CS 61AInterfaces, Linked Lists, and Generators Fall 2019 Discussion 7: October 16, 2019 Solutions

1 Interfaces

In computer science, an **interface** is a shared set of attributes, along with a specification of the attributes' behavior. For example, an interface for vehicles might consist of the following methods:

- def drive(self): Drives the vehicle if it has stopped.
- def stop(self): Stops the vehicle if it is driving.

Data types can implement the same interface in different ways. For example, a Car class and a Train can both implement the interface described above, but the Car probably has a different mechanism for drive than the Train.

The power of interfaces is that other programs don't have to know *how* each data type implements the interface – only that they *have* implemented the interface. The following travel function can work with both Cars and Trains:

```
def travel(vehicle):
    while not at_destination():
        vehicle.drive()
    vehicle.stop()
```

Magic Methods

Python defines many interfaces that can be implemented by user-defined classes. For example, the interface for arithmetic consists of the following methods:

```
• def __add__(self, other): Allows objects to do self + other.
```

- def __sub__(self, other): Allows objects to do self other.
- def __mul__(self, other): Allows objects to do self * other.

In addition, there is also an interface for sequences:

- def __len__(self): Allows objects to do len(self).
- def __getitem__(self, index): Allows objects to do self[i].

Questions

```
1.1 What would Python display?
   class A():
        def __init__(self, x):
            self.x = x
        def __repr__(self):
             return self.x
        def __str__(self):
             return self.x * 2
   class B():
        def __init__(self):
             print("boo!")
             self.a = []
        def add_a(self, a):
             self.a.append(a)
        def __repr__(self):
             print(len(self.a))
             ret = ""
             for a in self.a:
                 ret += str(a)
             return ret
   >>> A("one")
    one
   >>> print(A("one"))
   oneone
   >>> repr(A("two"))
    'two'
   >>> b = B()
   boo!
   >>> b.add_a(A("a"))
   >>> b.add_a(A("b"))
   >>> b
    2
    aabb
   >>> c = A("c")
   >>> b.add_a(c)
   >>> str(b)
```

'aabbcc'

4 Interfaces, Linked Lists, and Generators

return True

1.2 Write the function is_palindrome such that it works for any data type that implements the sequence interface.

Assume that the Link class has implemented the __len__ method and a __getitem_ method which takes in integers.

```
def is_palindrome(seq):
    """ Returns True if the sequence is a palindrome. A palindrome is a sequence
    that reads the same forwards as backwards
    >>> is_palindrome(Link("l", Link("i", Link("n", Link("k")))))
    False
   >>> is_palindrome(["l", "i", "n", "k"])
   >>> is_palindrome("link")
   False
   >>> is_palindrome(Link.empty)
   True
    >>> is_palindrome([])
    True
    >>> is_palindrome("")
   True
   >>> is_palindrome(Link("a", Link("v", Link("a"))))
    >>> is_palindrome(["a", "v", "a"])
    True
    >>> is_palindrome("ava")
    True
    11 11 11
    for i in range(len(seq)//2):
        if seq[i] != seq[len(seq) - 1 - i]:
          return False
```

Linked Lists

There are many different implementations of sequences in Python. Today, we'll explore the linked list implementation.

A linked list is either an empty linked list, or a Link object containing a first value and the rest of the linked list.

To check if a linked list is an empty linked list, compare it against the class attribute Link.empty:

```
if link is Link.empty:
    print('This linked list is empty!')
else:
    print('This linked list is not empty!')
```

```
Implementation
class Link:
    empty = ()
    def __init__(self, first, rest=empty):
        assert rest is Link.empty or isinstance(rest, Link)
        self.first = first
        self.rest = rest
    def __repr__(self):
        if self.rest:
            rest_str = ', ' + repr(self.rest)
        else:
            rest_str = ''
        return 'Link({0}{1})'.format(repr(self.first), rest_str)
    def __str__(self):
        string = '<'
        while self.rest is not Link.empty:
            string += str(self.first) + ' '
            self = self.rest
        return string + str(self.first) + '>'
```

Questions

2.1 Write a function that takes in a a linked list and returns the sum of all its elements. You may assume all elements in lnk are integers.

```
def sum_nums(lnk):
    """
    >>> a = Link(1, Link(6, Link(7)))
    >>> sum_nums(a)
    14
    """

if lnk == Link.empty:
    return 0
return lnk.first + sum_nums(lnk.rest)
```

2.2 Write a function that takes in a Python list of linked lists and multiplies them element-wise. It should return a new linked list.

If not all of the Link objects are of equal length, return a linked list whose length is that of the shortest linked list given. You may assume the Link objects are shallow linked lists, and that lst_of_lnks contains at least one linked list.

```
def multiply_lnks(lst_of_lnks):
    >>> a = Link(2, Link(3, Link(5)))
    >>> b = Link(6, Link(4, Link(2)))
    >>> c = Link(4, Link(1, Link(0, Link(2))))
    >>> p = multiply_lnks([a, b, c])
    >>> p.first
    48
    >>> p.rest.first
    >>> p.rest.rest.rest is Link.empty
    True
Recursive solution:
    product = 1
    for lnk in lst_of_lnks:
        if lnk is Link.empty:
            return Link.empty
        product *= lnk.first
    lst_of_lnks_rests = [lnk.rest for lnk in lst_of_lnks]
    return Link(product, multiply_lnks(lst_of_lnks_rests))
```

For our base case, if we detect that any of the lists in the list of Links is empty, we can return the empty linked list as we're not going to multiply anything.

Otherwise, we compute the product of all the firsts in our list of Links. Then, the subproblem we use here is the rest of all the linked lists in our list of Links. Remember that the result of calling multiply_lnks will be a linked list! We'll use the product we've built so far as the first item in the returned Link, and then the result of the recursive call as the rest of that Link.

Iterative solution:

```
import operator
from functools import reduce
def prod(factors):
     return reduce(operator.mul, factors, 1)
head = Link.empty
tail = head
while Link.empty not in lst_of_lnks:
    all_prod = prod([l.first for l in lst_of_lnks])
    if head is Link.empty:
        head = Link(all_prod)
        tail = head
    else:
        tail.rest = Link(all_prod)
        tail = tail.rest
    lst_of_lnks = [l.rest for l in lst_of_lnks]
return head
```

The iterative solution is a bit more involved than the recursive solution. Instead of building the list "backwards" as in the recursive solution (because of the order that the recursive calls result in, the last item in our list will be finished first), we'll build the resulting linked list as we go along.

We use head and tail to track the front and end of the new linked list we're creating. Our stopping condition for the loop is if any of the Links in our list of Links runs out of items.

Finally, there's some special handling for the first item. We need to update both head and tail in that case. Otherwise, we just append to the end of our list using tail, and update tail.

3 Iterators and Generators

An **iterable** is a data type which contains a collection of values which can be processed one by one sequentially. Some examples of iterables we've seen include lists, tuples, strings, and dictionaries. In general, any object that can be iterated over in a **for** loop can be considered an iterable.

While an iterable contains values that can be iterated over, we need another type of object called an **iterator** to actually retrieve values contained in an iterable. Calling the **iter** function on an iterable will create an iterator over that iterable. Each iterator keeps track of its position within the iterable. Calling the **next** function on an iterator will give the current value in the iterable and move the iterator's position to the next value.

In this way, the relationship between an iterable and an iterator is analogous to the relationship between a book and a bookmark - an iterable contains the data that is being iterated over, and an iterator keeps track of your position within that data.

Once an iterator has returned all the values in an iterable, subsequent calls to **next** on that iterable will result in a **StopIteration** exception. In order to be able to access the values in the iterable a second time, you would have to create a second iterator.

One important application of iterables and iterators is the **for** loop. We've seen how we can use **for** loops to iterate over iterables like lists and dictionaries.

This only works because the **for** loop implicitly creates an iterator using the builtin **iter** function. Python then calls **next** repeatedly on the iterator, until it raises StopIteration.

The code to the right shows how we can mimic the behavior of **for** loops using **while** loops.

Note that most iterators are also iterables - that is, calling **iter** on them will return an iterator. This means that we can use them inside **for** loops. However, calling **iter** on most iterators will not create a new iterator - instead, it will simply return the same iterator.

We can also iterate over iterables in a list comprehension or pass in an iterable to the built-in function **list** in order to put the items of an iterable into a list.

In addition to the sequences we've learned, Python has some built-in ways to create iterables and iterators. Here are a few useful ones:

- range(start, end) returns an iterable containing numbers from start to end1. If start is not provided, it defaults to 0.
- map(f, iterable) returns a new iterator containing the values resulting from applying f to each value in iterable.
- filter(f, iterable) returns a new iterator containing only the values in iterable for which f(value) returns True.

```
>>> a = [1, 2]
>>> a_iter = iter(a)
>>> next(a_iter)
1
>>> next(a_iter)
2
>>> next(a_iter)
StopIteration
```

```
counts = [1, 2, 3]

for i in counts:
    print(i)

items = iter(counts)
while True:
    try:
        i = next(items)
        print(i)
    except StopIteration:
        break #Exit the while loop
```

Questions

3.1 What would Python display? If a StopIteration Exception occurs, write StopIteration, and if another error occurs, write Error.

```
>>> lst = [6, 1, "a"]
>>> next(lst)

Error

>>> lst_iter = iter(lst)
>>> next(lst_iter)

6

>>> next(lst_iter)

1

>>> next(iter(lst))

6

>>> [x for x in lst_iter]

["a"]
```

Generators

A generator function is a special kind of Python function that uses a yield statement instead of a return statement to report values. When a generator function is called, it returns a generator object, which is a type of iterator. To the right, you can see a function that returns an iterator over the natural numbers. The yield statement is similar to a return statement. However, while a return statement closes the current frame after the function exits, a yield statement causes the frame to be saved until the next time next is called, which allows the generator to automatically keep track of the iteration state.

Once **next** is called again, execution resumes where it last stopped and continues until the next **yield** statement or the end of the function. A generator function can have multiple **yield** statements.

Including a **yield** statement in a function automatically tells Python that this function will create a generator. When we call the function, it returns a generator object instead of executing the body. When the generator's **next** method is called, the body is executed until the next **yield** statement is executed.

When yield from is called on an iterator, it will yield every value from that iterator. It's similar to doing the following:

>>> square = lambda x: x*x

for x in s:

yield square(x)

>>> **list**(many_squares([1, 2, 3]))

yield from map(square, s)

>>> **def** many_squares(s):

[1, 4, 9, 1, 4, 9]

. . .

```
for x in an_iterator:
    yield x
```

The example to the right demonstrates different ways of computing the same result.

Questions

Implement filter_link, which takes in a linked list link and a function f and returns a generator which yields the values of link for which f returns True.

Try to implement this both using a while loop and without using any form of iteration.

```
def filter_link(link, f):
   >>> link = Link(1, Link(2, Link(3)))
   >>> g = filter_link(link, lambda x: x % 2 == 0)
   >>> next(g)
   2
   >>> next(g)
   StopIteration
   >>> list(filter_link(link, lambda x: x % 2 != 0))
   [1, 3]
   .. .. ..
   while _____:
       if _____:
def filter_link(link, f):
   while link is not Link.empty:
       if f(link.first):
           yield link.first
       link = link.rest
def filter_no_iter(link, f):
   >>> link = Link(1, Link(2, Link(3)))
   >>> list(filter_no_iter(link, lambda x: x % 2 != 0))
   [1, 3]
   .....
```

| | if | : |
|-----|--|---|
| | return | |
| | elif | : |
| | | |
| | | |
| def | filter_no_iter(link, f): | |
| | <pre>if link is Link.empty: return</pre> | |
| | <pre>elif f(link.first):</pre> | |
| | <pre>yield link.first</pre> | |
| | <pre>yield from filter_no_iter(link.</pre> | rest, f) |
| | tor which yields the sum of all the no | n a Tree instance t and and returns a gen- odes from a path from the root of a tree to |
| You | may yield the sums in any order. | |
| | sum_paths_gen(t): | |
| | >>> t1 = Tree(5) | |
| | >>> next(sum_paths_gen(t1)) | |
| | 5 >>> t2 = Tree(1, [Tree(2, [Tree | (3) Tree(4)]) Tree(9)]) |
| | >>> sorted(sum_paths_gen(t2)) | (3), 1166(4)3), 1166(3)3) |
| | [6, 7, 10] | |
| | if: | |
| | yield | |
| | for: | |
| | for | : |
| | yield | |
| def | sum_paths_gen(t): | |
| | <pre>if t.is_leaf():</pre> | |

yield t.label for b in t.branches:

3.2

```
for s in sum_paths_gen(b):
   yield s + t.label
```