Modeling of the P2P service migration problem 1

We suppose there are M videos, and N ISPs. There are one on-premise server and one cloud node in each ISP.

1.1 Optimization of the problem without Lyapunov optimization

Notation definition:

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C_s^j: storage capacity of the on-premise server at the j-th ISP
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$$C_n^j$$
: upload bandwidth capacity of the on-premise server at the $j-th$ ISP

$$h_i$$
: charging rate for storage on the cloud at the $j-th$ ISP

$$k_j$$
: charging rate for upload bandwidth on the cloud at the $j-th$ ISP

$$s_m$$
: storage of $m - th$ video

$$x_m^j=\{0,1\}, m=1,...,M\colon x_m^j=1$$
 if the placement of the $m-th$ video is on the on-premise server at the $j-th$ ISP; $x_m^j=0$ otherwise;

$$y_m^j=\{0,1\}, m=1,...,M$$
: $y_m^j=1$ if the placement of the $m-th$ video is on the cloud at the $j-th$ ISP; $y_m^j=0$ otherwise;

$$r_m^j$$
 : request rate of the $m-th$ video from the $j-th$ ISP, i.e., the bandwidth demand is $s_m r_m^j$.

$$R_{ji}^m$$
: percentage of requests from j for video m is routed to on-premise server i

$$T_{ji}^m$$
: percentage of requests from j for video m is routed to cloud i

$$\min \sum_{m=1}^{M} \sum_{j=1}^{N} \sum_{i=1}^{N} (s_m r_m^j T_{ji} k + s_m h) y_m^j - \alpha \sum_{m=1}^{M} \sum_{j=1}^{N} s_m r_m^j (T_{jj} + R_{jj})$$
 (maximize local traffic, i.e., minimize delay)

subject to:
$$y_m^j = \{0,1\}, \forall j=1,...,N, \forall m=1,...M \\ x_m^j = \{0,1\}, \forall j=1,...,N, \forall m=1,...M$$

$$x_m^j = \{0, 1\}, \forall j = 1, ..., N, \forall m = 1, ...M$$

$$\sum_{i=1}^{N} (R_{ji}^{m} + T_{ji}^{m}) = 1, \forall j = 1, ..., N, \forall m = 1, ..., M$$

$$0 \leq R_{ji}^{m} \leq x_{m}^{i}, \forall j = 1, ..., N, \forall i = 1, ..., N, \forall m = 1, ..., N$$

$$0 \le T_{ji}^m \le y_m^i, \forall j = 1, ..., N, \forall i = 1, ..., N, \forall m = 1, ..., N$$

$$\sum_{i=1}^{M} s_m x_m^j < C_i^j, \forall i \text{ (on-premise server's storage constraint)}$$

$$\sum_{m=1}^{M} s_m x_m^j \leq C_s^j, \forall j \text{ (on-premise server's storage constraint)}$$

$$\sum_{m=1}^{M} \sum_{j=1}^{N} s_m r_m^j R_{ji}^m \leq C_u^i, \forall i=1,...,N \text{ (on-premise server's upload bandwidth constraint)}$$

known values: C_s^j , C_u^j , h_j , k_j , s_m , r_m^j optimization variables: $x_m^j, y_m^j, R_{ii}^m, T_{ii}^m$

1.2 Optimization of the problem with Lyapunov optimization

This is a combination of optimization for one time deployment and time-average variables. The placement of content is one time deployment while the schedule is for time-average.

Notation definition:

 C_s^j : storage capacity of the on-premise server at the j-th ISP

 C_u^j : upload bandwidth capacity of the on-premise server at the j-th ISP

 h_j : charging rate for storage on the cloud at the j-th ISP

 k_i : charging rate for upload bandwidth on the cloud at the j-th ISP

 s_m : storage of m - th video

 $x_m^j=\{0,1\}, m=1,...,M\colon x_m^j=1$ if the placement of the m-th video is on the on-premise server at the j-th ISP; $x_m^j=0$ otherwise;

 $y_m^j=\{0,1\}, m=1,...,M\colon y_m^j=1$ if the placement of the m-th video is on the cloud at the j-th ISP; $y_m^j=0$ otherwise;

 D^s_{ji} is the delay from source j to on premise server i, and D^c_{ji} is the delay from source j to on cloud node i.

 $r_m^j(t)$: at time slot t, number of requests of the m-th video from the j-th ISP, i.e., the bandwidth demand is $s_m r_m^j$.

 $R_{ji}^m(t)$: at time slot t, number of requests from j for video m is routed to on-premise server i

 $T_{ii}^{m}(t)$: at time slot t, number of requests from j for video m is routed to cloud i

 $Q_m^j(t)$: at time slot t, queues of requests from video m from ISP j.

Note: The queue update is: $Q_m^j(t+1) = \max[Q_m^j(t) + r_m^j(t) - \sum_{i=1}^N R_{ji}^m - \sum_{i=1}^N T_{ji}^m, 0]$

Different from the previous sub section, $R_{ji}^m(t)$ and $T_{ji}^m(t)$ is not a schedule of fraction of arrival rates for all time slots. Now they are schedule of number of requests (integers) for each time slot.

Queues $Q_m^j(t)$ is stable, $\forall m, j$, i.e., $\overline{r_m^j(t)} \leq \overline{\sum_{i=1}^N R_{ji}^m + \sum_{i=1}^N T_{ji}^m}$ Note:

known values: C_s^j , C_u^j , h_j , k_j , s_m , optimization variables: x_m^j , y_m^j , $R_{ii}^m(t)$, $T_{ii}^m(t)$