Optimization for Fully Connected Networks

In this notebook, we will implement different optimization rules for gradient descent. We have provided starter code; however, you will need to copy and paste your code from your implementation of the modular fully connected nets in HW #3 to build upon this.

Utils has a solid API for building these modular frameworks and training them, and we will use this very well implemented framework as opposed to "reinventing the wheel." This includes using the Solver, various utility functions, and the layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils.

In [1]:

```
## Import and setups
import time
import numpy as np
import matplotlib.pyplot as plt
from nndl.fc_net import *
from utils.data utils import get CIFAR10 data
from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
from utils.solver import Solver
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray
# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load ext autoreload
%autoreload 2
def rel_error(x, y):
       returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

In [2]:

```
# Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
for k in data.keys():
    print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000, 3)
```

Building upon your HW #3 implementation

Copy and paste the following functions from your HW #3 implementation of a modular FC net:

- affine_forward in nndl/layers.py
- affine_backward in nndl/layers.py
- relu_forward in nndl/layers.py
- relu_backward in nndl/layers.py
- affine_relu_forward in nndl/layer_utils.py
- affine_relu_backward in nndl/layer_utils.py
- The FullyConnectedNet class in nndl/fc_net.py

Test all functions you copy and pasted

In [3]:

```
from nndl.layer tests import *
affine forward test(); print('\n')
affine backward_test(); print('\n')
relu_forward_test(); print('\n')
relu_backward_test(); print('\n')
affine_relu_test(); print('\n')
fc_net_test()
If affine forward function is working, difference should be less than 1e-9:
difference: 9.769849468192957e-10
If affine backward is working, error should be less than 1e-9::
dx error: 1.2455458114089566e-09
dw error: 1.0100861375257425e-10
db error: 8.694433375463264e-12
If relu forward function is working, difference should be around 1e-8:
difference: 4.999999798022158e-08
If relu forward function is working, error should be less than 1e-9:
dx error: 3.2755929343887946e-12
If affine_relu_forward and affine_relu_backward are working, error should be less than 1e-9::
dx error: 9.978775843138903e-11
dw error: 5.584063719505243e-11
db error: 8.186275172646318e-12
Running check with reg = 0
Initial loss: 2.302831138122639
W1 relative error: 1.755746613954502e-07
W2 relative error: 2.830768166750822e-07
W3 relative error: 5.264069974571739e-08
b1 relative error: 4.1372599460877857e-08
b2 relative error: 1.5703656015961528e-08
b3 relative error: 1.506572443464428e-10
Running check with reg = 3.14
Initial loss: 7.0201342602243155
W1 relative error: 6.293623940679278e-08
W2 relative error: 1.7880526681525946e-08
W3 relative error: 1.828946274046096e-08
b1 relative error: 4.603002111865993e-08
b2 relative error: 8.21908049827187e-09
b3 relative error: 9.70907154708018e-11
```

Training a larger model

In general, proceeding with vanilla stochastic gradient descent to optimize models may be fraught with problems and limitations, as discussed in class. Thus, we implement optimizers that improve on SGD.

SGD + momentum

In the following section, implement SGD with momentum. Read the nndl/optim.py API, which is provided by CS231n, and be sure you understand it. After, implement sgd_momentum in nndl/optim.py . Test your implementation of sgd_momentum by running the cell below.

```
from nndl.optim import sgd_momentum
N, D = 4, 5
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
config = {'learning_rate': 1e-3, 'velocity': v}
next_w, _ = sgd_momentum(w, dw, config=config)
expected_next_w = np.asarray([
     [ 0.1406,
                       0.20738947, 0.27417895, 0.34096842, 0.40775789],
     [ 0.47454737, 0.54133684, 0.60812632, 0.67491579, 0.74170526], [ 0.80849474, 0.87528421, 0.94207368, 1.00886316, 1.07565263], [ 1.14244211, 1.20923158, 1.27602105, 1.34281053, 1.4096 ]]
expected_velocity = np.asarray([
                      0.55475789, 0.56891579, 0.58307368, 0.59723158],
     [ 0.5406,
     [ 0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],
[ 0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053],
[ 0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096 ]]
print('next w error: {}'.format(rel error(next w, expected next w)))
print('velocity error: {}'.format(rel error(expected velocity, config['velocity'])))
```

next_w error: 8.882347033505819e-09
velocity error: 4.269287743278663e-09

SGD + Nesterov momentum

Implement sgd nesterov momentum in ndl/optim.py .

In [6]:

```
from nndl.optim import sgd_nesterov_momentum
N, D = 4, 5
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
config = {'learning_rate': 1e-3, 'velocity': v}
next_w, _ = sgd_nesterov_momentum(w, dw, config=config)
expected_next_w = np.asarray([
                     0.15246105, 0.21778211, 0.28310316, 0.34842421],
    [0.08714.
    [0.41374526, 0.47906632, 0.54438737, 0.60970842, 0.67502947], [0.74035053, 0.80567158, 0.87099263, 0.93631368, 1.00163474], [1.06695579, 1.13227684, 1.19759789, 1.26291895, 1.32824 ]]
                                                                                 ]])
expected_velocity = np.asarray([
                      0.55475789, 0.56891579, 0.58307368, 0.59723158],
    [ 0.5406,
      \hbox{\tt [ 0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],} \\
    [ 0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053], [ 0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096 ]]
print('next_w error: {}'.format(rel_error(next_w, expected_next_w)))
print('velocity error: {}'.format(rel error(expected velocity, config['velocity'])))
```

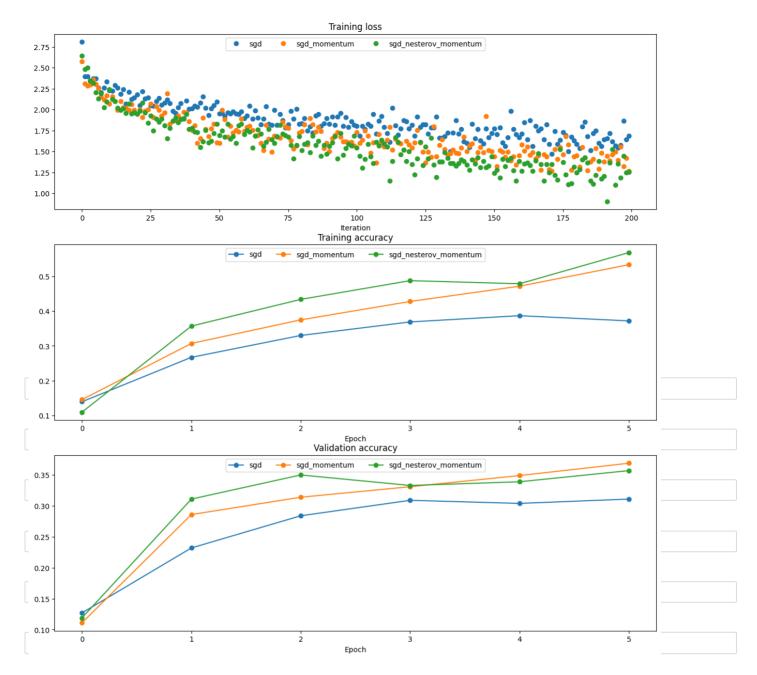
next_w error: 1.0875186845081027e-08
velocity error: 4.269287743278663e-09

Evaluating SGD, SGD+Momentum, and SGD+NesterovMomentum

Run the following cell to train a 6 layer FC net with SGD, SGD+momentum, and SGD+Nesterov momentum. You should see that SGD+momentum achieves a better loss than SGD, and that SGD+Nesterov momentum achieves a slightly better loss (and training accuracy) than SGD+momentum.

```
num_train = 4000
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
solvers = {}
for update_rule in ['sgd', 'sgd_momentum', 'sgd_nesterov_momentum']:
    print('Optimizing with {}'.format(update_rule))
    model = FullyConnectedNet([100, 100, 100, 100, 100], weight_scale=5e-2)
    solver = Solver(model, small data,
                     num epochs=5, batch size=100,
                     update_rule=update_rule,
                     optim_config={
                       'learning_rate': 1e-2,
                     verbose=False)
    solvers[update_rule] = solver
    solver.train()
    print
fig, axes = plt.subplots(3, 1)
ax = axes[0]
ax.set_title('Training loss')
ax.set_xlabel('Iteration')
ax = axes[1]
ax.set_title('Training accuracy')
ax.set_xlabel('Epoch')
ax = axes[2]
ax.set_title('Validation accuracy')
ax.set_xlabel('Epoch')
for update rule, solver in solvers.items():
    ax = axes[0]
    ax.plot(solver.loss_history, 'o', label=update_rule)
   ax.plot(solver.train_acc_history, '-o', label=update_rule)
    ax = axes[2]
    ax.plot(solver.val_acc_history, '-o', label=update_rule)
for i in [1, 2, 3]:
    ax = axes[i - 1]
    ax.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show()
```

Optimizing with sgd Optimizing with sgd_momentum Optimizing with sgd_nesterov_momentum



RMSProp

Now we go to techniques that adapt the gradient. Implement ${\tt rmsprop}$ in ${\tt nndl/optim.py}$. Test your implementation by running the cell below.

```
from nndl.optim import rmsprop
N. D = 4.5
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
a = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
config = {'learning_rate': 1e-2, 'a': a}
next_w, _ = rmsprop(w, dw, config=config)
expected_next_w = np.asarray([
  [-0.39223849, -0.34037513, -0.28849239, -0.23659121, -0.18467247],
  [-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774], [ 0.12716641, 0.17918792, 0.23122175, 0.28326742, 0.33532447],
  [ 0.38739248, 0.43947102, 0.49155973, 0.54365823, 0.59576619]])
expected cache = np.asarray([
  [ 0.5976,
                                0.6277108, 0.64284931, 0.65804321],
               0.6126277,
  [ 0.67329252, 0.68859723, 0.70395734, 0.71937285, 0.73484377],
  [ 0.75037008, 0.7659518, 0.78158892, 0.79728144, 0.81302936], [ 0.82883269, 0.84469141, 0.86060554, 0.87657507, 0.8926 ]]
print('next w error: {}'.format(rel error(expected next w, next w)))
print('cache error: {}'.format(rel error(expected cache, config['a'])))
```

next_w error: 9.524687511038133e-08
cache error: 2.6477955807156126e-09

Adaptive moments

Now, implement adam in nndl/optim.py . Test your implementation by running the cell below.

In [9]:

```
# Test Adam implementation; you should see errors around 1e-7 or less
from nndl.optim import adam
N. D = 4.5
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
a = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)
config = {'learning_rate': 1e-2, 'v': v, 'a': a, 't': 5}
next_w, _ = adam(w, dw, config=config)
expected_next_w = np.asarray([
  [-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],
  \hbox{\tt [-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],}
  [ 0.1248705, 0.17744702, 0.23002243, 0.28259667, 0.33516969], [ 0.38774145, 0.44031188, 0.49288093, 0.54544852, 0.59801459]])
expected_a = np.asarray([
  [ 0.69966,
                0.68908382, 0.67851319, 0.66794809, 0.65738853,],
  [ 0.64683452, 0.63628604, 0.6257431, 0.61520571, 0.60467385,],
  [ 0.59414753, 0.58362676, 0.57311152, 0.56260183, 0.55209767,], [ 0.54159906, 0.53110598, 0.52061845, 0.51013645, 0.49966, ]]
expected v = np.asarray([
  [ 0.67473684, 0.69421053, 0.71368421, 0.73315789, 0.75263158], [ 0.77210526, 0.79157895, 0.81105263, 0.83052632, 0.85 ]]
print('next_w error: {}'.format(rel_error(expected_next_w, next_w)))
print('a error: {}'.format(rel_error(expected_a, config['a'])))
print('v error: {}'.format(rel_error(expected_v, config['v'])))
```

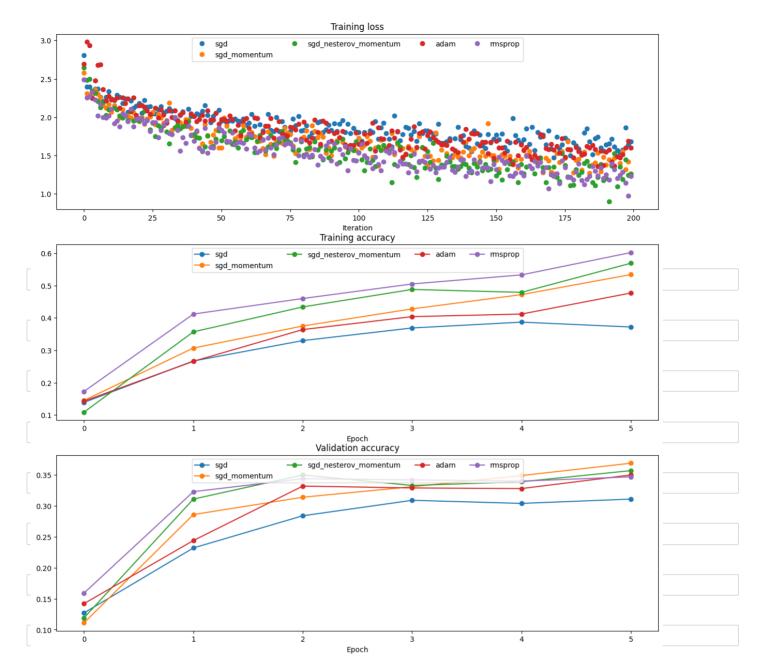
next_w error: 0.20720703668629928
a error: 4.208314038113071e-09
v error: 4.214963193114416e-09

Comparing SGD, SGD+NesterovMomentum, RMSProp, and Adam

The following code will compare optimization with SGD, Momentum, Nesterov Momentum, RMSProp and Adam. In our code, we find that RMSProp, Adam, and SGD + Nesterov Momentum achieve approximately the same training error after a few training epochs.

```
learning_rates = {'rmsprop': 2e-4, 'adam': 1e-3}
for update_rule in ['adam', 'rmsprop']:
    print('Optimizing with {}'.format(update_rule))
   model = FullyConnectedNet([100, 100, 100, 100, 100], weight_scale=5e-2)
    solver = Solver(model, small data,
                    num_epochs=5, batch_size=100,
                    update_rule=update_rule,
                    optim_config={
                      'learning_rate': learning_rates[update_rule]
                    verbose=False)
    solvers[update_rule] = solver
    solver.train()
    print
fig, axes = plt.subplots(3, 1)
ax = axes[0]
ax.set_title('Training loss')
ax.set_xlabel('Iteration')
ax = axes[1]
ax.set_title('Training accuracy')
ax.set_xlabel('Epoch')
ax = axes[2]
ax.set_title('Validation accuracy')
ax.set_xlabel('Epoch')
for update_rule, solver in solvers.items():
    ax = axes[0]
    ax.plot(solver.loss_history, 'o', label=update_rule)
   ax = axes[1]
   ax.plot(solver.train_acc_history, '-o', label=update_rule)
    ax = axes[2]
   ax.plot(solver.val acc history, '-o', label=update rule)
for i in [1, 2, 3]:
    ax = axes[i - 1]
    ax.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show()
```

Optimizing with adam Optimizing with rmsprop



Easier optimization

In the following cell, we'll train a 4 layer neural network having 500 units in each hidden layer with the different optimizers, and find that it is far easier to get up to 50+% performance on CIFAR-10. After we implement batchnorm and dropout, we'll ask you to get 55+% on CIFAR-10.

```
(Iteration 1 / 4900) loss: 2.339523
(Epoch 0 / 10) train acc: 0.164000; val acc: 0.166000
(Iteration 51 / 4900) loss: 1.864994
(Iteration 101 / 4900) loss: 1.839498
(Iteration 151 / 4900) loss: 1.823122
(Iteration 201 / 4900) loss: 1.570007
(Iteration 251 / 4900) loss: 1.507193
(Iteration 301 / 4900) loss: 1.557978
(Iteration 351 / 4900) loss: 1.577377
(Iteration 401 / 4900) loss: 1.614922
(Iteration 451 / 4900) loss: 1.378437
(Epoch 1 / 10) train acc: 0.499000; val acc: 0.482000
(Iteration 501 / 4900) loss: 1.391719
(Iteration 551 / 4900) loss: 1.570582
(Iteration 601 / 4900) loss: 1.620913
(Iteration 651 / 4900) loss: 1.470027
(Iteration 701 / 4900) loss: 1.262180
(Iteration 751 / 4900) loss: 1.356196
(Iteration 801 / 4900) loss: 1.225809
(Iteration 851 / 4900) loss: 1.095218
(Iteration 901 / 4900) loss: 1.122905
(Iteration 951 / 4900) loss: 1.062350
(Epoch 2 / 10) train acc: 0.561000; val acc: 0.512000
(Iteration 1001 / 4900) loss: 1.334675
(Iteration 1051 / 4900) loss: 1.266972
(Iteration 1101 / 4900) loss: 1.341187
(Iteration 1151 / 4900) loss: 1.058048
(Iteration 1201 / 4900) loss: 1.036392
(Iteration 1251 / 4900) loss: 1.271014
(Iteration 1301 / 4900) loss: 1.188443
(Iteration 1351 / 4900) loss: 1.130898
(Iteration 1401 / 4900) loss: 1.087218
(Iteration 1451 / 4900) loss: 1.091161
(Epoch 3 / 10) train acc: 0.600000; val acc: 0.529000
(Iteration 1501 / 4900) loss: 1.114358
(Iteration 1551 / 4900) loss: 1.100497
(Iteration 1601 / 4900) loss: 0.932592
(Iteration 1651 / 4900) loss: 1.041202
(Iteration 1701 / 4900) loss: 1.038536
(Iteration 1751 / 4900) loss: 1.061793
(Iteration 1801 / 4900) loss: 1.032083
(Iteration 1851 / 4900) loss: 0.987002
(Iteration 1901 / 4900) loss: 1.108678
(Iteration 1951 / 4900) loss: 0.967156
(Epoch 4 / 10) train acc: 0.631000; val_acc: 0.529000
(Iteration 2001 / 4900) loss: 1.142238
(Iteration 2051 / 4900) loss: 1.060735
(Iteration 2101 / 4900) loss: 0.838040
(Iteration 2151 / 4900) loss: 0.943058
(Iteration 2201 / 4900) loss: 1.002068
(Iteration 2251 / 4900) loss: 0.781785
(Iteration 2301 / 4900) loss: 1.191865
(Iteration 2351 / 4900) loss: 0.994876
(Iteration 2401 / 4900) loss: 0.761747
(Epoch 5 / 10) train acc: 0.665000; val acc: 0.565000
(Iteration 2451 / 4900) loss: 0.943584
(Iteration 2501 / 4900) loss: 0.891617
(Iteration 2551 / 4900) loss: 1.026547
(Iteration 2601 / 4900) loss: 1.149509
(Iteration 2651 / 4900) loss: 0.994164
(Iteration 2701 / 4900) loss: 0.742358
(Iteration 2751 / 4900) loss: 0.925337
(Iteration 2801 / 4900) loss: 0.839610
(Iteration 2851 / 4900) loss: 0.973336
(Iteration 2901 / 4900) loss: 0.791999
(Epoch 6 / 10) train acc: 0.723000; val_acc: 0.549000
(Iteration 2951 / 4900) loss: 0.931007
(Iteration 3001 / 4900) loss: 0.676802
(Iteration 3051 / 4900) loss: 0.882952
(Iteration 3101 / 4900) loss: 0.908387
(Iteration 3151 / 4900) loss: 0.736899
(Iteration 3201 / 4900) loss: 0.595184
(Iteration 3251 / 4900) loss: 0.689698
(Iteration 3301 / 4900) loss: 0.811953
(Iteration 3351 / 4900) loss: 0.834028
(Iteration 3401 / 4900) loss: 0.736455
(Epoch 7 / 10) train acc: 0.761000; val_acc: 0.559000
(Iteration 3451 / 4900) loss: 0.703637
(Iteration 3501 / 4900) loss: 0.957256
(Iteration 3551 / 4900) loss: 0.674790
(Iteration 3601 / 4900) loss: 0.668202
(Iteration 3651 / 4900) loss: 0.629193
(Iteration 3701 / 4900) loss: 0.641186
(Iteration 3751 / 4900) loss: 0.488022
(Iteration 3801 / 4900) loss: 0.614350
(Iteration 3851 / 4900) loss: 0.681368
```

```
(Iteration 3901 / 4900) loss: 0.998869
(Epoch 8 / 10) train acc: 0.791000; val_acc: 0.569000
(Iteration 3951 / 4900) loss: 0.747314
(Iteration 4001 / 4900) loss: 0.732575
(Iteration 4051 / 4900) loss: 0.676731
(Iteration 4101 / 4900) loss: 0.713107
(Iteration 4151 / 4900) loss: 0.605859
(Iteration 4201 / 4900) loss: 0.684736
(Iteration 4251 / 4900) loss: 0.594708
(Iteration 4301 / 4900) loss: 0.783845
(Iteration 4351 / 4900) loss: 0.571674
(Iteration 4401 / 4900) loss: 0.603575
(Epoch 9 / 10) train acc: 0.802000; val_acc: 0.550000
(Iteration 4451 / 4900) loss: 0.635926
(Iteration 4501 / 4900) loss: 0.760623
(Iteration 4551 / 4900) loss: 0.672312
(Iteration 4601 / 4900) loss: 0.646120
(Iteration 4651 / 4900) loss: 0.375363
(Iteration 4701 / 4900) loss: 0.593653
(Iteration 4751 / 4900) loss: 0.630438
(Iteration 4801 / 4900) loss: 0.498765
(Iteration 4851 / 4900) loss: 0.431046
(Epoch 10 / 10) train acc: 0.848000; val_acc: 0.550000
In [24]:
y test pred = np.argmax(model.loss(data['X test']), axis=1)
y_val_pred = np.argmax(model.loss(data['X_val']), axis=1)
print('Validation set accuracy: {}'.format(np.mean(y_val_pred == data['y_val'])))
print('Test set accuracy: {}'.format(np.mean(y_test_pred == data['y_test'])))
Validation set accuracy: 0.559
Test set accuracy: 0.563
In [ ]:
```

```
In [ ]:
def sgd(w, dw, config=None):
   Performs vanilla stochastic gradient descent.
   config format:
   - learning_rate: Scalar learning rate.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   w -= config['learning_rate'] * dw
   return w, config
def sgd_momentum(w, dw, config=None):
   Performs stochastic gradient descent with momentum.
   config format:
   - learning_rate: Scalar learning rate.
   - momentum: Scalar between 0 and 1 giving the momentum value.
    Setting momentum = 0 reduces to sgd.
   - velocity: A numpy array of the same shape as w and dw used to store a moving
   average of the gradients.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
   v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.
   # YOUR CODE HERE:
     Implement the momentum update formula. Return the updated weights
      as next w, and the updated velocity as v.
   v = config['momentum'] * v - config['learning rate'] * dw
   next w = w + v
   # END YOUR CODE HERE
   config['velocity'] = v
   return next w, config
def sgd_nesterov_momentum(w, dw, config=None):
   Performs stochastic gradient descent with Nesterov momentum.
   config format:
   - learning_rate: Scalar learning rate.
   - momentum: Scalar between 0 and 1 giving the momentum value.
     Setting momentum = 0 reduces to sgd.
   - velocity: A numpy array of the same shape as w and dw used to store a moving
   average of the gradients.
   if config is None: config = {}
   config.setdefault('learning_rate', 1e-2)
   config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
   v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.
   # YOUR CODE HERE:
     Implement the momentum update formula. Return the updated weights
      as next w, and the updated velocity as v.
   vnew = config['momentum'] * v - config['learning_rate'] * dw
   next_w = w + vnew + config['momentum'] * (vnew - v)
   v = vnew
                   # END YOUR CODE HERE
   config['velocity'] = v
   return next_w, config
def rmsprop(w, dw, config=None):
   Uses the RMSProp update rule, which uses a moving average of squared gradient
   values to set adaptive per-parameter learning rates.
   config format:
   - learning_rate: Scalar learning rate.
   - decay_rate: Scalar between 0 and 1 giving the decay rate for the squared
```

```
gradient cache.
    - epsilon: Small scalar used for smoothing to avoid dividing by zero.
    - beta: Moving average of second moments of gradients.
    if config is None: config = {}
    config.setdefault('learning_rate', 1e-2)
    config.setdefault('decay_rate', 0.99)
    config.setdefault('epsilon', 1e-8)
    config.setdefault('a', np.zeros_like(w))
    next_w = None
    # YOUR CODE HERE:
       Implement RMSProp. Store the next value of w as next_w. You need
       to also store in config['a'] the moving average of the second
       moment gradients, so they can be used for future gradients. Concretely,
      config['a'] corresponds to "a" in the lecture notes.
   config['a'] = config['decay_rate'] * config['a'] + (1 - config['decay_rate']) * (dw ** 2) #update
next_w = w - config['learning_rate'] / (np.sqrt(config['a']) + config['epsilon']) * dw
    # END YOUR CODE HERE
    return next w, config
def adam(w, dw, config=None):
    Uses the Adam update rule, which incorporates moving averages of both the
    gradient and its square and a bias correction term.
   config format:
    - learning_rate: Scalar learning rate.
    - betal: Decay rate for moving average of first moment of gradient.
    - beta2: Decay rate for moving average of second moment of gradient.
    - epsilon: Small scalar used for smoothing to avoid dividing by zero.
    - m: Moving average of gradient.
    - v: Moving average of squared gradient.
    - t: Iteration number.
    if config is None: config = {}
    config.setdefault('learning_rate', 1e-3)
   config.setdefault('beta1', 0.9)
config.setdefault('beta2', 0.999)
    config.setdefault('epsilon', 1e-8)
   config.setdefault('v', np.zeros_like(w))
config.setdefault('a', np.zeros_like(w))
config.setdefault('t', 0)
    next_w = None
    # ----- #
    # YOUR CODE HERE:
      Implement Adam. Store the next value of w as next w. You need
       to also store in config['a'] the moving average of the second moment gradients, and in config['v'] the moving average of the
    # first moments. Finally, store in config['t'] the increasing time.
     \begin{split} & \text{config['v'] = config['beta1'] * config['v'] + (1 - config['beta1']) * dw} \\ & \text{config['a'] = config['beta2'] * config['a'] + (1 - config['beta2']) * (dw ** 2)} \\ \end{aligned} 
    next_w = w - config['learning_rate'] / (np.sqrt(config['a']) + config['epsilon']) * config['v']
    config['t'] += 1
    # END YOUR CODE HERE
    return next_w, config
```

Batch Normalization

In this notebook, you will implement the batch normalization layers of a neural network to increase its performance. Please review the details of batch normalization from the lecture notes.

Utils has a solid API for building these modular frameworks and training them, and we will use this very well implemented framework as opposed to "reinventing the wheel." This includes using the Solver, various utility functions, and the layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils.

```
In [31]:
```

```
## Import and setups
import time
import numpy as np
import matplotlib.pyplot as plt
from nndl.fc_net import *
from nndl.layers import *
from utils.data_utils import get_CIFAR10_data
from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
from utils.solver import Solver
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray
# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load ext autoreload
%autoreload 2
def rel_error(x, y):
     "" returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

The autoreload extension is already loaded. To reload it, use: %reload_ext autoreload

```
In [32]:
```

```
# Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
for k in data.keys():
    print('{}: {} '.format(k, data[k].shape))

V. troins (40000 2 23 23 23)
```

```
X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

Batchnorm forward pass

Implement the training time batchnorm forward pass, batchnorm_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
# Check the training-time forward pass by checking means and variances
# of features both before and after batch normalization
# Simulate the forward pass for a two-layer network
N, D1, D2, D3 = 200, 50, 60, 3
X = np.random.randn(N, D1)
W1 = np.random.randn(D1, D2)
W2 = np.random.randn(D2, D3)
a = np.maximum(0, X.dot(W1)).dot(W2)
print('Before batch normalization:')
print(' means: ', a.mean(axis=0))
print(' stds: ', a.std(axis=0))
# Means should be close to zero and stds close to one
print('After batch normalization (gamma=1, beta=0)')
a_norm, _ = batchnorm_forward(a, np.ones(D3), np.zeros(D3), {'mode': 'train'})
print(' mean: ', a_norm.mean(axis=0))
print(' std: ', a_norm.std(axis=0))
# Now means should be close to beta and stds close to gamma
gamma = np.asarray([1.0, 2.0, 3.0])
beta = np.asarray([11.0, 12.0, 13.0])
a_norm, _ = batchnorm_forward(a, gamma, beta, {'mode': 'train'})
print('After batch normalization (nontrivial gamma, beta)')
print(' means: ', a_norm.mean(axis=0))
print(' stds: ', a_norm.std(axis=0))
Before batch normalization:
  means: [ 17.50740868 23.68828646 -42.85448866]
  stds: [30.28971963 33.06647874 32.62687985]
After batch normalization (gamma=1, beta=0)
 mean: [ 6.38378239e-18 3.82471832e-16 -1.17794663e-15]
  std: [0.99999999 1.
                              1.
After batch normalization (nontrivial gamma, beta)
 means: [11. 12. 13.]
  stds: [0.99999999 1.99999999 2.99999999]
```

Implement the testing time batchnorm forward pass, batchnorm_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
In [34]:
```

```
# Check the test-time forward pass by running the training-time
# forward pass many times to warm up the running averages, and then
# checking the means and variances of activations after a test-time
# forward pass.
N, D1, D2, D3 = 200, 50, 60, 3
W1 = np.random.randn(D1, D2)
W2 = np.random.randn(D2, D3)
bn_param = {'mode': 'train'}
gamma = np.ones(D3)
beta = np.zeros(D3)
for t in np.arange(50):
   X = np.random.randn(N, D1)
    a = np.maximum(0, X.dot(W1)).dot(W2)
   batchnorm_forward(a, gamma, beta, bn_param)
bn_param['mode'] = 'test
X = np.random.randn(N, D1)
a = np.maximum(0, X.dot(W1)).dot(W2)
a_norm, _ = batchnorm_forward(a, gamma, beta, bn param)
# Means should be close to zero and stds close to one, but will be
# noisier than training-time forward passes.
print('After batch normalization (test-time):')
print('
       means: ', a_norm.mean(axis=0))
print(' stds: ', a_norm.std(axis=0))
```

After batch normalization (test-time):
means: [-0.06350491 0.03171062 0.01656171]
stds: [1.02030978 1.02996531 0.94404507]

Batchnorm backward pass

Implement the backward pass for the batchnorm layer, batchnorm_backward in nndl/layers.py . Check your implementation by running the following cell.

```
# Gradient check batchnorm backward pass
N, D = 4, 5
x = 5 * np.random.randn(N, D) + 12
gamma = np.random.randn(D)
beta = np.random.randn(D)
dout = np.random.randn(N, D)
bn_param = {'mode': 'train'}
fx = lambda x: batchnorm_forward(x, gamma, beta, bn_param)[0]
fg = lambda gamma: batchnorm_forward(x, gamma, beta, bn_param)[0]
fb = lambda beta: batchnorm_forward(x, gamma, beta, bn_param)[0]
dx_num = eval_numerical_gradient_array(fx, x, dout)
da num = eval numerical gradient array(fg, gamma, dout)
db num = eval numerical gradient array(fb, beta, dout)
_, cache = batchnorm_forward(x, gamma, beta, bn_param)
dx, dgamma, dbeta = batchnorm_backward(dout, cache)
print('dx error: ', rel_error(dx_num, dx))
print('dgamma error: ', rel_error(da_num, dgamma))
print('dbeta error: ', rel_error(db_num, dbeta))
dx error: 7.034989829044836e-09
dgamma error: 3.8998354465625325e-12
```

Implement a fully connected neural network with batchnorm layers

Modify the FullyConnectedNet() class in nndl/fc net.py to incorporate batchnorm layers. You will need to modify the class in the following areas:

(1) The gammas and betas need to be initialized to 1's and 0's respectively in $__init__$.

dbeta error: 1.4895268504438587e-11

- (2) The batchnorm_forward layer needs to be inserted between each affine and relu layer (except in the output layer) in a forward pass computation in loss. You may find it helpful to write an affine_batchnorm_relu() layer in nndl/layer_utils.py although this is not necessary.
- (3) The batchnorm backward layer has to be appropriately inserted when calculating gradients.

After you have done the appropriate modifications, check your implementation by running the following cell.

Note, while the relative error for W3 should be small, as we backprop gradients more, you may find the relative error increases. Our relative error for W1 is on the order of 1e-4.

```
In [37]:
```

```
N, D, H1, H2, C = 2, 15, 20, 30, 10
X = np.random.randn(N, D)
y = np.random.randint(C, size=(N,))
for reg in [0, 3.14]:
   print('Running check with reg = ', reg)
   model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                              reg=reg, weight_scale=5e-2, dtype=np.float64,
                              use_batchnorm=True)
    loss, grads = model.loss(X, y)
   print('Initial loss: ', loss)
    for name in sorted(grads):
        f = lambda : model.loss(X, y)[0]
        grad_num = eval_numerical_gradient(f, model.params[name], verbose=False, h=1e-5)
        print('{} relative error: {}'.format(name, rel_error(grad_num, grads[name])))
    if reg == 0: print('\n')
Running check with reg = 0
Initial loss: 2.2935346674211794
W1 relative error: 0.0005009680592850923
W2 relative error: 7.395806301996755e-06
W3 relative error: 4.2089262000522015e-10
b1 relative error: 0.0022204460492503126
b2 relative error: 0.0022204516003654358
b3 relative error: 9.075378324134053e-11
beta1 relative error: 6.918009311012682e-08
beta2 relative error: 5.015672160407703e-09
gammal relative error: 1.1490468017985962e-07
gamma2 relative error: 1.4790856694307631e-08
Running check with reg = 3.14
Initial loss: 7.261913911720129
W1 relative error: 2.09814262721487e-06
W2 relative error: 1.684454741829195e-05
W3 relative error: 4.3804316316982865e-08
b1 relative error: 1.7763568394002505e-07
```

Training a deep fully connected network with batch normalization.

To see if batchnorm helps, let's train a deep neural network with and without batch normalization.

b2 relative error: 1.1102230246251565e-08 b3 relative error: 4.093167813140914e-10 beta1 relative error: 5.154144671019582e-09 beta2 relative error: 1.603277514243205e-08 gamma1 relative error: 3.984707077635263e-09 gamma2 relative error: 2.3746487208291254e-08

```
In [40]:
# Try training a very deep net with batchnorm
hidden_dims = [100, 100, 100, 100, 100]
num train = 1000
small_data = {
   'X_train': data['X_train'][:num_train],
    'y train': data['y train'][:num train],
   'X val': data['X_val'],
    'y_val': data['y_val'],
weight scale = 2e-2
bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=True)
model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=False)
bn solver = Solver(bn model, small data,
               num_epochs=10, batch_size=50,
                update_rule='adam',
                optim_config={
                  'learning_rate': 1e-3,
               }.
                verbose=True, print every=200)
bn solver.train()
solver = Solver(model, small data,
               num_epochs=10, batch_size=50,
                update_rule='adam',
               optim config={
                  'learning_rate': 1e-3,
                verbose=True, print_every=200)
solver.train()
(Iteration 1 / 200) loss: 2.318635
(Epoch 0 / 10) train acc: 0.103000; val_acc: 0.108000
(Epoch 1 / 10) train acc: 0.258000; val_acc: 0.223000
(Epoch 2 / 10) train acc: 0.347000; val_acc: 0.263000
(Epoch 3 / 10) train acc: 0.429000; val_acc: 0.283000
(Epoch 4 / 10) train acc: 0.444000; val acc: 0.282000
(Epoch 5 / 10) train acc: 0.547000; val acc: 0.319000
(Epoch 6 / 10) train acc: 0.569000; val_acc: 0.308000
(Epoch 7 / 10) train acc: 0.599000; val_acc: 0.317000
(Epoch 8 / 10) train acc: 0.687000; val_acc: 0.307000
(Epoch 9 / 10) train acc: 0.692000; val_acc: 0.298000
```

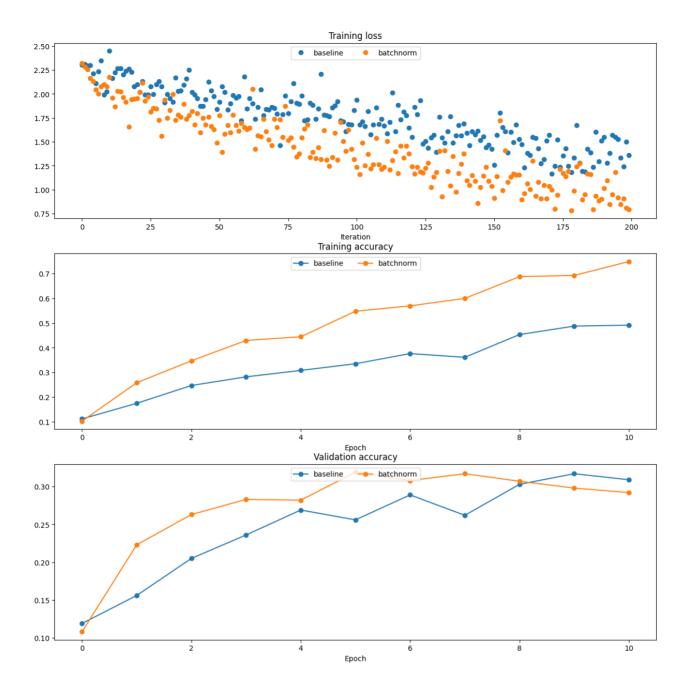
(Epoch 10 / 10) train acc: 0.748000; val_acc: 0.292000

(Epoch 0 / 10) train acc: 0.112000; val_acc: 0.119000 (Epoch 1 / 10) train acc: 0.175000; val_acc: 0.156000 (Epoch 2 / 10) train acc: 0.247000; val_acc: 0.205000 (Epoch 3 / 10) train acc: 0.282000; val_acc: 0.236000 (Epoch 4 / 10) train acc: 0.308000; val_acc: 0.269000 (Epoch 5 / 10) train acc: 0.335000; val_acc: 0.256000 (Epoch 6 / 10) train acc: 0.376000; val_acc: 0.289000 (Epoch 7 / 10) train acc: 0.361000; val_acc: 0.262000 (Epoch 8 / 10) train acc: 0.453000; val_acc: 0.262000 (Epoch 9 / 10) train acc: 0.487000; val_acc: 0.317000 (Epoch 10 / 10) train acc: 0.491000; val_acc: 0.309000

(Iteration 1 / 200) loss: 2.302244

```
In [41]:
```

```
fig, axes = plt.subplots(3, 1)
ax = axes[0]
ax.set_title('Training loss')
ax.set_xlabel('Iteration')
ax = axes[1]
ax.set_title('Training accuracy')
ax.set_xlabel('Epoch')
ax = axes[2]
ax.set_title('Validation accuracy')
ax.set_xlabel('Epoch')
ax.plot(solver.loss_history, 'o', label='baseline')
ax.plot(bn_solver.loss_history, 'o', label='batchnorm')
ax.plot(solver.train_acc_history, '-o', label='baseline')
ax.plot(bn_solver.train_acc_history, '-o', label='batchnorm')
ax = axes[2]
ax.plot(solver.val_acc_history, '-o', label='baseline')
ax.plot(bn_solver.val_acc_history, '-o', label='batchnorm')
for i in [1, 2, 3]:
    ax = axes[i - 1]
ax.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show()
```



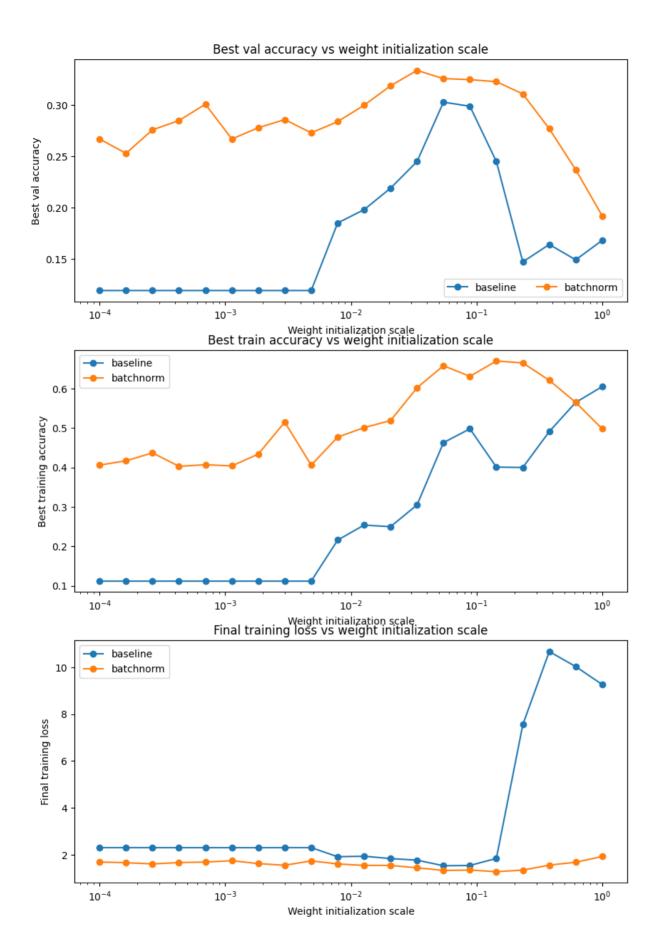
Batchnorm and initialization

The following cells run an experiment where for a deep network, the initialization is varied. We do training for when batchnorm layers are and are not included.

```
# Try training a very deep net with batchnorm
hidden_dims = [50, 50, 50, 50, 50, 50, 50]
num train = 1000
small_data = {
   'X_train': data['X_train'][:num_train],
    'y train': data['y train'][:num train],
   'X_val': data['X_val'],
    'y_val': data['y_val'],
bn solvers = {}
solvers = {}
weight_scales = np.logspace(-4, 0, num=20)
for i, weight scale in enumerate(weight scales):
   print('Running weight scale {} / {}'.format(i + 1, len(weight scales)))
   bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=True)
   model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, use_batchnorm=False)
   bn_solver = Solver(bn_model, small_data,
                    num_epochs=10, batch_size=50,
                    update rule='adam',
                    optim config={
                      'learning_rate': 1e-3,
                    verbose=False, print_every=200)
    bn_solver.train()
    bn solvers[weight scale] = bn solver
    solver = Solver(model, small_data,
                    num_epochs=10, batch_size=50,
                    update rule='adam',
                    optim config={
                       'learning_rate': 1e-3,
                    verbose=False, print_every=200)
    solver.train()
    solvers[weight_scale] = solver
Running weight scale 1 / 20
```

Running weight scale 2 / 20 Running weight scale 3 / 20 Running weight scale 4 / 20 Running weight scale 5 / 20 Running weight scale 6 / 20 Running weight scale 7 / 20 Running weight scale 8 / 20 Running weight scale 9 / 20 Running weight scale 10 / 20 Running weight scale 11 / 20 Running weight scale 12 / 20 Running weight scale 13 / 20 Running weight scale 14 / 20 Running weight scale 15 / 20Running weight scale 16 / 20 Running weight scale 17 / 20 Running weight scale 18 / 20 Running weight scale 19 / 20 Running weight scale 20 / 20

```
# Plot results of weight scale experiment
best_train_accs, bn_best_train_accs = [], []
best val accs, bn_best_val_accs = [], []
final train loss, bn final train loss = [], []
for ws in weight_scales:
   best train accs.append(max(solvers[ws].train acc history))
   bn_best_train_accs.append(max(bn_solvers[ws].train_acc_history))
    best_val_accs.append(max(solvers[ws].val_acc_history))
   bn_best_val_accs.append(max(bn_solvers[ws].val_acc_history))
    final_train_loss.append(np.mean(solvers[ws].loss_history[-100:]))
    bn_final_train_loss.append(np.mean(bn_solvers[ws].loss_history[-100:]))
plt.subplot(3, 1, 1)
plt.title('Best val accuracy vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Best val accuracy')
plt.semilogx(weight_scales, best_val_accs, '-o', label='baseline')
plt.semilogx(weight_scales, bn_best_val_accs, '-o', label='batchnorm')
plt.legend(ncol=2, loc='lower right')
plt.subplot(3, 1, 2)
plt.title('Best train accuracy vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Best training accuracy')
plt.semilogx(weight_scales, best_train_accs, '-o', label='baseline')
plt.semilogx(weight_scales, bn_best_train_accs, '-o', label='batchnorm')
plt.legend()
plt.subplot(3, 1, 3)
plt.title('Final training loss vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Final training loss')
plt.semilogx(weight_scales, final_train_loss, '-o', label='baseline')
plt.semilogx(weight_scales, bn_final_train_loss, '-o', label='batchnorm')
plt.legend()
plt.gcf().set size inches(10, 15)
plt.show()
```



Question:

In the cell below, summarize the findings of this experiment, and WHY these results make sense.

Answer:

Findings: Compared to baseline, we can see that the training with Batchnorm has higher best val accuracy and best training accuracy while having the lower final training loss. Also, the training with Batchnorm is less sensitive to the weight initialization scale.

Why: This makes sense since the idea of Batchnorm is to make the output of each layer have unit statistics.

In []:

```
def batchnorm forward(x, gamma, beta, bn param):
   Forward pass for batch normalization.
   During training the sample mean and (uncorrected) sample variance are
   computed from minibatch statistics and used to normalize the incoming data.
   During training we also keep an exponentially decaying running mean of the mean
   and variance of each feature, and these averages are used to normalize data
   at test-time.
   At each timestep we update the running averages for mean and variance using
   an exponential decay based on the momentum parameter:
   running_mean = momentum * running_mean + (1 - momentum) * sample_mean
   running_var = momentum * running_var + (1 - momentum) * sample_var
   Note that the batch normalization paper suggests a different test-time
   behavior: they compute sample mean and variance for each feature using a
   large number of training images rather than using a running average. For
   this implementation we have chosen to use running averages instead since
   they do not require an additional estimation step; the torch7 implementation
   of batch normalization also uses running averages.
   Input:
   - x: Data of shape (N, D)
   - gamma: Scale parameter of shape (D,)
   - beta: Shift paremeter of shape (D,)
   - bn_param: Dictionary with the following keys:
     - mode: 'train' or 'test'; required
     - eps: Constant for numeric stability
     - momentum: Constant for running mean / variance.
     - running_mean: Array of shape (D,) giving running mean of features
     - running var Array of shape (D,) giving running variance of features
   Returns a tuple of:
   - out: of shape (N, D)
    - cache: A tuple of values needed in the backward pass
   mode = bn param['mode']
   eps = bn_param.get('eps', 1e-5)
   momentum = bn_param.get('momentum', 0.9)
   N.D = x.shape
   running_mean = bn_param.get('running_mean', np.zeros(D, dtype=x.dtype))
   running_var = bn_param.get('running_var', np.zeros(D, dtype=x.dtype))
   out, cache = None, None
   if mode == 'train':
                         # YOUR CODE HERE.
          A few steps here:
            (1) Calculate the running mean and variance of the minibatch.
            (2) Normalize the activations with the running mean and variance.
            (3) Scale and shift the normalized activations. Store this
               as the variable 'out'
            (4) Store any variables you may need for the backward pass in
                the 'cache' variable.
       #calculate the sample_mean and sample_var
       sample_mean = np.mean(x, axis = 0)
       sample\_var = np.var(x, axis = 0)
       #Calculate the running mean and variance of the minibatch
       running mean = momentum * running mean + (1 - momentum) * sample mean
       running var = momentum * running var + (1 - momentum) * sample var
       #Normalize the activations with the running mean and variance
       x hat = (x - sample mean) / (np.sqrt(sample var + eps))
       #based on the unit activations function
       #Scale and shift the normalized activations
       out = gamma * x_hat + beta
       #Store any variables you may need for the backward pass
       cache = (sample_mean, sample_var, x, x_hat, gamma, eps)
       # ------ #
       # END YOUR CODE HERE
       # ======
                ______ #
   elif mode == 'test':
                     # YOUR CODE HERE:
       # Calculate the testing time normalized activation. Normalize using
          the running mean and variance, and then scale and shift appropriately.
       # Store the output as 'out'.
```

```
out = gamma * ((x - running_mean) / (np.sqrt(running_var + eps))) + beta
      # ----- #
      # END YOUR CODE HERE
      # ----- #
   else:
      raise ValueError('Invalid forward batchnorm mode "%s"' % mode)
   # Store the updated running means back into bn_param
   bn_param['running_mean'] = running_mean
   bn_param['running_var'] = running_var
   return out, cache
def batchnorm backward(dout, cache):
   Backward pass for batch normalization.
   For this implementation, you should write out a computation graph for
   batch normalization on paper and propagate gradients backward through
   intermediate nodes.
   - dout: Upstream derivatives, of shape (N. D)
   - cache: Variable of intermediates from batchnorm_forward.
   Returns a tuple of:
   - dx: Gradient with respect to inputs x, of shape (N, D)
   - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
   - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
   dx, dgamma, dbeta = None, None, None
   # ------ #
   # YOUR CODE HERE:
   # Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
   #First, we will get the params we need from cache
   sample_mean, sample_var, x, x_hat, gamma, eps = cache
   m = dout.shape[0]
   #Then, calculate the derivatives based on lecture slides
   dldx hat = dout * gamma #derivative for x hat
   #derivative for a(in slides)
   dlda = (1 / (np.sqrt(sample var + eps))) * dldx hat
   #derivative for mu
   dldmu = (-1 / np.sqrt(sample_var + eps)) * (np.sum(dldx_hat, axis = 0))
   #derivative for e(in slides)
   dlde = (-1 / 2) * (1 / ((sample_var + eps) ** 1.5)) * (x - sample_mean) * dldx_hat
   dldvar = np.sum(dlde, axis = 0) #derivative for variance
   #derivative for x
   dx = dlda + ((2 * (x - sample_mean)) / m) * dldvar + (1 / m) * dldmu
   dgamma = np.sum(dout * x_hat, axis = 0) #derivative for gamma
   dbeta = np.sum(dout, axis = 0) #derivate for beta
   # ------ #
   # END YOUR CODE HERE
   # ----- #
   return dx, dgamma, dbeta
```

```
class FullyConnectedNet(object):
   A fully-connected neural network with an arbitrary number of hidden layers,
   ReLU nonlinearities, and a softmax loss function. This will also implement
   dropout and batch normalization as options. For a network with L layers,
   the architecture will be
   {affine - [batch norm] - relu - [dropout]} x (L - 1) - affine - softmax
   where batch normalization and dropout are optional, and the {...} block is
   repeated L - 1 times.
   Similar to the TwoLayerNet above, learnable parameters are stored in the
   self.params dictionary and will be learned using the Solver class.
   def __init__(self, hidden_dims, input_dim=3*32*32, num classes=10,
              dropout=1, use_batchnorm=False, reg=0.0,
              weight scale=1e-2, dtype=np.float32, seed=None):
       Initialize a new FullyConnectedNet.
       - hidden dims: A list of integers giving the size of each hidden layer.
       - input dim: An integer giving the size of the input.
       - num_classes: An integer giving the number of classes to classify.
       - dropout: Scalar between 0 and 1 giving dropout strength. If dropout=1 then
         the network should not use dropout at all.
       - use batchnorm: Whether or not the network should use batch normalization.
       - reg: Scalar giving L2 regularization strength.
       - weight_scale: Scalar giving the standard deviation for random
         initialization of the weights.
       - dtype: A numpy datatype object; all computations will be performed using
         this datatype. float32 is faster but less accurate, so you should use
         float64 for numeric gradient checking.
        - seed: If not None, then pass this random seed to the dropout layers. This
         will make the dropout layers deteriminstic so we can gradient check the
        model.
       self.use batchnorm = use batchnorm
       self.use_dropout = dropout < 1</pre>
       self.reg = reg
       self.num_layers = 1 + len(hidden_dims)
       self.dtype = dtype
       self.params = {}
       # YOUR CODE HERE:
           Initialize all parameters of the network in the self.params dictionary.
           The weights and biases of layer 1 are W1 and b1; and in general the
           weights and biases of layer i are Wi and bi. The
           biases are initialized to zero and the weights are initialized
           so that each parameter has mean 0 and standard deviation weight scale.
           BATCHNORM: Initialize the gammas of each layer to 1 and the beta
           parameters to zero. The gamma and beta parameters for layer 1 should
           be self.params['gamma1'] and self.params['beta1']. For layer 2, they
           should be gamma2 and beta2, etc. Only use batchnorm if self.use batchnorm
           is true and DO NOT do batch normalize the output scores.
       #we will Initialize them based on layers:
       for i in np.arange(1, self.num_layers + 1): #for all layers
           if i == 1: #for the layer 1
               self.params['b1'] = np.zeros(hidden_dims[i - 1]) #based on the size of the first hidden layer
               #the weights will have mean 0 and standard deviation weight_scale
               self.params['Wl'] = np.random.normal(0, weight_scale, (input_dim, hidden_dims[i - 1]))
               #if the network uses batch normalization
               if self.use batchnorm == True:
                   self.params['gamma1'] = np.ones(hidden_dims[i - 1]) #the gammas should be 1
                   self.params['betal'] = np.zeros(hidden_dims[i - 1]) #the betas should be zero
           elif i == self.num_layers: #for the last layer
               #the size after the last layer will be the number of classes
               self.params['b' + str(i)] = np.zeros(num_classes)
               self.params['W' + str(i)] = np.random.normal(0, weight\_scale, (hidden\_dims[i - 2], num\_classes))
           else: #for the layer except the first and the last
               #based on the size of the ith hidden laver
```

```
self.params['b' + str(i)] = np.zeros(hidden_dims[i - 1])
           self.params['W' + str(i)] = np.random.normal(0, weight_scale, (hidden_dims[i - 2], hidden_dims[i - 1])
           #if the network uses batch normalization
           if self.use batchnorm == True:
              self.params['gamma' + str(i)] = np.ones(hidden_dims[i - 1]) #the gammas should be 1
              self.params['beta' + str(i)] = np.zeros(hidden_dims[i - 1]) #the betas should be zero
   # ----- #
   # END YOUR CODE HERE
   # -----
   # When using dropout we need to pass a dropout_param dictionary to each
   # dropout layer so that the layer knows the dropout probability and the mode
   # (train / test). You can pass the same dropout param to each dropout layer.
   self.dropout param = {}
   if self.use_dropout:
       self.dropout_param = {'mode': 'train', 'p': dropout}
   if seed is not None:
       self.dropout param['seed'] = seed
   # With batch normalization we need to keep track of running means and
   # variances, so we need to pass a special bn_param object to each batch
   # normalization layer. You should pass self.bn params[0] to the forward pass
   # of the first batch normalization layer, self.bn params[1] to the forward
   # pass of the second batch normalization layer, etc.
   self.bn_params = []
   if self.use batchnorm:
       self.bn_params = [{'mode': 'train'} for i in np.arange(self.num_layers - 1)]
   # Cast all parameters to the correct datatype
   for k, v in self.params.items():
       self.params[k] = v.astype(dtype)
def loss(self, X, y=None):
   Compute loss and gradient for the fully-connected net.
   Input / output: Same as TwoLayerNet above.
   X = X.astype(self.dtype)
   mode = 'test' if y is None else 'train'
   # Set train/test mode for batchnorm params and dropout param since they
   # behave differently during training and testing.
   if self.dropout_param is not None:
       self.dropout_param['mode'] = mode
   if self.use batchnorm:
       for bn_param in self.bn_params:
          bn_param['mode'] = mode
   scores = None
   # YOUR CODE HERE:
     Implement the forward pass of the FC net and store the output
      scores as the variable "scores".
      BATCHNORM: If self.use_batchnorm is true, insert a bathnorm layer
      between the affine_forward and relu_forward layers. You may
      also write an affine batchnorm relu() function in layer utils.py.
      DROPOUT: If dropout is non-zero, insert a dropout layer after
      every ReLU layer.
                        ______ #
   out_list = []
   cache_list = []
   dropcache list = []
   X = X.reshape([X.shape[0], -1])
   for i in np.arange (1, self.num layers + 1):
       #we will consider three instances:
       if i == 1: #for the layer 1
           #if the network uses batch normalization
           if self.use_batchnorm:
              #affine -> batchnorm -> relu
              out1, cache1 = affine_batchnorm_relu_forward(X, self.params['W' + str(i)], self.params['b' + str(i
                                 self.params['gamma' + str(i)], self.params['beta' + str(i)], self.bn_params[i
           else:
              #affine -> relu
```

```
out1, cache1 = affine_relu_forward(X, self.params['W' + str(i)], self.params['b1'])
             cache list.append(cache1)
              #If dropout is non-zero
              if self.use dropout:
                     #insert a dropout after ReLU laver
                     out1, cached = dropout_forward(out1, self.dropout_param)
                     dropcache_list.append(cached)
             out list.append(out1)
       elif i == self.num layers: #for the last layer
              #do the last layer affine forward
              scores, \ cachescores = affine\_forward(out\_list[i - 2], \ self.params['W' + str(i)], \ self.params['b' + str(i)], \ self.params['b
             cache list.append(cachescores)
       else: #for the layers except the first and the last
              #if the network uses batch normalization
              if self.use batchnorm:
                     #affine -> batchnorm -> relu
                     outnow, cachenow = affine_batchnorm_relu_forward(out_list[i - 2], self.params['W' + str(i)], self.
                                                                                    self.params['gamma' + str(i)], self.params['beta' + str(i)], self.params['beta' + str(i)]
              else:
                     #affine -> relu
                     outnow, cachenow = affine relu forward(out list[i - 2], self.params['W' + str(i)], self.params['b'
              cache list.append(cachenow)
              #If dropout is non-zero
             if self.use_dropout:
                     #insert a dropout after ReLU layer
                     outnow, cached = dropout forward(outnow, self.dropout param)
                     dropcache_list.append(cached)
              out_list.append(outnow)
# END YOUR CODE HERE
# If test mode return early
if mode == 'test':
       return scores
loss, grads = 0.0, {}
# YOUR CODE HERE:
     Implement the backwards pass of the FC net and store the gradients
     in the grads dict, so that grads[k] is the gradient of self.params[k]
     Be sure your L2 regularization includes a 0.5 factor.
      BATCHNORM: Incorporate the backward pass of the batchnorm.
     DROPOUT: Incorporate the backward pass of dropout.
loss, dx = softmax_loss(scores, y) #calculate loss and dx by given softmax loss
for j in np.arange (self.num_layers, 0, -1): #loop from the last layer to the first layer
       \#L2 regularization by multiplying the regularization loss by 0.5(with factor reg)
       loss += (self.reg) * (np.sum(self.params['W' + str(j)] ** 2)) * 0.5
       if j == self.num_layers: #from the last layer
              #backward affine of the second layer
              currentdx, grads['W' + str(j)], grads['b' + str(j)] = affine_backward(dx, cache_list[j - 1])
       else: #for other lavers:
              #If dropout is non-zero
             if self.use dropout:
                    currentdx = dropout backward(currentdx, dropcache list[j - 1])
              #if the network uses batch normalization
              if self.use_batchnorm:
                    currentdx, grads['W' + str(j)], grads['b' + str(j)], grads['gamma' + str(j)], grads['beta' + str(j)]
                    currentdx, grads['W' + str(j)], grads['b' + str(j)] = affine relu backward(currentdx, cache list[j
```

```
#update the gradients of W
   grads['W' + str(j)] += (self.reg) * self.params['W' + str(j)]
# ------ #
# END YOUR CODE HERE
# ----- #
```

return loss, grads

Dropout

In this notebook, you will implement dropout. Then we will ask you to train a network with batchnorm and dropout, and acheive over 55% accuracy on CIFAR-10.

Utils has a solid API for building these modular frameworks and training them, and we will use this very well implemented framework as opposed to "reinventing the wheel." This includes using the Solver, various utility functions, and the layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils.

In [1]:

```
## Import and setups
import time
import numpy as np
import matplotlib.pyplot as plt
from nndl.fc_net import
from nndl.layers import *
from utils.data_utils import get_CIFAR10_data
from utils.gradient_check import eval_numerical_gradient, eval_numerical_gradient_array
from utils.solver import Solver
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray
# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load_ext autoreload
%autoreload 2
def rel_error(x, y):
      "" returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

In [2]:

```
# Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
for k in data.keys():
    print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
```

```
M_train: (49000,)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y test: (1000,)
```

Dropout forward pass

Implement the training and test time dropout forward pass, dropout_forward, in nndl/layers.py. After that, test your implementation by running the following cell.

```
x = np.random.randn(500, 500) + 10

for p in [0.3, 0.6, 0.75]:
    out, _ = dropout_forward(x, {'mode': 'train', 'p': p})
    out_test, _ = dropout_forward(x, {'mode': 'test', 'p': p})

print('Running tests with p = ', p)
    print('Mean of input: ', x.mean())
    print('Mean of train-time output: ', out.mean())
    print('Mean of test-time output: ', out_test.mean())
    print('Fraction of train-time output set to zero: ', (out == 0).mean())
    print('Fraction of test-time output set to zero: ', (out_test == 0).mean())
```

```
Running tests with p = 0.3
Mean of input: 10.000075654537444
Mean of train-time output: 9.991849518681061
Mean of test-time output: 10.000075654537444
Fraction of train-time output set to zero: 0.700248
Fraction of test-time output set to zero: 0.0
Running tests with p = 0.6
Mean of input: 10.000075654537444
Mean of train-time output: 9.973702372669695
Mean of test-time output: 10.000075654537444
Fraction of train-time output set to zero: 0.401652
Fraction of test-time output set to zero: 0.0
Running tests with p = 0.75
Mean of input: 10.000075654537444
Mean of train-time output: 9.991893782187312
Mean of test-time output: 10.000075654537444
Fraction of train-time output set to zero: 0.25066
Fraction of test-time output set to zero: 0.0
```

Dropout backward pass

Implement the backward pass, dropout backward, in nndl/layers.py. After that, test your gradients by running the following cell:

```
In [4]:
```

```
x = np.random.randn(10, 10) + 10
dout = np.random.randn(*x.shape)

dropout_param = {'mode': 'train', 'p': 0.8, 'seed': 123}
out, cache = dropout_forward(x, dropout_param)
dx = dropout_backward(dout, cache)
dx_num = eval_numerical_gradient_array(lambda xx: dropout_forward(xx, dropout_param)[0], x, dout)
print('dx relative error: ', rel_error(dx, dx_num))
```

dx relative error: 5.4456027087706535e-11

Implement a fully connected neural network with dropout layers

Modify the FullyConnectedNet() class in nndl/fc_net.py to incorporate dropout. A dropout layer should be incorporated after every ReLU layer. Concretely, there shouldn't be a dropout at the output layer since there is no ReLU at the output layer. You will need to modify the class in the following areas:

- (1) In the forward pass, you will need to incorporate a dropout layer after every relu layer.
- (2) In the backward pass, you will need to incorporate a dropout backward pass layer.

Check your implementation by running the following code. Our W1 gradient relative error is on the order of 1e-6 (the largest of all the relative errors).

```
In [5]:
```

```
N, D, H1, H2, C = 2, 15, 20, 30, 10
X = np.random.randn(N, D)
y = np.random.randint(C, size=(N,))
for dropout in [0.5, 0.75, 1.0]:
   print('Running check with dropout = ', dropout)
   model = FullyConnectedNet([H1, H2], input dim=D, num classes=C,
                              weight_scale=5e-2, dtype=np.float64,
                              dropout=dropout, seed=123)
   loss, grads = model.loss(X, y)
   print('Initial loss: ', loss)
    for name in sorted(grads):
        f = lambda _: model.loss(X, y)[0]
        grad_num = eval_numerical_gradient(f, model.params[name], verbose=False, h=1e-5)
       print('{} relative error: {}'.format(name, rel_error(grad_num, grads[name])))
    print('\n')
Running check with dropout = 0.5
Initial loss: 2.309771209610118
W1 relative error: 2.694274363733021e-07
W2 relative error: 7.439246147919978e-08
W3 relative error: 1.910371122296728e-08
b1 relative error: 4.112891126518e-09
b2 relative error: 5.756217724722137e-10
b3 relative error: 1.3204470857080166e-10
Running check with dropout = 0.75
Initial loss: 2.306133548427975
W1 relative error: 8.72986097970181e-08
W2 relative error: 2.9777307885797295e-07
W3 relative error: 1.8832780806174298e-08
b1 relative error: 5.379486003985169e-08
b2 relative error: 3.6529949080385546e-09
b3 relative error: 9.987242764516995e-11
Running check with dropout = 1.0
Initial loss: 2.3053332250963194
W1 relative error: 1.2744095365229032e-06
W2 relative error: 4.678743300473988e-07
W3 relative error: 4.331673892536035e-08
b1 relative error: 4.0853539035931665e-08
b2 relative error: 1.951342257912746e-09
b3 relative error: 9.387142701440351e-11
```

Dropout as a regularizer

In class, we claimed that dropout acts as a regularizer by effectively bagging. To check this, we will train two small networks, one with dropout and one without dropout.

```
In [9]:
# Train two identical nets, one with dropout and one without
num_train = 500
small data = {
    'X train': data['X train'][:num train],
    'y_train': data['y_train'][:num_train],
    'X val': data['X val'],
   'y_val': data['y_val'],
solvers = {}
dropout choices = [0.6, 1.0]
for dropout in dropout choices:
   model = FullyConnectedNet([100, 100, 100], dropout=dropout)
   solver = Solver(model, small data.
                   num_epochs=25, batch_size=100,
                    update_rule='adam',
                    optim_config={
                      'learning_rate': 5e-4,
                    verbose=True, print_every=100)
   solver.train()
   solvers[dropout] = solver
(Iteration 1 / 125) loss: 2.300340
(Epoch 0 / 25) train acc: 0.224000; val acc: 0.167000
(Epoch 1 / 25) train acc: 0.170000; val acc: 0.150000
(Epoch 2 / 25) train acc: 0.318000; val acc: 0.261000
(Epoch 3 / 25) train acc: 0.296000; val acc: 0.213000
(Epoch 4 / 25) train acc: 0.326000; val acc: 0.246000
(Epoch 5 / 25) train acc: 0.338000; val_acc: 0.266000
(Epoch 6 / 25) train acc: 0.380000; val acc: 0.243000
(Epoch 7 / 25) train acc: 0.440000; val_acc: 0.285000
(Epoch 8 / 25) train acc: 0.446000; val_acc: 0.294000
(Epoch 9 / 25) train acc: 0.410000; val_acc: 0.263000
(Epoch 10 / 25) train acc: 0.414000; val_acc: 0.278000
(Epoch 11 / 25) train acc: 0.480000; val_acc: 0.266000
(Epoch 12 / 25) train acc: 0.492000; val_acc: 0.312000
(Epoch 13 / 25) train acc: 0.482000; val_acc: 0.306000
(Epoch 14 / 25) train acc: 0.528000; val_acc: 0.313000
(Epoch 15 / 25) train acc: 0.526000; val_acc: 0.313000
(Epoch 16 / 25) train acc: 0.538000; val_acc: 0.312000
(Epoch 17 / 25) train acc: 0.534000; val acc: 0.303000
(Epoch 18 / 25) train acc: 0.566000; val_acc: 0.307000
(Epoch 19 / 25) train acc: 0.546000; val_acc: 0.312000
(Epoch 20 / 25) train acc: 0.590000; val acc: 0.305000
(Iteration 101 / 125) loss: 1.449814
(Epoch 21 / 25) train acc: 0.566000; val_acc: 0.299000
```

(Epoch 22 / 25) train acc: 0.578000; val_acc: 0.308000 (Epoch 23 / 25) train acc: 0.610000; val_acc: 0.324000 (Epoch 24 / 25) train acc: 0.622000; val_acc: 0.300000 (Epoch 25 / 25) train acc: 0.628000; val_acc: 0.307000

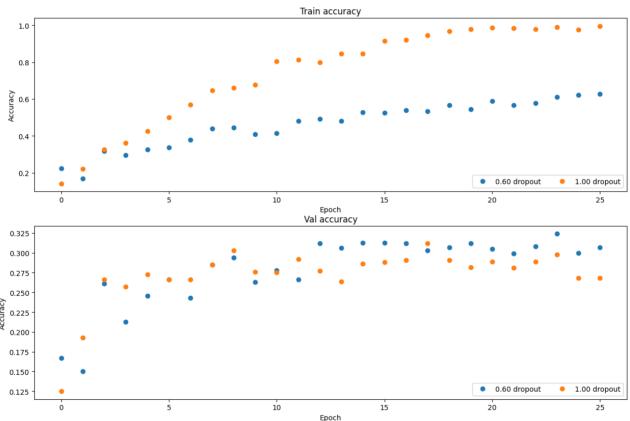
(Epoch 0 / 25) train acc: 0.142000; val_acc: 0.125000 (Epoch 1 / 25) train acc: 0.222000; val acc: 0.193000 (Epoch 2 / 25) train acc: 0.326000; val acc: 0.266000 (Epoch 3 / 25) train acc: 0.362000; val acc: 0.257000 (Epoch 4 / 25) train acc: 0.426000; val_acc: 0.273000 (Epoch 5 / 25) train acc: 0.500000; val acc: 0.266000 (Epoch 6 / 25) train acc: 0.570000; val_acc: 0.266000 (Epoch 7 / 25) train acc: 0.646000; val acc: 0.285000 (Epoch 8 / 25) train acc: 0.662000; val_acc: 0.303000 (Epoch 9 / 25) train acc: 0.678000; val acc: 0.276000 (Epoch 10 / 25) train acc: 0.804000; val_acc: 0.275000 (Epoch 11 / 25) train acc: 0.814000; val acc: 0.292000 (Epoch 12 / 25) train acc: 0.800000; val_acc: 0.277000 (Epoch 13 / 25) train acc: 0.846000; val_acc: 0.264000 (Epoch 14 / 25) train acc: 0.846000; val_acc: 0.286000 (Epoch 15 / 25) train acc: 0.916000; val_acc: 0.288000 (Epoch 16 / 25) train acc: 0.922000; val_acc: 0.291000 (Epoch 17 / 25) train acc: 0.946000; val acc: 0.312000 (Epoch 18 / 25) train acc: 0.968000; val_acc: 0.291000 (Epoch 19 / 25) train acc: 0.980000; val_acc: 0.282000 (Epoch 20 / 25) train acc: 0.986000; val_acc: 0.289000

(Iteration 1 / 125) loss: 2.303964

(Iteration 101 / 125) loss: 0.076472

(Epoch 21 / 25) train acc: 0.984000; val_acc: 0.281000 (Epoch 22 / 25) train acc: 0.978000; val_acc: 0.289000 (Epoch 23 / 25) train acc: 0.990000; val_acc: 0.298000 (Epoch 24 / 25) train acc: 0.976000; val_acc: 0.268000 (Epoch 25 / 25) train acc: 0.996000; val_acc: 0.268000

```
# Plot train and validation accuracies of the two models
train_accs = []
val accs = []
for dropout in dropout choices:
    solver = solvers[dropout]
    train_accs.append(solver.train acc history[-1])
    val_accs.append(solver.val_acc_history[-1])
plt.subplot(3, 1, 1)
for dropout in dropout_choices:
   plt.plot(solvers[dropout].train_acc_history, 'o', label='%.2f dropout' % dropout)
plt.title('Train accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.legend(ncol=2, loc='lower right')
plt.subplot(3, 1, 2)
for dropout in dropout_choices:
   plt.plot(solvers[dropout].val_acc_history, 'o', label='%.2f dropout' % dropout)
plt.title('Val accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.legend(ncol=2, loc='lower right')
plt.gcf().set_size_inches(15, 15)
plt.show()
```



Question

Based off the results of this experiment, is dropout performing regularization? Explain your answer.

Answer:

Yes, the dropout is performing regularization. As we can see that the validation accuracy for two drops are similar while the train accuracy for dropout = 1 is higher, the model without dropout is overfitting the samples. Therefore, we can tell that the dropout is forcing the model to be more generalised and is performing regularization.

Final part of the assignment

Get over 55% validation accuracy on CIFAR-10 by using the layers you have implemented. You will be graded according to the following equation:

min(floor((X - 32%)) / 23%, 1) where if you get 55% or higher validation accuracy, you get full points.

```
(Iteration 1 / 6125) loss: 2.378138
(Epoch 0 / 25) train acc: 0.135000; val acc: 0.150000
(Iteration 101 / 6125) loss: 1.605421
(Iteration 201 / 6125) loss: 1.542825
(Epoch 1 / 25) train acc: 0.476000; val acc: 0.474000
(Iteration 301 / 6125) loss: 1.538562
(Iteration 401 / 6125) loss: 1.443305
(Epoch 2 / 25) train acc: 0.524000; val acc: 0.490000
(Iteration 501 / 6125) loss: 1.398444
(Iteration 601 / 6125) loss: 1.372567
(Iteration 701 / 6125) loss: 1.280711
(Epoch 3 / 25) train acc: 0.553000; val acc: 0.519000
(Iteration 801 / 6125) loss: 1.318911
(Iteration 901 / 6125) loss: 1.319420
(Epoch 4 / 25) train acc: 0.555000; val_acc: 0.553000
(Iteration 1001 / 6125) loss: 1.352377
(Iteration 1101 / 6125) loss: 1.217266
(Iteration 1201 / 6125) loss: 1.322373
(Epoch 5 / 25) train acc: 0.618000; val_acc: 0.549000
(Iteration 1301 / 6125) loss: 1.207786
(Iteration 1401 / 6125) loss: 1.103696
(Epoch 6 / 25) train acc: 0.620000; val_acc: 0.550000
(Iteration 1501 / 6125) loss: 1.177861
(Iteration 1601 / 6125) loss: 1.125841
(Iteration 1701 / 6125) loss: 1.151310
(Epoch 7 / 25) train acc: 0.662000; val_acc: 0.562000
(Iteration 1801 / 6125) loss: 1.199407
(Iteration 1901 / 6125) loss: 1.039357
(Epoch 8 / 25) train acc: 0.697000; val_acc: 0.559000
(Iteration 2001 / 6125) loss: 1.100534
(Iteration 2101 / 6125) loss: 1.104138
(Iteration 2201 / 6125) loss: 1.008565
(Epoch 9 / 25) train acc: 0.692000; val_acc: 0.581000
(Iteration 2301 / 6125) loss: 1.074277
(Iteration 2401 / 6125) loss: 1.062424
(Epoch 10 / 25) train acc: 0.689000; val_acc: 0.582000
(Iteration 2501 / 6125) loss: 0.999744
(Iteration 2601 / 6125) loss: 0.920426
(Epoch 11 / 25) train acc: 0.738000; val_acc: 0.589000
(Iteration 2701 / 6125) loss: 0.969963
(Iteration 2801 / 6125) loss: 0.858363
(Iteration 2901 / 6125) loss: 0.969156
(Epoch 12 / 25) train acc: 0.738000; val acc: 0.594000
(Iteration 3001 / 6125) loss: 0.916767
(Iteration 3101 / 6125) loss: 0.992136
(Epoch 13 / 25) train acc: 0.746000; val_acc: 0.586000
(Iteration 3201 / 6125) loss: 0.809947
(Iteration 3301 / 6125) loss: 0.806089
(Iteration 3401 / 6125) loss: 0.800861
(Epoch 14 / 25) train acc: 0.757000; val_acc: 0.588000
(Iteration 3501 / 6125) loss: 0.676210
(Iteration 3601 / 6125) loss: 0.942014
(Epoch 15 / 25) train acc: 0.784000; val_acc: 0.600000 (Iteration 3701 / 6125) loss: 0.830425
(Iteration 3801 / 6125) loss: 0.839415
(Iteration 3901 / 6125) loss: 0.828776
(Epoch 16 / 25) train acc: 0.803000; val_acc: 0.602000
(Iteration 4001 / 6125) loss: 0.744202
(Iteration 4101 / 6125) loss: 0.800064
(Epoch 17 / 25) train acc: 0.820000; val_acc: 0.592000
(Iteration 4201 / 6125) loss: 0.868332
(Iteration 4301 / 6125) loss: 0.801582
(Iteration 4401 / 6125) loss: 0.774704
(Epoch 18 / 25) train acc: 0.812000; val acc: 0.589000
(Iteration 4501 / 6125) loss: 0.717396
(Iteration 4601 / 6125) loss: 0.869917
(Epoch 19 / 25) train acc: 0.796000; val_acc: 0.609000
(Iteration 4701 / 6125) loss: 0.690982
(Iteration 4801 / 6125) loss: 0.699279
(Epoch 20 / 25) train acc: 0.844000; val acc: 0.586000
(Iteration 4901 / 6125) loss: 0.714194
(Iteration 5001 / 6125) loss: 0.864611
(Iteration 5101 / 6125) loss: 0.790376
(Epoch 21 / 25) train acc: 0.836000; val acc: 0.604000
(Iteration 5201 / 6125) loss: 0.698636
(Iteration 5301 / 6125) loss: 0.612872
(Epoch 22 / 25) train acc: 0.850000; val acc: 0.592000
(Iteration 5401 / 6125) loss: 0.705771
(Iteration 5501 / 6125) loss: 0.745434
(Iteration 5601 / 6125) loss: 0.653437
(Epoch 23 / 25) train acc: 0.855000; val_acc: 0.599000
(Iteration 5701 / 6125) loss: 0.513506
(Iteration 5801 / 6125) loss: 0.552587
(Epoch 24 / 25) train acc: 0.880000; val acc: 0.604000
(Iteration 5901 / 6125) loss: 0.585078
(Iteration 6001 / 6125) loss: 0.539350
(Iteration 6101 / 6125) loss: 0.680519
(Epoch 25 / 25) train acc: 0.879000; val_acc: 0.593000
```

```
In [ ]:
def dropout forward(x, dropout param):
   Performs the forward pass for (inverted) dropout.
   Inputs:
   - x: Input data, of any shape
   - dropout param: A dictionary with the following keys:
    - p: Dropout parameter. We keep each neuron output with probability p.
     - mode: 'test' or 'train'. If the mode is train, then perform dropout;
      if the mode is test, then just return the input.
    - seed: Seed for the random number generator. Passing seed makes this
      function deterministic, which is needed for gradient checking but not in
      real networks.
   Outputs:
   - out: Array of the same shape as x.
   - cache: A tuple (dropout_param, mask). In training mode, mask is the dropout
    mask that was used to multiply the input; in test mode, mask is None.
   p, mode = dropout_param['p'], dropout_param['mode']
   assert (0<p<=1), "Dropout probability is not in (0,1]"</pre>
   if 'seed' in dropout_param:
      np.random.seed(dropout_param['seed'])
   mask = None
   out = None
   if mode == 'train':
      # YOUR CODE HERE:
      # Implement the inverted dropout forward pass during training time.
         Store the masked and scaled activations in out, and store the
        dropout mask as the variable mask.
      mask = (np.random.rand(*x.shape) < p) / p #sample random mask AND normalization by p</pre>
      out = x * mask #dropout on the layer
      # END YOUR CODE HERE
   elif mode == 'test':
      # ----- #
      # YOUR CODE HERE:
      # Implement the inverted dropout forward pass during test time.
      out = x
              # END YOUR CODE HERE
                cache = (dropout_param, mask)
   out = out.astype(x.dtype, copy=False)
   return out, cache
def dropout_backward(dout, cache):
   Perform the backward pass for (inverted) dropout.
   - dout: Upstream derivatives, of any shape
   - cache: (dropout_param, mask) from dropout_forward.
   dropout param, mask = cache
   mode = dropout_param['mode']
   dx = None
   if mode == 'train':
                   # YOUR CODE HERE:
      # Implement the inverted dropout backward pass during training time.
      dx = dout * mask
      # ------ #
      # END YOUR CODE HERE
      # ----- #
   elif mode == 'test':
      # YOUR CODE HERE:
      # Implement the inverted dropout backward pass during test time.
```

```
dx = dout
# ------ #
# END YOUR CODE HERE
# ------ #
return dx
```