

## REVIEW FOR FIRST MIDTERM MATH 104

You are expected to be able to...

- State the completeness axiom of  $\mathbb{R}$ . Use the completeness axiom to prove, for instance, the denseness of  $\mathbb{Q}$ , and any bounded monotone sequence converges.
- State the definition of a convergent sequence, a Cauchy sequence, the  $\liminf$  and  $\limsup$  of a bounded sequence.
- Prove the convergent of a sequence based on the definition (§8, 9.7).
- Prove the limit theorems (§9.1, 9.2, 9.3, 9.4, 9.5, 9.6) based on the definition.
- Prove that all of the following statements are equivalent:
  - $(a_n)$  converges.
  - $(a_n)$  is a Cauchy sequence.
  - $(a_n)$  is bounded and  $\liminf a_n = \limsup a_n$ .
- Prove the theorems related to subsequences that we discussed in class (§11.2(i), 11.3, 11.4, 11.5, 11.7)
- State the definition of a metric space, open/closed subsets, limit points, closure, and understand basic examples.

In short, the exam will cover all the things we've discussed in class, and the homework problems.