\partial x} = w$$

$$\text{grad-x} = \text{grad-out} * \frac{\partial \text{output}}{\partial x}$$

$$\begin{matrix} \text{Dout.} \\ N \end{matrix}$$

$$\begin{matrix} \text{Dout} \\ \text{Din} \end{matrix} \quad \begin{matrix} \text{Dout} \\ N \end{matrix}$$

$$\begin{matrix} N \times \text{Din} \\ \text{Dout.} \\ N \end{matrix}$$

$$g_{\text{out}} = g_{\text{in}} * f$$

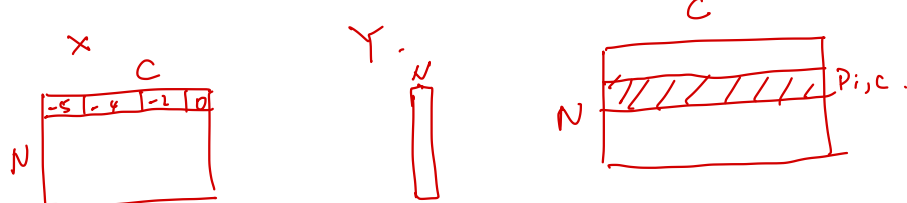
$$y = x * f$$

$$g_{-x} = \text{grad-out} * f$$

$$\text{grad-y} = \text{grad-out} * 1$$

$$\begin{matrix} \text{Dout.} \\ N \end{matrix}$$

$$\begin{matrix} \text{Dout.} \\ N \end{matrix}$$



$$L = -\frac{1}{N} \sum_{i=1}^N \log(P)$$

$$\frac{e^{x_{j,c}}}{\sum_{j=1}^C e^{x_j}}$$

$$\frac{\partial L}{\partial x} = -\frac{1}{N} \sum_{i=1}^N \frac{1}{P} \cdot \frac{\partial P}{\partial x} \quad j=c.$$

$$J(W) = \frac{\lambda}{2} \sum_i W_i^2$$

$$\frac{\partial J(W)}{\partial W_i} = \frac{\lambda}{2} \cdot \frac{1}{1} \cdot 2 \cdot W_i = \lambda W_i$$

