ECE C147/247, Winter 2023 Neural Networks & Deep Learning

Neural Networks & Deep Learning UCLA, ECE

Homework #5 Prof. J.C. Kao

TAs: T.M, P.L, R.G, K.K, N.N, S.R, S.P, M.E

Due Friday, 3 March 2023, by 11:59pm to Gradescope. 100 points total.

1. (10 points) Understanding receptive fields

In a fully connected network, the value/output of every unit (i.e. neuron) depends on the entire input to the network. However, in convolutional neural networks, we typically use filters smaller in size than the input and hence the value of a neuron depends on a part of the input. This region of input space that affects the value of a neuron is called receptive field of the neuron.

In other words, we say that the receptive field of a neuron is n if it's output depends on an $n \times n$ patch of the input. More rigorously, receptive field is a region of space and must be represented as $n \times n$. However, when we consider square kernels, we can denote it using a single variable, since both dimensions are equal. Receptive fields are key to diagnosing potential issue with CNNs. They also help us identify any blind spots in the input and ensure visibility of all input pixels at the output so that no relevant information is missed out while making a prediction.

Consider a toy CNN with 3 convolution layers (CL), powered by ReLU activations, a fully connected layer followed by the output, as shown below:

$$(Input) \rightarrow (CL_1) \rightarrow (ReLU_1) \rightarrow (CL_2) \rightarrow (ReLU_2) \rightarrow (CL_3) \rightarrow (ReLU_3) \rightarrow (FCL) \rightarrow (Output) \rightarrow (Softmax) \rightarrow Loss$$

The kernel size of these layers are $CL_1: m_1 \times m_1, CL_2: m_2 \times m_2, CL_3: m_3 \times m_3$ and stride is set to 1 for all layers.

(**Note**: For the following questions it maybe be helpful to draw a couple of layers of a simple network to visualize the neurons' fields of view)

- (a) (1 point) What is the receptive field of each neuron in (CL_1) ?
- (b) (2 points) What is the receptive field of each neuron in (CL_2) ?
- (c) (3 points) Suppose we introduced a stride of s_1 , s_2 , s_3 on conv layers CL_1 , CL_2 and CL_3 respectively, how would this affect the receptive fields of CL_1 and CL_2 ?
- (d) (2 points) Based on the patterns you observed in the previous question, write down a generalized expression for the receptive field of a neuron in the k^{th} layer of a CNN with n convolution layers (take m_i and s_i as the kernel size and stride of each layer).
- (e) (2 points) Mention two ways to increase the receptive field of neurons in a CNN.

Coding: You should complete the notebooks in order, i.e., CNN-Layers, followed by CNN-BatchNorm, followed by CNN. This is due to potential dependencies. Note however, that CNN can be completed without CNN-Layers, since we provide the fast implementation of the CNN layers to be used in question 4.

- 2. (40 points) Implement convolutional neural network layers. Complete the CNN-Layers.ipynb Jupyter notebook. Print out the entire workbook and relevant code and submit it as a pdf to gradescope. Download the CIFAR-10 dataset, as you did in earlier homework.
- 3. (20 points) Implement spatial normalization for CNNs. Complete the CNN-BatchNorm.ipynb Jupyter notebook. Print out the entire workbook and relevant code and submit it as a pdf to gradescope.
- 4. (30 points) **Optimize your CNN for CIFAR-10.** Complete the CNN ipynb Jupyter notebook. Print out the entire workbook and relevant code and submit it as a pdf to gradescope.