# ME 231\_HW3

#### Problem 1

1(1)

```
p = sdpvar(2,1);
%u=sdpvar(4,1);
C1=(-3*p(1)+2*p(2)-30)<=0;
C2=(-2*p(1)+p(2)-12)<=0;
C3=-1*p(1)<=0;
C4=-1*p(2)<=0;
%KKT
%C5=-5+u(1)*(-3)+u(2)*(-2)+u(3)*(-1);
%C6=-7+u(1)*(2)+u(2)*(1)+u(4)*(-1);
%C7=-1*u<=0;
%C=[C1,C2,C3,C4,C5,C6,C7];
C=[C1,C2,C3,C4];
%obj=
-5*p(1)-7*p(2)+u(1)*(-3*p(1)+2*p(2)-30)+u(2)*(-2*p(1)+p(2)-12)+u(3)*-1*p(1)+u(4)*-1*p(1)+u(2)*(-2*p(1)+p(2)-12)+u(3)*-1*p(1)+u(4)*-1*p(1)+u(2)*(-2*p(1)+p(2)-12)+u(3)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(2)*(-2*p(1)+p(2)-12)+u(3)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(2)*(-2*p(1)+p(2)-12)+u(3)*-1*p(1)+u(4)*-1*p(1)+u(2)*(-2*p(1)+p(2)-12)+u(3)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(2)*(-2*p(1)+p(2)-12)+u(3)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(1)+u(4)*-1*p(
2);
obj=-5*p(1)-7*p(2);
%options = sdpsettings('verbose', 'bnb', 'bnb.solver', 'fmincon');
options = sdpsettings('verbose',1,'savesolveroutput',1);
out=optimize(C,obj,options);
out.solveroutput.LAMBDA
double(p);
double(obj)
```

```
%double(u)
\% unbounded , KKT is notsatisfied
* 0: obj = 0.000000000e+000 infeas = 0.000e+000 (0)
* 4: obj = -1.200000000e+007 infeas = 0.000e+000 (0)
ans =
   0
    0
   0
    0
ans =
   1000000
   1000000
ans =
  -12000000
1(2)
p = sdpvar(2,1);
C1=(p(1)-p(2))<=1;
C2=(3*p(1)+2*p(2))<=12;
```

```
C3=(2*p(1)+3*p(2))<=3;
C4=(-2*p(1)+3*p(2))>=9;
C5=p(1)>=0;
C6=p(2)>=0;
C=[C1,C2,C3,C4,C5,C6];
obj= 3*p(1)+p(2);
options = sdpsettings('verbose',1,'savesolveroutput',1);
out=optimize(C,obj,options);
out.solveroutput.LAMBDA
double(p);
double(obj)
%KKT is not satisfied
    0: obj = 0.0000000000e+000 infeas = 9.000e+000 (0)
    1: obj = 1.0000000000e+000 infeas = 6.000e+000 (0)
glp_simplex: unable to recover undefined or non-optimal solution
ans =
    0
    0
    0
    0
    0
```

```
0
0
ans =
```

0

## 1(3)

```
p = sdpvar(2,1);
t1=sdpvar(1,1);
t2= sdpvar(2,1);
C1=(3*p(1)+2*p(2))<=-3;
C2=p(1)>=0;
C3=p(1)<=2;
C4=p(2)>=-2;
C5=p(2)<=3;
C6=[abs(p(1)-2) <=t1,t1>=0];
C7=abs(p(2))<=t1;
C8=[abs(p(1)) <= t2(1), t2(1) >= 0];
C9=[abs(p(2)+5)<=t2(2),t2(2)>=0];
C=[C1,C2,C3,C4,C5,C6,C7,C8,C9];
obj= t1+t2(1)+t2(2);
options = sdpsettings('verbose',1,'savesolveroutput',1);
out=optimize(C,obj,options);
out.solveroutput.LAMBDA
```

```
double(p);
double(obj)
%KKT is not satisfied
    0: obj = -2.000000000e+006 infeas = 1.000e+007 (0)
* 13: obj = 5.200000000e+000 infeas = 0.000e+000 (0)
* 14: obj = 5.000000000e+000 infeas = 0.000e+000 (0)
ans =
       0
       0
       0
       0
  -0.0000
  -1.0000
  -1.0000
     0
  -1.0000
     0
  -0.0000
  -1.0000
  -0.5000
  -0.5000
  -1.0000
      0
```

```
ans =

0
-2

ans =
```

## 1(4)

```
p = sdpvar(2,1);
tl=sdpvar(1,1);
t2= sdpvar(2,1);
cl=p(1)<=-3;
c2=p(2)<=4;
c3=(4*p(1)+3*p(2))<=0;
c=[c1,c2,c3];
obj= p(1)^2+p(2)^2;
options = sdpsettings('verbose',1,'savesolveroutput',1);
out=optimize(C,obj,options);
%out.solveroutput.LAMBDA
double(p);
double(obj)</pre>
%KKT is satisfied
```

feasible solution found by trysol heuristic after 0.0 seconds, objective value 2.000000e+10 presolving:

(round 1, fast) 0 del vars, 3 del conss, 0 add conss, 3 chg bounds, 0 chg sides, 0

(round 2, fast) 0 del vars, 3 del conss, 0 add conss, 6 chg bounds, 0 chg sides, 0 chg coeffs, 0 upgd conss, 0 impls, 0 clqs

presolving (3 rounds: 3 fast, 1 medium, 1 exhaustive):

O deleted vars, 3 deleted constraints, 0 added constraints, 6 tightened bounds, 0 added holes, 0 changed sides, 0 changed coefficients

O implications, O cliques

presolved problem has 3 variables (0 bin, 0 int, 0 impl, 3 cont) and 1 constraints

1 constraints of type <quadratic>

chg coeffs, 0 upgd conss, 0 impls, 0 clqs

Presolving Time: 0.02

transformed 1/1 original solutions to the transformed problem space

time | node | left | LP iter|LP it/n| mem | mdpt | frac | vars | cons | cols | rows | cuts | confs|strbr| | dualbound | primalbound | gap | 0.0s| 1 | 0 | 0 | - | 199k| 0 | 0 | 3 | 1 | 3 | 6 | 0 | 0 | 0 | 0 | 9.000000e+00 | 2.000000e+10 | Large | q 0.1s| 1 | 0 | 0 | - | 199k| 0 | - | 3 | 1 | 3 | 6 | 0 | 0 | 0 | 0 | 9.000000e+00 | 9.000000e+00 | 0.00 | 0.1s| 1 | 0 | 0 | - | 199k| 0 | - | 3 | 1 | 3 | 6 | 0 | 0 | 0 | 0 | 9.000000e+00 | 9.000000e+00 | 0.00

SCIP Status : problem is solved [optimal solution found]

Solving Time (sec) : 0.05

Solving Nodes : 1

Primal Bound : +8.999999900000e+00 (2 solutions)

Dual Bound : +8.9999999900000e+00

Gap : 0.00

```
ans =
-3.0000
-0.0000
ans =
```

### Problem 2

#### HW2

```
Al=[1,0;0,1];
bl=[0;-5];
Ainf=[1,0;0,1];
binf=[2;0];
Ac=[3,2;1,0;-1,0;0,1;0,-1];
bc=[-3;2;0;3;2];
[xopt, J] = reglinf(Al, bl, Ainf, binf, Ac, bc);
double(xopt)
double(yopt)
double(J)
% Hw3
p = sdpvar(2,1);
tl=sdpvar(1,1);
t2= sdpvar(2,1);
c1=(3*p(1)+2*p(2))<=-3;
c2=p(1)>=0;
```

```
C3=p(1)<=2;
C4=p(2)>=-2;
C5=p(2)<=3;
C6=[abs(p(1)-2)<=t1,t1>=0];
C7=abs(p(2))<=t1;
C8=[abs(p(1)) <= t2(1), t2(1) >= 0];
C9=[abs(p(2)+5) <= t2(2), t2(2) >= 0];
C=[C1,C2,C3,C4,C5,C6,C7,C8,C9];
obj = t1+t2(1)+t2(2);
options = sdpsettings('verbose',1,'savesolveroutput',1);
out=optimize(C,obj,options);
out.solveroutput.LAMBDA
double(p);
double(obj)
Optimization terminated.
ans =
   0.0000
  -2.0000
```

ans =

5.0000

0: obj = -2.0000000000e+006 infeas = 1.000e+007 (0)

\* 13: obj = 5.200000000e+000 infeas = 0.000e+000 (0)

14: obj = 5.000000000e+000 infeas = 0.000e+000 (0)

ans =

0

0

0

0

0

-0.0000

0

-1.0000

-1.0000

0

-1.0000

0

0

-0.0000

0

-1.0000

-0.5000

-0.5000

-1.0000

0

ans =

0

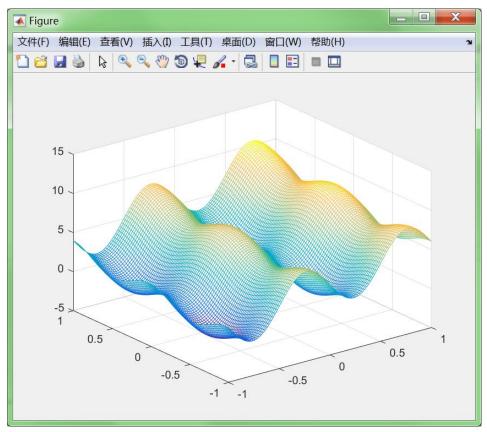
-2

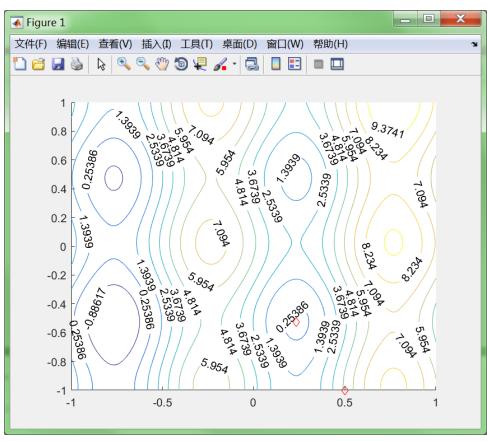
5

#### **%% Problem 3**

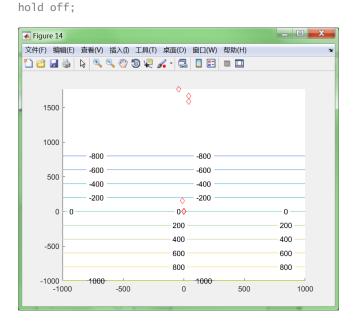
```
%% 3(a)
p = sdpvar(2,1);
C1=abs(p(1))-1<=0;
C2=abs(p(2))-1<=0;
C=[C1,C2];
obj=3*sin(-2*pi*p(1))+2*p(1)+4+cos(2*pi*p(2))+p(2);
options = sdpsettings('verbose',1,'savesolveroutput',1);
out=optimize(C,obj,options);
out.solveroutput.lambda
d=double(p);
double(obj)
% ans [0.2331;-0.5254]
%KKT is satisfied
%% 3(b)
%3D plot
[X,Y] = meshgrid(-1:.02:1, -1:.02:1);
Z = 3*sin(-2*pi*X) + 2*X + 4 + cos(2*pi*Y) + Y;
mesh(X,Y,Z)
figure
hold on;
contour(X,Y,Z,10,'ShowText','on')
plot(0.5,-1,'dr');
plot(d(1),d(2),'dr');
```

#### hold off;





```
%% 3(c)
for i=1:20
p = sdpvar(2,1);
pint = 2*rand(2,1)-1;
assign(p, pint);
C = -(1+p(1)^2)^2+p(2)^2==4;
obj=log(1+p(1)^2)-p(2);
options = sdpsettings('usex0',1);
optimize(C,obj,options);
P(:,i)=double(p);
end
[X,Y] = meshgrid(-1000:1:1000, -1000:1:1000);
Z = log(1+X^2)-Y;
figure
hold on;
contour(X,Y,Z,'ShowText','on')
for i=1:20
plot(P(1,i),P(2,i),'dr');
end
```



### **%% Problem 4**

```
%% 4(a)
p = intvar(2,1);
C1=(p(1)+4*p(2)-16)<=0;
C2=(6*p(1)+4*p(2)-28)<=0;
C3=(2*p(1)-5*p(2)-6)<=6;
C4=p(1) <= 10;
C5=p(2) <= 10;
C=[C1,C2,C3,C4,C5,p(1)>=0,p(2)>=0];
obj=-6*p(1)-5*p(2);
options = sdpsettings('verbose', 'bnb', 'bnb.solver', 'fmincon');
optimize(C,obj,options);
double(p)
double(obj)
ans =
    4
ans =
  -29
%% 4(b)
p=sdpvar(2,1);
b=binvar(1,1);
obj=-1*p(1)-2*p(2);
C1=(1-b)*(3*p(1)+4*p(2)-12)<=0;
```

```
C2=b*(4*p(1)+3*p(2)-12)<=0;
C=[C1,C2,p(1)>=0,p(2)>=0];
options = sdpsettings('verbose', 'bnb', 'bnb.solver', 'fmincon');
optimize(C,obj,options);
double(p)
double(obj)
ans =
   4
    1
ans =
  -29
ans =
   0.0000
   3.0000
ans =
  -6.0000
%% Problem 5
%% 5(a)
TS = 0.2;
```

```
N = 70;
TFinal = TS*N;
1r=1.738;
lf=lr;
x=sdpvar(N+1,1);
y=sdpvar(N+1,1);
v=sdpvar(N+1,1);
psi=sdpvar(N+1,1);
a=sdpvar(N+1,1);
beta=sdpvar(N+1,1);
z = [x,y,v,psi];
zref=[0, 0, 0,-1*pi/2];
Cinit=z(1,:)==[0,3,0,0];
Cfinal=z(N+1,:)==[0,0,0,-1*pi/2];
CIE=[abs(a(N+1)) <= 1.5*TS, abs(beta(N+1)) <= 0.6];
CE=[Cinit,Cfinal];
for i=1:N
   CIE=[CIE;
      [-20,-5,-10,-2*pi] \le z(i,:) \le [20,10,10,2*pi];
      abs(a(i)) <= 1.5*TS;
      abs(beta(i))<=0.6;
      abs(beta(i+1)-beta(i)) \le 0.2
      1;
   CE=[CE;
      x(i+1) == x(i) + TS*v(i)*cos(psi(i) + beta(i));
      y(i+1) == y(i) + TS*v(i)*sin(psi(i) + beta(i));
      v(i+1) == v(i) + TS*a(i);
      psi(i+1) == psi(i) + TS*v(i)/1.738*sin(beta(i));
      ];
```

```
C=[CIE,CE];
obj=norm(z(N+1,:)-zref)^2+norm(z(N-1,:)-zref)^2+norm(z(N,:)-zref)^2;
options = sdpsettings('verbose','IPOPT','savesolveroutput',1);
optimize(C,obj,options);
xopt=double(x);
yopt=double(y);
vopt=double(v);
psiopt=double(psi);
aopt=double(a);
betaopt=double(beta);
T=(1:(N+1)).*TS;
figure
subplot(2,2,1)
plot(T,xopt)
xlabel('time')
ylabel('x_opt')
subplot(2,2,2)
plot(T,yopt)
xlabel('time')
ylabel('y_opt')
subplot(2,2,3)
plot(T,vopt)
xlabel('time')
ylabel('v_opt')
subplot(2,2,4)
plot(T,psiopt)
xlabel('time')
ylabel('psi_opt')
```

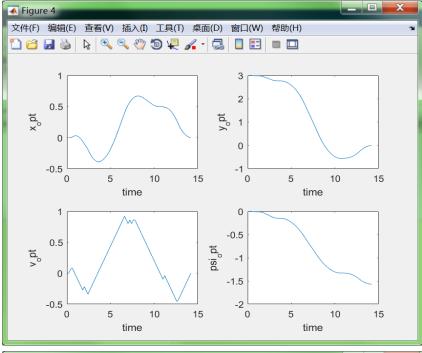
figure

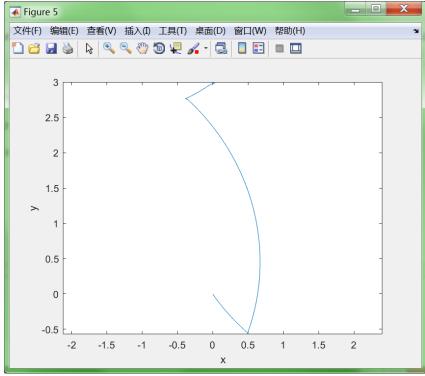
plot(xopt,yopt)

xlabel('x')

ylabel('y')

axis equal





```
TS = 0.2;
N = 70;
TFinal = TS*N;
1r=1.738;
lf=lr;
x=sdpvar(N+1,1);
y=sdpvar(N+1,1);
v=sdpvar(N+1,1);
psi=sdpvar(N+1,1);
a=sdpvar(N+1,1);
beta=sdpvar(N+1,1);
z = [x,y,v,psi];
zref=[0, 0, 0,-1*pi/2];
Cinit=z(1,:)==[0,3,0,0];
Cfinal=z(N+1,:)==[0,0,0,-1*pi/2];
CIE=[abs(a(N+1)) <= 1.5*TS, abs(beta(N+1)) <= 0.6];
CE=[Cinit,Cfinal];
for i=1:N
   CIE=[CIE;
       [-20,-0.2,-10,-2*pi] \leftarrow z(i,:) \leftarrow [20,10,10,2*pi];
       abs(a(i)) <= 1.5*TS;
       abs(beta(i))<=0.6;
       abs(beta(i+1)-beta(i)) \le 0.2
      ];
   CE=[CE;
       x(i+1) == x(i) + TS*v(i)*cos(psi(i) + beta(i));
       y(i+1) == y(i) + TS*v(i)*sin(psi(i) + beta(i));
       v(i+1) == v(i) + TS*a(i);
       psi(i+1) == psi(i) + TS*v(i)/1.738*sin(beta(i));
       ];
```

```
end
C=[CIE,CE];
obj = norm(z(N+1,:)-zref) \land 2 + norm(z(N-1,:)-zref) \land 2 + norm(z(N,:)-zref) \land 2;
options = sdpsettings('verbose','IPOPT','savesolveroutput',1);
optimize(C,obj,options);
xopt=double(x);
yopt=double(y);
vopt=double(v);
psiopt=double(psi);
aopt=double(a);
betaopt=double(beta);
T=(1:(N+1)).*TS;
figure
subplot(2,2,1)
plot(T,xopt)
xlabel('time')
ylabel('x_opt')
subplot(2,2,2)
plot(T,yopt)
xlabel('time')
ylabel('y_opt')
subplot(2,2,3)
plot(T,vopt)
xlabel('time')
ylabel('v_opt')
subplot(2,2,4)
plot(T,psiopt)
xlabel('time')
ylabel('psi_opt')
```

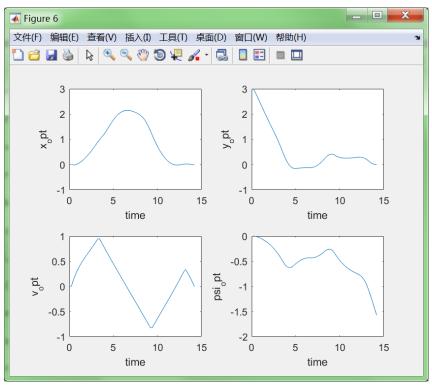
figure

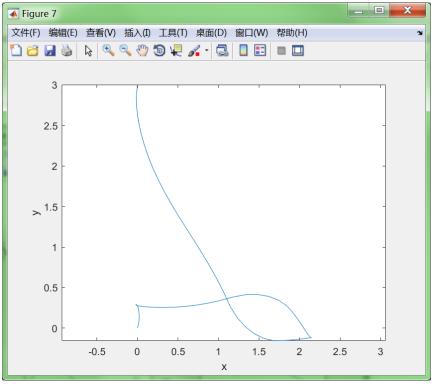
plot(xopt,yopt)

xlabel('x')

ylabel('y')

axis equal

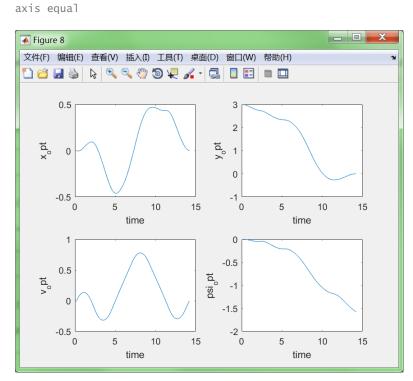


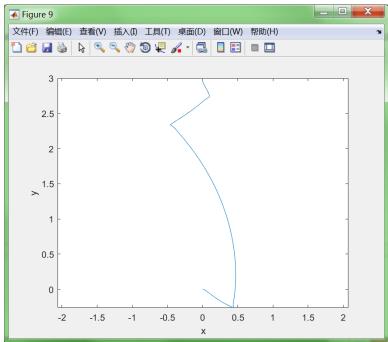


```
%% 5(c)
TS = 0.2;
N = 70;
TFinal = TS*N;
1r=1.738;
lf=lr;
x=sdpvar(N+1,1);
y=sdpvar(N+1,1);
v=sdpvar(N+1,1);
psi=sdpvar(N+1,1);
a=sdpvar(N+1,1);
beta=sdpvar(N+1,1);
z = [x,y,v,psi];
zref=[0, 0, 0,-1*pi/2];
Cinit=z(1,:)==[0,3,0,0];
Cfinal=z(N+1,:)==[0,0,0,-1*pi/2];
CIE=[abs(a(N+1)) <= 1.5*TS, abs(beta(N+1)) <= 0.6];
CE=[Cinit,Cfinal];
for i=1:N
   CIE=[CIE;
       [-20,-5,-10,-2*pi] \le z(i,:) \le [20,10,10,2*pi];
       abs(a(i)) <= 1.5 *TS;
       abs(a(i+1)-a(i)) \le 0.06;
       abs(beta(i))<=0.6;
       abs(beta(i+1)-beta(i)) \le 0.2
      ];
   CE=[CE;
       x(i+1) == x(i) + TS*v(i)*cos(psi(i) + beta(i));
       y(i+1) == y(i) + TS*v(i)*sin(psi(i) + beta(i));
       v(i+1) == v(i) + TS*a(i);
```

```
psi(i+1) == psi(i) + TS*v(i)/1.738*sin(beta(i));
      ];
end
C=[CIE,CE];
obj = norm(z(N+1,:)-zref) \land 2 + norm(z(N-1,:)-zref) \land 2 + norm(z(N,:)-zref) \land 2;
options = sdpsettings('verbose','IPOPT','savesolveroutput',1);
optimize(C,obj,options);
xopt=double(x);
yopt=double(y);
vopt=double(v);
psiopt=double(psi);
aopt=double(a);
betaopt=double(beta);
T=(1:(N+1)).*TS;
figure
subplot(2,2,1)
plot(T,xopt)
xlabel('time')
ylabel('x_opt')
subplot(2,2,2)
plot(T,yopt)
xlabel('time')
ylabel('y_opt')
subplot(2,2,3)
plot(T,vopt)
xlabel('time')
ylabel('v_opt')
subplot(2,2,4)
plot(T,psiopt)
```

```
xlabel('time')
ylabel('psi_opt')
figure
plot(xopt,yopt)
xlabel('x')
ylabel('y')
```





Published with MATLAB? R2015b