

## Group - 31

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# DCT IN VERILOG HDL

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## Abstract

DCT (Discrete Cosine Transform), a widely used lossy image compression technique, implemented in Verilog, a Hardware Description Language, mostly using in designing for FPGAs. The data retainment is approximately 99.95% for this implementation. A python script has been used to complement this process by converting an image into its RGB matrices format that is being fed into the verilog program. No processes related to DCT/IDCT has been implemented in the python script and thus can be modified as per the user's requirement.

DCT can be implemented in 2 ways, a direct approach using a DCT equation and a matrix approach which deals with the manipulation of matrices to achieve similar results. This project follows the latter approach to attain more accuracy in verilog's perspective. All the matrix operations are defined for 8 x 8 matrix as DCT is highly compatible for this specification. Inverse DCT(IDCT)has also been implemented in the similar fashion.

## Usage

1. We have chosen to implement the algorithm on a fixed image size of 256\*256 pixels which is automatically resized by the python script and ordered correctly according to the required specifications.
2. The verilog code is run for 3.72  $\mu$ s with each 8 x 8 matrix operated per ns(or 16 integers in the case of IDCT).

## Algorithm

1. The image is given as input in 256x256x3 format with each 8x8 per instantiation.
2.  $T * 10^3$ , Q matrices are attained by a generator written in python and  $T_*$   
 $10^3(\text{transpose of } T)$  is found in verilog
3. 128 is removed from each integer in the matrix to preserve a mean value of 0.
4. A set of operations are applied as mentioned below.
5. The result is encoded upto 32 integers.
  - $Z = T M T_*$
  - $P = Z / Q$  (element wise division)

Note: Q is multiplied by  $10^6$  to preserve a floating point precision upto 3 decimals which is negated during the division process with rounding off as per the usual trend.

## Modules

1. `mat_mul(c,a,b)`  
 Matrix multiplication of a and b each of port size 4096 bits.
2. `mat_transpose(b,a)`  
 Transpose for T matrix of port size 4096
3. `division(out,inp,q)` and `multiply(out,inp,q)`  
 Element wise division/multiplication of inp and q each of port size 4096 bits. Rounding off has been implemented in division module.
4. `encode(zig,W,x)` and `decode(X,C,d)`  
 Encoding in a zig-zag pattern as required for DCT algorithm and Decoding on a similar fashion keeping rest 0. Port size of W,X being 4096 bits, zig and C with 2048 bits, x and d with 192 bits(carrying a sequence to initiate the pattern which is also generated by the python code)

5. `dct_test1(C,M,T,T_,Q,x)` and `idct_test1(N,C,T,T_,ss,Q)`

Main module controlling the operations to be done as per the algorithm. Port size of M,N,T,T\_,Q being 4096 bits, C being 2048 bits and x and ss being 192 bits.

6. `dct_tb_final` and `idct_tb_final`

Testbench module which handles input/output matrices from "out\_dct.txt"/"out\_idct.txt" and constants from "Matrix.txt"

## Source Code

```
//##### Code consisting the algorithm#####

module mat_mul(c,a,b);

input [4095:0]a;

input [4095:0]b;

output reg [4095:0]c;

integer i,j,k,x,y,z,sum;

always @ (a or b)

begin

    for(i=0;i<8;i=i+1)

        begin

            for(j=0;j<8;j=j+1)

                begin

                    x = 8*i+j;

                    sum = 0;

                    for(k=0;k<8;k=k+1)

                        begin

                            y = 8*i+k;

                            z = 8*k+j;
```

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```
    sum = sum+a[y*64+:64]*b[z*64+:64];  
  
end  
  
c[x*64+:64] = sum;  
  
    end  
  
end  
  
end  
  
endmodule
```

```
module mat_transpose(b,a);  
  
output reg [4095:0]b;  
  
input [4095:0]a;  
  
integer i,j,x,y;  
  
always @ a  
  
begin  
  
    for(i=0;i<8;i=i+1)  
        begin  
            for(j=0;j<8;j=j+1)  
                begin  
                    x = 8*i+j;  
                    y = 8*j+i;  
                    b[x*64+:64] = a[y*64+:64];  
                end  
            end  
        end  
    end  
  
end  
  
end  
  
endmodule
```

```
module division(out,inp,q);

input [4095:0] inp;

input [4095:0]q;

output reg [4095:0] out ;

integer zz;

integer a,b;

integer i;


always@(inp) begin

for(i=0;i<=63;i=i+1)

begin

if(inp[63+64*i]!=1) begin

a=inp[i*64+: 64];

b=q[i*64+: 64];

zz=a/b + ((a%b>=b/2)?1:0);

out[i*64+: 64]=zz;

end

else begin

a=~(inp[i*64+: 64]-1 );

b=q[i*64+: 64];

zz= a/b + ((a%b>=b/2)?1:0);

out[i*64+: 64]=~zz+1;

end

end

end
```

```
end
```

```
endmodule
```

```
module multiply(out,inp,q);
```

```
input [4095:0] inp;
```

```
input [4095:0]q;
```

```
output reg[4095:0] out ;
```

```
integer i;
```

```
always@(inp) begin
```

```
for(i=0;i<=63;i=i+1)
```

```
out[i*64+:64]=inp[i*64+:64]*q[i*64+:64];
```

```
end
```

```
endmodule
```

```
module encode(zig,W,x);
```

```
input [4095:0] W;
```

```
output reg [2047:0]zig;
```

```
integer i;
```

```
integer j,k;
```

```
input [191:0]x;
```

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```
always@(W)
```

```
begin
```

```
for(i=0;i<=31;i=i+1)
```

```
begin
```

```
  j=x[i*6+:6];
```

```
  zig[i*64+:64]=W[j*64+:64];
```

```
end
```

```
end
```

```
endmodule
```

```
module decode(X,C,d);
```

```
  input [2047:0]C;
```

```
  output reg [4095:0]X;
```

```
  input [191:0]d;
```

```
  integer i,j;
```

```
  always@(C)
```

```
  begin
```

```
    X=4095'b0;
```

```
    for(i=0;i<=31;i=i+1)
```

```
    begin
```



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```
j=d[i*6+:6];
```

```
X[j*64+:64]=C[i*64+:64];
```

```
end
```

```
end
```

```
endmodule
```

```
module dct_test1(C,M,T,T_,Q,x);
```

```
output [2047:0]C;
```

```
input [4095:0]M;
```

```
input [4095:0]T,T_;
```

```
input [4095:0]Q;
```

```
input [191:0]x;
```

```
reg [4095:0]X;
```

```
wire [4095:0]Y;
```

```
wire [4095:0]Z;
```

```
wire [4095:0]W;
```

```
wire [4095:0]P;
```

```
reg [4095:0]D;
```

```
integer i;
```

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```
always@(M)
```

```
begin
```

```
for(i = 0;i <=63;i = i+1)
```

```
begin
```

```
    D[i*64 +: 64] = 64'd1000000;
```

```
    X[i*64 +: 64] = M[i*64 +: 64]-128 ;
```

```
end
```

```
end
```

```
mat_mul mat_mul1(Y,T,X);
```

```
mat_mul mat_mul2(Z,Y,T_);
```

```
multiply multiply_1(W,D,Q);
```

```
division division_1(P,Z,W);
```

```
encode encode_1(C,P,x);
```

```
endmodule
```

```
module idct_test1(N,C,T,T_ss,Q);
```

```
output reg[4095:0]N;
```

```
input [2047:0]C;
```

```
input [4095:0]T_,T;
```

```
input [4095:0]Q;
```

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```
input [191:0]ss;
```

```
integer i;
```

```
wire [4095:0]X;
```

```
reg [4095:0]Y;
```

```
wire [4095:0]Z;
```

```
wire [4095:0]W;
```

```
wire [4095:0]R;
```

```
wire [4095:0]P;
```

```
decode decode_1(X,C,ss);
```

```
multiply multiply_1(R,X,Q);
```

```
mat_mul mat_mul_1(Z,T,R);
```

```
mat_mul mat_mul_2(W,Z,T);
```

```
initial
```

```
begin
```

```
for(i=0;i<=63;i=i+1)
```

```
begin
```

```
Y[i*64+: 64] =64'd1000000;
```

```
end
```

```
end
```

```
division division_1(P,W,Y);
```

```
always @( P )
```

```
begin
```

```
for(i=0;i<=63;i=i+1)
```

```
begin
```

```
N[i*64+: 64]=P[i*64+: 64]+128;
```

```
end
```

```
end
```

```
endmodule
```

```
##### End of source code #####
```

```
##### Start of Testbench (input/output) code #####
```

```
module dct_tb_final;
```

```
integer M,i,j,Matrix,image,out,x,y;
```

```
reg [4095:0]T;
```

```
wire [4095:0]T_trans;
```

```
reg [4095:0]Q;
```

```
reg [4095:0]original;
```

```
reg [191:0]ss;
```

```
integer zz,k,l;
```

```
wire [2047:0]C;
```

```
wire [4095:0]P;
```

```
dct_test1 dct(C,original,T,T_trans,Q,ss);
```

```
mat_transpose transpose(T_trans,T);
```

```
initial
```

```
begin
```

```
    Matrix=$fopen("Matrix.txt","r");
```

```
    image=$fopen("image.txt","r");
```

```
    out=$fopen("out_dct.txt","w");
```

```
    for(i=0;i<64;i=i+1)
```

```
    begin
```

```
        x=$fscanf(Matrix,"%d",y);
```

```
        T[i*64+:64]=y;
```

```
    end
```

```
    for(i=0;i<64;i=i+1)
```

```
    begin
```

```
        x=$fscanf(Matrix,"%d",y);
```

```
        Q[i*64+:64]=y;
```

```
    end
```

```
    for(i=0;i<=31;i=i+1)
```

```
    begin
```

```
        x=$fscanf(Matrix,"%d",y);
```

```

        ss[i*6 +:6]=y;

    end

for(k=0;k<3072;k=k+1) begin

    for(i=0;i<64;i=i+1)

        begin

            x=$fscanf(image,"%d",y);

            original[i*64 +:64]=y;

        end

        #1

        for(j=0;j<=31;j=j+1)

            begin

                $display("%0d # %0d $ %0d ",$signed(C[64*j +:64]),Q[j*64 +:64],T[j*64 +:64]);

            end

            for(l=0;l<=31&&k<=3072;l = l+1) begin

                $fwrite(out,"%0d ",$signed(C[l*64 +:64]));

            end

            $fwrite(out,"\n");

        end

    end

end

endmodule

```

```
module idct_tb_final;

integer M,i,j,Matrix,image,out,x,y,k,l;

reg [4095:0]T;

wire [4095:0]T_trans;

reg [4095:0]Q;

wire [4095:0]original;

reg [2047:0]C;

reg [191:0]ss;


idct_test1 idct(original,C,T,T_trans,ss,Q);

mat_transpose transpose(T_trans,T);

initial begin

    Matrix=$fopen("Matrix.txt","r");

    image=$fopen("out_dct.txt","r");

    out=$fopen("out_idct.txt","w");

    for(i=0;i<64;i=i+1)

        begin

            x=$fscanf(Matrix,"%d",y);

            T[i*64+:64]=y;

        end

    for(i=0;i<64;i=i+1)

        begin

            x=$fscanf(Matrix,"%d",y);

            Q[i*64+:64]=y;

        end

    end
```

```

    for(i=0;k<=31;i=i+1)

    begin

        x=$fscanf(Matrix,"%d",y);

        ss[i*6 +:6]=y;

    end

for(k=0;k<3072;k=k+1) begin

    for(i=0;k<=31;i=i+1)

    begin

        x=$fscanf(image,"%d",y);

        C[i*64 +:64]=y;

    end #1

    for(j=0;j<=63;j=j+1)

    begin

        $display("%0d # %0d $ %0d ",$signed(original[64*j +:64]),Q[j*64 +:64],T[j*64 +:64]);

    end

    for(l=0;l<=63&& k<=3072;l = l+1) begin

        $fwrite(out,"%0d ",$signed(original[l*64 +:64]));

    end

    $fwrite(out,"\n");

end

end

endmodule

```

```
##### End of Testbench #####
```



## References

- <https://www.math.cuhk.edu.hk/~lmlui/dct.pdf>
- <https://www.geeksforgeeks.org/discrete-cosine-transform-algorithm-program/>
- PPT for reference:  
<https://docs.google.com/presentation/d/1BwLgxYBSefvEc3VN8k9dOJzzW3v2QyhqxcZhMWfgLJs/edit#slide=id.p>