

Characterizing Cascade Dynamics in A Microblogging System

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Diffusion in Social Networks

A fundamental process in social networks: behaviors that cascade from node to node

- News, opinions, rumors, . . .
- Virus, disease propagation
- Localized effects: riots

Microblogging Changes How People Discover and Consume Information Online

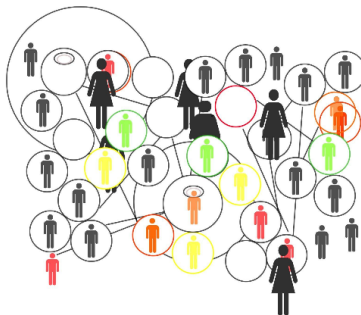
Every person
has at least one secret
that would break your heart.



youku 优酷
.com

YouTube

Post



Case Study: Gangnam Style



Katy Perry ✓
@katyperry

Help, I'm in a gangnam style k hole:
bit.ly/PVPJ4p

12K reposts



Britney Spears ✓
@britneyspears

I am LOVING this video - so fun! Thinking that I should possibly learn the choreography. Anybody wanna teach me?!
haha.britspears.me/159zje

4K reposts



T-Pain ✓
@TPAIN

Words cannot even describe how amazing this video is... youtube.com/watch?v=9bZkp7...

2K reposts

Study the temporal dynamics of an information cascade in a microblogging system

- The number of users influenced at any given time

- Epidemic model:
 - SIS model
 - SIIRP model
- Independent Cascade (IC) Model
- Linear Threshold (LT) Model
- Linear Influence Model

Data-driven Approach: Measurement Study

Tencent Weibo.

- 0.5B users - one of the largest social network services in China

A sample of video sharing in 20 days

- 1M users - social relation, behaviors
- 2M entries - each entry corresponds to one post or repost
- 350K video links - 5 video sharing websites, 14 categories

A Glance of Microblogging Diffusion

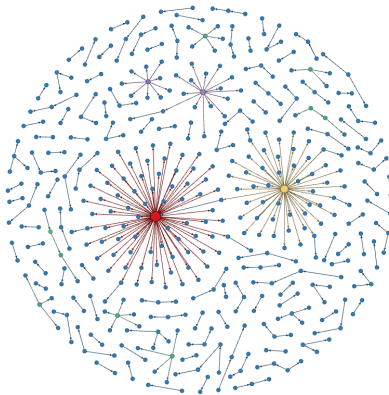
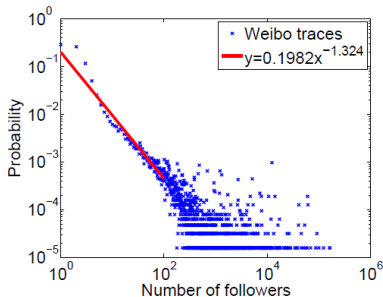
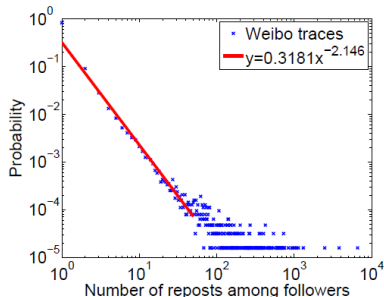


Figure: Example diffusion cascades in Tencent Weibo.

Power-law Distributions of the Number of Followers and the Number of Reposts



(a)



(b)

Figure: Distribution of the number of followers of users, and the number of reposts to their microblogs.

Evolution of Cascade Size

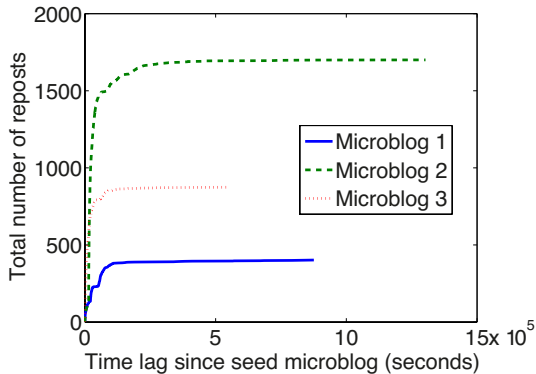


Figure: The total number of reposts versus the time lag since when the seed microblogs are posted.

Gamma Distribution of the Response Delays

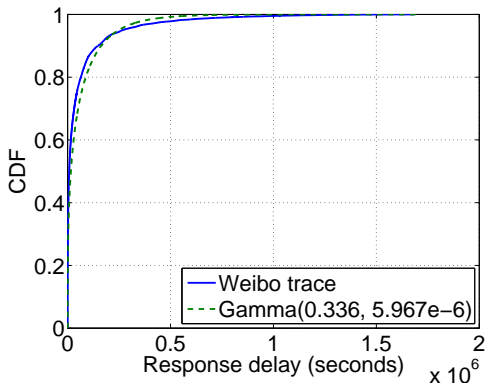


Figure: CDF of response delays of all reposts in our traces.

Objective

How many users in total are expected to have reposted the microblog after a certain time t ?

Branching Process

Branching process

- Each individual gives birth to a random number of offsprings independently according to a certain distribution

Age-dependent branching process

- The lifetimes of individuals are considered based on a lifetime distribution

Mapping

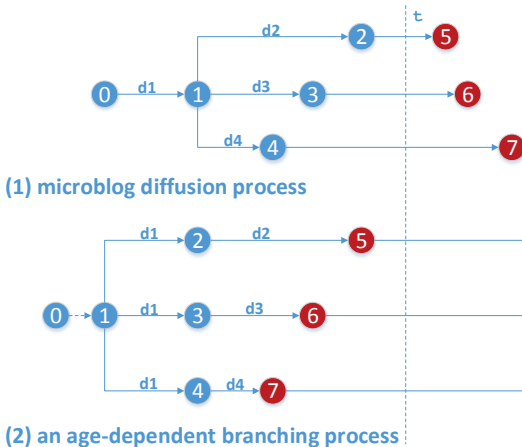
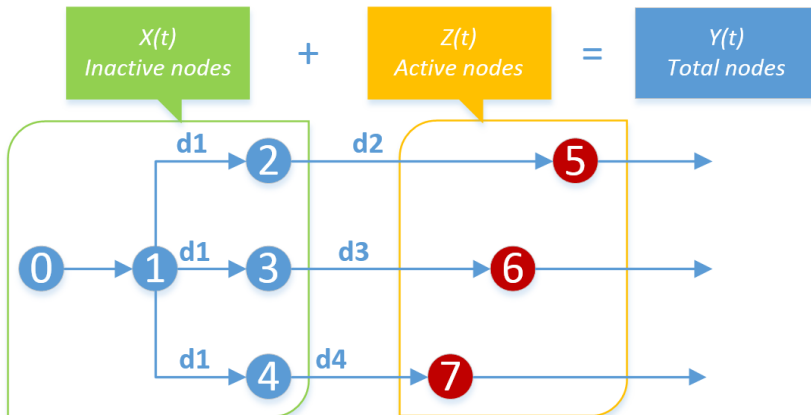
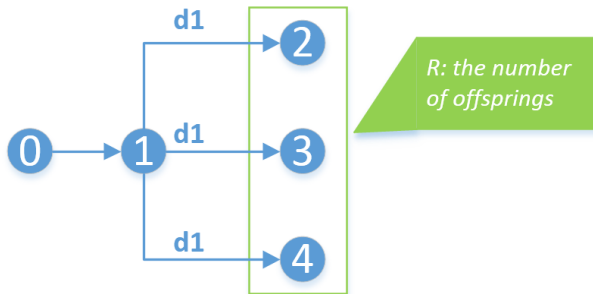


Figure: Mapping between the microblog diffusion cascade and an age-dependent branching tree.

Basic Notations

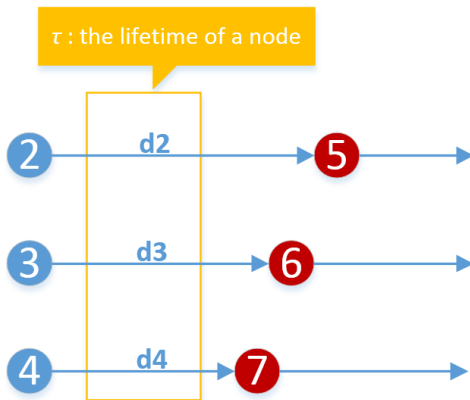


Degree Distribution



- $p(R = k) = p_k$: the probability density function of the number of offsprings of a node in the branching tree
 - $\mu = \sum_k^{\infty} p_k k$: the reproductive number of a node in the branching process

CDF of Lifetimes



- $G(\tau)$: the cumulative distribution function of the lifetimes of nodes in a branching process

The Probability $P(Z(t) = k)$

- Probability density function of $Z(t)$

$$P(Z(t) = k) = [1 - G(t)]\delta_{1k} + \int_0^t dG(\tau) \sum_{j=0}^{\infty} p_j P^{*j}(Z(t - \tau) = k)$$

- P^{*j} is the j -fold convolution of P
- δ_{1k} is the Kronecker delta

Probability Generating Function

- Probability generating function of $Z(t)$

$$\begin{aligned} F(s, t) &= [1 - G(t)] \sum_{k=0}^{\infty} s^k \delta_{1k} \\ &\quad + \int_0^t dG(\tau) \sum_{j=0}^{\infty} p_j \sum_{k=0}^{\infty} P^{*j}(Z(t - \tau) = k) s^k \\ &= s[1 - G(t)] + \int_0^t h[F(s, t - \tau)] dG(\tau) \end{aligned}$$

- Taking derivative

$$\begin{aligned}\frac{\partial F(s, t)}{\partial s} = & [1 - G(t)] \\ & + \int_0^t h'[F(s, t - \tau)] \frac{\partial F(s, t - \tau)}{\partial s} dG(\tau)\end{aligned}$$

- Taking limit $s \rightarrow 1$

$$z(t) = [1 - G(t)] + \mu \int_0^t z(t - \tau) dG(\tau)$$

- Similarly

$$y(t) = 1 + \mu \int_0^t y(t - \tau) dG(\tau)$$

Expressions of $z(t)$ and $y(t)$

- Solutions using renewal theory

$$z(t) = [1 - G(t)] * U(t)$$

and

$$y(t) = U(t)$$

- Renewal function $U(t) = \sum_{n=0}^{\infty} \mu^n G^{*n}(t)$

Expected Number of Inactive Nodes in a Branching Tree

- Solution of $x(t)$

$$x(t) = y(t) - z(t) = G(t) * U(t)$$

- Analytic form of $x(t)$ via Laplace transform and inverse Laplace transform

Overall Size of a Microblog Cascade

- Overall size of a microblog cascade

$$\tilde{x}(t) = \sum_{k=0}^{\infty} p_k kx(t) + 1 = \mu x(t) + 1$$

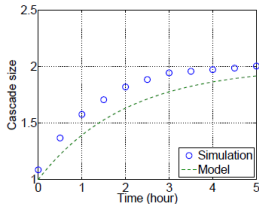
- 1 corresponds to the seed post

Experiment Setup

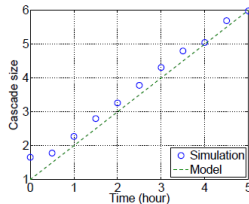
Simulate a microblogging network

- The number of followers and response delays follow the same distributions in the measurement study
- Run 10^4 times for every set of parameters

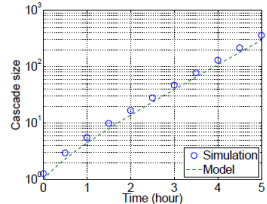
Evolution of Cascade Size



(a) $\mu = 0.5$.



(b) $\mu = 1$.



(c) $\mu = 2$.

Figure: Comparison of the evolution of cascade sizes generated by simulations and our model.

Cascade Size over Time with Two-stage Degree Distributions

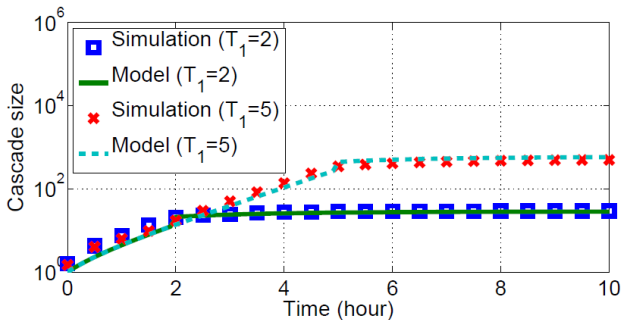
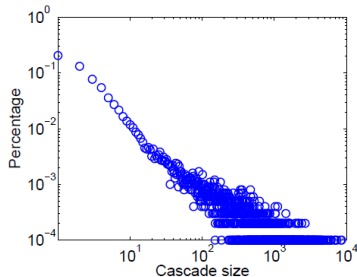
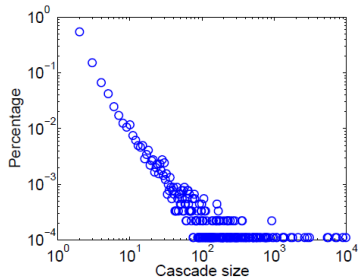


Figure: Comparison of the evolution of cascade sizes generated by simulations and our model: two-stage μ .

Final Cascade Size



(a) Simulation



(b) Tencent Weibo

Figure: Distribution of final cascade sizes.

Summary

- A large-scale measurement study reveals several facts on microblog propagation
- Detailed mathematical derivation of the expected cascade size at any time during a microblog diffusion process is given
- Trace-based simulation experiments demonstrate the effectiveness of our model



More information: <http://i.cs.hku.hk/cwu/papers/sshi-icc14.pdf>