

1. Given  $\alpha = 0.1$ , we have:

$$S(p) \leq \frac{1}{0.1 + 0.9/p}, \quad 1 < p < 128$$

2. The total time  $T$  taken to complete  $k$  tasks is:

$$T = k(\tau + \alpha)$$

Since  $k\alpha$  represents the serial portion of the task which does not benefit from parallelization, the throughput becomes  $k/(k\alpha) = 1/\alpha$ .

3. Tuning should be avoided when: (a) the man hour cost of tuning exceeds the computation time saved; (b) it potentially converts the codebase to spaghetti *al dente*; (c) and when it does not target or significantly affect the code bottleneck.
4. The peak double precision FLOPS for an Intel Xeon Phi coprocessor 5110P is 1010.88 GF/s<sup>1</sup>. where the performance is obtained by:

$$16 \frac{\text{FLOPS}}{\text{clock}} \times 60 \text{ cores} \times 1.053 \text{ GHz} = 1010.88 \text{ GF/s}$$

The peak double precision FLOPS for a single Intel E5-2620 v3 with Turbo Boost is 120 GF/s<sup>2</sup>. This came straight from Intel's data sheet without specifying how it is calculated, though it *probably* uses only AVX2 instructions.

Since we have a total of 96 cores and 15 accelerators, the overall peak FLOPS for the system is:

$$96(120) + 15(1010.88) = 26683.2 \text{ GF/s} = 26.683 \text{ TF/s}$$

5. My machine is a Late 2013 15" Apple Retina Macbook Pro. The processor is an Intel Core i7-4850HQ with a maximum clock speed of 3.5 GHz, 4 cores, 16 vector instructions per cycle, and a 64-bit wide AVX instruction set (which works out to 1 double-precision operand). This gives:

$$3.5 \times 4 \times 16 \times 1 = 224 \text{ GF/s}$$

<sup>1</sup><https://www-ssl.intel.com/content/www/us/en/benchmarks/server/xeon-phi/xeon-phi-theoretical-maximums.html>

<sup>2</sup>[http://download.intel.com/support/processors/xeon/sb/xeon\\_E5-2600.pdf](http://download.intel.com/support/processors/xeon/sb/xeon_E5-2600.pdf)

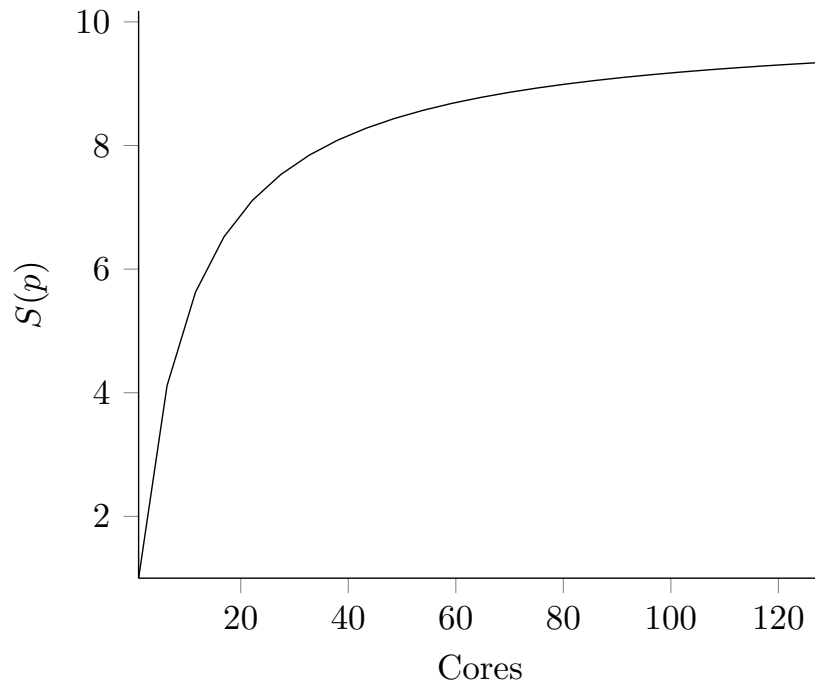


Figure 1: Plot of idealized speedup vs. number of cores used for  $p = 1$  to  $p = 128$  and  $\alpha = 0.1$ . The graph asymptotes at  $S(p) = 1/\alpha = 10$ .

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\begin{tikzpicture}
  \begin{axis}[
    enlarge x limits=false,enlarge y limits=upper,
    xlabel=Cores,ylabel=$S(p)$,tick align=outside,
    axis lines*=left,axis on top]
    \newcommand{\ALPHA}{0.1}
    \addplot[black,domain=1:128]
      {1/(\ALPHA + (1-\ALPHA)/x)};
  \end{axis}
\end{tikzpicture}
```

Figure 2: Graph Generation Code, using  $\text{\LaTeX}$ 's TikZ and PGFPlots packages

In addition, the machine also has an integrated GPU as well as a dedicated GPU, both of which we assume can serve as accelerators. The former is an Intel Iris Pro 5200 with peak FLOPS of 832 GF/s<sup>3</sup>, and the latter is an NVIDIA GeForce GT 750M, with peak FLOPS of 722.7 GF/s<sup>4</sup>. Thus the total theoretical peak flop rate for my machine is:

$$224 + 832 + 722.7 = 1778.7 \text{ GF/s} = 1.78 \text{ TF/s}$$

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<sup>3</sup><http://www.anandtech.com/show/6993/intel-iris-pro-5200-graphics-review-core-i74950hq-tested/2>

<sup>4</sup><https://www.techpowerup.com/gpudb/2224/geforce-gt-750m.html>