

# **Data Review**

Yi Xie

May 23, 2022

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### Intermolecular Energies

Supermolecular approach

$$E_{int} = E_{AB} - E_A - E_B$$

- ► Straightforward, but cannot separate different types of interactions
- ► Can adopt to different electronic structure methods
- ► DFT-D3 with proper functional can be both cheap and accurate
- Symmetry-Adapted Perturbation Theory
  - ► Can give details about interactions (electrostatic, induction/polarization, exchange repulsion, London dispersion components); important in understanding their nature
  - ► Not as cheap as DFT-D3
  - SAPT0 is somewhat cheap, but does not include intramonomer correlation

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# SAPT(DFT)

- Attempt to inlude intramonomer correlation in a cheap way
- Replaces HF orbitals with KS orbitals
- Needs to consider orbital response for dispersion terms
- Exchange-dispersion term needs to be estimated from scaling
- Investigate the accuracy and efficiency of SAPT(DFT)

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### Three-Body Interaction

- Crucial in computing high accuracy lattice energies (5% for benzene)
- DFT-D3 does not perform well for three-body interaction
- MP2.5 scales as  $O(N^6)$ , MP2 is  $O(N^5)$  but lacks three-body dispersion
- Three-body dispersion can be implemented with SAPT(DFT) in  ${\cal O}(N^5)$
- Combine MP2 with SAPT(DFT) dispersion to model three-body interaction

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### Idea of SAPT(DFT)

SAPT energy in orders of interaction and fluctuation potentials; n denotes order in V and k, l for  $W_A, W_B$ 

$$H = F_A + F_B + V + W_A + W_B$$

$$E_{int} = \sum_{n=1}^{\infty} \sum_{k=0}^{\infty} \sum_{l=0}^{\infty} \left( E_{pol}^{(nkl)} + E_{exch}^{(nkl)} \right)$$

- SAPT0: n = 2, k = l = 0, no intramonomer correlation,  $O(N^5)$  cost
- ▶ Many-body SAPT:  $k + l \ge 2$ ,  $O(N^6)$  or higher cost
- SAPT(DFT): Use Kohn-Sham operator  $K_{A,B}$  instead of Fock operator  $F_{A,B},\,O(N^5)$  cost
- Primitive SAPT(DFT) works well on 1st-order terms, but not 2nd-order terms (especially dispersion). Needs orbital response for these terms

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### Coupled Dispersion Energy

Uncoupled dispersion energy in terms of frequency-dependent density susceptibility (FDDS):

$$E_{disp,u}^{(2)} = -4 \sum_{ia \in A, jb \in B} \frac{|(ia|jb)|^2}{\epsilon_{ij}^{ab}}$$

$$= -\frac{1}{2\pi} \int_0^\infty d\omega \int d\mathbf{r}_A d\mathbf{r}'_A d\mathbf{r}_B d\mathbf{r}'_B$$

$$= \frac{1}{|\mathbf{r}_A - \mathbf{r}_B|} \frac{1}{|\mathbf{r}'_A - \mathbf{r}'_B|} \chi_0^A \left(\mathbf{r}_A, \mathbf{r}'_A | i\omega\right) \chi_0^B \left(\mathbf{r}_B, \mathbf{r}'_B | i\omega\right)$$

- Kohn-Sham DFT constructs a fictitious system of non-interacting particles, which reproduces the density and energy of the real electronic system
- Kohn-Sham FDDS does not reflect the correct response properties of the electronic system

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# **Dispersion Term**

Coupled FDDS from solving TDDFT equations<sup>1</sup>:

$$oldsymbol{\chi} = oldsymbol{\chi}_0 + oldsymbol{\chi}_0 \mathbf{S}^{-1} \mathbf{W} \left( \mathbf{S} - oldsymbol{\chi}_0 \mathbf{S}^{-1} \mathbf{W} 
ight)^{-1} oldsymbol{\chi}_0$$

- ▶ S and W corresponds to Coulomb metric and xc kernel
- Pure ALDA kernel good for pure GGA functional, but not for hybrid functional
- lacktriangle Exact exchange in  $v_{xc} 
  ightarrow$  increased  $\epsilon^{ab}_{ij} 
  ightarrow$  decreased  $E^{(2)}_{disp}$

$$E_{disp,u}^{(2)} = -4 \sum_{ia \in A, jb \in B} \frac{|(ia|jb)|^2}{\epsilon_{ij}^{ab}}$$

- ► Hybrid ALDA kernel to compensate, or localized HF (LHF) exchange to avoid increase in  $\epsilon_{ij}^{ab}$
- Reformulating solution of hybrid TDDFT equations<sup>2</sup> in density-fitting basis on next slide

<sup>&</sup>lt;sup>1</sup>M. Pitoňák and A. Hesselmann. J. Chem. Theory Comput. **6**. 168 (2010).



# Coupled FDDS with hybrid kernel

$$\chi = \chi'_0 + (\chi'_0 \mathbf{S}^{-1} \mathbf{W} + \mathbf{K}') \left[ \mathbf{S} - (\chi'_0 \mathbf{S}^{-1} \mathbf{W} + \mathbf{K}') \right]^{-1} \chi'_0$$

$$\mathbf{K}' = \left[ -\xi \mathbf{K}_1 (\lambda d) - \xi \mathbf{K}_2 (\lambda d) + \xi^2 \mathbf{K}_{21} (\lambda) \right] (\mathbf{R}^T)^{-1} \mathbf{S}$$

$$\left[ \mathbf{K}_1 (\lambda d) \right]_{PQ} = (P|ar) \lambda_{ar} d_{ar} \left[ (aa'|rr') + (ar'|a'r) \right] (a'r'|\mathbf{Q}|Q)$$

$$\left[ \mathbf{K}_2 (\lambda d) \right]_{PQ} = (P|ar) \lambda_{ar} d_{ar} \left[ (aa'|rr') - (ar'|a'r) \right] (a'r'|\mathbf{Q}|Q)$$

$$\left[ \mathbf{K}_{21} (\lambda) \right]_{PQ} = (P|ar) \lambda_{ar} \left[ (aa''|rr'') - (ar''|a''r') \right]$$

$$\left[ (a'a''|r'r'') - (a'r''|a''r') \right] (a'r'|\mathbf{Q}|Q)$$

$$\left[ \mathbf{K}'_2 (\lambda) \right]_{PQ} = (P|ar) \lambda_{ar} \left[ (aa'|rr') - (ar'|a'r) \right] (a'r'|Q)$$

$$\chi'_0 = \chi_0 - \xi \mathbf{K}_2 (\lambda)$$

$$(ar|Q) = (ar|\mathbf{Q}|P) (P|\mathbf{R}|Q)$$

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# Equation for $E_{disp}^{(2)}$

- Coupled Kohn-Sham (CKS) FDDS reflects correct response properties of electrons
- ${\cal O}(N^5)$  scaling is limited to forming  ${\bf K}_1,\,{\bf K}_2,\,{\bf K}_{21}$  and  ${\bf K}_2'$ . These quantities are frequency-dependent, but could store frequency-independent intermediates from the  $O(N^5)$  contractions on disk, and the frequency-dependent contractions are only  $O(N^4)$
- $E_{disp}^{(2)}$  from coupled FDDS: (Integration is approximated by Gauss-Legendre quadrature)

$$E_{disp,r}^{(2)} = -\frac{1}{2\pi} \int_{0}^{\infty} d\omega \int d\mathbf{r}_{A} d\mathbf{r}'_{A} d\mathbf{r}_{B} d\mathbf{r}'_{B}$$

$$\frac{1}{|\mathbf{r}_{A} - \mathbf{r}_{B}|} \frac{1}{|\mathbf{r}'_{A} - \mathbf{r}'_{B}|} \chi^{A} \left(\mathbf{r}_{A}, \mathbf{r}'_{A} | i\omega\right) \chi^{B} \left(\mathbf{r}_{B}, \mathbf{r}'_{B} | i\omega\right)$$

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## **Exchange-Dispersion Term**

- Explicit coupled exchange-dispersion not trivial to implement; currently working on this
- Estimate from scaling uncoupled exchange-dispersion; Scale with ratio in dispersion term or with pre-fitted (with S22×5) fixed factor

$$\tilde{E}_{exch-disp,r}^{(2)} = E_{exch-disp,u}^{(2)} \cdot \frac{E_{disp,r}^{(2)}}{E_{disp,u}^{(2)}}$$

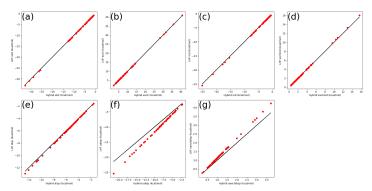
$$\tilde{E}_{exch-disp,r}^{(2)} = \alpha \cdot E_{exch-disp,u}^{(2)}(\alpha = 0.686)$$

- ► The value above is fitted from  $E_{exch-disp,u}^{(2)}$  with LHF orbitals
- Non-LHF orbitals have greater o-v gaps and smaller  $E_{disp,u}^{(2)}$ , needs to re-fit with non-LHF results

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#### LHF vs non-LHF orbitals



Hybrid vs. LHF values in kcal/mol for each term for S66 data set: (a)  $E_{elst}^{(1)}$ , (b)  $E_{exch}^{(1)}$ , (c)  $E_{ind}^{(2)}$ , (d)  $E_{exch-ind}^{(2)}$ , (e)  $E_{disn\,v}^{(2)}$ , (f)  $E_{disn\,v}^{(2)}$ , (g)  $E_{exch-disn\,v}^{(2)}$ 

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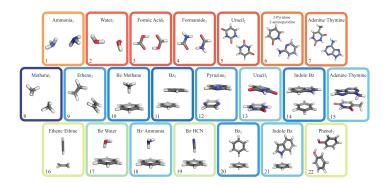
# **Exchange-Dispersion Refitting**

- Need to fit the uncoupled  $E^{(2)}_{exch-disp,r}$  with non-LHF orbitals on the coupled LHF orbital values (implemented in Molpro)
- Assuming coupled LHF and non-LHF orbital  $E^{(2)}_{exch-disp,r}$  from the behavior of  $E^{(2)}_{disp,r}$
- Exchange-related components depend heavily on distance between monomers, sets like S22×5 and S66×8 would be preferred (S22/S66 with various non-equilibrium intermolecular distances)
- Determine the scaling factor with S22×5, validate with S66×8

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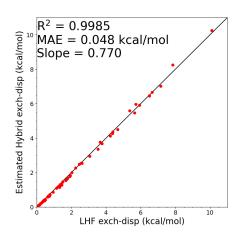
#### S22 dimer set



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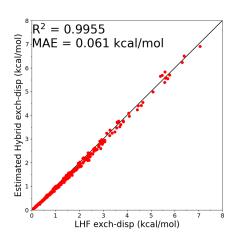
# S22×5 Fitting Results



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# S66×8 Validating Results



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#### Termwise results

- Compared the SAPT(DFT)/aug-cc-pVTZ results of our code to SAPT(CCSD)/aug-cc-pVTZ results from Korona S2<sup>3</sup>
- Also comparing the results for S66 with SAPT2+3(CCD)δMP2/aug-cc-pVTZ as reference. Also added SAPT0/aug-cc-pVDZ, SAPT2+/aug-cc-pVDZ and SAPT2+(3)δMP2/aug-cc-pVTZ into comparison as side-reference.
- Errors of each system with respect to reference shown as vertical lines
- Mean absolute error (MAE) and mean unsigned relative error (MURE) listed for S2. MAE indicated by black box in the diagram
- Color scheme for S66 systems: Hydrogen-bonded (HB, red), mixed-influence (MX, green), dispersion-dominated (DD, blue)

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<sup>&</sup>lt;sup>3</sup>T. Korona, Mol. Phys. **111**, 3705 (2013).



#### Korona S2 Results

Method	MAE	MURE	Error Distribution								
			4	OB	1		0		1	UB	4
Electrostatics											
SAPT(DFT) hybrid	0.112	2.39				Ш	Ш				
SAPT(DFT) LHF	0.114	3.68				Ш	Ш				
SAPT0	0.520	8.61	1	1		Ш					
Exchange											
SAPT(DFT) hybrid	0.251	3.38		1	- [1		Ш				
SAPT(DFT) LHF	0.258	3.09		- 1	- [1	ı					
SAPT0	1.757	12.88		ı	11 1						
Induction											
SAPT(DFT) hybrid	0.148	2.79					Ш				
SAPT(DFT) LHF	0.192	2.97									
SAPT0	1.993	16.83				-		Ш		- 1	
Exchange-Induction											
SAPT(DFT) hybrid	0.144	4.03									
SAPT(DFT) LHF	0.165	4.76									
SAPT0	1.551	26.80				П	П				

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#### Korona S2 Results

Method	MAE	MURE			Error	Distri	bution	n		
			4	OB	1	0	1	UB		4
Dispersion										
SAPT(DFT) hybrid	0.175	3.68								
SAPT(DFT) LHF	0.141	2.77								
SAPT(DFT) non-hybrid	0.326	9.58				11111				
SAPT0	0.811	24.86					Ш		1	- 1
Exchange-Dispersion										
SAPT(DFT) hybrid	0.062	12.47								
SAPT(DFT) LHF	0.039	3.25								
SAPT0	0.265	36.11		- 1	П	П				
Total										
SAPT(DFT) hybrid	0.155	4.98								
SAPT(DFT) LHF	0.189	4.17					+ -			
SAPT(DFT) hon-hybrid	0.244	10.64								
SAPT0	1.237	19.63	1 1		1 11	101				

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#### S66 Results

Method	Total	нв	MX	DD	Error Distribution
				4	OB 1   0   1 UB 4
Electrostatics					
SAPT(DFT) hybrid	0.374	0.556	0.177	0.311	)
SAPT(DFT) LHF	0.423	0.666	0.196	0.319	
SAPT0	0.613	1.034	0.439	0.297	i i i i i i ili i ili ili ili ili ili i
SAPT2+	0.236	0.270	0.136	0.263	m <b>@</b> m
$SAPT2+(3)\delta MP2$	0.000	0.000	0.000	0.000	
Exchange					
SAPT(DFT) hybrid	0.886	1.127	0.426	0.926	
SAPT(DFT) LHF	0.886	1.121	0.431	0.928	11 II I
SAPT0	0.675	0.942	0.263	0.658	
SAPT2+	0.337	0.467	0.222	0.277	<b>                 </b>
$SAPT2+(3)\delta MP2$	0.000	0.000	0.000	0.000	
Induction					
SAPT(DFT) hybrid	0.211	0.201	0.212	0.220	
SAPT(DFT) LHF	0.224	0.223	0.223	0.225	•••
SAPT0	0.241	0.200	0.261	0.271	•••
SAPT2+	0.327	0.384	0.250	0.318	
$_{\rm SAPT2+(3)\delta MP2}$	0.152	0.179	0.121	0.145	

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#### S66 Results

Method	Total	нв	MX	DD	Error Distribution
					4 OB 1   0   1 UB 4
Dispersion					
SAPT(DFT) hybrid	0.370	0.260	0.219	0.573	<b>                                    </b>
SAPT(DFT) LHF	0.308	0.200	0.173	0.499	
SAPT(DFT) non-hybrid	0.635	0.581	0.419	0.822	<b>                                    </b>
SAPT0	0.443	0.862	0.162	0.195	<b>   (10)</b>    (11011    111   1
SAPT2+	0.235	0.397	0.169	0.115	
$SAPT2+(3)\delta MP2$	0.093	0.129	0.056	0.080	••
Total					
SAPT(DFT) hybrid	0.334	0.588	0.107	0.217	
SAPT(DFT) LHF	0.234	0.382	0.046	0.199	<b>III    III                           </b>
SAPT(DFT) non-hybrid	0.604	0.955	0.389	0.385	<b>                                    </b>
SAPT0	0.990	1.197	0.692	0.965	
SAPT2+	0.230	0.235	0.138	0.280	111   <b>                  </b>
$SAPT2+(3)\delta MP2$	0.105	0.056	0.082	0.169	1.0(0.1)

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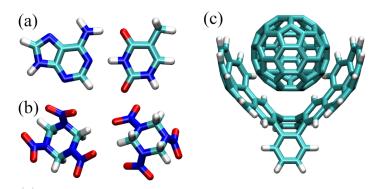
# Timing Performance

- Analyzing breakdown wall times for subroutines in SAPT(DFT) for a few systems with 500–3000 basis functions
- Using Intel Core i7-6800K processor with 6 cores for Watson-Crick adenine-thymine complex and RDX dimer
- ▶ Using Intel Core i9-10980XE processor with 18 cores for C<sub>60</sub>-buckycatcher ( $N_{bf}=3012$ ), completed entire calculation in 4.03 days
- $\,\blacktriangleright\,$  Contribution of  $O(N^5)$  dispersion terms not dominant for smaller systems
- Cost of SCF (HF/DFT) calculations and induction terms are usually non-negligible

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# **Timing Systems**

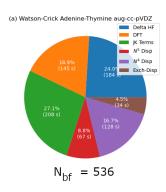


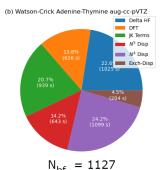
Dimer systems for timing: (a) Watson-Crick adenine-thymine complex, (b) RDX dimer, (c)  $C_{60}$ -buckycather complex.

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### Watson-Crick Adenine-Thymine

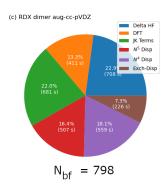


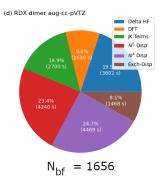


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#### **RDX Dimer**





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## Comparison with LHF Approach

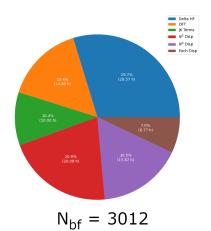
- Comparison of subrountine wall times between hyybrid xc kernel approach implemented in Psi4 1.4 and LHF approach implemented in Molpro 2019.2
- Some subroutines does not exist or not included by default in the Molpro DFT-SAPT program

Subroutine	Psi4 hybrid time (h)	Molpro LHF time (h)
Delta HF	0.96	N/A
DFT	0.45	2.29
xc kernel	0.08	4.17
$O(N^5)$ objects formation	2.35	N/A
$E_{disp}^{\left( 2 ight) }$ time integration	0.37	3.59
$E_{exch-disp}^{(2)}$	0.41	1.99
Total	5.03	12.80

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# C<sub>60</sub>-Buckycatcher Complex



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#### 3B-69 Benchmark Set

- Benchmark set for 3-body interaction energies<sup>4</sup>
- 69 trimers extracted from 23 different molecular crystal structures (3 each)
- Used focal point approach to obtain CCSD(T) (and other wavefunction method) energies

$$E = E^{HF}(aQZ) + \Delta E^{MP2}(aTZ/aQZ) + \Delta E^{CCSD(T)}(aDZ)$$

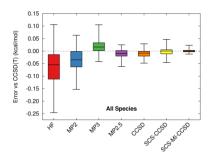
- Assessing accuracy for various wavefunction and DFT methods
- ▶ Authors recommended MP2.5 and SCS-MI-CCSD, both  $O(N^6)$
- We will extend this work to assess the performance of MP2+FDDS (dispersion) for 3B-69 systems

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<sup>&</sup>lt;sup>4</sup>J. Řezáč et al., J. Chem. Theory Comput. 11, 3065 (2015).



#### 3B-69 Wavefunctional Methods

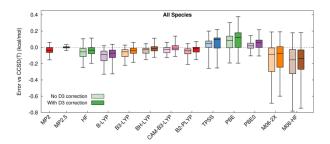


- MP2.5 and SCS-MI-CCSD exhibits best cost performance, as in the two-body case
- MP2.5, MP3: Non-iterative  $O(N^6)$
- ▶ CCSD and variants: Iterative  $O(N^6)$

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#### 3B-69 DFT Methods



- ▶ DFT-D3 accuracies comparable to MP2 at the best, in contrast to the two-body case where DFT-D3 models significantly outperform MP2
- Delocalization error leads to errors in many-body polarization and exchange

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### Three-Body FDDS Dispersion

Three-body dispersion energy in terms of FDDS, analogous to the two-body dispersion:

$$E_{disp,r}^{(3)} = -\frac{1}{\pi} \int_{0}^{\infty} d\omega \int d\mathbf{r}_{A} d\mathbf{r}'_{A} d\mathbf{r}_{B} d\mathbf{r}'_{B} d\mathbf{r}_{C} d\mathbf{r}'_{C}$$

$$\frac{1}{|\mathbf{r}_{A} - \mathbf{r}_{B}|} \frac{1}{|\mathbf{r}'_{A} - \mathbf{r}_{C}|} \frac{1}{|\mathbf{r}'_{B} - \mathbf{r}'_{C}|}$$

$$\chi^{A} (\mathbf{r}_{A}, \mathbf{r}'_{A}|i\omega) \chi^{B} (\mathbf{r}_{B}, \mathbf{r}'_{B}|i\omega) \chi^{C} (\mathbf{r}_{B}, \mathbf{r}'_{B}|i\omega)$$

Transform from position space into density-fitting auxiliary basis space:

$$E_{disp,r}^{(3)} = \int_0^\infty d\omega \operatorname{Tr} \left( \mathbf{S}^{-1} \boldsymbol{\chi}^A \mathbf{S}^{-1} \boldsymbol{\chi}^B \mathbf{S}^{-1} \boldsymbol{\chi}^C \right)$$

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#### New Set from X23

- Aiming to construct a "three-body version" of S22×5/S66×8 to investigate three-body interaction for trimers with different intermolecular distances and alignments
- Sampling trimer geometries from X23 crystal structures
- Distance: Geometric mean and mininum of 3 pairwise closest contact distances
- Alignment: Angles of the COM triangle; mainly looking at the greatest angle

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#### Research Plan

- Check if MP2+FDDS (dispersion) is a good model for three-body non-additive interaction energy
- If not, compare FDDS dispersion with estimated three-body dispersion energy from  $E^{\rm CCSD(T)}-E^{\rm MP2}$
- Investigate the dependence of three-body dispersion energies on intermolecular distances and alignments, and the difference between FDDS dispersion and  $E^{\rm CCSD(T)}-E^{\rm MP2}$  for different trimer geometries
- Choosing dispersion dominated systems (such as benzene) in X23 to avoid zero dispersion energies at longer distance.

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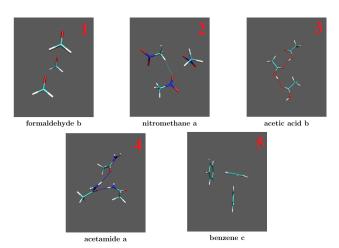
Results

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## 3B-69 Initial Test: Systems



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### 3B-69 Initial Test: Results

- Total three-body non-additive interaction energies in kcal/mol
- CCSD(T) and MP2.5 interaction energies from focus point approach

System	CCSD(T)	MP2+	MP2+	MP2	MP2.5
		FDDS/aDZ	FDDS/aTZ		
1	0.181	0.207	0.210	0.161	0.179
2	-0.122	-0.069	-0.065	-0.178	-0.143
3	-0.922	-0.905	-0.904	-0.937	-0.913
4	-0.089	-0.003	-0.003	-0.239	-0.151
5	-0.027	0.002	0.003	-0.061	-0.023

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### 3B-69 Initial Test: Results

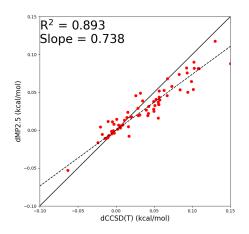
- Comparison of estimated 3-body dispersion energies
- ho hoCCSD(T) corresponds to dispersion energy estimated by  $E^{
  m CCSD(T)} E^{
  m MP2}$

System	$\Delta \text{CCSD(T)}$	FDDS/aDZ	FDDS/aTZ
1	0.020	0.046	0.049
2	0.056	0.109	0.113
3	0.015	0.032	0.033
4	0.150	0.236	0.242
5	0.034	0.063	0.064

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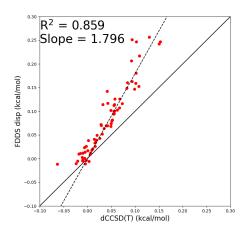
# 3B-69 Three-Body Dispersion: $\Delta$ MP2.5



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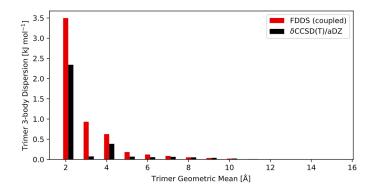
## 3B-69 Three-Body Dispersion: FDDS



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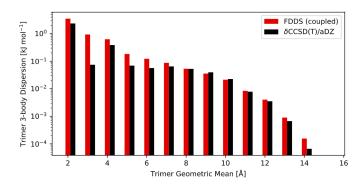
## Crystalline Benzene 3-Body Dispersion



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# Crystalline Benzene 3-Body Dispersion



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