

Part 2.

From part 1, we know that the parabola curve is determined by the function $D = \frac{T^2}{4}$.

We can rewrite the equation as $4 = \frac{T^2}{D}$

$$\Rightarrow 4 = \frac{(\lambda_1 + \lambda_2)^2}{\lambda_1 \lambda_2} \quad (\because T = \lambda_1 + \lambda_2, D = \lambda_1 \lambda_2)$$

$$= \frac{\lambda_1^2 + \lambda_2^2 + 2\lambda_1 \lambda_2}{\lambda_1 \lambda_2}$$

$$= \frac{\lambda_1}{\lambda_2} + \frac{\lambda_2}{\lambda_1} + 2.$$

from the red line to the right,
 λ_1 and λ_2 have same signs.

We assume that $|\lambda_1| > |\lambda_2|$.

\Rightarrow the convergence rate will be exponential in $|\frac{\lambda_2}{\lambda_1}|$

From the cited graph and knowledge, we know that if λ_1 and λ_2 have different signs, the position of (D, T) of that matrix will be on the saddle part.

From the graph what we plot, the red color is almost a vertex line.

In this case, $D = \lambda_1 \lambda_2 \approx 0$, which means λ_2 has a very small value. then

$T = \lambda_1 + \lambda_2 \approx \lambda_1$, which means $(0, \lambda_1)$ is almost the position of these kind of

iteration. In our case, the red color represents iterations from 1 to 5. It

also verified that if $|\lambda_2|/|\lambda_1|$ is small, the power method will converge quickly.

If $|\lambda_2|/|\lambda_1|$ is closed to 1, then the power method will converge slowly and need more iteration to succeed. and also the position of (D, T) is will be more close to the curve $D = \frac{T^2}{4}$.

If $\lambda_1 + \lambda_2 = 0$, then the position will be on the axis of determinant.