

# **Data Review**

Yi Xie

May 16, 2022

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- Overview
- SAPT(DFT) Implementation Theory Results
- 3 Three-Body FDDS Dispersion Background Results

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### Intermolecular Energies

Supermolecular approach

$$E_{int} = E_{AB} - E_A - E_B$$

- ► Straightforward, but cannot separate different types of interactions
- ► Can adopt to different electronic structure methods
- ► DFT-D3 with proper functional can be both cheap and accurate
- Symmetry-Adapted Perturbation Theory
  - ► Can give details about different types of interactions; important in understanding their nature
  - ▶ Not as cheap as DFT-D3
  - SAPT0 is somewhat cheap, but does not include intramonomer correlation

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# SAPT(DFT)

- Attempt to inlude intramonomer correlation in a cheap way
- Replaces HF orbitals with KS orbitals
- Needs to consider orbital response for dispersion terms
- Exchange-dispersion term needs to be estimated from scaling
- Investigate the accuracy and efficiency of SAPT(DFT)

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### Three-Body Interaction

- Crucial in computing lattice energies
- DFT-D3 does not perform well for three-body interaction
- ▶ MP2.5 scales as  $O(N^6)$ , MP2 is  $O(N^5)$  but lacks three-body dispersion
- Three-body dispersion can be implemented with SAPT(DFT) in  ${\cal O}(N^5)$
- Combine MP2 with SAPT(DFT) dispersion to model three-body interaction

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### Idea of SAPT(DFT)

SAPT energy in orders of interaction and fluctuation potentials; n denotes order in V and k,l for  $W_A,W_B$ 

$$H = F_A + F_B + V + W_A + W_B$$

$$E_{int} = \sum_{n=1}^{\infty} \sum_{k=0}^{\infty} \sum_{l=0}^{\infty} \left( E_{pol}^{(nkl)} + E_{exch}^{(nkl)} \right)$$

- SAPT0: n = 2, k = l = 0, no intramonomer correlation,  $O(N^5)$  cost
- ▶ Many-body SAPT:  $k + l \ge 2$ ,  $O(N^6)$  or higher cost
- SAPT(DFT): Use Kohn-Sham operator  $K_{A,B}$  instead of Fock operator  $F_{A,B},\,O(N^5)$  cost
- Primitive SAPT(DFT) works well on 1st-order terms, but not 2nd-order terms (especially dispersion). Needs orbital response for these terms

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### Coupled Dispersion Energy

Uncoupled dispersion energy in terms of frequency-dependent density susceptibility (FDDS):

$$E_{disp,u}^{(2)} = -4 \sum_{ia \in A, jb \in B} \frac{|(ia|jb)|^2}{\epsilon_{ij}^{ab}}$$

$$= -\frac{1}{2\pi} \int_0^\infty d\omega \int d\mathbf{r}_A d\mathbf{r}'_A d\mathbf{r}_B d\mathbf{r}'_B$$

$$= \frac{1}{|\mathbf{r}_A - \mathbf{r}_B|} \frac{1}{|\mathbf{r}'_A - \mathbf{r}'_B|} \chi_0^A \left(\mathbf{r}_A, \mathbf{r}'_A | i\omega\right) \chi_0^B \left(\mathbf{r}_B, \mathbf{r}'_B | i\omega\right)$$

- Kohn-Sham DFT constructs a fictitious system of non-interacting particles, which reproduces the density and energy of the real electronic system
- Kohn-Sham FDDS does not reflect the correct response properties of the electronic system

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## Dispersion Term

Coupled FDDS from solving TDDFT equations:

$$oldsymbol{\chi} = oldsymbol{\chi}_0 + oldsymbol{\chi}_0 \mathbf{S}^{-1} \mathbf{W} \left( \mathbf{S} - oldsymbol{\chi}_0 \mathbf{S}^{-1} \mathbf{W} 
ight)^{-1} oldsymbol{\chi}_0$$

- S and W corresponds to Coulomb metric and xc kernel
- Pure ALDA kernel good for pure GGA functional, but not for hybrid functional
- lacktriangleright Exact exchange in  $v_{xc} 
  ightarrow$  increased  $\epsilon^{ab}_{ij} 
  ightarrow$  decreased  $E^{(2)}_{disp}$

$$E_{disp,u}^{(2)} = -4 \sum_{ia \in A, jb \in B} \frac{|(ia|jb)|^2}{\epsilon_{ij}^{ab}}$$

▶ Hybrid ALDA kernel to compensate, or localized HF (LHF) exchange to avoid increase in  $\epsilon^{ab}_{ij}$ 



# Coupled FDDS with hybrid kernel

$$\chi = \chi'_0 + (\chi'_0 \mathbf{S}^{-1} \mathbf{W} + \mathbf{K}') \left[ \mathbf{S} - (\chi'_0 \mathbf{S}^{-1} \mathbf{W} + \mathbf{K}') \right]^{-1} \chi'_0$$

$$\mathbf{K}' = \left[ -\xi \mathbf{K}_1 (\lambda d) - \xi \mathbf{K}_2 (\lambda d) + \xi^2 \mathbf{K}_{21} (\lambda) \right] (\mathbf{R}^T)^{-1} \mathbf{S}$$

$$\left[ \mathbf{K}_1 (\lambda d) \right]_{PQ} = (P|ar) \lambda_{ar} d_{ar} \left[ (aa'|rr') + (ar'|a'r) \right] (a'r'|\mathbf{Q}|Q)$$

$$\left[ \mathbf{K}_2 (\lambda d) \right]_{PQ} = (P|ar) \lambda_{ar} d_{ar} \left[ (aa'|rr') - (ar'|a'r) \right] (a'r'|\mathbf{Q}|Q)$$

$$\left[ \mathbf{K}_{21} (\lambda) \right]_{PQ} = (P|ar) \lambda_{ar} \left[ (aa''|rr'') - (ar''|a''r') \right] (a'r'|\mathbf{Q}|Q)$$

$$\left[ \mathbf{K}'_2 (\lambda) \right]_{PQ} = (P|ar) \lambda_{ar} \left[ (aa'|rr') - (ar'|a'r) \right] (a'r'|Q)$$

$$\chi'_0 = \chi_0 - \xi \mathbf{K}_2 (\lambda)$$

$$(ar|Q) = (ar|\mathbf{Q}|P) (P|\mathbf{R}|Q)$$

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# Equation for $E_{disp}^{(2)}$

- Coupled Kohn-Sham (CKS) FDDS reflects correct response properties of electrons
- ullet  $O(N^5)$  scaling is limited to forming  ${f K}_1,\,{f K}_2,\,{f K}_{21}$  and  ${f K}_2'$
- Separates "nontrivial" and "trivial" parts of the code, also highly reduces need of disk I/O operations
- $ightharpoonup E_{disp}^{(2)}$  from coupled FDDS:

$$E_{disp,u}^{(2)} = -\frac{1}{2\pi} \int_0^\infty d\omega \int d\mathbf{r}_A d\mathbf{r}'_A d\mathbf{r}_B d\mathbf{r}'_B$$
$$\frac{1}{|\mathbf{r}_A - \mathbf{r}_B|} \frac{1}{|\mathbf{r}'_A - \mathbf{r}'_B|} \chi^A \left(\mathbf{r}_A, \mathbf{r}'_A | i\omega\right) \chi^B \left(\mathbf{r}_B, \mathbf{r}'_B | i\omega\right)$$

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### **Exchange-Dispersion Term**

- Explicit coupled exchange-dispersion not trivial to implement;
   currently working on this
- Estimate from scaling uncoupled exchange-dispersion; Scale with ratio in dispersion term or with pre-fitted (with S22×5) fixed factor

$$\tilde{E}_{exch-disp,r}^{(2)} = E_{exch-disp,u}^{(2)} \cdot \frac{E_{disp,r}^{(2)}}{E_{disp,u}^{(2)}}$$

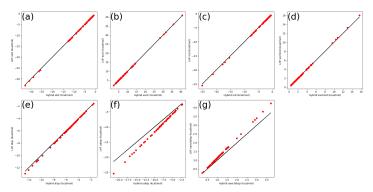
$$\tilde{E}_{exch-disp,r}^{(2)} = \alpha \cdot E_{exch-disp,u}^{(2)}(\alpha = 0.686)$$

- ► The value above is fitted from  $E^{(2)}_{exch-disp,u}$  with LHF orbitals
- Non-LHF orbitals have greater o-v gaps and smaller  $E_{disp,u}^{(2)}$ , needs to re-fit with non-LHF results

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#### LHF vs non-LHF orbitals



Hybrid vs. LHF values in kcal/mol for each term for S66 data set: (a)  $E_{elst}^{(1)}$ , (b)  $E_{exch}^{(1)}$ , (c)  $E_{ind}^{(2)}$ , (d)  $E_{exch-ind}^{(2)}$ , (e)  $E_{disn\,v}^{(2)}$ , (f)  $E_{disn\,v}^{(2)}$ , (g)  $E_{exch-disn\,v}^{(2)}$ 

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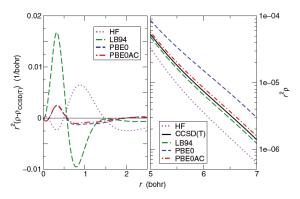
#### **GRAC**

- ► (Hybrid-)GGA functionals does not have correct long-range behavior  $v_{xc}(r) \rightarrow -1/r + (I_p + \epsilon_{\text{HOMO}})$
- Underestimates o-v gap as a consequence
- Functionals like LB94 have correct asymptotic behavior, but poor in bulk region
- ▶ Using gradient-regulated asymptotic correction (GRAC) scheme to connect PBE0 and LB94 with the switching function f[g(r)]:

$$\begin{split} v_{xc}^{\text{GRAC}} &= \{1 - f[g(\boldsymbol{r})]\} \, v_{xc}^{\text{PBE0}} + f[g(\boldsymbol{r})] v_{xc}^{\text{LB94}} \\ &f[g(\boldsymbol{r})] = \left(1 + e^{-\alpha[g(\boldsymbol{r}) - \beta]}\right)^{-1} \\ &g(\boldsymbol{r}) = \frac{|\nabla \rho(\boldsymbol{r})|}{\rho^{4/3}(\boldsymbol{r})} \end{split}$$



### **GRAC & Long-Range Behavior**



Radial densities  $r^2\rho(r)$  of Ne atom (right) and errors compared to CCSD(T) density (left) for various xc potentials.<sup>1</sup>

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<sup>&</sup>lt;sup>1</sup>G. Jansen, WIREs Comput. Mol. Sci. 4, 127 (2014).



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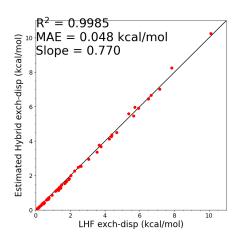


### **Exchange-Dispersion Refitting**

- Need to fit the uncoupled  $E^{(2)}_{exch-disp,r}$  with non-LHF orbitals on the coupled LHF orbital values (implemented in Molpro)
- Assuming coupled LHF and non-LHF orbital  $E^{(2)}_{exch-disp,r}$  from the behavior of  $E^{(2)}_{disp,r}$
- Exchange-related components depend heavily on distance between monomers, sets like S22×5 and S66×8 would be preferred
- ▶ Determine the scaling factor with S22×5, validate with S66×8



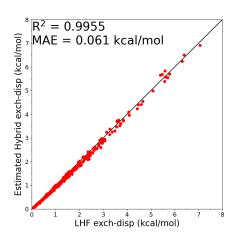
# S22×5 Fitting Results



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# S66×8 Validating Results



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#### Termwise results

- Compared the SAPT(DFT)/aug-cc-pVTZ results of our code to SAPT(CCSD)/aug-cc-pVTZ results from Korona S2<sup>2</sup>
- Also comparing the results for S66 with SAPT2+3(CCD)δMP2/aug-cc-pVTZ as reference. Also added SAPT0/aug-cc-pVDZ, SAPT2+/aug-cc-pVDZ and SAPT2+(3)δMP2/aug-cc-pVTZ into comparison as side-reference.
- Errors of each system with respect to reference shown as vertical lines
- Mean absolute error (MAE) and mean unsigned relative error (MURE) listed for S2. MAE indicated by black box in the diagram
- Color scheme for S66 systems: Hydrogen-bonded (HB, red), mixed-influence (MX, green), dispersion-dominated (DD, blue)

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<sup>&</sup>lt;sup>2</sup>T. Korona, Mol. Phys. **111**, 3705 (2013).



#### Korona S2 Results

| Methoda            | MAE   | MURE  | Error Distribution <sup>b</sup> |    |   |   |   |   |   |   |   |   |    |   |
|--------------------|-------|-------|---------------------------------|----|---|---|---|---|---|---|---|---|----|---|
|                    |       |       | 4                               | OB | 1 |   | 1 | 0 |   | 1 |   |   | UB | 4 |
| Electrostatics     |       |       |                                 |    |   |   |   |   |   |   |   |   |    |   |
| SAPT(DFT) hybrid   | 0.112 | 2.39  |                                 |    |   | l |   | Ш |   |   |   |   |    |   |
| SAPT(DFT) LHF      | 0.114 | 3.68  |                                 |    |   |   |   | Ш |   |   |   |   |    |   |
| SAPT0              | 0.520 | 8.61  | 1                               |    |   |   | I |   |   |   |   |   |    |   |
| Exchange           |       |       |                                 |    |   |   |   |   |   |   |   |   |    |   |
| SAPT(DFT) hybrid   | 0.251 | 3.38  |                                 |    |   |   |   | Ш |   |   |   |   |    |   |
| SAPT(DFT) LHF      | 0.258 | 3.09  |                                 |    |   |   |   |   |   |   |   |   |    |   |
| SAPT0              | 1.757 | 12.88 |                                 | ı  | Ш | l |   |   |   |   |   |   |    |   |
| Induction          |       |       |                                 |    |   |   |   |   |   |   |   |   |    |   |
| SAPT(DFT) hybrid   | 0.148 | 2.79  |                                 |    |   |   |   | Ш |   |   |   |   |    |   |
| SAPT(DFT) LHF      | 0.192 | 2.97  |                                 |    |   |   |   | П | l |   |   | 1 |    |   |
| SAPT0              | 1.993 | 16.83 |                                 | I  |   |   |   |   |   |   |   |   |    |   |
| Exchange-Induction |       |       |                                 |    |   |   |   |   |   |   |   |   |    |   |
| SAPT(DFT) hybrid   | 0.144 | 4.03  |                                 |    |   |   |   | Ш |   |   |   |   |    |   |
| SAPT(DFT) LHF      | 0.165 | 4.76  |                                 |    |   |   |   | Ш | - |   | 1 |   |    |   |
| SAPT0              | 1.551 | 26.80 | I                               | 1  |   | Ш |   |   |   |   |   |   |    |   |

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#### Korona S2 Results

| Dispersion           |       |       |                      |
|----------------------|-------|-------|----------------------|
| SAPT(DFT) hybrid     | 0.175 | 3.68  |                      |
| SAPT(DFT) LHF        | 0.141 | 2.77  | <b>   </b>           |
| SAPT(DFT) non-hybrid | 0.326 | 9.58  | <b>     </b>         |
| SAPT0                | 0.811 | 24.86 | [ <b>1</b> ] [1] [1] |
| Exchange-Dispersion  |       |       |                      |
| SAPT(DFT) hybrid     | 0.062 | 12.47 |                      |
| SAPT(DFT) LHF        | 0.039 | 3.25  | (1                   |
| SAPT0                | 0.265 | 36.11 |                      |
| Total                |       |       |                      |
| SAPT(DFT) hybrid     | 0.155 | 4.98  |                      |
| SAPT(DFT) LHF        | 0.189 | 4.17  | <b>     </b>         |
| SAPT(DFT) hon-hybrid | 0.244 | 10.64 | <b>        </b>      |
| SAPT0                | 1.237 | 19.63 |                      |

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#### S66 Results

| Methoda               | Total | $^{\mathrm{HB}}$ | MX    | DD    |      | $\mathbf{E}$ | rro | r I | Distr | ribu | $ition^{l}$ | )  |  |
|-----------------------|-------|------------------|-------|-------|------|--------------|-----|-----|-------|------|-------------|----|--|
|                       |       |                  |       |       | 4 (  | ОВ           |     | 1   | 0     |      | 1           | UB |  |
| Electrostatics        |       |                  |       |       |      |              |     |     |       |      |             |    |  |
| SAPT(DFT) hybrid      | 0.374 | 0.556            | 0.177 | 0.311 |      |              |     |     | Щ     |      | 1           |    |  |
| SAPT(DFT) LHF         | 0.423 | 0.666            | 0.196 | 0.319 |      |              |     | Ш   |       |      | 1           |    |  |
| SAPT0                 | 0.613 | 1.034            | 0.439 | 0.297 |      | 1111         | П   | Ш   |       | (III |             |    |  |
| SAPT2+                | 0.236 | 0.270            | 0.136 | 0.263 |      |              |     |     |       |      |             |    |  |
| $SAPT2+(3)\delta MP2$ | 0.000 | 0.000            | 0.000 | 0.000 |      |              |     |     |       |      |             |    |  |
| Exchange              |       |                  |       |       |      |              |     |     |       |      |             |    |  |
| SAPT(DFT) hybrid      | 0.886 | 1.127            | 0.426 | 0.926 | - 11 |              | Ш   | П   |       | ļIII |             |    |  |
| SAPT(DFT) LHF         | 0.886 | 1.121            | 0.431 | 0.928 | H.   |              | Ш   |     | 0.00  |      |             |    |  |
| SAPT0                 | 0.675 | 0.942            | 0.263 | 0.658 | 11.1 | 11           |     | П   |       | ļII. |             |    |  |
| SAPT2+                | 0.337 | 0.467            | 0.222 | 0.277 |      |              |     |     |       |      | Ш           |    |  |
| $SAPT2+(3)\delta MP2$ | 0.000 | 0.000            | 0.000 | 0.000 |      |              |     |     |       |      |             |    |  |
| Induction             |       |                  |       |       |      |              |     |     |       |      |             |    |  |
| SAPT(DFT) hybrid      | 0.211 | 0.201            | 0.212 | 0.220 |      |              |     | П   |       |      |             |    |  |
| SAPT(DFT) LHF         | 0.224 | 0.223            | 0.223 | 0.225 |      |              |     | Ш   |       |      |             |    |  |
| SAPT0                 | 0.241 | 0.200            | 0.261 | 0.271 |      |              |     |     |       |      |             |    |  |
| SAPT2+                | 0.327 | 0.384            | 0.250 | 0.318 |      |              | -11 | Ш   | Ш     |      |             |    |  |
| $SAPT2+(3)\delta MP2$ | 0.152 | 0.179            | 0.121 | 0.145 |      |              |     |     |       |      |             |    |  |

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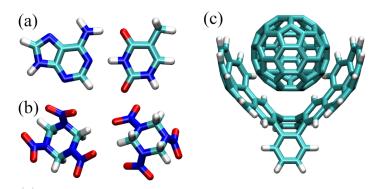
#### S66 Results

| Dispersion                               |       |       |       |       |                                              |
|------------------------------------------|-------|-------|-------|-------|----------------------------------------------|
| SAPT(DFT) hybrid                         | 0.370 | 0.260 | 0.219 | 0.573 | <b>                                    </b>  |
| SAPT(DFT) LHF                            | 0.308 | 0.200 | 0.173 | 0.499 |                                              |
| SAPT(DFT) non-hybrid                     | 0.635 | 0.581 | 0.419 | 0.822 | <b>                                    </b>  |
| SAPT0                                    | 0.443 | 0.862 | 0.162 | 0.195 | <b>                                     </b> |
| SAPT2+                                   | 0.235 | 0.397 | 0.169 | 0.115 | <b>                 </b>                     |
| $SAPT2+(3)\delta MP2$                    | 0.093 | 0.129 | 0.056 | 0.080 |                                              |
| Total                                    |       |       |       |       |                                              |
| SAPT(DFT) hybrid                         | 0.334 | 0.588 | 0.107 | 0.217 |                                              |
| SAPT(DFT) LHF                            | 0.234 | 0.382 | 0.046 | 0.199 | III <b>Bujurj</b> i                          |
| SAPT(DFT) non-hybrid                     | 0.604 | 0.955 | 0.389 | 0.385 | <b>                                    </b>  |
| SAPT0                                    | 0.990 | 1.197 | 0.692 | 0.965 |                                              |
| SAPT2+                                   | 0.230 | 0.235 | 0.138 | 0.280 | i i i                                        |
| $\mathrm{SAPT2}{+}(3)\delta\mathrm{MP2}$ | 0.105 | 0.056 | 0.082 | 0.169 |                                              |

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## **Timing Performance**

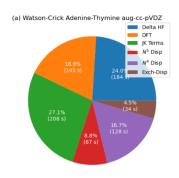


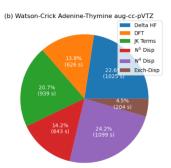
Dimer systems for timing: (a) Watson-Crick adenine-thymine complex, (b) RDX dimer, (c)  $C_{60}$ -buckycather complex.

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### Watson-Crick Adenine-Thymine

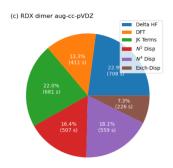


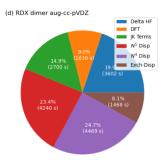


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#### **RDX Dimer**





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## Comparison with LHF Approach

TABLE IV. Wall times (in hours) for SAPT(DFT) computations of RDX dimer/aug-cc-pVTZ with hybrid and LHF algorithm.

| Subroutine               | $\mathbf{Hybrid}$ | LHF     |
|--------------------------|-------------------|---------|
| Delta HF                 | 0.96              | $N/A^a$ |
| DFT                      | 0.45              | 2.29    |
| xc kernel                | 0.08              | 4.17    |
| FDDS object <sup>b</sup> | 2.35              | N/A     |
| Disp time integration    | 0.37              | 3.59    |
| Exch-disp                | 0.41              | 1.99    |
| Total                    | 5.03              | 12.80   |

<sup>&</sup>lt;sup>a</sup> The δHF correction, recommended for SAPT(DFT) computations of polar molecules, is performed by default in Psi4 but not in Molpro.

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b Including integral transformation, form X/form Y (the O(N<sup>5</sup>) part) and QR factorization. In Molpro, the integral transformation is integrated with other terms, and the other steps are not relevant for LHF.



## C<sub>60</sub>-Buckycatcher Complex

- $ightharpoonup N_{bf} = 3012, N_{aux} = 9284$  with aug-cc-pVDZ basis set
- Using Intel i9-10980XE processor with 18 cores, completed entire calculation in 4.03 days
- ▶ 42.7 hours for  $E_{disp}^{(2)}$ ; 20.1 hours for the  $O(N^5)$  subroutines
- ▶ Cost of DFT and  $E_{ind}^{(2)}$  still somewhat significant



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#### 3B-69 Benchmark Set

- Benchmark set for 3-body interaction energies
- 69 trimers extracted from 23 different molecular crystal structures (3 each)
- Used focal point approach to obtain CCSD(T) (and other wavefunction method) energies

$$E = E^{HF}(aQZ) + \Delta E^{MP2}(aTZ/aQZ) + \Delta E^{CCSD(T)}(aDZ)$$

- Assessing accuracy for various wavefunction and DFT methods
- ▶ Recommended MP2.5 and SCS-MI-CCSD, both  $O(N^6)$
- Trying to assess performance of MP2 + FDDS dispersion for 3B-69 systems

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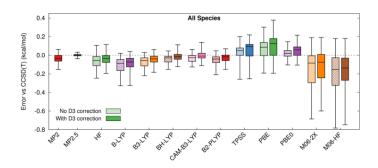
#### 3B-69 Wavefunctional Methods



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#### 3B-69 DFT Methods



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#### New Set from X23

- Sampling trimer geometries from X23 crystal structures
- Trying to include trimer with different intermolecular distances and alignment
- Aiming to serve as a "three-body version" of S22×5/S66×8
- Distance: Geometry mean of 3 pairwise closest contact distance
- Alignment: Angles of the COM triangle; mainly looking at the greatest angle

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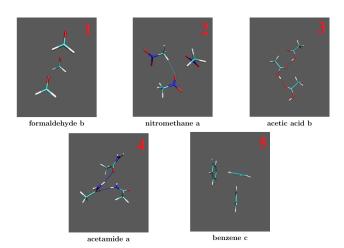
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# 3B-69 Systems



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#### 3B-69 Results

- Total interaction energies in kcal/mol
- FDDS(aDZ) and FDDS(aTZ) correspond to estimated total IE with MP2 + FDDS

| System | CCSD(T) | FDDS(aDZ) | FDDS(aTZ) | MP2    | MP2.5  |
|--------|---------|-----------|-----------|--------|--------|
| 1      | 0.181   | 0.207     | 0.210     | 0.161  | 0.179  |
| 2      | -0.122  | -0.069    | -0.065    | -0.178 | -0.143 |
| 3      | -0.922  | -0.905    | -0.904    | -0.937 | -0.913 |
| 4      | -0.089  | -0.003    | -0.003    | -0.239 | -0.151 |
| 5      | -0.027  | 0.002     | 0.003     | -0.061 | -0.023 |

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#### 3B-69 Results

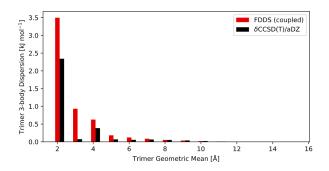
- Estimated 3-body dispersion energies comparison
- CCSD(T) corresponds to dispersion energy estimated by  $E^{CCSD(T)} E^{\mathrm{MP2}}$

| System | CCSD(T) | FDDS(aDZ) | FDDS(aTZ) |
|--------|---------|-----------|-----------|
| 1      | 0.020   | 0.046     | 0.049     |
| 2      | 0.056   | 0.109     | 0.113     |
| 3      | 0.015   | 0.032     | 0.033     |
| 4      | 0.150   | 0.236     | 0.242     |
| 5      | 0.034   | 0.063     | 0.064     |

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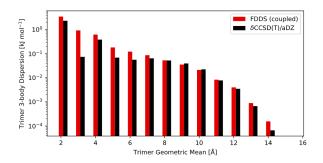
# Distance Dependence



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# Distance Dependence



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