



- a. (5 pts) How many times smaller would a chip containing the same number of transistors be?
- b. (5 pts) How many transistors would a chip of the original size be able to contain?
4. [20 points] **Boolean Equations:** You are an employee at Bamazon, a company that ships many products to its customers. Packages can be small, heavy, and/or expensive. Your location has 4 trucks, each specialized to carry different combinations of packages. Write Boolean equations to represent the packages each truck is specialized to carry using the encodings:  $s$  for small,  $h$  for heavy, and  $e$  for expensive
- a. (5pts) Truck 1 is specialized to carry all packages that are both small and light (i.e. not heavy), but also packages that are expensive, small, and heavy.  $sh' + esh$
- b. (5pts) Truck 2 is specialized to carry packages that are large (i.e. not small) and inexpensive (i.e. not expensive), but also packages that are heavy and expensive.  $s'e' + he$
- c. (5pts) Truck 3 is specialized to carry packages that are large, light, and inexpensive, but also packages that are both small and expensive.  $s'h'e' + se$
- d. (5pts) Oh no! Truck 4 broke down and you need to buy a new truck. Write a Boolean equation that describes what packages your other three trucks *cannot* carry so you can buy a truck to carry the other packages.  $sh'(e'+e) + esh + s'e'(h'+h) + he(s'+s) + s'h'e' + se(h'+h)$
5. [10 points] **Circuit Drawing:** please draw a circuit diagram using an appropriate combination of logical gates (i.e. AND, OR, NOT XOR, NAND, NOR, or XNOR) for the following boolean equations.
- a. (5 pts)  $s = c_{in} \oplus (a \oplus b)$   $= sh'e' + sh'e + she + s'h'e' + s'he' + s'he + she + s'h'e'$
- b. (5 pts)  $c_{out} = ab + bc_{in} + ac_{in}$   $100 \ 101 \ 111 \ 000 \ 010 \ 011 \ 111 \ 000$
- c. (Optional: bonus points) If you wanted to implement both equations, could you manipulate the boolean equations to use less logical gates than a straightforward implementation of the above equations? Explain. (hint: think if there are partial results that could be shared by both equations.)
- $s \ h \ e \ 100, 101, 111, 000, 010, 011$   
 $m_4 \ m_5 \ m_7 \ m_0 \ m_2 \ m_3$   
 $m_1 + m_6$   
 $001 \ 110$   
 $s'h'e' + she'$

