Is an automatic or manual transmission better for MPG?

Executive Summary

Fuel consumption is often an important factor to consider when deciding an economic car to purchase. It has always been recommended that buyers opt for a manual transmission for an improvement in fuel consumption. Is statement justified? A study was done on 32 cars models from 1973 and 1974, 13 of which had manual transmissions with the rest automatic. After controlling for a number of variables such as weight of the car and engine power, it was concluded cars with manual transmission indeed showed a better fuel consumption (+0.5056 miles per gallon) than those with automatic transmission. However, it may not be an important factor of fuel consumption compared to the other variables.

Data

The data was obtained from the datasets R package (documentation). According to the documentation, it was extracted from the 1974 Motor Trend US magazine. It comprised of fuel consumption and 10 aspects of automobile design and performance for 32 automobiles from 1973 and 1974; 13 of them had manual transmission compared to 19 on automatic.

The variables included were: fuel consumption in miles per US gallon (MPG) (mpg), number of cylingers (cyl), iengine displacement in cubic inches (disp), gross housepower(hp), real axle ratio (drat), weight in 1000 pounds (wt), quarter mile time in seconds (qsecs), engine configuration (vs), transmission (am), number of forward gears (gears) and number of carburetors (carb).

Exploratory Data Analysis

The comparison between the fuel consumption of cars with manual and automatic transmission can be easily done through through a boxplot which was shown in the appendix.

It was evident from the boxplots that cars with manual transmission had higher MPG. The ANOVA comparing the fuel consumption against different transmission showed that the cars with manual transmission was associated with **7.2449** increase in MPG. However, such an analysis did not take into account controlling other variables which might have affected MPG, hence the conclusion could not be taken at face value.

The pairs scatterplots in the appendix gave us a brief idea of how some of the continuous variables were related to MPG and each other. It could be observed that mpg appeared to be highly correlated with all the variables except rear axle ratio and transmission, but showed some correlation with those nonetheless.

Analysis

It would be easy to simply include all the variables into a single regression model and obtain the coefficient for the transimission variable for the difference in MPG between manual and automatic cars. However, such a model would be unnecessarily complex, difficult to interprete and include insignificant variables. Nevertheless, it would be a model based on which the subsequent models would be constructed. The p-values of the coefficients of this model were as followed.

##	wt	ammanual	qsec	hp	disp	(Intercept)
##	0.06325	0.23399	0.27394	0.33496	0.46349	0.51812
##	drat	gear	carb	vsIengine	cyl	
##	0.63528	0.66521	0.81218	0.88142	0.91609	

By ranking the p-value of the coefficients in the ascending order, I removed the variables corresponding to the 3 least significant coefficients. The variable for quarter mile time was also removed since it was not a manufacturer specification and, hence, the coefficient would be difficult to interprete.

```
##
   (Intercept)
                          hp
                                        wt
                                               ammanual
                                                                 drat
                                                                              disp
     0.0002817
                   0.0077548
                                0.0166362
                                              0.4710325
                                                           0.5190745
                                                                         0.6052971
##
##
           gear
##
     0.7491696
```

From the table of coefficients of the resulting model, engine power (p-value: 0.654) and car weight (p-value: 0.5191) were the only 2 significant variables. Transmission would also be included since the coefficient of which was of interest.

To ensure that variables were not rejected carelessly, the ANOVA was conducted between the final model and the previous model. With a large p-value (0.857), the final model was not rejected for the alternative model which included 3 more variables. Hence, it was a valid model.

It would also be necessary to check the diagnostic plots to check for the model fit and outliers. From the diagnostic plots in the appendix, the points for Chrysler Imperial, Fiat 128 and Toyota Corolla appeared to be a significant outliers. They were removed from subsequent analysis as they may influence the analysis. The diagnostic plots were more satisfactory after their removal.

Results

The final model and its coefficients were as followed:

Therefore, controlling for engine power and car weight, cars with manual transmission have a better fuel consumption of **0.5056** increase in MPG. The 95% confidence interval for the increase in MPG was (-1.6357, 2.6468). Since the confidence interval contained 0, it meant that the difference in fuel consumption between cars with manual and automatic transmission was not significant. Other factors such as engine power and car weight were more important factors affecting fuel consumption.

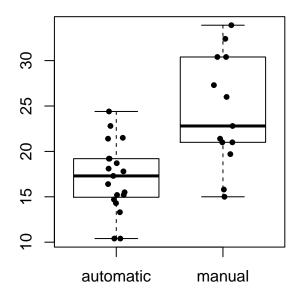
Hence, this study was inconclusive on whether the transmission type affected fuel consumption. Part of the reason was due to the limited dataset of just 32 observations. Perhaps a study conducted on a larger dataset would yield a different conclusion.

Appendix

R codes and outputs were included for reproducibility.

```
data(mtcars)
mtcars2 <- within(mtcars, {
    am <- factor(am, labels = c("automatic", "manual"))
    vs <- factor(vs, labels = c("Vengine", "Iengine"))
})

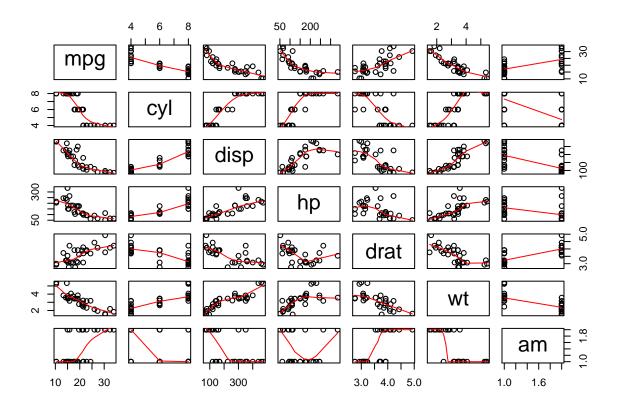
op <- par(mar = c(2,2,1,1))
boxplot(mpg ~ am, data = mtcars2)
stripchart(mpg ~ am, data = mtcars2, vertical = T, method = "jitter", pch = 20, add = T)
par(op)</pre>
```



```
fit1 <- lm(mpg ~ am, data = mtcars2)
coef1 <- summary(fit1)$coef
coef1</pre>
```

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 17.147 1.125 15.247 1.134e-15
## ammanual 7.245 1.764 4.106 2.850e-04
```

```
pairs(mtcars2[, c(1:6,9)], panel = panel.smooth)
```



```
fit2 <- lm(mpg ~ ., data = mtcars2)
summary(fit2)$coef</pre>
```

```
Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 12.30337
                         18.71788 0.6573 0.51812
                          1.04502 -0.1066 0.91609
## cyl
              -0.11144
## disp
               0.01334
                          0.01786 0.7468 0.46349
## hp
              -0.02148
                          0.02177 -0.9868 0.33496
                          1.63537 0.4813 0.63528
## drat
               0.78711
## wt
              -3.71530
                          1.89441 -1.9612 0.06325
## qsec
               0.82104
                          0.73084 1.1234 0.27394
## vsIengine
               0.31776
                          2.10451 0.1510 0.88142
## ammanual
               2.52023
                          2.05665 1.2254 0.23399
## gear
               0.65541
                          1.49326 0.4389 0.66521
## carb
              -0.19942
                          0.82875 -0.2406 0.81218
fit3 <- lm(mpg ~ disp + hp + drat + wt + am + gear, data = mtcars2)
summary(fit3)$coef
```

```
## (Intercept) 28.962452 6.86448 4.2192 0.0002817

## disp 0.006283 0.01200 0.5234 0.6052971

## hp -0.041919 0.01448 -2.8952 0.0077548

## drat 1.006269 1.53861 0.6540 0.5190745

## wt -3.065995 1.19449 -2.5668 0.0166362
```

```
## ammanual
                   1.349766
                                 1.84418 0.7319 0.4710325
## gear
                   0.413313
                                 1.27849 0.3233 0.7491696
fit4 <- lm(mpg \sim hp + wt + am, data = mtcars2)
anova(fit4, fit3)
## Analysis of Variance Table
## Model 1: mpg ~ hp + wt + am
## Model 2: mpg ~ disp + hp + drat + wt + am + gear
      Res.Df RSS Df Sum of Sq
                                      F Pr(>F)
          28 180
## 1
## 2
          25 175 3
                            5.35 0.26
                                           0.86
outliers <- c("Chrysler Imperial", "Fiat 128", "Toyota Corolla")
mtcars3 <- mtcars2[!is.element(rownames(mtcars2), outliers), ]</pre>
fit5 <-lm(mpg \sim hp + wt + am, data = mtcars3)
op \leftarrow par(mfrow = c(2,4), mar = c(4,2,2,1))
plot(fit4)
plot(fit5)
par(op)
      Residuals vs Fitted
                                    Normal Q-Q
                                                              Scale-Location
                                                                                      Residuals vs Leverage
                                                                                         OToyota Corolla
                                                      0.
0
0
                                                                                 0
                                                                                       0000
                                                                                       7
            o
                                                      0.0
   10
             20
                                                         10
                                                                              30
                                                                                             0.2
                                   Theoretical Quantiles
          Fitted values
                                                                Fitted values
                                                                                            Leverage
      Residuals vs Fitted
                                    Normal Q-Q
                                                              Scale-Location
                                                                                      Residuals vs Leverage
          oPontiac Firebird Otus Europ
                                                      1.2
                                                      0.8
                                                               ၀၀၀၀
0
                                                                                       8° 0 ° 8
        000
              φ
                                                      0.4
                  ω°
-2
                                 000
             OAMC Javelin
                                                                                       OCook's distance
    10
              20
                                                         10
                                                               15
                                                                    20
                                                                                        0.1
                                                                                             0.2
                                                                                                  0.3
                                   Theoretical Quantiles
          Fitted values
                                                                Fitted values
                                                                                            Leverage
print(coef5 <- summary(fit5)$coef)</pre>
                  Estimate Std. Error t value Pr(>|t|)
                               2.071991 17.1195 2.556e-15
## (Intercept) 35.47152
                  -0.02802
## hp
                               0.007148 -3.9203 6.079e-04
## wt
                  -3.75030
                               0.712337 -5.2648 1.881e-05
## ammanual
                   0.50558
                             1.039672 0.4863 6.310e-01
print(CI \leftarrow coef5[4, 1] + c(-1, 1) * qt(0.975, df = fit5$df))
```

[1] -1.554 2.565