## CSCI 301, Winter 2018 Math Exercises #5

## YOUR NAME HERE

Due date: Monday, February 12, midnight.

- 1. Consider the relation | (divides) on the set  $\mathbb{Z}$ .
  - (a) Prove or disprove: | is reflexive.
  - (b) Prove or disprove: | is symmetric.
  - (c) Prove or disprove: | is transitive.
- 2. Prove or disprove: If R and S are two equivalence relations on a set A, then  $R \cup S$  is also an equivalence relation on A.
- 3. Consider the function  $\theta:\{0,1\}\times\mathbb{N}\to\mathbb{Z}$  defined as  $\theta(a,b)=a-2ab+b$ 
  - (a) Prove or disprove:  $\theta$  is injective.
  - (b) Prove or disprove:  $\theta$  is surjective.