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    gradient cache.
- epsilon: Small scalar used for smoothing to avoid dividing by zero.
- beta: Moving average of second moments of gradients.
"""
if config is None: config = {}
config.setdefault('learning_rate', 1e-2)
config.setdefault('decay_rate', 0.99)
config.setdefault('epsilon', 1e-8)
config.setdefault('a', np.zeros_like(w))

next_w = None

# ===== #
# YOUR CODE HERE:
# Implement RMSProp. Store the next value of w as next_w. You need
# to also store in config['a'] the moving average of the second
# moment gradients, so they can be used for future gradients. Concretely,
# config['a'] corresponds to "a" in the lecture notes.
# ===== #

config['a'] = config['decay_rate'] * config['a'] + (1 - config['decay_rate']) * (dw ** 2) #update
next_w = w - config['learning_rate'] / (np.sqrt(config['a']) + config['epsilon']) * dw

# ===== #
# END YOUR CODE HERE
# ===== #

return next_w, config

def adam(w, dw, config=None):
    """
    Uses the Adam update rule, which incorporates moving averages of both the
    gradient and its square and a bias correction term.

    config format:
    - learning_rate: Scalar learning rate.
    - beta1: Decay rate for moving average of first moment of gradient.
    - beta2: Decay rate for moving average of second moment of gradient.
    - epsilon: Small scalar used for smoothing to avoid dividing by zero.
    - m: Moving average of gradient.
    - v: Moving average of squared gradient.
    - t: Iteration number.
    """
    if config is None: config = {}
    config.setdefault('learning_rate', 1e-3)
    config.setdefault('beta1', 0.9)
    config.setdefault('beta2', 0.999)
    config.setdefault('epsilon', 1e-8)
    config.setdefault('v', np.zeros_like(w))
    config.setdefault('a', np.zeros_like(w))
    config.setdefault('t', 0)

    next_w = None

    # ===== #
    # YOUR CODE HERE:
    # Implement Adam. Store the next value of w as next_w. You need
    # to also store in config['a'] the moving average of the second
    # moment gradients, and in config['v'] the moving average of the
    # first moments. Finally, store in config['t'] the increasing time.
    # ===== #

    config['v'] = config['beta1'] * config['v'] + (1 - config['beta1']) * dw
    config['a'] = config['beta2'] * config['a'] + (1 - config['beta2']) * (dw ** 2)
    next_w = w - config['learning_rate'] / (np.sqrt(config['a']) + config['epsilon']) * config['v']
    config['t'] += 1

    # ===== #
    # END YOUR CODE HERE
    # ===== #

    return next_w, config

```