Scheme Notes 03

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Recursion vs. Tail-recursion

```
a^b = \left\{ \begin{array}{ll} 1 & \text{if } b = 0 \\ a(a^{b-1}) & \text{otherwise} \end{array} \right. (define pow-rec (lambda (a b) (if (zero? b) 1 & (* \text{ a (pow-rec a (- b 1)) ))))
```

Recursion vs. Tail-recursion

```
a^b = \begin{cases} 1 & \text{if } b = 0 \\ a(a^{b-1}) & \text{otherwise} \end{cases}
(define pow-rec
  (lambda (a b)
     (if (zero? b)
          (* a (pow-rec a (- b 1)) ))))
(define pow-iter
  (lambda (a b)
     (define loop
        (lambda (b product)
          (if (zero? b)
               product
                (loop (- b 1) (* a product)) )))
     (loop b 1)))
```

Named let

```
(define pow-iter
  (lambda (a b)
    (define loop
      (lambda (b product)
        (if (zero? b)
            product
            (loop (- b 1) (* a product)))))
    (loop b 1)))
(define pow-iter-2
  (lambda (a b)
    (let loop ((b b) (product 1))
      (if (zero? b)
          product
          (loop (- b 1) (* a product))))))
```

Fast recursion

Lists

A **list** is either:

- 1. the empty list, or
- 2. an item and a list

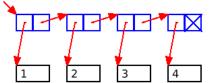
Lists

A list is either:

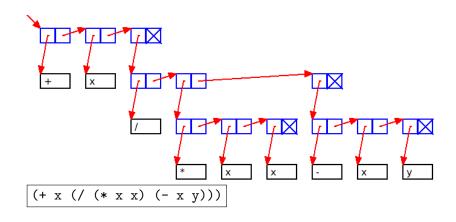
- 1. the **empty list**, or
- 2. an item and a list

Scheme uses:

- 1. the null pointer for the empty list, and
- 2. a cons cell of two pointers for a non-empty list.
- 3. The first pointer in a cons cell is called car.
- 4. The second pointer in a cons cell is called **cdr**.
- 5. The empty list has predicate empty?.



Scheme Programs are Lists



Building Lists in Scheme:

- 1. The empty list in Scheme: ()
- 2. Create a list from 3 and the empty list:

```
(cons 3 '()) \Rightarrow (3)
```

3. Create the list (4 7 2):

(cons 4 (cons 7 (cons 2 '())))
$$\Rightarrow$$
 (4 7 2)

4. Shorthand for long lists: (list 4 7 2) \Rightarrow (4 7 2)

Building Lists in Scheme:

- 1. The empty list in Scheme: ()
- 2. Create a list from 3 and the empty list:

```
(\cos 3 '()) \Rightarrow (3)
```

3. Create the list (4 7 2):

$$(\cos 4 (\cos 7 (\cos 2 ()))) \Rightarrow (4 7 2)$$

- 4. Shorthand for long lists: (list 4 7 2) \Rightarrow (4 7 2)
- 5. Using quote: $(4 7 2) \Rightarrow (4 7 2)$

$$(+ 4 7 2) \Rightarrow (+ 4 7 2)$$

$$(a b c) \Rightarrow (a b c)$$

(a b c)
$$\Rightarrow$$
 error

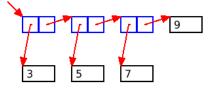
$$(+ 4 7 2) \Rightarrow 13$$

'(list (+ 2 2) 7 2)
$$\Rightarrow$$
 (list (+ 2 2) 7 2)

(list (+ 2 2) 7 2)
$$\Rightarrow$$
 (4 7 2)

An improper list results in a dot:

- $(cons 4 8) \Rightarrow (4 . 8)$
- (cons 3 (cons 5 (cons 7 9))) \Rightarrow (3 5 7 . 9)
- Run boxarrow.rkt for pictures.



length

length

nth

nth

last

last

scale-list

scale-list

increment-list

increment-list

map

map

scale-list using map

scale-list using map

```
(define (scale-list lst n)
  (map lst (lambda (x) (* n x))))
```

increment-list using map

increment-list using map

```
(define (increment-list lst)
  (map lst (lambda (x) (+ x 1))))
```

${\sf append}$

append

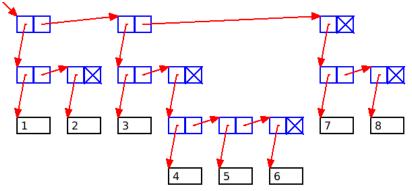
remove

remove

Trees

Trees

► Run boxarrow.rkt for pictures.



count-leaves

count-leaves

fringe

fringe

sum-fringe

sum-fringe

map-tree

map-tree

scale-tree using map-tree

scale-tree using map-tree

```
(define (scale-tree tree factor)
  (map-tree tree (lambda (x) (* x factor))))
```

increment-tree using map-tree

increment-tree using map-tree

```
(define (increment-tree tree)
  (map-tree tree inc))
```