

EECS 280 - Lecture 21

Auto, Maps, Range-Based For Loops

Reminders/Updates

Check [EECS280.org](https://eeecs280.org) for updates

Project 5 is due Monday June 20th at 8pm

- BST and Map done by Tuesday June 13th

- main.cpp done by Monday June 20th

Final Exam - Thursday June 23 4-6pm

Lab Tomorrow!

Optional Special Topics
Lecture Monday June 20th

AI, machine learning, and
cognitive science!

Agenda

Functors Review

Containers Review

- BSTs

- Sets

- Maps

C++ Shortcuts

Recursion Practice

Review

Classes - we define our own type and its behavior

Iterator - a class that acts like a pointer

-overloaded *, ++, !=

Functors - a class that acts like a function

-overloaded ()

Types of Functions/Functors

Predicate - takes an input and returns a bool

ex) isEven, isNegative

Comparator - Takes in two objects and returns true if the first object is less than the second object

ex) less

<https://onlinegdb.com/pg0gaCUON>

Functor Exercise

Write a functor that prints out an element to cout that can be used with this `for_each` function.

```
template <typename Iter_t, typename Func_t>
Func_t for_each(Iter_t begin, Iter_t end, Func_t func) {
    for (Iter_t it = begin; it != end; ++it) {
        func(*it);
    }
    return func;
}
```

Printer Functor Solution

```
template <typename T>
class Printer {
public:
    void operator()(const T &n) const {
        cout << n;
    }
};
```

```
int main(){
    list<int> lis; //fill with numbers

    for_each(lis.begin(), lis.end(),
Printer<int>());
}
```

How to modify Printer so it can use any stream?

```
template <typename T>
class Printer {

public:

    void operator()(const T &n) const {
        cout << n;
    }

};
```

Hint: Which of the following should you add?

- a. Member variable
- b. constructor
- c. Destructor
- d. operator*
- e. Multiple of above

How to modify Printer so it can use any stream?

```
template <typename T>
class Printer {
    ostream &os;
public:
    Printer(ostream &os_in) : os(os_in) {}
    void operator()(const T &n) const {
        os << n;
    }
};
```

Hint: Which of the following should you add?

- a. Member variable
- b. constructor
- c. Destructor
- d. operator*
- e. Multiple of above

How to modify Printer so it can use any stream?

```
template <typename T>
class Printer {
    ostream &os;
public:
    Printer(ostream &os_in) : os(os_in)
    {}

    void operator()(const T &n) const {
        os << n; }
};
```

```
int main(){
    list<int> lis; //fill with numbers
    ofstream fout("list.out");
    for_each(lis.begin(), lis.end(),
        Printer<int>(fout));
}
```

Agenda

Functors Review

Containers Review

- BSTs**

- Sets

- Maps

C++ Shortcuts

Recursion Practice

Review: Containers - holds elements

- Arrays
- Vectors
- Unordered_Set
- Sorted_Set
- List
- **Binary Search Tree (BST)**

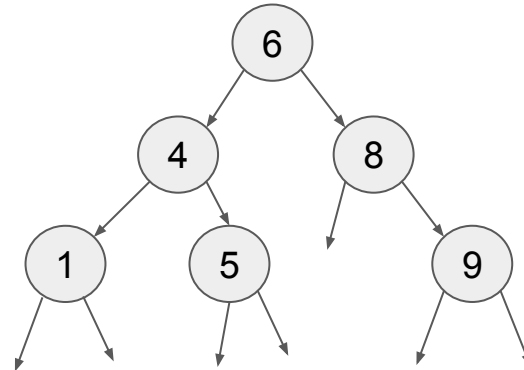
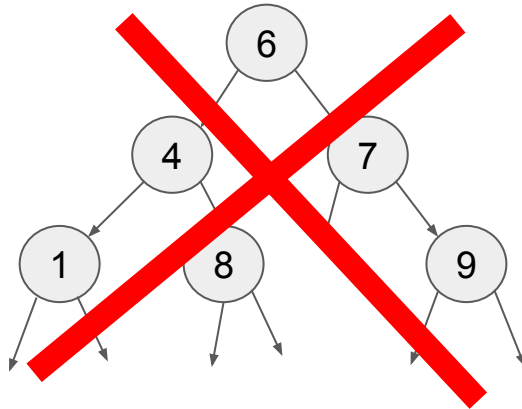
... many more!

Has things like:

- Insert (push_front, push_back...)
- Contains
- Size
- Remove
- Iterators

Review: Binary Search Trees (BSTs)

- A tree whose subtrees are also binary search trees
- Every element in the left subtree is strictly less than the root datum
- Every element in the right subtree is strictly greater than the root datum



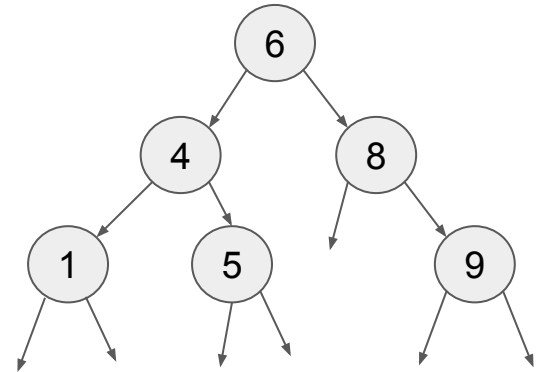
Binary Search Tree Interface

```
template <typename T>
class BinarySearchTree {
public:
    BinarySearchTree();
    BinarySearchTree(const BinarySearchTree &other);
    BinarySearchTree & operator=(const BinarySearchTree &other);
    ~BinarySearchTree();

    bool empty() const;
    int size() const;
    bool contains(const T &item) const;
    void insert(const T &item);

private:
    struct Node {
        T datum;
        Node *left, *right;
    };

    Node *root;
};
```



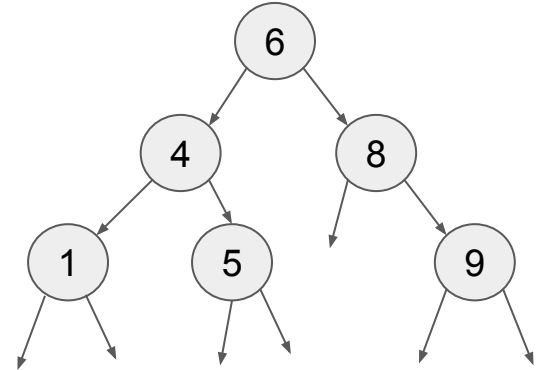
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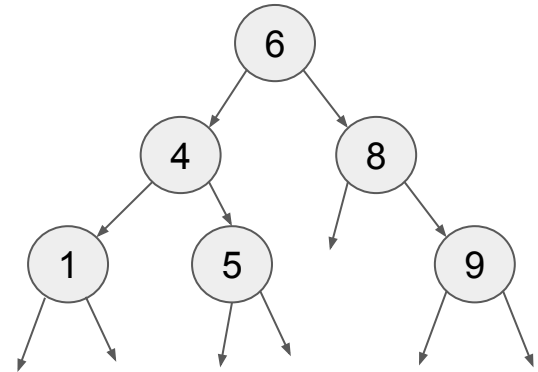


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};
```



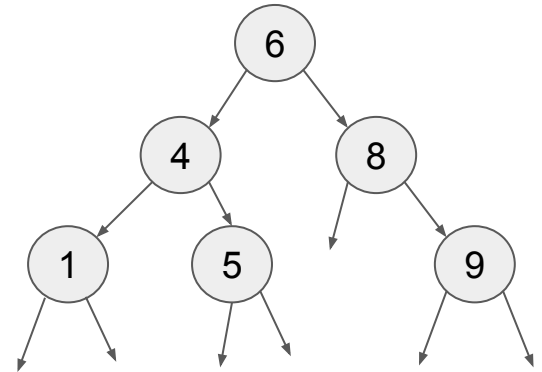
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private:
    struct Node {
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};
```



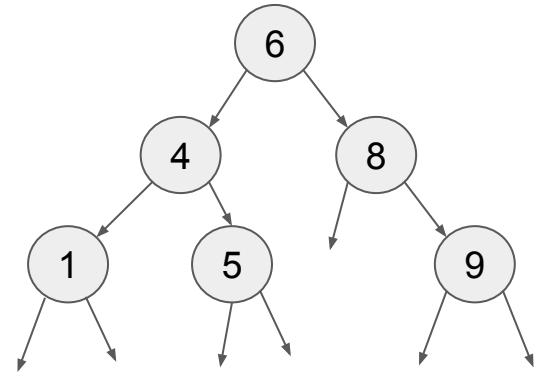
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    Node *root;
};
```



Agenda

Functors Review

Containers Review

- BSTs

- Sets**

- Maps

C++ Shortcuts

Recursion Practice

Review: Containers - holds elements

- Arrays
- Vectors
- **Unordered_Set**
- **Sorted_Set**
- List
- Binary Search Tree (BST)

... many more!

Has things like:

- Insert (push_front, push_back...)
- Contains
- Size
- Remove
- Iterators

Partner: What is a set?

Review: Containers - holds elements

- Arrays
- Vectors
- **Unordered_Set**
- **Sorted_Set**
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- Binary Search Tree (BST)

... many more!

Has things like:

- Insert (push_front, push_back...)
- Contains
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- Remove
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Partner: What is a set?

Set - holds only unique items

Set Efficiency

Function	Unsorted_Set	Sorted_Set
size	$O(1)$	$O(1)$
contains	$O(n)$	$O(\log n)$
insert	$O(n)$	$O(n)$

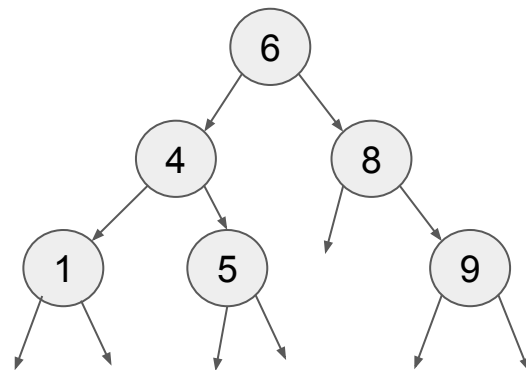


Binary Search!

Set Efficiency

A Set using a BST
under the hood?

Function	Unsorted_Set	Sorted_Set	BST_Set
size	$O(1)$	$O(1)$	
contains	$O(n)$	$O(\log n)$	
insert	$O(n)$	$O(n)$	



Set using a BST

```
template <typename T>
class BST_Set {
public:
    bool contains(const T &v) const { return elts.contains(v); }
    void insert(const T &v){ if(!contains(v)) elts.insert(); }
    int size() const { return elts.size(); }

private:
    BinarySearchTree<T> elts;
};
```


Set using a BST

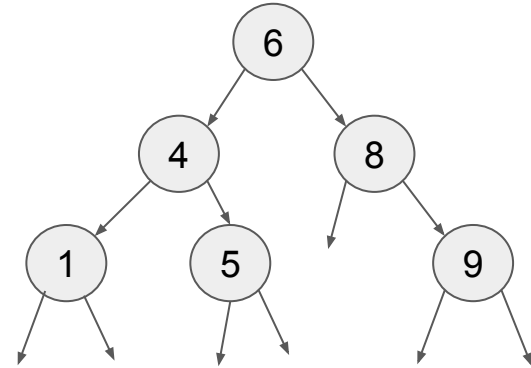
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    BinarySearchTree<T> elts;
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Set using a BST

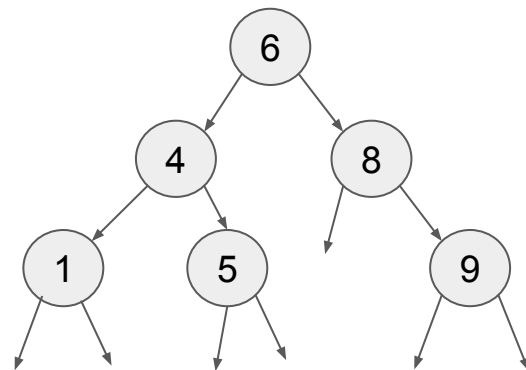
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Set using a BST

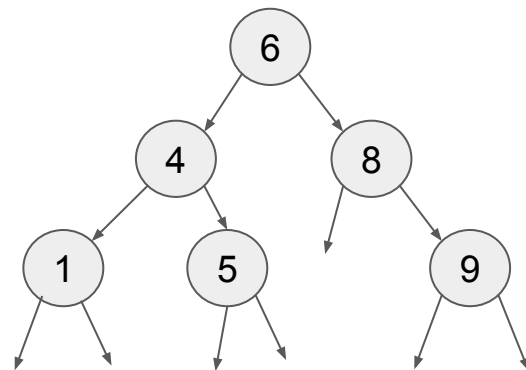
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private:
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- Binary Search Tree (BST)
- **Map**

Has things like:

- Insert (push_front, push_back...)
- Contains
- Size
- Remove
- Iterators

Map

Data structure that associates keys with values

Example: We want to keep
track of definitions of words

“Tree” → “Green tall thing outside”

“Candle” → “Smells good and lights on fire”

Map

```
int main(){  
    Map<string, string> dictionary;  
    dictionary["Tree"] = "Green tall thing outside";  
    dictionary["Candle"] = "Smells good and lights on fire";  
}
```

Key

Value

"Tree" → "Green Tall thing outside"

Keys<string>	Value<string>
"Tree"	"Green tall thing outside"
"Candle"	"Smells good and lights on fire"

Map

Data structure that associates keys with values

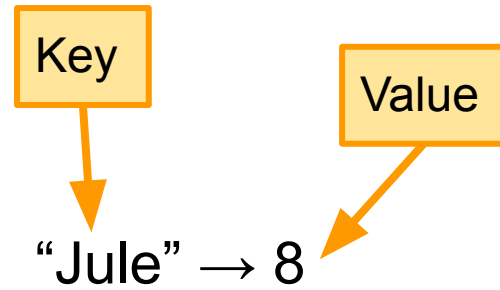
Example: We want to keep track of scores in a friendly neighborhood euchre tournament

“Jule” → 8

“Daniel” → 9

“Sophia” → 11

Map



```
int main(){  
    Map<string, int> scores;  
    scores[“Jule”] = 8;  
    scores[“Daniel”] = 9;  
    scores[“Sophia”] = 11;  
}
```

Keys<string>	Value<int>
“Jule”	8
“Daniel”	9
“Sophia”	11


Using a map

```
int main(){  
    Map<string, int> scores;  
    scores["Jule"] = 8;  
    cout << scores["Jule"] << endl;  
    scores["Jule"] = scores["Jule"] + 1000;  
}
```

Using a map

```
int main(){  
    Map<string, int> scores;  
    scores["Jule"] = 8;  
    cout << scores["Jule"] << endl;  
    scores["Jule"] = scores["Jule"] + 1000;  
}
```


Inserts the key "Jule" with
the value 8



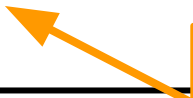
Using a map

```
int main(){  
    Map<string, int> scores;  
    scores["Jule"] = 8;  
    cout << scores["Jule"] << endl;  
    scores["Jule"] = scores["Jule"] + 1000;  
}
```

Inserts the key "Jule" with the value 8



Changes the value at key "Jule" by 1000



How to represent a Map Under the hood?

- **Fast insertion of a new key value pair**
- Fast access to a value given a key

```
int main(){  
    Map<string, int> scores;  
  
    scores["Jule"] = 8;  
  
    cout << scores["Jule"] << endl;  
  
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}
```


How to represent a Map Under the hood?

- Fast insertion of a new key value pair
- **Fast access to a value given a key**

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    Map<string, int> scores;  
  
    scores["Jule"] = 8;  
  
    cout << scores["Jule"] << endl;  
  
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}
```

How to represent a Map Under the hood?

- Fast insertion of a new key value pair
- Fast access to a value given a key

Binary Search Tree!

```
int main(){  
    Map<string, int> scores;  
    scores["Jule"] = 8;  
    cout << scores["Jule"] << endl;  
    scores["Jule"] = scores["Jule"] + 1000;  
}
```

Representing a Map using a BST

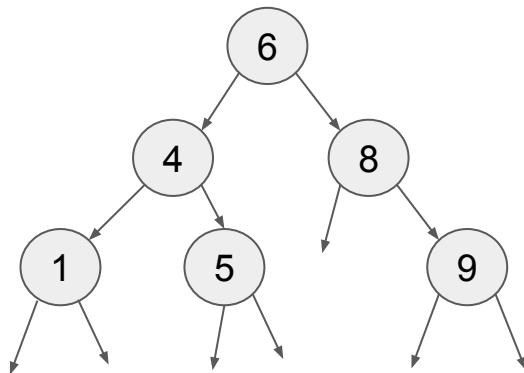
```
template <typename T>
class BinarySearchTree {
public:
    BinarySearchTree();
    BinarySearchTree(const BinarySearchTree &other);
    BinarySearchTree & operator=(const BinarySearchTree &other);
    ~BinarySearchTree();

    bool empty() const;
    int size() const;
    bool contains(const T &item) const;
    void insert(const T &item);

private:
    struct Node {
        T datum;
        Node *left, *right;
    };

    Node *root;
};
```

What will be type T?



Pair! A struct that holds two values.

std::pair

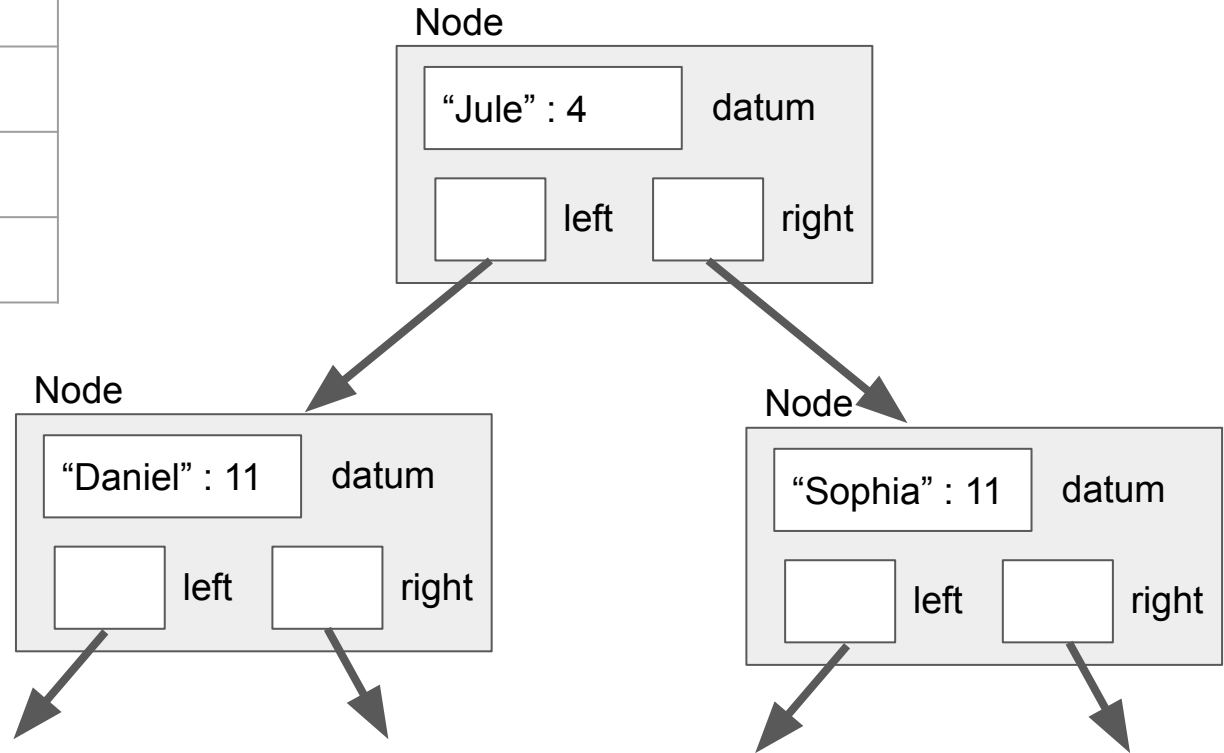
- A templated struct with a member called `first` and another called `second`

```
int main(){  
    std::pair<int, bool> p1;  
    p1.first = 5;  
    p1.second = false;  
}
```

Representing a Map using a BST under the hood

Keys<string>	Value<int>
"Jule"	4
"Daniel"	11
"Sophia"	11

```
typename T =  
pair<string, int>
```

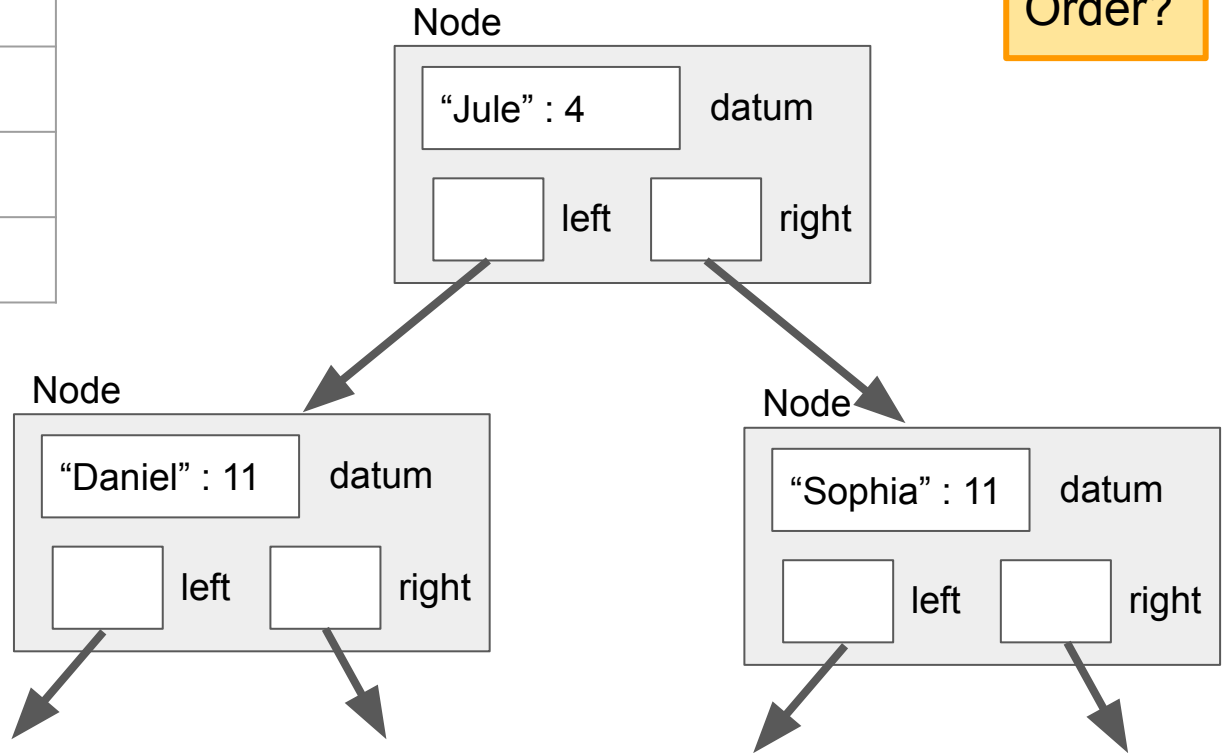


Representing a Map using a BST under the hood

Keys<string>	Value<int>
"Jule"	4
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Order?

typename T =
pair<string, int>



Problem: Comparing Pairs

- Computer doesn't know how to compare two pairs

```
int main(){  
    std::pair<int, double> p1 = {5, 45.2};  
    std::pair<int, double> p2 = {50, 6.7};  
}
```

Key?
Value?

Problem: Comparing Pairs

- Computer doesn't know how to compare two pairs

```
int main(){  
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    std::pair<int, double> p2 = {50, 6.7};  
}
```

Key?
Value?

Map - sorted based on key

Map using a BST

Making a BST work with pairs

1. Change BST to use a custom comparator functor when comparing two elements in the tree

ex) insert

2. Create a custom comparator functor for the `std::pair` used in a map to then use in the underlying BST

Map using a BST

Making a BST work with pairs

1. **Change BST to use a custom comparator functor when comparing two elements in the tree**

ex) insert

2. Create a custom comparator functor for the `std::pair` used in a map to then use in the underlying BST

BST with custom comparator

```
template <typename T, typename Compare=std::less<T>>
class BinarySeachTree {
    ...
private:
    Node* root;
    Compare less;
}
```

BST with custom comparator

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template <typename T, typename Compare=std::less<T>>
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1. Create a template for the type of the comparator

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1. Create a template for the type of the comparator
2. Create an object of that templated type

BST with custom comparator

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template <typename T, typename Compare=std::less<T>>
class BinarySearchTree {
    ...
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    Node* root;
    Compare less;
}
```

1. Create a template for the type of the comparator
2. Create an object of that templated type

Can now use on two objects of type T with less to determine which is less than the other!

```
cout << less(a, b) << endl;
```

BST with custom comparator

```
template <typename T,  
typename Compare=std::less<T>>  
class BinarySeachTree {  
    ...  
private:  
    Node* root;  
    Compare less;  
}
```

```
class DuckNameLess {  
public:  
    bool operator()(const Duck &d1, const  
Duck &d2) const{ return d1.getName() <  
d2.getName(); }  
};
```


```
int main(){  
    BinarySearchTree<Duck, DuckNameLess> bst;  
}
```

BST with custom comparator

```
template <typename T,  
typename Compare=std::less<T>>  
class BinarySeachTree {  
    ...  
private:  
    Node* root;  
    Compare less;  
}
```

```
class DuckNameLess {  
public:  
    bool operator()(const Duck &d1, const  
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};
```

Type of the
comparator!



```
int main(){  
    BinarySearchTree<Duck, DuckNameLess> bst;  
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BST with custom comparator


```
template <typename T,  
typename Compare=std::less<T>>  
class BinarySeachTree {  
    ...  
private:  
    Node* root;  
    Compare less;  
}
```

Actual object of type
DuckNameLess



```
class DuckNameLess {  
public:  
    bool operator()(const Duck &d1, const  
Duck &d2) const{ return d1.getName() <  
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};
```

Type of the
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int main(){  
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Making a Map using a BST

1. Change BST to use a custom comparator functor when comparing two elements in the tree

ex) insert

2. **Create a custom comparator functor for the `std::pair` used in a map to then use in the underlying BST**

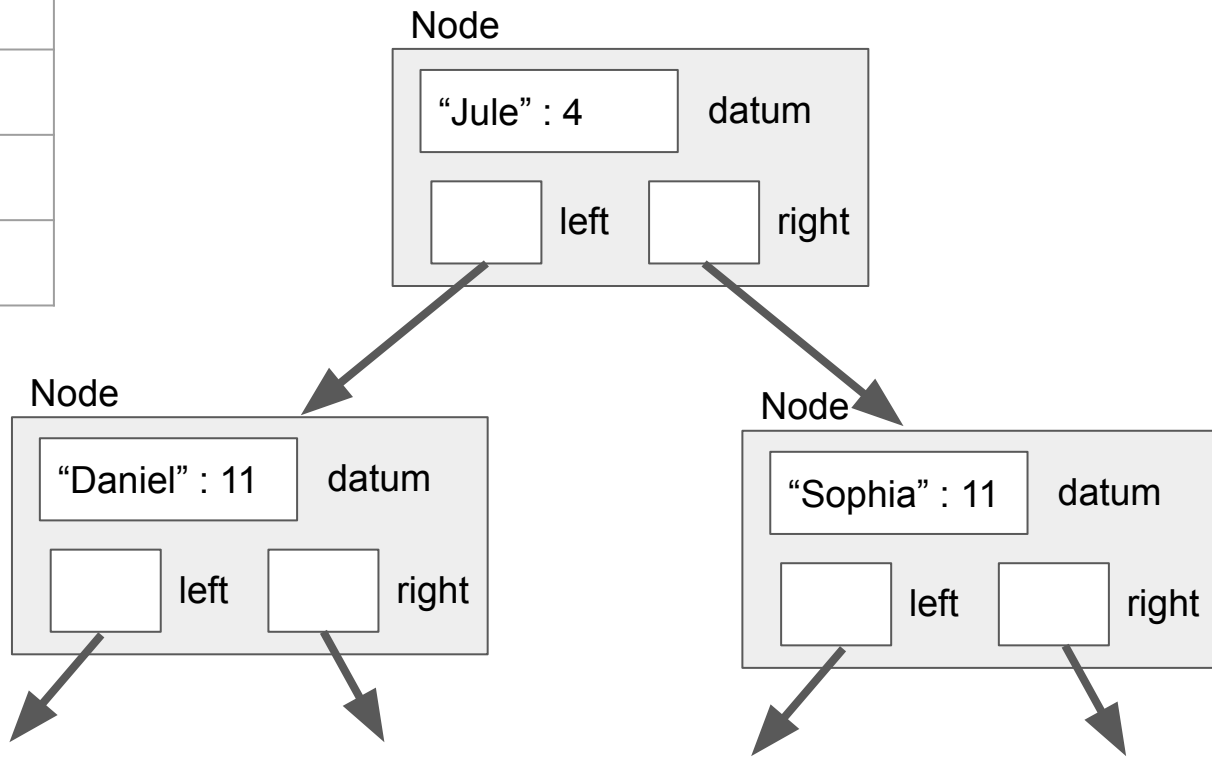
Sorted by key! AKA
first thing in the pair

Representing a map using a BST

Pairs Sorted by key

Keys<string>	Value<int>
"Jule"	4
"Daniel"	11
"Sophia"	11

typename T =
pair<string, int>



Implementing a Map

```
template <typename Key_type, typename Value_type, typename Key_compare>
```

```
class Map {
```

```
    ...
```

```
private:
```

```
    using Pair_type = std::pair<Key_type, Value_type>;
```

```
    BinarySearchTree<Pair_type, ???? > entries;
```

```
}
```

Implementing a Map

```
template <typename Key_type, typename Value_type, typename Key_compare>
```


```
class Map {
```

```
    ...
```

```
private:
```

```
    using Pair_type = std::pair<Key_type, Value_type>;
```

Key compare takes in two values of type Key_type and tells you which is less



```
    BinarySearchTree<Pair_type, ???? > entries;
```

```
}
```

Implementing a Map

```
template <typename Key_type, typename Value_type, typename Key_compare>
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```
class Map {
```

```
    ...
```

```
private:
```

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    using Pair_type = std::pair<Key_type, Value_type>;
```

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    BinarySearchTree<Pair_type, ???? > entries;
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```
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```

Implementing a Map

```
template <typename Key_type, typename Value_type, typename Key_compare>
```


```
class Map {
```

```
    ...
```

```
private:
```

```
    using Pair_type = std::pair<Key_type, Value_type>;
```

Key compare takes in two values of type Key_type and tells you which is less



```
    BinarySearchTree<Pair_type, ???? > entries;
```

```
}
```

Implementing a Map

```
template <typename Key_type, typename Value_type, typename Key_compare>
```


```
class Map {
```

```
    ...
```

```
private:
```

```
    using Pair_type = std::pair<Key_type, Value_type>;
```

Key compare takes in two values of type Key_type and tells you which is less



Could we pass in Key_compare?

```
    BinarySearchTree<Pair_type, ???? > entries;
```

```
}
```


Implementing a Map

```
template <typename Key_type, typename Value_type, typename Key_compare>
```


```
class Map {
```

```
    ...
```

```
private:
```

```
    using Pair_type = std::pair<Key_type, Value_type>;
```

Key compare takes in two values of type Key_type and tells you which is less



Need a functor that can compare pairs given a the functor type Key_compare!

```
    BinarySearchTree<Pair_type, ???? > entries;
```

```
}
```

Implementing a Map

```
template <typename Key_type, typename Value_type, typename Key_compare>
class Map {
    ...
private:
    using Pair_type = std::pair<Key_type, Value_type>;

    class PairComp {
    public:
        bool operator() {...}
    };

    BinarySearchTree<Pair_type, PairComp> entries;
}
```

Need a functor that can compare pairs given a the functor type Key_compare!

Agenda

Functors Review

Containers Review

- BSTs

- Sets

- Maps

C++ Shortcuts

Recursion Practice

Using a map...

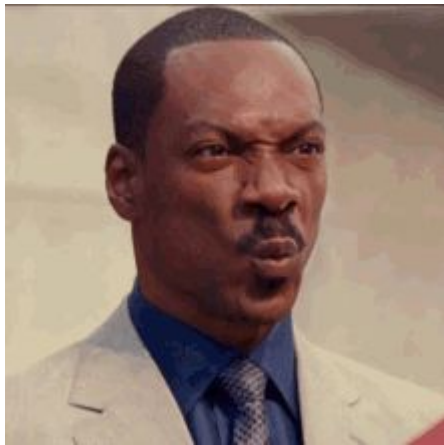
```
int main(){  
    Map<Duck, int, DuckNameLess> ducks; //insert ducks  
  
    //loop through ducks?  
  
}
```

Using a map...

```
int main(){  
    Map<Duck, int, DuckNameLess> ducks; //insert ducks  
  
    //loop through ducks?  
  
    Iterators!  
  
}
```

Using a map...

```
int main(){  
    Map<Duck, int, DuckNameLess> ducks; //insert ducks  
  
    for(typename Map<Duck, int, DuckNameLess>::Iterator it = ducks.begin();  
it != ducks.end(); ++it){  
        cout << it->first.getName() << endl;  
        cout << it->second << endl;  
    }  
}
```



Using a map...

```
int main(){  
  
    Map<Duck, int, DuckNameLess> ducks; //insert ducks  
  
    for(auto it = ducks.begin(); it != ducks.end(); ++it){  
  
        cout << it->first.getName() << endl;  
  
        cout << it->second << endl;  
  
    }  
  
}
```



C++ Shortcuts

Auto - Compiler deduces the type for you

Using a map...

```
int main(){  
    Map<Duck, int, DuckNameLess> ducks; //insert ducks  
    for(auto it = ducks.begin(); it != ducks.end(); ++it){  
        cout << it->first.getName() << endl;  
        cout << it->second << endl;  
    }  
}
```

Using a map...

```
int main(){  
    Map<Duck, int, DuckNameLess> ducks; //insert ducks  
    for(auto item : ducks){  
        cout << item.first.getName() << endl;  
        cout << item.second << endl;  
    }  
}
```

C++ Simplified

Auto - Compiler deduces the type for you

Range-Based For Loops - loops through a container using an iterator

Range-Based For Loops

```
vector<int> vec = {1, 2, 3};  
  
for(int item : vec) {  
    cout << item << endl;  
}
```

item = *iterator = int

```
for (auto it = vec.begin(); it != vec.end(); ++it) {  
    int item = *it;  
    cout << item << endl;  
}
```

Range-Based For Loops

```
vector<int> vec = {1, 2, 3};  
  
for(int item : vec) {  
    cout << item << endl;  
}
```

item = *iterator = int

What if we want to
change elements
in the vector?

```
for (auto it = vec.begin(); it != vec.end(); ++it) {  
    int item = *it;  
    cout << item << endl;  
}
```

If we want to change the items in vector

```
vector<int> vec = {1, 2, 3};  
  
for(int &item : vec) {  
    item = 42;  
}
```

item = *iterator = int

```
for (auto it = vec.begin(); it != vec.end(); ++it) {  
    int &item = *it;  
    item = 42;  
}
```

Using a map...

```
int main(){  
    Map<Duck, int, DuckNameLess> ducks; //insert ducks  
    for(auto item : ducks){  
        cout << item.first.getName() << endl;  
        cout << item.second << endl;  
    }  
}
```

item = *iterator = pair<duck, int>

Agenda

Functors Review

Containers Review

- BSTs

- Sets

- Maps

C++ Shortcuts

Recursion Practice

Writing Recursion

<https://onlinegdb.com/Lq-V3U2U0>

Reverse an array using recursion!

1	2	3	4	5
---	---	---	---	---

Can you break this up into smaller pieces?

Writing Recursion

<https://onlinegdb.com/Lq-V3U2U0>

Reverse an array using recursion!

1	2	3	4	5
---	---	---	---	---

Can you break this up into smaller pieces?

```
void reverse(int *left, int *right){ ... }
```

Writing Recursion

<https://onlinegdb.com/Lq-V3U2U0>

Reverse an array using recursion!

1	2	3	4	5
---	---	---	---	---

Can you break this up into smaller pieces?

```
void reverse(int *left, int *right){ ... }
```

If you switch the first and last element, what is left to do?

Writing Recursion

<https://onlinegdb.com/Lq-V3U2U0>

Reverse an array using recursion!

1	2	3	4	5
---	---	---	---	---

```
void reverse(int *left, int *right){  
    //base case  
    int temp = *left;  
    *left = *right;  
    *right = temp;  
    //recursive call  
}
```

Writing Recursion

<https://onlinegdb.com/Lq-V3U2U0>

Reverse an array using recursion!

1	2	3	4	5
---	---	---	---	---

```
void reverse(int *left, int *right){  
    //base case  
    int temp = *left;  
    *left = *right;  
    *right = temp;  
    reverse(left + 1, right - 1); //recursive call  
}
```

Writing Recursion

<https://onlinegdb.com/Lq-V3U2U0>

Reverse an array using recursion!

1	2	3	4	5
---	---	---	---	---

```
void reverse(int *left, int *right){  
    if(left >= right) return; //base case  
  
    int temp = *left;  
    *left = *right;  
    *right = temp;  
  
    reverse(left + 1, right - 1); //recursive call  
}
```

Writing Recursion

<https://onlinegdb.com/Lq-V3U2U0>

Reverse an array using recursion!

1	2	3	4	5
---	---	---	---	---

```
void reverse(int *left, int *right){  
    if(left >= right) return; //base case  
    int temp = *left;  
    *left = *right;  
    *right = temp;  
    reverse(left + 1, right - 1); //recursive call  
}
```

Tail recursive?

Writing Recursion

<https://onlinegdb.com/Lq-V3U2U0>

Reverse an array using recursion!

1	2	3	4	5
---	---	---	---	---

```
void reverse(int *left, int *right){  
    if(left >= right) return; //base case  
  
    int temp = *left;  
    *left = *right;  
    *right = temp;  
  
    reverse(left + 1, right - 1); //recursive call  
}
```

Tail recursive?
YES!

Exercise: Fibonacci

$$F(n) = \left\{ \begin{array}{ll} 0 & n = 0 \\ 1 & n = 1 \\ F(n-1) + F(n-2) & n > 1 \end{array} \right\}$$

Write a fibonacci function using iteration
Write a fibonacci function using recursion
Write a fibonacci function using tail-recursion

https://onlinegdb.com/nEAU_vo6E