

In the lectures, logical inference techniques are only applied to tiny toy problems. The objective of this assignment is for you to solve a not-so-tiny problem automatically by using logical inference techniques explicitly. The target problem is the automatic playing of the Minesweeper game. (There have been a number of AI programs developed for Minesweeper on the web. However, this assignment will require you to use logical inference (specifically, the rule of **resolution**) explicitly so that you'll gain the experience. This is not the most efficient approach though. A typical approach will be more like what you did in Assignment#2, that is, as a constraint satisfaction problem.)

For simplicity, you are only required to use **propositional logic** in your implementation. Treat each cell in the board as a symbol that can be either False ("safe") or True ("mined"). The game proceeds as the player continues to mark the cells as safe or mined.

Your program should consist of two main modules, one for game control and one for the player.

Tasks of the game control module:

- Initialize the board with a preset number of mines. (For your reference, the three difficulty levels of the original Minesweeper are: Easy (9x9 board with 10 mines), Medium (16x16 board with 25 mines), and Hard (30x16 board with 99 mines).)
- Provide the hint (number of surrounding mines) when queried for a cell by the player module.
- Provide an initial list of "safe" cells.
 - ♦ The first few clicks of a Minesweeper game are usually random clicks intended to find connected regions of safe cells.
 - ♦ In this assignment, this is replaced by the initial safe cells.
 - ♦ To start, use `round(sqrt(#cells))` as the number of initial safe cells. You can vary this number later to see how it affects the success rate of games.

Tasks of the player module:

- Here you need to maintain your KB containing CNF clauses.
- Also keep a list of single-literal clauses that represent marked cells. This list is called KB0 below.

如果一個格子已經被mark過了 那就不會出現在KB裡面 只會出現在KB₀裡面

Below are some sample game-play results:

1	1	1	1	x	1	0	0	0
1	x	1	1	1	1	1	1	1
1	1	2	1	1	0	1	x	1
0	0	1	x	1	0	2	2	2
0	0	1	1	1	0	1	x	1
0	0	0	0	0	0	1	1	1
0	0	1	1	2	1	2	1	1
0	0	1	x	4	x	3	x	1
0	0	1	2	x	x	3	1	1

0	0	1	1	2	2	2	x	1	0	0	0	0	0		
0	1	1	2	x	2	x	x	3	2	1	0	0	0	0	
0	1	x	3	2	3	2	x	1	0	0	0	0	0	0	
0	2	3	4	x	1	0	1	1	0	0	0	0	1	1	
0	1	x	x	3	1	0	0	0	0	0	0	0	1	x	
0	1	3	x	3	2	1	2	1	1	0	0	0	1	2	
0	0	1	2	x	2	x	1	0	1	1	2	x	1		
0	0	0	1	1	2	1	3	2	2	0	1	x	2	1	
0	0	0	0	1	1	1	x	1	0	2	2	2	0	0	
1	1	0	0	1	x	1	1	1	0	1	1	0	1	0	
x	1	0	0	1	1	1	0	0	0	0	2	2	2	0	0
1	2	1	1	0	0	0	1	1	1	1	x	1	0	0	
1	x	1	0	0	0	1	1	1	0	0	0	0	0	0	0
1	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0

0	0	1	2	x	1	0	1	x	x	2	0	0	0	0	0	0	1	x	1	0	1	1	1	0	0	2	x	2		
2	2	3	x	3	2	2	3	4	x	3	1	1	0	0	0	0	0	1	1	0	1	x	2	1	1	3	x	3		
x	x	3	x	2	1	x	x	2	1	2	x	1	0	1	1	1	0	0	1	1	2	3	x	1	2	x	1	2		
3	3	2	1	1	1	2	2	1	1	2	3	3	2	2	x	1	0	0	1	x	1	2	x	4	3	2	2	1	1	
x	2	0	0	0	0	0	1	2	4	x	3	x	x	3	1	1	0	0	1	1	1	2	x	x	3	x	3	1	0	
x	4	1	1	0	0	0	1	x	x	x	4	x	4	x	1	1	0	0	1	1	1	2	3	4	x	x	1	0		
x	3	x	3	2	1	1	2	4	x	x	3	3	x	3	x	1	1	1	2	x	1	1	x	1	3	x	5	2	0	
1	2	2	x	x	2	2	x	3	2	3	x	3	2	3	1	1	1	x	2	2	2	2	1	2	3	x	x	1	0	
0	0	2	4	x	2	3	x	3	0	1	1	2	x	1	0	0	2	3	3	2	x	2	2	2	x	5	4	2	0	
1	1	2	x	3	3	5	x	3	0	0	0	1	2	1	1	1	x	x	4	3	x	2	x	5	x	x	1	0		
2	x	3	2	3	x	x	x	2	0	0	0	1	1	2	x	1	2	4	x	x	2	2	3	3	x	x	5	4	2	
3	x	5	x	3	3	2	1	0	0	0	2	x	4	2	1	1	x	3	2	1	1	x	2	2	3	x	x	x		
2	x	x	x	2	1	0	1	1	0	0	2	x	x	1	0	1	1	1	1	2	1	1	1	0	1	3	x	x		
3	4	4	2	1	1	1	3	x	2	0	0	2	3	3	1	0	0	0	0	1	x	1	0	0	0	0	2	3	x	
x	x	1	0	0	2	x	5	x	3	1	1	2	x	1	0	0	0	0	1	2	2	1	0	0	0	0	1	x		
2	2	1	0	0	2	x	4	x	2	1	x	2	1	1	0	0	0	0	1	x	1	0	0	0	0	0	1	x		

* In the boards, gray cells are unmarked, green cells are those marked as safe, and yellow cells are those marked as mined. The numbers are hints of actually safe cells and the x's indicate actually mined cells.

Game flow:

- When the game starts, the KB contains (negative) single-lateral clauses representing the initial safe cells. KB0 is empty initially.
- The game play proceeds in a loop. Within each iteration:
 - If there is a single-lateral clause in the KB (if there are several, just pick one):
 - Mark that cell as safe or mined.
 - Move that clause to KB0.

Process the "matching" of that clause to all the remaining clauses in the KB.

If new clauses are generated due to resolution, insert them into the KB.

If this cell is safe:

Query the game control module for the hint at that cell.

Insert the clauses regarding its unmarked neighbors into the KB.

Otherwise:

Apply pairwise "matching" of the clauses in the KB.

If new clauses are generated by resolution, insert them into the KB.

* For the step of pairwise matching, to keep the KB from growing too fast, only match clause pairs where one clause has only at most two literals.

• Game termination:

兩個做matching的literal 至少其中一個長度為2 如果兩個都超過2 就不做matching

- Success: When all the cells are marked. (KB should become empty.)
- From time to time, a game can be stuck in a state where no new markings can be made as there are multiple solutions to the unmarked cells. This commonly occurs when the difficulty level is Hard, especially near the end of the game.
- For this assignment, if several iterations pass without marking a new cell, you can just stop the game. The game is likely "stuck". (You can try to make guesses as in real games, but this is not required here.)
- Here is an example of a "stuck" game; there are 6 unmarked cells remaining (bottom-left corner).

0	0	0	1	2	3	3	2	2	x	1	0	1	2	2	1	0	1	1	1	1	2	1	1	0	0	1	1	1		
1	2	1	2	x	x	x	x	3	2	1	0	1	x	x	2	1	2	x	1	1	x	2	x	1	0	0	1	x	1	
x	2	x	3	4	3	3	x	1	0	0	1	3	3	3	3	2	2	1	1	2	1	1	1	2	3	2	1	1	1	
1	3	3	4	x	2	1	1	1	1	1	1	1	2	x	4	2	3	x	2	0	0	0	0	0	0	1	x	2	1	
0	1	x	x	4	x	1	0	0	0	1	x	1	2	x	x	2	3	x	3	1	0	0	0	1	2	3	2	2	x	
0	1	4	x	5	3	2	2	1	1	2	2	2	3	4	x	4	x	1	0	0	1	2	x	2	1	2	1	1	1	
0	0	2	x	x	4	x	3	x	2	2	x	3	3	x	3	3	2	3	2	1	1	x	4	4	x	3	2	2	1	
0	0	1	3	x	4	x	4	3	x	2	2	x	x	5	x	4	3	3	x	x	1	1	3	x	x	4	x	x	x	
2	2	1	1	2	3	2	2	x	2	1	2	3	4	x	x	2	1	x	x	3	2	1	0	2	x	4	4	x	3	
x	x	2	0	1	x	1	2	2	2	0	2	x	3	2	2	2	3	2	1	0	0	0	1	1	2	x	4	3	1	
x	x	2	0	2	2	2	2	x	2	0	3	x	4	1	0	1	x	2	1	1	0	0	0	0	0	1	2	x	x	
2	3	2	1	1	x	1	2	x	3	1	2	x	x	2	0	2	2	4	x	2	0	1	1	2	1	1	2	3	3	1
2	3	x	1	1	1	2	2	3	x	1	1	3	x	2	0	1	x	3	x	2	1	2	x	2	x	2	3	x	2	
x	x	3	1	0	0	1	x	2	1	1	0	1	1	1	0	1	2	4	3	2	1	x	3	3	3	x	4	x	3	
4	x	3	0	0	0	1	1	1	0	0	0	0	0	0	0	0	1	x	1	1	1	2	x	3	2	4	x	2	1	
2	x	2	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	2	1	0	0	1	1	2	x	2	1	1	1	

這兩個是特殊情形

About generating clauses from the hints: 30:00

- Each hint provides the following information: There are n mines in a list of m unmarked cells.
- ($n == m$): Insert the m single-literal positive clauses to the KB, one for each unmarked cell. 剩下的都地雷
- ($n == 0$): Insert the m single-literal negative clauses to the KB, one for each unmarked cell. 剩下的都不是地雷
- ($m > n > 0$): General cases (need to generate CNF clauses and add them to the KB):
 - $C(m, m-n+1)$ clauses, each having $m-n+1$ positive literals
 - $C(m, n+1)$ clauses, each having $n+1$ negative literals.For example, for $m=5$ and $n=2$, let the cells be x_1, x_2, \dots, x_5 :
There are $C(5,4)$ all-positive-literal clauses:
 $(x_1 \vee x_2 \vee x_3 \vee x_4), (x_1 \vee x_2 \vee x_3 \vee x_5), \dots, (x_2 \vee x_3 \vee x_4 \vee x_5)$
There are $C(5,3)$ all-negative-literal clauses:
 $(\neg x_1 \vee \neg x_2 \vee \neg x_3), (\neg x_1 \vee \neg x_2 \vee \neg x_4), (\neg x_1 \vee \neg x_2 \vee \neg x_5), \dots, (\neg x_3 \vee \neg x_4 \vee \neg x_5)$
- The global constraint (total number of mines) can be considered a hint as well. However, it is too large to use in the beginning. You can add clauses from this hint when the total number of unmarked cells is small enough. 把對應的clause加進KB裡面

About inserting a new clause to the KB:

使得要放進KB的clause裡面不會包含存在於KB₀的symbols

- Do resolution of the new clause with all the clauses in KB₀ if applicable. Keep only the resulting clause.
- Skip the insertion if there is an identical clause in KB.
- Check for **subsumption** with all the clauses in KB.
 - An example of subsumption:
 $(x_2 \vee x_3)$ is stricter than $(x_1 \vee x_2 \vee x_3)$: The former entails the latter.
As a result, we do not need the less strict clause anymore.
- New clause is stricter than an existing clause: Delete the existing clause.
- An existing clause is stricter than the new clause: Skip (no insertion).

前面的比後面的嚴格 如果前面的為true後面的必為true 所以後面那個是沒有用的

18:00

About "matching" two clauses:

一個symbol在一個clause是positive
在另一個clause是negative

- Check for duplication or subsumption first. Keep only the more strict clause.
- If no duplication or subsumption, and they have complementary literals:

If there is only **one pair** of complementary literals:

Apply resolution to generate a new clause, which will be inserted into the KB.

If there are **more than one pairs** of complementary literals:

Do nothing here. (Resolution will result in tautology (always true).)

Example: $(\neg x_2 \vee x_3)$ and $(x_1 \vee x_2 \vee \neg x_3)$

不一定要寫(寫在報告 不是寫成程式) 可以跳過

如果這邊把x2消掉 就會剩下(x1 or x3 or not x3) which is always true

↖ [Optional / Extra Credits] These are for discussion only; no implementation/experiments required.

- How to use first-order logic here?
- Discuss whether forward chaining or backward chaining applicable to this problem.
- Propose some ideas about how to improve the success rate of "guessing" when you want to proceed from a "stuck" game.
- Discuss ideas of modifying the method in Assignment#2 to solve the current problem.

You submission is a report file in PDF format. The report (maximum 5 pages single-spaced) should describe your experiments and results. In your report, also include a section describing your observations, interpretations, things you have learned, remaining questions, and ideas of future investigation. Include your program code as an appendix (not counting toward the 5-page limit), starting from a separate page. You can use C/C++, Java, Python, or MATLAB to write your program. In general, the TAs will not actually compile or run your programs. The code listing is used to understand your thoughts during your implementation, and to find problems if your results look strange. Therefore, the code listing should be well-organized and contain comments that help the readers understand your code; this will also affect your grade.

The submission is to be through E3. Late submission is accepted for up to a week, with a 5% deduction per day.