

CSCI 480, Winter 2018

Math Exercises # 4

YOUR NAME HERE

Due date: Thursday, February 8, midnight.

Prove each of the following by induction, for all $n \in \mathbb{N}$. You may use SymPy or other symbolic algebra package to simplify algebraic expressions.

1.

$$\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$$

2.

$$\sum_{i=1}^n i(i+1) = \frac{n(n+1)(n+2)}{3}$$

3.

$$\sum_{i=1}^n (8i-5) = 4n^2 - n$$

4.

$$3 \mid (5^{2n} - 1)$$

5.

$$9 \mid (4^{3n} + 8)$$