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Convolutional neural network layers

In this notebook, we will build the convolutional neural network layers. This will be followed by a spatial batchnorm, and then in the final notebook of this assignment, we will train a CNN to further improve the validation accuracy on CIFAR-10.

```
In [1]:
## Import and setups
import time
import numpy as np
import matplotlib.pyplot as plt
from nndl.conv layers import
from utils.data_utils import get_CIFAR10_data
from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
from utils.solver import Solver
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray
# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load_ext autoreload
%autoreload 2
def rel_error(x, y):
   "" returns relative error """
 return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

Implementing CNN layers

Just as we implemented modular layers for fully connected networks, batch normalization, and dropout, we'll want to implement modular layers for convolutional neural networks. These layers are in nndl/conv layers.py.

Convolutional forward pass

Begin by implementing a naive version of the forward pass of the CNN that uses for loops. This function is conv_forward_naive in nndl/conv_layers.py. Don't worry about efficiency of implementation. Later on, we provide a fast implementation of these layers. This version ought to test your understanding of convolution. In our implementation, there is a triple for loop.

After you implement conv_forward_naive, test your implementation by running the cell below.

```
In [2]:
```

```
x \text{ shape} = (2, 3, 4, 4)
w_{shape} = (3, 3, 4, 4)
x = np.linspace(-0.1, 0.5, num=np.prod(x_shape)).reshape(x_shape)
w = np.linspace(-0.2, 0.3, num=np.prod(w_shape)).reshape(w_shape)
b = np.linspace(-0.1, 0.2, num=3)
conv_param = {'stride': 2, 'pad': 1}
out, _ = conv_forward_naive(x, w, b, conv_param)
[[ 0.21027089, 0.21661097], [ 0.22847626, 0.23004637]],
                           [[ 0.50813986, 0.54309974],
                             [ 0.64082444, 0.67101435]]],
                           [[[-0.98053589, -1.03143541],
                             [-1.19128892, -1.24695841]],
                           [[ 0.69108355, 0.66880383],
                             [ 0.59480972, 0.56776003]],
                           [[ 2.36270298, 2.36904306],
[ 2.38090835, 2.38247847]]]])
# Compare your output to ours; difference should be around 1e-8
print('Testing conv_forward_naive')
print('difference: ', rel_error(out, correct_out))
Testing conv_forward_naive
```

Convolutional backward pass

difference: 2.2121476417505994e-08

Now, implement a naive version of the backward pass of the CNN. The function is conv_backward_naive in nnd1/conv_layers.py . Don't worry about efficiency of implementation. Later on, we provide a fast implementation of these layers. This version ought to test your understanding of convolution. In our implementation, there is a guadruple for loop.

After you implement conv_backward_naive, test your implementation by running the cell below.

```
x = np.random.randn(4, 3, 5, 5)
w = np.random.randn(2, 3, 3, 3)
b = np.random.randn(2,)
dout = np.random.randn(4, 2, 5, 5)
conv_param = {'stride': 1, 'pad': 1}
out, cache = conv forward naive(x,w,b,conv param)
dx_num = eval_numerical_gradient_array(lambda x: conv_forward_naive(x, w, b, conv_param)[0], x, dout)
dw_num = eval_numerical_gradient_array(lambda w: conv_forward_naive(x, w, b, conv_param)[0], w, dout)
db_num = eval_numerical_gradient_array(lambda b: conv_forward_naive(x, w, b, conv_param)[0], b, dout)
out, cache = conv forward naive(x, w, b, conv param)
dx, dw, db = conv_backward_naive(dout, cache)
# Your errors should be around 1e-9
print('Testing conv_backward_naive function')
print('dx error: ', rel_error(dx, dx_num))
print('dw error: ', rel_error(dw, dw_num))
print('db error: ', rel_error(db, db_num))
Testing conv_backward_naive function
dx error: 7.062629979321658e-09
dw error: 8.294887090081975e-11
db error: 2.522745337869892e-11
```

Max pool forward pass

In this section, we will implement the forward pass of the max pool. The function is $max_pool_forward_naive$ in $nndl/conv_layers.py$. Do not worry about the efficiency of implementation.

After you implement max_pool_forward_naive , test your implementation by running the cell below.

```
In [4]:
```

```
x \text{ shape} = (2, 3, 4, 4)
x = np.linspace(-0.3, 0.4, num=np.prod(x_shape)).reshape(x_shape)
pool_param = {'pool_width': 2, 'pool_height': 2, 'stride': 2}
out, _ = max_pool_forward_naive(x, pool_param)
correct_out = np.array([[[[-0.26315789, -0.24842105],
                          [-0.20421053, -0.18947368]],
                         [[-0.14526316, -0.13052632],
                          [-0.08631579, -0.07157895]],
                         [[-0.02736842, -0.01263158],
                          [ 0.03157895, 0.04631579]]],
                        [[[ 0.09052632, 0.10526316],
                          [ 0.14947368, 0.16421053]],
                         [[ 0.20842105, 0.22315789],
                          [ 0.26736842, 0.28210526]],
                         [[ 0.32631579, 0.34105263],
                          [ 0.38526316, 0.4
                                                   1111)
# Compare your output with ours. Difference should be around 1e-8.
print('Testing max_pool_forward_naive function:')
print('difference: ', rel_error(out, correct_out))
```

Testing max_pool_forward_naive function: difference: 4.1666665157267834e-08

Max pool backward pass

In this section, you will implement the backward pass of the max pool. The function is <code>max_pool_backward_naive</code> in <code>nndl/conv_layers.py</code>. Do not worry about the efficiency of implementation.

After you implement max_pool_backward_naive , test your implementation by running the cell below.

```
In [5]:
```

```
x = np.random.randn(3, 2, 8, 8)
dout = np.random.randn(3, 2, 4, 4)
pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2}

dx_num = eval_numerical_gradient_array(lambda x: max_pool_forward_naive(x, pool_param)[0], x, dout)

out, cache = max_pool_forward_naive(x, pool_param)
dx = max_pool_backward_naive(dout, cache)

# Your error should be around le-12
print('Testing max_pool_backward_naive function:')
print('dx error: ', rel_error(dx, dx_num))
```

Testing max_pool_backward_naive function: dx error: 3.275628827601359e-12

Fast implementation of the CNN layers

Implementing fast versions of the CNN layers can be difficult. We will provide you with the fast layers implemented by utils. They are provided in utils/fast_layers.py.

The fast convolution implementation depends on a Cython extension ('pip install Cython' to your virtual environment); to compile it you need to run the following from the utils directory:

```
python setup.py build ext --inplace
```

NOTE: The fast implementation for pooling will only perform optimally if the pooling regions are non-overlapping and tile the input. If these conditions are not met then the fast pooling implementation will not be much faster than the naive implementation.

You can compare the performance of the naive and fast versions of these layers by running the cell below.

You should see pretty drastic speedups in the implementation of these layers. On our machine, the forward pass speeds up by 17x and the backward pass speeds up by 840x. Of course, these numbers will vary from machine to machine, as well as on your precise implementation of the naive layers.

In [7]:

```
from utils.fast_layers import conv_forward_fast, conv_backward_fast
from time import time
x = np.random.randn(100, 3, 31, 31)
w = np.random.randn(25, 3, 3, 3)
b = np.random.randn(25,)
dout = np.random.randn(100, 25, 16, 16)
conv_param = {'stride': 2, 'pad': 1}
t0 = time()
out naive, cache naive = conv forward naive(x, w, b, conv param)
t1 = time()
out fast, cache fast = conv forward fast(x, w, b, conv param)
t2 = time()
print('Testing conv forward fast:')
print('Naive: %fs' % (t1 - t0))
print('Fast: %fs' % (t2 - t1))
print('Speedup: %fx' % ((t1 - t0) / (t2 - t1)))
print('Difference: ', rel_error(out_naive, out_fast))
t0 = time()
dx_naive, dw_naive, db_naive = conv_backward_naive(dout, cache_naive)
t1 = time()
dx_fast, dw_fast, db_fast = conv_backward_fast(dout, cache_fast)
t2 = time()
print('\nTesting conv_backward_fast:')
print('Naive: %fs' % (t1 - t0))
print('Fast: %fs' % (t2 - t1))
print('Speedup: %fx' % ((t1 - t0) / (t2 - t1)))
print('dx difference: ', rel_error(dx_naive, dx_fast))
print('dw difference: ', rel_error(dw_naive, dw_fast))
print('db difference: ', rel_error(db_naive, db_fast))
```

Naive: 4.797780s
Fast: 0.016260s
Speedup: 295.063739x
Difference: 3.358910813299561e-10

Testing conv_backward_fast:
Naive: 6.411861s
Fast: 0.015437s
Speedup: 415.353277x
dx difference: 3.312114063590566e-11
dw difference: 8.591711550812164e-13
db difference: 1.2210168488921396e-15

Testing conv_forward_fast:

```
from utils.fast layers import max pool forward fast, max pool backward fast
x = np.random.randn(100, 3, 32, 32)
dout = np.random.randn(100, 3, 16, 16)
pool param = {'pool height': 2, 'pool width': 2, 'stride': 2}
t0 = time()
out_naive, cache_naive = max_pool_forward_naive(x, pool_param)
t1 = time()
out_fast, cache_fast = max_pool_forward_fast(x, pool_param)
t2 = time()
print('Testing pool_forward_fast:')
print('Naive: %fs' % (t1 - t0))
print('fast: %fs' % (t2 - t1))
print('speedup: %fx' % ((t1 - t0) / (t2 - t1)))
print('difference: ', rel_error(out_naive, out_fast))
t0 = time()
dx_naive = max_pool_backward_naive(dout, cache_naive)
t1 = time()
dx_fast = max_pool_backward_fast(dout, cache_fast)
t2 = time()
print('\nTesting pool_backward_fast:')
print('Naive: %fs' % (t1 - t0))
print('speedup: %fx' % ((t1 - t0) / (t2 - t1)))
print('dx difference: ', rel_error(dx_naive, dx_fast))
Testing pool forward fast:
Naive: 0.383168s
```

fast: 0.003068s speedup: 124.892990x difference: 0.0 Testing pool backward fast: Naive: 0.472052s speedup: 43.260116x dx difference: 0.0

Implementation of cascaded layers

 $We've provided the following functions in \verb| nndl/conv_layer_utils.py : -conv_relu_forward -conv_relu_backward -conv_relu_ba$ conv_relu_pool_backward

These use the fast implementations of the conv net layers. You can test them below:

In [9]:

```
from nndl.conv_layer_utils import conv_relu_pool_forward, conv_relu_pool_backward
x = np.random.randn(2, 3, 16, 16)
w = np.random.randn(3, 3, 3, 3)
b = np.random.randn(3,)
dout = np.random.randn(2, 3, 8, 8)
conv param = {'stride': 1, 'pad': 1}
pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2}
out, cache = conv_relu_pool_forward(x, w, b, conv_param, pool_param)
dx, dw, db = conv_relu_pool_backward(dout, cache)
 dx\_num = eval\_numerical\_gradient\_array(lambda x: conv\_relu\_pool\_forward(x, w, b, conv\_param, pool\_param)[0], x, dout) \\
dw_num = eval_numerical_gradient_array(lambda w: conv_relu_pool_forward(x, w, b, conv_param, pool_param)[0], w, dout)
db_num = eval_numerical_gradient_array(lambda b: conv_relu_pool_forward(x, w, b, conv_param, pool_param)[0], b, dout)
print('Testing conv_relu_pool')
print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
Testing conv_relu_pool
```

dx error: 1.1909928367748963e-08 dw error: 6.429429858441912e-09 db error: 3.2342564403597503e-12

In [10]:

```
from nndl.conv layer utils import conv relu forward, conv relu backward
x = np.random.randn(2, 3, 8, 8)
w = np.random.randn(3, 3, 3, 3)
b = np.random.randn(3,)
dout = np.random.randn(2, 3, 8, 8)
conv param = {'stride': 1, 'pad': 1}
out, cache = conv_relu_forward(x, w, b, conv_param)
dx, dw, db = conv_relu_backward(dout, cache)
dx num = eval_numerical_gradient_array(lambda x: conv_relu_forward(x, w, b, conv_param)[0], x, dout)
dw_num = eval_numerical_gradient_array(lambda w: conv_relu_forward(x, w, b, conv_param)[0], w, dout)
db_num = eval_numerical_gradient_array(lambda b: conv_relu_forward(x, w, b, conv_param)[0], b, dout)
print('Testing conv_relu:')
print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
Testing conv_relu:
dx error: 6.463163991826658e-09
dw error: 3.327983168314795e-09
db error: 8.305987802894473e-11
```

What next?

We saw how helpful batch normalization was for training FC nets. In the next notebook, we'll implement a batch normalization for convolutional neural networks, and then finish off by implementing a CNN to improve our validation accuracy on CIFAR-10.

```
In [ ]:
def conv forward naive(x, w, b, conv param):
 A naive implementation of the forward pass for a convolutional layer.
 The input consists of N data points, each with C channels, height H and width
 W. We convolve each input with F different filters, where each filter spans
 all C channels and has height HH and width HH.
 Input:
 - x: Input data of shape (N, C, H, W)
 - w: Filter weights of shape (F, C, HH, WW)
 - b: Biases, of shape (F.)
 - conv_param: A dictionary with the following keys:
   - 'stride': The number of pixels between adjacent receptive fields in the
     horizontal and vertical directions.
   - 'pad': The number of pixels that will be used to zero-pad the input.
 Returns a tuple of:
 - out: Output data, of shape (N, F, H', W') where H' and W' are given by
   H' = 1 + (H + 2 * pad - HH) / stride

W' = 1 + (W + 2 * pad - WW) / stride
 - cache: (x, w, b, conv_param)
 out = None
 pad = conv_param['pad']
 stride = conv_param['stride']
 # YOUR CODE HERE:
     Implement the forward pass of a convolutional neural network.
     Store the output as 'out'.
     Hint: to pad the array, you can use the function np.pad.
 N, C, H, W = x.shape #get the shape of x
 F, C, HH, WW = w.shape #get the shape of w
 #calculate the output size
 Hout = int(1 + (H + 2 * pad - HH) / stride)
 Wout = int(1 + (W + 2 * pad - WW) / stride)
 #x pad
 padx = np.pad(x, ((0, 0), (0, 0), (pad, pad), (pad, pad)), mode = 'constant')
 #make the output to be the correct size
 out = np.zeros([N, F, Hout, Wout])
 #compute the out
 for data in np.arange(N): #for each data point
   for filter in np.arange(F): #for each filter
     for height in np.arange(Hout): #for each row
       for width in np.arange(Wout): #for each column
          out[data, filter, height, width] = np.sum(padx[data, :, height * stride : height * stride + HH, width * stride : w
 # ----- #
 # END YOUR CODE HERE
 # ______ #
 cache = (x, w, b, conv_param)
 return out, cache
def conv_backward_naive(dout, cache):
 A naive implementation of the backward pass for a convolutional layer.
 Inputs:
 - dout: Upstream derivatives.
 - cache: A tuple of (x, w, b, conv_param) as in conv_forward_naive
 Returns a tuple of:
 - dx: Gradient with respect to x
 - dw: Gradient with respect to w
 - db: Gradient with respect to b
 dx, dw, db = None, None, None
 N, F, out_height, out_width = dout.shape
 x, w, b, conv_param = cache
 stride, pad = [conv_param['stride'], conv_param['pad']]
 xpad = np.pad(x, ((0,0), (0,0), (pad,pad), (pad,pad)), mode='constant')
 num_filts, _, f_height, f_width = w.shape
 # ----- #
 # YOUR CODE HERE:
    Implement the backward pass of a convolutional neural network.
     Calculate the gradients: dx, dw, and db.
```

```
N, C, H, W = x.shape #get the shape of x
 F, C, HH, WW = w.shape #get the shape of w
  #make the output to be the correct size
 dxpad = np.zeros(xpad.shape)
 dx = np.zeros(x.shape)
 dw = np.zeros(w.shape)
 db = np.zeros(b.shape)
  #calculate db
 for filter in np.arange(F):
     db[filter] += np.sum(dout[:, filter, :, :]) # sum all data point's filters
 for data in np.arange(N): #for each data point
      for filter in np.arange(F): #for each filter
          for height in np.arange(out_height): #for each row
              for width in np.arange(out_width): #for each column
                  #dw = xpad[] * dout
                  dw[filter] += xpad[data, :, height * stride : height * stride + HH, width * stride : width * stride + WW] *
                  \#dx = w * dout
                  dxpad[data, :, height * stride : height * stride + HH, width * stride : width * stride + WW] += w[filter] *
 #update dx
 dx = dxpad[:, :, pad : -pad, pad : -pad]
 # END YOUR CODE HERE
 return dx. dw. db
def max_pool_forward_naive(x, pool_param):
 A naive implementation of the forward pass for a max pooling layer.
 Inputs:
   x: Input data, of shape (N, C, H, W)
  - pool_param: dictionary with the following keys:
      'pool height': The height of each pooling region
    - 'pool_width': The width of each pooling region
    - 'stride': The distance between adjacent pooling regions
 Returns a tuple of:
 - out: Output data
  - cache: (x, pool_param)
 out = None
  # YOUR CODE HERE:
     Implement the max pooling forward pass.
 #get the params of pool filter
 pool_height = pool_param.get('pool_height')
pool_width = pool_param.get('pool_width')
 stride = pool_param.get('stride')
 N, C, H, W = x.shape #get the shape of x
 #calculate the output size
 Hout = int(1 + (H - pool_height) / stride)
Wout = int(1 + (W - pool_width) / stride)
 #make the output to be the correct size
 out = np.zeros([N, C, Hout, Wout])
 for data in np.arange(N): # for each data point
   for channel in np.arange(C): # for each channel
        for height in np.arange(Hout): #for each row
           for width in np.arange(Wout): #for each column
               out[data, channel, height, width] = np.max(x[data, channel, height * stride : height * stride + pool_height, w
 # ------ #
 # END YOUR CODE HERE
 cache = (x, pool_param)
 return out, cache
def max pool backward naive(dout, cache):
 A naive implementation of the backward pass for a max pooling layer.
 Inputs:
 - dout: Upstream derivatives
 - cache: A tuple of (x, pool_param) as in the forward pass.
 Returns:
 - dx: Gradient with respect to x
```

```
dx = None
x, pool_param = cache
pool_height, pool_width, stride = pool_param['pool_height'], pool_param['pool_width'], pool_param['stride']
# ============= #
# YOUR CODE HERE:
   Implement the max pooling backward pass.
N, C, H, W = x.shape #get the shape of x
_, _, dout_height, dout_width = dout.shape #get the shape of dout
#make the output to be the correct size
dx = np.zeros(x.shape)
for data in np.arange(N): #for each data point
  for channel in np.arange(C): #for each channel
      for height in np.arange(dout_height): #for each row
          for width in np.arange(dout width): #for each column
              maxnum = np.argmax(x[data, channel, height * stride : height * stride + pool_height, width * stride : width * s maxfield = np.unravel_index(maxnum, [pool_height, pool_width]) dx[data, channel, height * stride : height * stride + pool_height, width * stride : width * stride + pool_width]
# END YOUR CODE HERE
return dx
```

Spatial batch normalization

In fully connected networks, we performed batch normalization on the activations. To do something equivalent on CNNs, we modify batch normalization slightly.

Normally batch-normalization accepts inputs of shape (N, D) and produces outputs of shape (N, D), where we normalize across the minibatch dimension N. For data coming from convolutional layers, batch normalization accepts inputs of shape (N, C, H, W) and produces outputs of shape (N, C, H, W) where the N dimension gives the minibatch size and the (H, W) dimensions give the spatial size of the feature map.

How do we calculate the spatial averages? First, notice that for the C feature maps we have (i.e., the layer has C filters) that each of these ought to have its own batch norm statistics, since each feature map may be picking out very different features in the images. However, within a feature map, we may assume that across all inputs and across all locations in the feature map, there ought to be relatively similar first and second order statistics. Hence, one way to think of spatial batch-normalization is to reshape the (N, C, H, W) array as an (N*H*W, C) array and perform batch normalization on this array.

Since spatial batch norm and batch normalization are similar, it'd be good to at this point also copy and paste our prior implemented layers from HW #4. Please copy and paste your prior implemented code from HW #4 to start this assignment. If you did not correctly implement the layers in HW #4, you may collaborate with a classmate to use their implementations from HW #4. You may also visit TA or Prof OH to correct your implementation.

You'll want to copy and paste from HW #4: - layers.py for your FC network layers, as well as batchnorm and dropout. - layer_utils.py for your combined FC network layers. - optim.py for your optimizers.

Be sure to place these in the nnd1/ directory so they're imported correctly. Note, as announced in class, we will not be releasing our solutions.

If you use your prior implementations of the batchnorm, then your spatial batchnorm implementation may be very short. Our implementations of the forward and backward pass are each 6 lines of code.

In [1]:

```
## Import and setups
import time
import numpy as np
import matplotlib.pyplot as plt
from nndl.conv_layers import
from utils.data utils import get CIFAR10 data
from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
from utils.solver import Solver
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray
# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load_ext autoreload
%autoreload 2
def rel_error(x, y):
     returns relative error """
 return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

Spatial batch normalization forward pass

Implement the forward pass, spatial_batchnorm_forward in nndl/conv_layers.py . Test your implementation by running the cell below.

```
# Check the training-time forward pass by checking means and variances
# of features both before and after spatial batch normalization
N, C, H, W = 2, 3, 4, 5
x = 4 * np.random.randn(N, C, H, W) + 10
print('Before spatial batch normalization:')
print(' Shape: ', x.shape)
print(' Means: ', x.mean(axis=(0, 2, 3)))
print(' Stds: ', x.std(axis=(0, 2, 3)))
# Means should be close to zero and stds close to one
gamma, beta = np.ones(C), np.zeros(C)
bn_param = {'mode': 'train'}
out, _ = spatial_batchnorm_forward(x, gamma, beta, bn_param)
print('After spatial batch normalization:')
print(' Shape: ', out.shape)
print(' Means: ', out.mean(axis=(0, 2, 3)))
print(' Stds: ', out.std(axis=(0, 2, 3)))
# Means should be close to beta and stds close to gamma
gamma, beta = np.asarray([3, 4, 5]), np.asarray([6, 7, 8])
out, _ = spatial_batchnorm_forward(x, gamma, beta, bn_param)
print('After spatial batch normalization (nontrivial gamma, beta):')
print(' Shape: ', out.shape)
print(' Means: ', out.mean(axis=(0, 2, 3)))
print(' Stds: ', out.std(axis=(0, 2, 3)))
Before spatial batch normalization:
  Shape: (2, 3, 4, 5)
Means: [9.05477759 10.20247671 10.88945699]
  Stds: [3.56072987 3.71327858 4.30309899]
After spatial batch normalization:
  Shape: (2, 3, 4, 5)
Means: [ 1.11022302e-17 6.93889390e-17 -2.22044605e-17]
  Stds: [0.99999965 0.99999967 0.99999997 ]
After spatial batch normalization (nontrivial gamma, beta):
  Shape: (2, 3, 4, 5)
Means: [6. 7. 8.]
  Stds: [2.99999895 3.99999866 4.99999851]
```

Spatial batch normalization backward pass

Implement the backward pass, spatial_batchnorm_backward in nndl/conv_layers.py . Test your implementation by running the cell below.

```
In [3]:
N. C. H. W = 2, 3, 4, 5
x = 5 * np.random.randn(N, C, H, W) + 12
gamma = np.random.randn(C)
beta = np.random.randn(C)
dout = np.random.randn(N, C, H, W)
bn_param = {'mode': 'train'}
fx = lambda x: spatial_batchnorm_forward(x, gamma, beta, bn_param)[0]
fg = lambda a: spatial_batchnorm_forward(x, gamma, beta, bn_param)[0]
fb = lambda b: spatial_batchnorm_forward(x, gamma, beta, bn_param)[0]
dx_num = eval_numerical_gradient_array(fx, x, dout)
da_num = eval_numerical_gradient_array(fg, gamma, dout)
db_num = eval_numerical_gradient_array(fb, beta, dout)
 _, cache = spatial_batchnorm_forward(x, gamma, beta, bn_param)
dx, dgamma, dbeta = spatial_batchnorm_backward(dout, cache)
print('dx error: ', rel_error(dx_num, dx))
print('dgamma error: ', rel_error(da_num, dgamma))
print('dbeta error: ', rel_error(db_num, dbeta))
dx error: 7.549500110129972e-09
```

dx error: 7.549500110129972e-09 dgamma error: 1.0955086773552313e-11 dbeta error: 1.1595067532532086e-11

```
In [ ]:
def spatial batchnorm forward(x, gamma, beta, bn param):
 Computes the forward pass for spatial batch normalization.
 Inputs:
 - x: Input data of shape (N, C, H, W)
 - gamma: Scale parameter, of shape (C,)
 - beta: Shift parameter, of shape (C,)
 - bn param: Dictionary with the following keys:
   - mode: 'train' or 'test'; required
   - eps: Constant for numeric stability
   - momentum: Constant for running mean / variance. momentum=0 means that
     old information is discarded completely at every time step, while
     momentum=1 means that new information is never incorporated. The
     default of momentum=0.9 should work well in most situations.
   - running_mean: Array of shape (D,) giving running mean of features
   - running_var Array of shape (D,) giving running variance of features
 Returns a tuple of:
 - out: Output data, of shape (N, C, H, W)
 - cache: Values needed for the backward pass
 out, cache = None, None
 # ------ #
 # YOUR CODE HERE:
    Implement the spatial batchnorm forward pass.
     You may find it useful to use the batchnorm forward pass you
     implemented in HW #4.
 N, C, H, W = x.shape #get the shape of x
 #reshape the input to 2D array for Batch Normalization
 x = x.reshape(N, H, W, C)
 x = x.reshape(N * H * W, C)
 #do the batchnorm forward
 out, cache = batchnorm forward(x, gamma, beta, bn param)
 #reshape the output to (N, C, H, W)
out = out.reshape((N, H, W, C)).transpose(0, 3, 1, 2)
 # END YOUR CODE HERE
 return out, cache
def spatial_batchnorm_backward(dout, cache):
 Computes the backward pass for spatial batch normalization.
 - dout: Upstream derivatives, of shape (N, C, H, W)
 - cache: Values from the forward pass
 Returns a tuple of:
 - dx: Gradient with respect to inputs, of shape (N, C, H, W)
 - dgamma: Gradient with respect to scale parameter, of shape (C,)
 - dbeta: Gradient with respect to shift parameter, of shape (C,)
 dx, dgamma, dbeta = None, None, None
 # ----- #
 # YOUR CODE HERE:
    Implement the spatial batchnorm backward pass.
     You may find it useful to use the batchnorm forward pass you
    implemented in HW #4.
 N, C, H, W = dout.shape #get the shape of dout
 #reshape the dout
 dout = (dout.transpose(0, 2, 3, 1)).reshape(N * H * W, C)
 #do the batchnorm backward
 dx, dgamma, dbeta = batchnorm_backward(dout, cache)
 #reshape the output to de desired format
 dx = dx.reshape(N, C, H, W)
 # END YOUR CODE HERE
```

Convolutional neural networks

In this notebook, we'll put together our convolutional layers to implement a 3-layer CNN. Then, we'll ask you to implement a CNN that can achieve > 65% validation error on CIFAR-10.

If you have not completed the Spatial BatchNorm Notebook, please see the following description from that notebook:

Please copy and paste your prior implemented code from HW #4 to start this assignment. If you did not correctly implement the layers in HW #4, you may collaborate with a classmate to use their layer implementations from HW #4. You may also visit TA or Prof OH to correct your implementation.

You'll want to copy and paste from HW #4: - layers.py for your FC network layers, as well as batchnorm and dropout. - layer_utils.py for your combined FC network layers. - optim.py for your optimizers.

Be sure to place these in the nnd1/ directory so they're imported correctly. Note, as announced in class, we will not be releasing our solutions.

```
In [106]:
```

```
# As usual, a bit of setup
import numpy as np
import matplotlib.pyplot as plt
from nndl.cnn import
from utils.data_utils import get_CIFAR10_data
from utils.gradient_check import eval_numerical_gradient_array, eval_numerical_gradient
from nndl.layers import *
from nndl.conv_layers import *
from utils.fast_layers import *
from utils.solver import Solver
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray
# for auto-reloading external modules
 see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load ext autoreload
%autoreload 2
def rel error(x, y):
  """ returns relative error """
 return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

The autoreload extension is already loaded. To reload it, use: %reload ext autoreload

```
In [107]:
```

```
# Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
for k in data.keys():
    print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
```

```
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

Three layer CNN

In this notebook, you will implement a three layer CNN. The ThreeLayerConvNet class is in nndl/cnn.py. You'll need to modify that code for this section, including the initialization, as well as the calculation of the loss and gradients. You should be able to use the building blocks you have either earlier coded or that we have provided. Be sure to use the fast layers.

The architecture of this CNN will be:

```
conv - relu - 2x2 max pool - affine - relu - affine - softmax
```

We won't use batchnorm yet. You've also done enough of these to know how to debug; use the cells below.

Note: As we are implementing several layers CNN networks. The gradient error can be expected for the eval_numerical_gradient() function. If your W1 max relative error and W2 max relative error are around or below 0.01, they should be acceptable. Other errors should be less than 1e-5.

```
In [109]:
```

```
num inputs = 2
input dim = (3, 16, 16)
reg = 0.0
num classes = 10
X = np.random.randn(num inputs, *input dim)
v = np.random.randint(num classes, size=num inputs)
model = ThreeLayerConvNet(num_filters=3, filter size=3,
                          input_dim=input_dim, hidden dim=7,
                          dtype=np.float64)
loss, grads = model.loss(X, y)
for param name in sorted(grads):
   f = lambda : model.loss(X, y)[0]
   param_grad_num = eval_numerical_gradient(f, model.params[param_name], verbose=False, h=1e-6)
   e = rel_error(param_grad_num, grads[param_name])
   print('{} max relative error: {}'.format(param_name, rel_error(param_grad_num, grads[param_name])))
W1 max relative error: 0.011821375430781197
W2 max relative error: 0.0016865050976615941
W3 max relative error: 1.1990575927951157e-05
b1 max relative error: 9.427363623190101e-06
b2 max relative error: 2.821574180080946e-08
b3 max relative error: 8.538894241102408e-10
```

Overfit small dataset

To check your CNN implementation, let's overfit a small dataset.

In [110]:

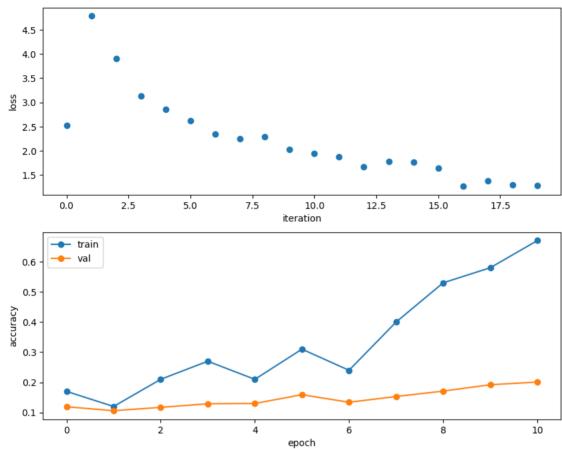
```
num train = 100
small data = {
  'X train': data['X train'][:num train],
  'y_train': data['y_train'][:num_train],
  'X val': data['X val'].
  'y_val': data['y_val'],
}
model = ThreeLayerConvNet(weight_scale=1e-2)
solver = Solver(model, small data,
                num epochs=10, batch size=50,
                update_rule='adam',
                optim_config={
                   'learning_rate': 1e-3,
                verbose=True, print_every=1)
solver.train()
(Iteration 1 / 20) loss: 2.524423
(Epoch 0 / 10) train acc: 0.170000; val acc: 0.119000
```

```
(Iteration 2 / 20) loss: 4.781698
(Epoch 1 / 10) train acc: 0.120000; val_acc: 0.106000
(Iteration 3 / 20) loss: 3.909344
(Iteration 4 / 20) loss: 3.136751
(Epoch 2 / 10) train acc: 0.210000; val_acc: 0.117000
(Iteration 5 / 20) loss: 2.850169
(Iteration 6 / 20) loss: 2.625665
(Epoch 3 / 10) train acc: 0.270000; val_acc: 0.129000
(Iteration 7 / 20) loss: 2.344947
(Iteration 8 / 20) loss: 2.254606
(Epoch 4 / 10) train acc: 0.210000; val_acc: 0.130000
(Iteration 9 / 20) loss: 2.285453
(Iteration 10 / 20) loss: 2.030125
(Epoch 5 / 10) train acc: 0.310000; val_acc: 0.159000
(Iteration 11 / 20) loss: 1.947709
(Iteration 12 / 20) loss: 1.879866
(Epoch 6 / 10) train acc: 0.240000; val_acc: 0.134000
(Iteration 13 / 20) loss: 1.668075
(Iteration 14 / 20) loss: 1.783985
(Epoch 7 / 10) train acc: 0.400000; val_acc: 0.153000
(Iteration 15 / 20) loss: 1.767605
(Iteration 16 / 20) loss: 1.644005
(Epoch 8 / 10) train acc: 0.530000; val_acc: 0.171000
(Iteration 17 / 20) loss: 1.268453
(Iteration 18 / 20) loss: 1.385116
(Epoch 9 / 10) train acc: 0.580000; val acc: 0.192000
(Iteration 19 / 20) loss: 1.297587
(Iteration 20 / 20) loss: 1.282454
(Epoch 10 / 10) train acc: 0.670000; val acc: 0.201000
```

In [111]:

```
plt.subplot(2, 1, 1)
plt.plot(solver.loss_history, 'o')
plt.xlabel('iteration')
plt.ylabel('loss')

plt.subplot(2, 1, 2)
plt.plot(solver.train_acc_history, '-o')
plt.plot(solver.val_acc_history, '-o')
plt.legend(['train', 'val'], loc='upper left')
plt.xlabel('epoch')
plt.ylabel('accuracy')
plt.show()
```



Train the network

Now we train the 3 layer CNN on CIFAR-10 and assess its accuracy.

```
model = ThreeLayerConvNet(weight scale=0.001, hidden dim=500, reg=0.001)
solver = Solver(model, data,
               num epochs=1, batch size=50,
                update rule='adam',
                optim config={
                   'learning_rate': 1e-3,
                verbose=True, print_every=20)
solver.train()
(Iteration 1 / 980) loss: 2.304379
(Epoch 0 / 1) train acc: 0.088000; val_acc: 0.119000
(Iteration 21 / 980) loss: 2.109635
(Iteration 41 / 980) loss: 2.076350
(Iteration 61 / 980) loss: 2.016401
(Iteration 81 / 980) loss: 2.114350
(Iteration 101 / 980) loss: 1.780723
(Iteration 121 / 980) loss: 1.679214
(Iteration 141 / 980) loss: 1.846902
(Iteration 161 / 980) loss: 1.686197
(Iteration 181 / 980) loss: 1.849539
(Iteration 201 / 980) loss: 1.848983
(Iteration 221 / 980) loss: 1.607722
(Iteration 241 / 980) loss: 1.408573
(Iteration 261 / 980) loss: 1.667033
(Iteration 281 / 980) loss: 1.774849
(Iteration 301 / 980) loss: 1.994323
(Iteration 321 / 980) loss: 1.878220
(Iteration 341 / 980) loss: 1.884071
(Iteration 361 / 980) loss: 1.707486
(Iteration 381 / 980) loss: 1.483961
(Iteration 401 / 980) loss: 1.907075
(Iteration 421 / 980) loss: 1.763213
(Iteration 441 / 980) loss: 1.760534
(Iteration 461 / 980) loss: 1.695799
(Iteration 481 / 980) loss: 1.714589
(Iteration 501 / 980) loss: 1.912646
(Iteration 521 / 980) loss: 1.412743
(Iteration 541 / 980) loss: 1.697497
(Iteration 561 / 980) loss: 1.799456
(Iteration 581 / 980) loss: 1.762910
(Iteration 601 / 980) loss: 1.662797
(Iteration 621 / 980) loss: 1.479918
(Iteration 641 / 980) loss: 1.925249
(Iteration 661 / 980) loss: 1.667685
(Iteration 681 / 980) loss: 1.878623
(Iteration 701 / 980) loss: 1.685491
(Iteration 721 / 980) loss: 1.682482
(Iteration 741 / 980) loss: 1.718161
(Iteration 761 / 980) loss: 1.618900
(Iteration 781 / 980) loss: 1.576266
(Iteration 801 / 980) loss: 1.567092
(Iteration 821 / 980) loss: 1.634341
(Iteration 841 / 980) loss: 1.870606
(Iteration 861 / 980) loss: 1.857803
(Iteration 881 / 980) loss: 1.689935
(Iteration 901 / 980) loss: 1.449273
(Iteration 921 / 980) loss: 1.558852
(Iteration 941 / 980) loss: 1.357863
(Iteration 961 / 980) loss: 1.314725
(Epoch 1 / 1) train acc: 0.474000; val acc: 0.445000
```

Get > 65% validation accuracy on CIFAR-10.

In the last part of the assignment, we'll now ask you to train a CNN to get better than 65% validation accuracy on CIFAR-10.

Things you should try:

- Filter size: Above we used 7x7; but VGGNet and onwards showed stacks of 3x3 filters are good.
- Number of filters: Above we used 32 filters. Do more or fewer do better?
- Batch normalization: Try adding spatial batch normalization after convolution layers and vanilla batch normalization aafter affine layers. Do your networks train faster?
- Network architecture: Can a deeper CNN do better? Consider these architectures:
 - [conv-relu-pool]xN conv relu [affine]xM [softmax or SVM]
 - [conv-relu-pool]XN [affine]XM [softmax or SVM]
 - [conv-relu-conv-relu-pool]xN [affine]xM [softmax or SVM]

Tips for training

For each network architecture that you try, you should tune the learning rate and regularization strength. When doing this there are a couple important things to keep in mind:

· If the parameters are working well, you should see improvement within a few hundred iterations

- Remember the coarse-to-fine approach for hyperparameter tuning: start by testing a large range of hyperparameters for just a few training iterations to find the combinations of parameters that are working at all.
- · Once you have found some sets of parameters that seem to work, search more finely around these parameters. You may need to train for more epochs.

In [115]:

```
# ------ #
# YOUR CODE HERE:
   Implement a CNN to achieve greater than 65% validation accuracy
   on CIFAR-10.
#I use 64 3 * 3 filters, with hidden_dim = 400
model = ThreeLayerConvNet(num_filters=64, filter_size=3, weight_scale=0.001, hidden_dim=400, reg=0.001)
#increase the num_epochs and batch_size while adding lr_decay
solver = Solver(model, data,
             num_epochs=8, batch_size=600,
              update_rule='adam',
              optim config={
                'learning_rate': 1e-3,
              1r decay = 0.95,
              verbose=True, print_every=20)
solver.train()
# END YOUR CODE HERE
```

```
(Iteration 1 / 648) loss: 2.305887
(Epoch 0 / 8) train acc: 0.096000; val_acc: 0.119000
(Iteration 21 / 648) loss: 1.776225
(Iteration 41 / 648) loss: 1.600341
(Iteration 61 / 648) loss: 1.443222
(Iteration 81 / 648) loss: 1.362421
(Epoch 1 / 8) train acc: 0.549000; val_acc: 0.557000
(Iteration 101 / 648) loss: 1.403169
(Iteration 121 / 648) loss: 1.212663
(Iteration 141 / 648) loss: 1.229137
(Iteration 161 / 648) loss: 1.167617
(Epoch 2 / 8) train acc: 0.626000; val acc: 0.593000
(Iteration 181 / 648) loss: 1.214655
(Iteration 201 / 648) loss: 1.087428
(Iteration 221 / 648) loss: 1.097019
(Iteration 241 / 648) loss: 1.077913
(Epoch 3 / 8) train acc: 0.648000; val_acc: 0.606000
(Iteration 261 / 648) loss: 1.013566
(Iteration 281 / 648) loss: 0.987600
(Iteration 301 / 648) loss: 0.998555
(Iteration 321 / 648) loss: 1.009989
(Epoch 4 / 8) train acc: 0.700000; val_acc: 0.617000
(Iteration 341 / 648) loss: 0.916954
(Iteration 361 / 648) loss: 0.952466
(Iteration 381 / 648) loss: 0.823338
(Iteration 401 / 648) loss: 0.889315
(Epoch 5 / 8) train acc: 0.757000; val_acc: 0.635000
(Iteration 421 / 648) loss: 0.924732
(Iteration 441 / 648) loss: 0.762855
(Iteration 461 / 648) loss: 0.797278
(Iteration 481 / 648) loss: 0.810951
(Epoch 6 / 8) train acc: 0.775000; val_acc: 0.638000
(Iteration 501 / 648) loss: 0.771332
(Iteration 521 / 648) loss: 0.739867
(Iteration 541 / 648) loss: 0.750929
(Iteration 561 / 648) loss: 0.763980
(Epoch 7 / 8) train acc: 0.775000; val_acc: 0.651000
(Iteration 581 / 648) loss: 0.635425
(Iteration 601 / 648) loss: 0.714568
(Iteration 621 / 648) loss: 0.685466
(Iteration 641 / 648) loss: 0.784730
(Epoch 8 / 8) train acc: 0.818000; val_acc: 0.652000
```

```
In [ ]:
class ThreeLayerConvNet(object):
 A three-layer convolutional network with the following architecture:
 conv - relu - 2x2 max pool - affine - relu - affine - softmax
 The network operates on minibatches of data that have shape (N, C, H, W)
 consisting of N images, each with height H and width W and with C input
 channels.
 def __init__(self, input_dim=(3, 32, 32), num_filters=32, filter size=7,
              hidden dim=100, num classes=10, weight scale=1e-3, reg=0.0,
              dtype=np.float32, use_batchnorm=False):
   Initialize a new network.
   Inputs:
   - input_dim: Tuple (C, H, W) giving size of input data
   - num filters: Number of filters to use in the convolutional layer
   - filter_size: Size of filters to use in the convolutional layer
   - hidden_dim: Number of units to use in the fully-connected hidden layer
   - num_classes: Number of scores to produce from the final affine layer.
   - weight_scale: Scalar giving standard deviation for random initialization
    of weights.
   - reg: Scalar giving L2 regularization strength
   - dtype: numpy datatype to use for computation.
   self.use batchnorm = use batchnorm
   self.params = {}
   self.reg = reg
   self.dtype = dtype
   # ----- #
   # YOUR CODE HERE:
      Initialize the weights and biases of a three layer CNN. To initialize:
         - the biases should be initialized to zeros.
         - the weights should be initialized to a matrix with entries
            drawn from a Gaussian distribution with zero mean and
            standard deviation given by weight scale.
   C, H, W = input_dim #get the input dimensions
   #initialize the weights and biases for three lavers
   #conv - relu - 2x2 max pool
   self.params['W1'] = np.random.normal(0, scale = weight_scale, size = (num_filters, C, filter_size, filter_size))
   self.params['b1'] = np.zeros(num_filters)
   #affine - relu
   self.params['W2'] = np.random.normal(0, scale = weight_scale, size = (num_filters * (H // 2) * (W // 2), hidden_dim))
   self.params['b2'] = np.zeros(hidden_dim)
   #affine - softmax
   self.params['W3'] = np.random.normal(0, scale = weight_scale, size = (hidden_dim, num_classes))
   self.params['b3'] = np.zeros(num_classes)
    # ------ #
   # END YOUR CODE HERE
   for k, v in self.params.items():
     self.params[k] = v.astype(dtype)
 def loss(self, X, y=None):
   Evaluate loss and gradient for the three-layer convolutional network.
   Input / output: Same API as TwoLayerNet in fc net.py.
   W1, b1 = self.params['W1'], self.params['b1']
   W2, b2 = self.params['W2'], self.params['b2']
W3, b3 = self.params['W3'], self.params['b3']
   # pass conv_param to the forward pass for the convolutional layer
   filter_size = W1.shape[2]
conv_param = {'stride': 1, 'pad': (filter_size - 1) / 2}
   # pass pool_param to the forward pass for the max-pooling layer
   pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2}
   scores = None
```

Implement the forward pass of the three layer CNN. Store the output

YOUR CODE HERE:

scores as the variable "scores".

```
#conv - relu - 2x2 max pool
convout, convcache = conv_relu_pool_forward(X, W1, b1, conv_param, pool_param)
#affine - relu
arout, arcache = affine relu forward(convout, W2, b2)
scores, ascache = affine_forward(arout, W3, b3)
# END YOUR CODE HERE
if y is None:
 return scores
loss, grads = 0, {}
# YOUR CODE HERE:
   Implement the backward pass of the three layer CNN. Store the grads
   in the grads dictionary, exactly as before (i.e., the gradient of
   self.params[k] will be grads[k]). Store the loss as "loss", and
  don't forget to add regularization on ALL weight matrices.
#calculate the softmax loss
loss, dscores = softmax_loss(scores, y)
#update the loss based on the regularization
loss += 0.5 * self.reg * (np.sum(W1 ** 2) + np.sum(W2 ** 2) + np.sum(W3 ** 2))
#affine backward
dab, grads['W3'], grads['b3'] = affine_backward(dscores, ascache)
#affine-relu backward
dconv, grads['W2'], grads['b2'] = affine_relu_backward(dab, arcache)
#conv-relu-pool backward
dx, grads['W1'], grads['b1'] = conv_relu_pool_backward(dconv, convcache)
#update the gradients of weights
grads['W1'] += grads['W1'] * self.reg
grads['W2'] += grads['W2'] * self.reg
grads['W3'] += grads['W3'] * self.reg
# END YOUR CODE HERE
return loss, grads
```

In []: