

## Lazy Evaluation

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## Announcements

# Promises

## Implementing Streams with Delay and Force

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(Demo)