

Accurate and Efficient Modeling of 802.15.4 Unslotted CSMA/CA through Event Chains Computation

Domenico De Guglielmo, Francesco Restuccia, Giuseppe Anastasi, Marco Conti, and Sajal K. Das

Abstract—Many analytical models have been proposed for evaluating the performance of event-driven 802.15.4 Wireless Sensor Networks (WSNs), in *Non-Beacon Enabled (NBE)* mode. However, existing models do not provide accurate analysis of large-scale WSNs, due to tractability issues and/or simplifying assumptions. In this paper, we propose a new approach called *Event Chains Computation (ECC)* to model the unslotted CSMA/CA algorithm used for channel access in NBE mode. ECC relies on the idea that outcomes of the CSMA/CA algorithm can be represented as *chains of events* that subsequently occur in the network. Although ECC can generate all the possible outcomes, it only considers chains with a probability to occur greater than a pre-defined threshold to reduce complexity. Furthermore, ECC parallelizes the computation by managing different chains through different threads. Our results show that, by an appropriate threshold selection, the time to derive performance metrics can be drastically reduced, with negligible impact on accuracy. We also show that the computation time decreases almost linearly with the number of employed threads. We validate our model through simulations and testbed experiments, and use it to investigate the impact of different parameters on the WSN performance, in terms of delivery ratio, latency, and energy consumption.

Index Terms—Wireless Sensor Networks, IEEE 802.15.4, Non-Beacon Enabled mode, unslotted CSMA/CA, Performance Analysis.



1 INTRODUCTION

The IEEE 802.15.4 standard is currently the reference communication technology for wireless sensor networks (WSNs) [1] and is expected to be a major enabling technology for the future Internet of Things (IoT) [3]. The 802.15.4 standard addresses the physical and medium access control (MAC) layers of the networking stack and is complemented by the ZigBee specifications [2] that cover the network and application layers.

Due to the wide range of potential applications, ranging from environmental monitoring to smart grids, from urban mobility to healthcare, from industrial applications to mobile ticketing and assisted driving, and so on, the 802.15.4 standard leverages a number of different access methods to cope with different quality of service (QoS) requirements. In particular, the standard defines a Beacon-Enabled (BE) mode and a Non-Beacon-Enabled (NBE) mode. The BE mode relies on a periodic superframe bounded by beacons, which are special synchronization messages generated by coordinator nodes. Each sensor node waits for the reception of a beacon, and then, starts transmitting its data packets using a slotted carrier sense multiple access with collision avoidance (CSMA/CA) algorithm. Conversely, in the NBE mode

there is no superframe; nodes are not synchronized, and use an unslotted CSMA/CA algorithm for packet transmissions.

The performance of 802.15.4 WSNs has been thoroughly investigated in the past [6]–[21]. However, most of the previous studies have focused on the BE mode and, hence, they have considered the slotted CSMA/CA algorithm. Although the NBE mode is the most suitable access method for applications generating sporadic and/or irregular traffic (e.g. event-driven WSN applications and upcoming IoT applications), significantly less attention has been devoted to it.

The most challenging aspect in analyzing the 802.15.4 unslotted CSMA/CA algorithm lies in its remarkable complexity, mainly due to its random nature and the multitude of parameters regulating its behavior. Nevertheless, having an accurate (yet tractable) model is imperative to investigate the QoS that can be provided to applications. The majority of previous models of unslotted CSMA/CA algorithm assume that packets are generated according to a specific stochastic distribution (e.g. Poisson). However, this assumption is not valid for WSN applications where nodes generate traffic according to an *event-driven* pattern (e.g. query-based applications, neighbor discovery, data aggregation). Although some works [16], [18] have proposed analytical models of the unslotted CSMA/CA algorithm for event-driven WSNs, literature still lacks models that are both *accurate* and *tractable*. For this reason, in this paper we present a new model of unslotted CSMA/CA, for event-driven WSNs, that is both accurate and tractable. We use it to derive performance metrics of interest such as delivery ratio,

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delay, and energy consumption. In order to deal with the significant complexity of the algorithm, we use an approach called *Event Chains Computation* (ECC).

ECC relies on the idea that *outcomes* of the CSMA/CA algorithm can be represented as a sequence (*chain*) of transmissions (*events*) that subsequently occur in the network. ECC is able to iteratively build all the possible sequences of events that can be experienced by sensor nodes while transmitting a data packet. However, to reduce complexity, only the event chains whose probability to occur is above a predefined threshold are considered. By appropriate selection of the threshold, it is possible to reduce the model complexity and, hence, the computational resources needed to calculate the performance metrics, with a limited loss of accuracy. In addition, it is possible to parallelize the algorithm, which further reduces the computation time.

To summarize, this paper makes the following contributions.

- We introduce the ECC modeling approach that leverages both the analysis of the most likely events and parallel computation, to reduce drastically the model computation time.
- We use ECC to derive performance metrics of interest such as delay, energy consumption, and packet delivery probability.
- We validate our model through simulation and experiments in a real testbed. Also, we analyze the performance of the unslotted 802.15.4 CSMA/CA algorithm as a function of different operating parameters. Our results demonstrate that the ECC approach allows to reduce drastically the computation time, while guaranteeing a good accuracy for the computed performance metrics.

The paper is organized as follows. Section 2 presents related work. Section 3 describes the unslotted 802.15.4 CSMA/CA algorithm. Section 4 presents the model assumptions. Section 5 and 6 detail the ECC algorithm and derive performance metrics. Section 7 presents the obtained results. Finally, Section 8 draws conclusions.

2 RELATED WORK

The 802.15.4 MAC protocol has been thoroughly investigated through analysis [6]-[18], simulations [19], [20] and real experiments [20], [21]. However, most of these studies have focused on the BE mode (i.e., slotted CSMA/CA), while significantly less attention has been devoted to the NBE mode. In this paper, we focus on the latter mode and, hence, on the unslotted CSMA/CA, hereafter referred to as CSMA/CA for brevity.

One of the first models for CSMA/CA was due to Goyal *et al.* [15], who proposed a stochastic model assuming that packet inter-arrival times follow an exponential distribution, and considering the effect of packet retransmissions. More recently, Di Marco *et al.* [13] analyzed the CSMA/CA algorithm in single and multi-hop scenarios, through an accurate model based on Discrete

Time Markov Chains (DTMCs). In [14] the authors improved the work in [13] by proposing an extended model considering the effect of a fading channel.

In [13]-[15] it is assumed that sensor nodes generate data packets according to a Poisson distribution. However, this assumption does not apply to a large number of WSN scenarios where sensor nodes typically follow an *event-driven* reporting paradigm [11]. In this paper, we consider event-driven applications and assume that, when an event is detected, all (or a large number of) sensor nodes in the network start reporting data simultaneously (the event-driven paradigm can be easily extended to model periodic traffic as well). A similar scenario is considered in [11] where the authors provide an accurate model of the 802.15.4 CSMA/CA (that considers both the case with and without retransmissions) and validate it through extensive simulations. We point out that, differently from this paper, [11] focuses on the slotted version of 802.15.4 CSMA/CA and this completely changes the analytical model. In addition, no real experiments are provided to validate the model.

Regarding event-driven WSNs and the unslotted CSMA/CA, the closest to our work are [16]-[18]. In [16] the authors derive the packet latency and delivery ratio experienced by N sensor nodes that attempt to transmit a single packet simultaneously to the sink node. The work was further extended in [17] by taking into account the hidden node problem using the theory of stochastic geometry. However, conversely from us, both [16] and [17] do not consider the effects of acknowledgements and retransmissions. In [18], Gribaudo *et al.* provide a very accurate and complete analytical model of CSMA/CA using stochastic automata networks (SANs) [22]. The analysis is mainly aimed at deriving the packet delay distribution and on-time delivery ratio (percentage of packets received by the sink node within a predefined threshold). As in [16] and [17], the analysis of the energy consumption of sensor nodes is neglected. Furthermore, although the use of SANs makes the analysis very accurate, it also raises serious complexity issues. In fact, the analysis in [18] is limited to WSNs with a low number of nodes (i.e. less than 6). This is because the size of the WSN global descriptor (i.e., a matrix) increases exponentially with the network size. Hence, the computation time and memory needed to solve the model increases accordingly.

Likewise the model proposed in [18], our analysis is very accurate. It considers acknowledgements and retransmissions, and no over-simplifying assumptions are made on the CSMA/CA algorithm. In terms of performance metrics, we derive delivery ratio, packet latency, and energy consumption of sensor nodes. However, our most important contribution is to provide an accurate analytical model of CSMA/CA which is able to analyze WSNs with a large number of nodes. This is because we do *not* use a matrix-based analytical model (like DTMCs or SANs). Instead we undertake an approach called *Event Chains Computation* (ECC), that makes the analysis very

accurate yet computationally tractable. As we will show in Section 6, ECC is scalable and, unlike previous techniques, is particularly suitable for parallelization, due to its intrinsic concurrent structure. This contributes to drastic reduction of computation time. To the best of our knowledge, ours is the first accurate analytical model of the (unslotted) CSMA/CA algorithm for event-driven scenarios investigating the performance of WSNs with a large number of sensor nodes. In addition, we present a comparison of analytical and experimental results.

3 CSMA/CA ALGORITHM

According to the IEEE 802.15.4 standard, in WSNs operating in the NBE mode, sensor nodes must associate with a coordinator node and send their packets to it, using the (unslotted) CSMA/CA algorithm. Unlike regular sensor nodes, coordinator nodes are energy-unconstrained devices that form a higher-level network aimed at forwarding data to the final destination. Specifically, coordinator nodes are always on and, thus, sensor nodes are allowed to start a packet transmission at any time. In addition, no synchronization is required. Below, we provide a short description of the CSMA/CA algorithm used by sensor nodes to transmit data to their coordinator node.

Upon receiving a data packet, the MAC layer at the sensor node performs the following steps.

- 1) A set of state variables is initialized, namely the number of backoff stages carried out for the ongoing transmission ($NB = 0$) and the backoff exponent ($BE = \text{macMinBE}$).
- 2) A random backoff time is generated and used to initialize a timer. The backoff time is obtained by multiplying an integer number uniformly distributed in $[0, 2^{BE-1}]$ by the duration of the backoff-period (D_{bp}). As soon as the timer expires the algorithm moves to step 3.
- 3) A Clear Channel Assessment (CCA) is performed to check the state of the wireless medium.
 - a) If the medium is free, the packet is immediately transmitted.
 - b) If the medium is busy, state variables are updated as follows: $NB = NB+1$ and $BE = \min(BE+1, \text{macMaxBE})$. If the number of backoff stages has exceeded the maximum allowed value (i.e. $NB > \text{macMaxCSMABackoffs}$), the packet is dropped. Otherwise, the algorithm falls back to step 2.

The CSMA/CA algorithm supports an optional retransmission scheme based on acknowledgements and timeouts. When the retransmissions are enabled, the destination node must send an acknowledgement upon receiving a correct data packet. On the sender side, if the acknowledgment is not (correctly) received within a pre-defined timeout, the packet is retransmitted, unless the maximum number of allowed retransmissions ($\text{macMaxFrameRetries}$) has been reached. Otherwise, the packet is dropped.

4 MODEL ASSUMPTIONS

In the following, we focus on the communication between sensor nodes and the coordinator node they are associated with. We assume that there are N nodes associated with the considered coordinator node. We refer to event-driven applications in which *all* sensor nodes start transmitting a data packet simultaneously to their coordinator, to report a detected physical event. This is one of the most challenging scenarios in terms of performance and energy consumption. We assume that each sensor node is in the carrier sensing range of each other and there are no obstacles in the sensing field. This assures that the hidden node problem never arises. In addition, we assume that the time between two consecutive physical events ph_1 and ph_2 is long enough to assure that the execution of the CSMA/CA algorithm, started by sensor nodes to report ph_1 , is surely terminated before ph_2 occurs. Hence, in the following, we focus on a single physical event ph . We indicate as $t = 0$ the time at which ph occurs and, hence, the time at which all the N nodes start executing the CSMA/CA algorithm. Finally, we make the following assumptions:

- Each sensor node transmits a single packet to report the detected event ph .
- Data packets transmitted by different sensor nodes have the same size. In particular, we assume that the packet size is such that the corresponding transmission time can assume a value D_{tx} such that $D_{tx} = D_{max} - k \cdot D_{bp}$, for $k \geq 0$, where D_{max} is the time required to transmit a maximum-size packet (133 bytes) and D_{bp} is the duration of the backoff period.
- The communication channel is ideal, i.e., data/acknowledgement packets are never corrupted, or lost, due to transmission errors.

5 EVENT CHAINS COMPUTATION

The CSMA/CA algorithm is a random access algorithm whose goal is to minimize the probability of collision between packets transmitted by different sensor nodes. Due to its random nature, different executions of the algorithm can yield completely different outcomes. For instance, if we consider N nodes simultaneously transmitting a single data packet to their coordinator node, a run of the algorithm can result in a transmission schedule such that all the N data packets are successfully transmitted to the coordinator (and, hence, 100% reliability is achieved) while another run can result in no successful transmissions at all (e.g. due to repeated collisions). Obviously, different outcomes have, in general, different probabilities to occur.

The ECC algorithm is able to generate all the possible *outcomes* an execution of CSMA/CA algorithm can yield, and the corresponding probabilities. However, to reduce the complexity of the analysis, it is possible to instruct the ECC algorithm to generate only the outcomes having a probability to occur greater than or equal to a certain

threshold θ ($0 \leq \theta < 1$). The set of possible outcomes produced by the algorithm is then used to calculate the performance metrics of interest such as delivery ratio, latency and energy consumption.

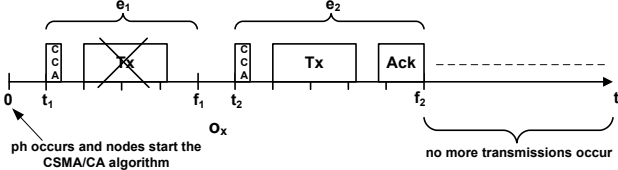


Fig. 1: o_x , a possible outcome of the CSMA/CA.

The ECC algorithm is based on the observation that an outcome of the CSMA/CA execution can always be represented as a series (*chain*) of successful/failure transmissions (*events*) occurring subsequently in the network. Figure 1 shows a possible outcome o_x of the CSMA/CA algorithm representing the case when a transmission failure (time $t = t_1$) followed by a successful transmission (time $t = t_2$) occur. Please note that time $t = 0$ is the time at which all the nodes start the CSMA/CA execution and that, in this specific example, no more transmissions occur in the network after those shown in the figure.

Let us indicate as e_1 and e_2 , respectively, the transmission failure and the successful transmission depicted in Figure 1. Then, the probability of outcome o_x is:

$$\mathbb{P}\{o_x\} = \mathbb{P}\{e_1 \wedge e_2 \wedge no_txs\} \quad (1)$$

where no_txs indicates that no more events (successful/failure transmissions) occur in the network after e_2 .

By recursively applying the Bayes' theorem, eq. 1 can be rewritten as:

$$\begin{aligned} \mathbb{P}\{o_x\} &= \mathbb{P}\{e_1 \wedge e_2 \wedge no_txs\} \\ &= \mathbb{P}\{e_1 \wedge e_2\} \mathbb{P}\{no_txs \mid e_1 \wedge e_2\} \\ &= \mathbb{P}\{e_1\} \mathbb{P}\{e_2 \mid e_1\} \mathbb{P}\{no_txs \mid e_1 \wedge e_2\} \end{aligned} \quad (2)$$

More generally, the probability of an outcome o_i , representing the series of events e_1, e_2, \dots, e_n , can be calculated as follows:

$$\begin{aligned} \mathbb{P}\{o_i\} &= \mathbb{P}\{e_1 \wedge e_2 \wedge \dots \wedge e_n \wedge no_txs\} \\ &= \mathbb{P}\{e_1 \wedge \dots \wedge e_n\} \mathbb{P}\{no_txs \mid e_1 \wedge \dots \wedge e_n\} \\ &= \mathbb{P}\{e_1\} \mathbb{P}\{e_2 \mid e_1\} \mathbb{P}\{e_3 \mid e_1 \wedge e_2\} \cdot \dots \\ &\quad \cdot \mathbb{P}\{no_txs \mid e_1 \wedge \dots \wedge e_n\} \end{aligned} \quad (3)$$

Eq. 3 suggests that, in order to calculate the probability of outcome o_i , $n+1$ different steps have to be performed. First, $\mathbb{P}\{e_1\}$ has to be computed, i.e. the probability that e_1 is the first event occurring in the network. Then, at each subsequent step k , $2 \leq k \leq n$, the probability $\mathbb{P}\{e_k \mid e_1 \wedge \dots \wedge e_{k-1}\}$ that event e_k occurs, given that all the previous $k-1$ events have occurred, has to be derived. Finally, $\mathbb{P}\{no_txs \mid e_1 \wedge \dots \wedge e_n\}$ has to be calculated, i.e. the probability that no other events will occur in the network after e_n . The ECC algorithm follows exactly these $n+1$ steps to compute the probability of an outcome.

Now, by means of a simple example, we give an overview of the actions performed by ECC to generate all the possible outcomes of a CSMA/CA execution and the corresponding probabilities.

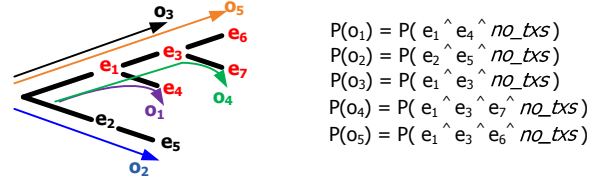


Fig. 2: Possible outcomes of the CSMA/CA.

Figure 2 represents a case where a CSMA/CA execution can produce five possible outcomes, namely o_1, o_2, o_3, o_4, o_5 . Initially (i.e. just after time $t = 0$), two possible events can occur, namely e_1 and e_2 . The ECC algorithm calculates that, with probability $\mathbb{P}\{e_1\}$, e_1 is the first event to occur in the network while, with probability $\mathbb{P}\{e_2\}$, e_2 occurs. Then, the algorithm checks if there are cases in which no other events occur in the network after e_1 or e_2 have occurred, i.e. if there are outcomes of the algorithm composed only of event e_1 or e_2 . To this end, both $\mathbb{P}\{no_txs \mid e_1\}$ and $\mathbb{P}\{no_txs \mid e_2\}$ are calculated. Since in this example there are no outcomes terminating with e_1 or e_2 , both $\mathbb{P}\{no_txs \mid e_1\}$ and $\mathbb{P}\{no_txs \mid e_2\}$ are equal to 0.

ECC then derives the events that can occur after e_1 or e_2 . It discovers that, with probability $\mathbb{P}\{e_3 \mid e_1\}$, e_3 will follow e_1 , while with probability $\mathbb{P}\{e_4 \mid e_1\}$, e_4 will follow e_1 . Also, event e_5 is the only event that can occur in the network after e_2 , i.e. $\mathbb{P}\{e_5 \mid e_2\} = 1$. As before, ECC checks if there are cases in which no other events occur in the network after e_3, e_4 or e_5 by computing $\mathbb{P}\{no_txs \mid e_1 \wedge e_3\}$, $\mathbb{P}\{no_txs \mid e_1 \wedge e_4\}$, $\mathbb{P}\{no_txs \mid e_2 \wedge e_5\}$. It discovers that both $\mathbb{P}\{no_txs \mid e_1 \wedge e_4\}$ and $\mathbb{P}\{no_txs \mid e_2 \wedge e_5\}$ are equal to 1, since no events can occur after e_4 and e_5 , while $0 < \mathbb{P}\{no_txs \mid e_1 \wedge e_3\} < 1$, i.e. there are cases in which no other events occur in the network after e_1 and e_3 . Thus, the algorithm stores three different outcomes namely o_1, o_2, o_3 and the corresponding probabilities $\mathbb{P}\{o_1\}, \mathbb{P}\{o_2\}, \mathbb{P}\{o_3\}$ given by eq. 3.

Since $\mathbb{P}\{no_txs \mid e_1 \wedge e_3\}$ is less than 1, there are also cases in which other events may occur in the network after e_1 and e_3 . Specifically, e_6 occurs with probability $\mathbb{P}\{e_6 \mid e_1 \wedge e_3\}$ while e_7 occurs with probability $\mathbb{P}\{e_7 \mid e_1 \wedge e_3\}$. Also, since no other events can occur after e_6 and e_7 both $\mathbb{P}\{no_txs \mid e_1 \wedge e_3 \wedge e_6\}$ and $\mathbb{P}\{no_txs \mid e_1 \wedge e_3 \wedge e_7\}$ are equal to 1. Hence, the algorithm stores outcomes o_4 and o_5 with $\mathbb{P}\{o_4\}$ and $\mathbb{P}\{o_5\}$ calculated according to eq. 3. Then, it terminates.

As mentioned above, to reduce the complexity of the analysis, the ECC algorithm can generate only outcomes with probability greater than, or equal to, a certain threshold θ ($0 \leq \theta < 1$). In this case, the algorithm stops to analyze a certain sequence of events as soon as it discovers that its probability to occur is lower than θ . For instance, let us assume that $\mathbb{P}\{e_1\} = 0.95$ while $\mathbb{P}\{e_2\} = 0.05$. In case $\theta = 0.1$, the algorithm analyzes only the sequences composed of events highlighted in red in figure 2, i.e. the outcomes starting with event e_1 . This is because, since $\mathbb{P}\{e_2\} = 0.05$, all the outcomes starting with event e_2 will have a probability to occur lower than or equal to $0.05 < \theta$.

The steps performed by the ECC algorithm are reported by the flowchart in Figure 4. Before describing it we define the concept of *event* and *chain of events*.

Definition 1. An *event* $e_i = \{T_i, t_i\}$ represents a transmission occurring in the network, where T_i indicates the type of the event and t_i denotes its starting time. The event type can be either a success ($T_i = S$) or a failure ($T_i = F$). A success occurs whenever a node successfully transmits its packet, while a failure happens when two or more nodes transmit their packets simultaneously and, therefore, a collision occurs. The starting time t_i of an event e_i is defined as the time instant at which the node(s) causing e_i start their CCA. Each event e_i is also associated with a finish time f_i , defined as the first time instant, following e_i , at which a new event can occur, i.e. as the time $t^* > t_i$ such that a (new) successful CCA can be performed.

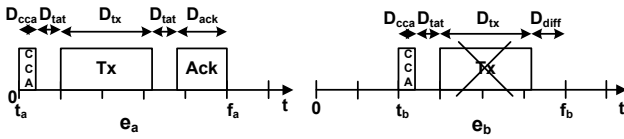


Fig. 3: Events e_a and e_b .

Figure 3 depicts two possible events, i.e., a successful transmission e_a and a transmission failure e_b (time is divided in slots of duration equal to the backoff period, D_{bp}). In Figure 3, D_{cca} is the duration of CCA, D_{tat} is the turnaround time (i.e., the time needed to switch the radio from receive to transmission mode, or vice versa), D_{ack} is the time to transmit/receive an acknowledgement and $D_{diff} = D_{bp} - (D_{tx} \bmod D_{bp})$ is the time between the end of a packet transmission and the beginning of the next slot. In this example, the starting time of event e_a is 0, while the starting time of event e_b is $t_b = 2 \cdot D_{bp}$. Hence, we can refer to e_a as $\{S, 0\}$ and to e_b as $\{F, 2D_{bp}\}$.

Definition 2. A *chain of events* $c = \{s_c, p_c, en_c\}$ represents a sequence of events that occur subsequently in the network. It is characterized by:

- the event sequence $s_c = \{e_1, \dots, e_m\}$, where m denotes the total number of events occurred;
- the aggregate probability $p_c = \mathbb{P}\{e_1 \wedge e_2 \dots \wedge e_m\} = \mathbb{P}\{e_1\}\mathbb{P}\{e_2 | e_1\} \dots \mathbb{P}\{e_m | e_1 \wedge e_2 \dots \wedge e_{m-1}\}$ that the event sequence s_c occurs;
- the average total energy en_c spent by all the nodes in the network during the time interval $[0, f_m]$, where f_m is the finish time of the last event in sequence s_c . \square

Please note that a chain $c : s_c = \{e_1, \dots, e_m\}$ represents a possible outcome of the CSMA/CA execution iff $\mathbb{P}\{no_txs | e_1 \wedge \dots \wedge e_m\} > 0$.

Hereafter, for brevity, we indicate as $\mathbb{P}\{e_x | c\} = \mathbb{P}\{e_x | e_1 \wedge \dots \wedge e_m\}$ the probability that event e_x occurs in the network, given that the sequence of events $s_c = \{e_1, \dots, e_m\}$ has occurred. Also, we denote by $\mathbb{P}\{no_txs | c\} = \mathbb{P}\{no_txs | e_1 \wedge \dots \wedge e_m\}$ the probability that no other events will occur in the network after the sequence represented by chain c .

To derive all the outcomes of the CSMA/CA execu-

tion, and the related probability, ECC follows an iterative approach summarized in Figure 4. Initially, ECC creates two empty sets, namely L_c and F_c . At a given point in time, L_c contains the chains still to be analyzed by the algorithm, while F_c contains chains representing possible outcomes of the CSMA/CA execution. ECC starts analyzing the network at time $t = 0$ and derives all the possible events e_i that can occur just after $t = 0$. For each such event e_i , the chain $c : s_c = \{e_i\}$ is added to set L_c , iff $p_c = \mathbb{P}\{e_i\} \geq \theta$. Then, the ECC algorithm enters a loop that ends when there are no more chains to be analyzed, i.e., $L_c = \{\emptyset\}$. At each iteration, a chain $c : s_c = \{e_1, e_2, \dots, e_m\}$ is extracted from set L_c to be analyzed. First, the algorithm checks if c can be a possible outcome of the CSMA/CA execution, i.e. if $\mathbb{P}\{no_txs | c\} > 0$. If so, the following operations are performed. First, a copy c_x of chain c is created. Second, since no more events have to occur in the network to consider c_x an outcome, the probability of chain c_x is updated as $p_{c_x} = p_c \cdot \mathbb{P}\{no_txs | c\}$. Finally, if $p_{c_x} \geq \theta$, the average energy en_{c_x} spent by the nodes in the network when the events reported by c_x occur is calculated and c_x is added to F_c since it represents an outcome of the CSMA/CA execution with a probability to occur $\geq \theta$.

If $\mathbb{P}\{no_txs | c\} \neq 1$, it means that other events can

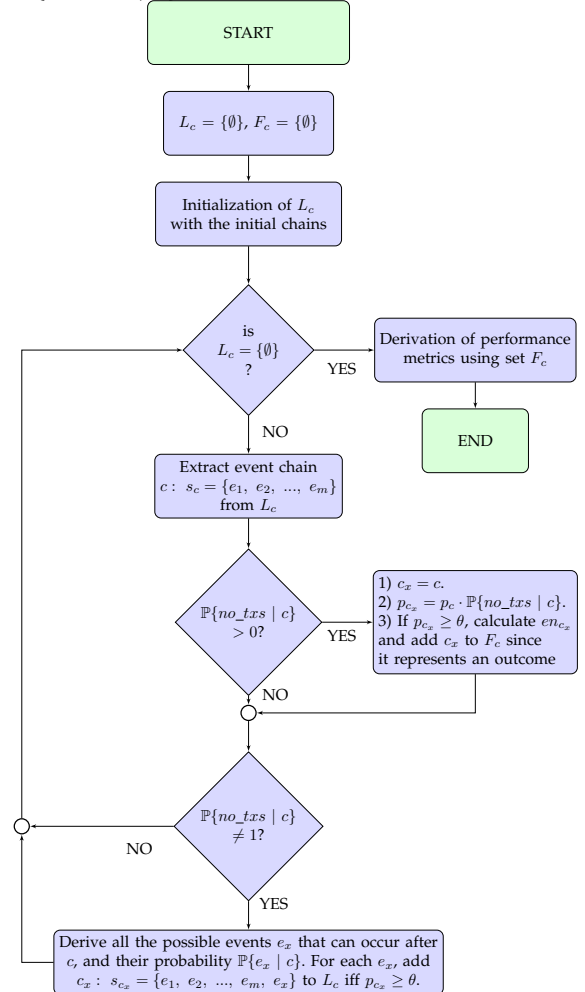


Fig. 4: Steps performed by the ECC algorithm.

occur in the network after those in c . In this case, the algorithm derives all the events e_x (and their probability $\mathbb{P}\{e_x | c\}$) that can occur *after* the last event e_m in chain c . For each such event e_x , the chain $c_x : s_{c_x} = \{e_1, e_2, \dots, e_m, e_x\}$ is added to set L_c , provided that the corresponding probability $p_{c_x} = \mathbb{P}\{e_x | c\} \cdot p_c$ is greater than, or equal to, θ . When the set L_c becomes empty it means that ECC has generated all the possible outcomes having a probability to occur greater than, or equal to, θ . Hence, the ECC algorithm proceeds with deriving the performance metrics of interest, using the chains in set F_c . Then, it terminates its execution.

6 MODEL DERIVATION

Now we detail each single step of the ECC algorithm. After a preliminary analysis in section 6.1, in Section 6.2 we focus on the ECC initialization phase and derive all the possible events that can occur in the network just after time $t = 0$ and the corresponding probabilities. In Section 6.3, we focus on the actions performed by ECC inside the loop (chains examination phase). Finally, in Section 6.4 we show how to parallelize ECC while in Section 6.5 we derive performance metrics of interest.

6.1 Preliminaries

Before proceedings into the details of the ECC algorithm, we derive a general formula for the probability that a sensor node performs a CCA (Clear Channel Assessment) at a given time t . To this end, we first derive the possible time instants at which a sensor node could start a CCA. Next, we compute the probability that it actually performs a CCA in one of these time instants.

As a preliminary step, we need to consider all the actions that may lead a node to start a CCA at a given time t . Let $B_{max} = \text{macMaxCSMABackoffs} + 1$ denote the maximum number of consecutive CCAs allowed for each transmission attempt, and $T_{max} = \text{macMaxFrameRetries} + 1$ be the maximum number of transmission attempts allowed per data packet. In addition, let us indicate by W_i , $1 \leq i \leq B_{max}$, the backoff window size at the i -th backoff stage. For simplicity, hereafter we will use the expression "the sensor node is in state B_{ij} " to indicate that a sensor node is performing a CCA during the i -th backoff stage of the j -th transmission attempt. Now we derive the set Λ_{ij} of all the possible instants at which a sensor node could start a CCA while in state B_{ij} .

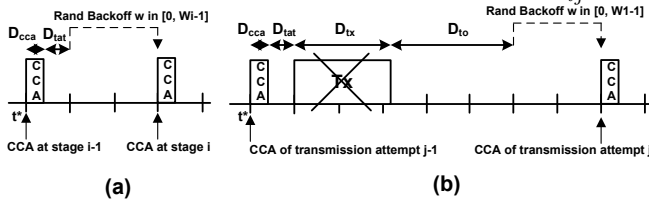


Fig. 5: CCA due to a failed CCA (a) and a failed transmission (b).

According to the CSMA/CA algorithm, at $t = 0$, each sensor node waits for a random number $w \in [0, W_1 - 1]$ of backoff periods and, then, it performs a CCA. Hence,

$\Lambda_{11} = \{0, D_{bp}, \dots, (W_1 - 1) \cdot D_{bp}\}$. Then, a sensor node can start a CCA after one of the two following events: (i) a previous CCA during which the channel was found busy (see Figure 5a), or (ii) an unsuccessful transmission attempt (see Figure 5b). In case (i), the sets Λ_{ij} , $2 \leq i \leq B_{max}$, $1 \leq j \leq T_{max}$, can be recursively derived from Λ_{i-1j} as follows:

$$\Lambda_{ij} = \{t \mid \exists w \in [0, W_i - 1] \wedge \exists t^* \in \Lambda_{i-1j} \wedge t = t^* + D_{cca} + D_{tat} + w \cdot D_{bp}\} \quad (4)$$

Equation 4 derives CCA instants in set Λ_{ij} by considering all the CCA instants $t^* \in \Lambda_{i-1j}$ and all the possible random backoff values $w \in [0, W_i - 1]$ a node can generate when it is in the i -th backoff stage and has found the channel busy.

In case (ii) the sensor node performs a CCA due to a previous unsuccessful transmission attempt and, hence, it is in one of the states B_{1j} , $2 \leq j \leq T_{max}$. Let us denote by $D_{rtx} \triangleq D_{cca} + D_{tat} + D_{tx} + D_{to}$ the total time needed to perform a CCA (D_{cca}), turn the radio in TX mode (D_{tat}), transmit a data packet (D_{tx}), and wait for the timeout (D_{to}). We indicate as R_{ij-1} the set of instants at which a node could perform a CCA after an unsuccessful transmission started at any $t^* \in \Lambda_{ij-1}$, $1 \leq i \leq B_{max}$. It can be expressed as follows.

$$R_{ij-1} = \{t \mid \exists w \in [0, W_1 - 1] \wedge \exists t^* \in \Lambda_{ij-1} \wedge t = t^* + D_{rtx} + w \cdot D_{bp}\} \quad (5)$$

Equation 5 calculates R_{ij-1} considering all time instants $t^* \in \Lambda_{ij-1}$ and all possible backoff values $w \in [0, W_1 - 1]$ the node can generate at the first backoff stage. Since a retransmission can occur during every backoff stage, the set Λ_{1j} , $2 \leq j \leq T_{max}$, is computed as the union of all the sets R_{ij-1} , i.e., $\Lambda_{1j} = \bigcup_{i=1}^{B_{max}} R_{ij-1}$.

Let Ω_{ij}^t denote the set of all time instants t^* at which a node can perform a CCA before performing a CCA at time t during state B_{ij} . The following claim holds.

Claim 1. The set Ω_{ij}^t can be derived as

$$\Omega_{ij}^t = \begin{cases} \{\emptyset\}, & \text{if } i = 1, j = 1 \\ \{t^* \in \Lambda_{i-1j} \mid \exists w \in [0, W_i - 1] \wedge t = t^* + D_{cca} + D_{tat} + w \cdot D_{bp}\}, & \text{if } 2 \leq i \leq B_{max}, 1 \leq j \leq T_{max} \\ \{t^* \in \Lambda_{i'j-1}, 1 \leq i' \leq B_{max} \mid \exists w \in [0, W_1 - 1] : t = t^* + D_{rtx} + w \cdot D_{bp}\}, & \text{if } i = 1, 2 \leq j \leq T_{max} \end{cases} \quad (6)$$

Proof: The set Ω_{11}^t is empty since no CCA can be performed before those occurring at time instants in set Λ_{11} . If $2 \leq i \leq B_{max}$, it means that the node performs a CCA at time t due to a previous failed CCA. In this case, all the CCA instants $t^* \in \Lambda_{i-1j}$ that can result in a CCA at t are selected (second term of Equation 6). In the last case, a CCA at time t is due to a previous unsuccessful transmission. Therefore, the set Ω_{1j}^t , $2 \leq j \leq T_{max}$, is

composed by all the $t^* \in \Lambda_{i'j-1}, 1 \leq i' \leq B_{max}$, which could cause the node to perform a CCA at t due to an unsuccessful transmission (third term of Equation 6). \square

Let us now derive the probability $\mathbb{P}\{\text{CCA}^t\}$ that a sensor node performs a CCA at time t . To this end, we calculate the probability $\mathbb{P}\{\text{CCA}_{ij}^t\}$ that a node performs a CCA at time t while in state B_{ij} and, then, we compute $\mathbb{P}\{\text{CCA}^t\}$ based on $\mathbb{P}\{\text{CCA}_{ij}^t\}$. Let us denote by $\mathbb{P}\{\text{CB}^t\}$ the probability to find the channel busy during a CCA started at time t , and by $\mathbb{P}\{F^t\}$ the probability that a transmission whose CCA started at time t fails. The following claims hold.

Claim 2. *The probability $\mathbb{P}\{\text{CCA}_{ij}^t\}$ that a sensor node performs a CCA at t while in state B_{ij} is*

$$\mathbb{P}\{\text{CCA}_{ij}^t\} = \begin{cases} 0 & \text{if } t \notin \Lambda_{ij} \\ \frac{1}{W_1}, & \text{if } i = 1, j = 1 \\ \sum_{t^* \in \Omega_{ij}^t} \mathbb{P}\{\text{CCA}_{i-1j}^{t^*}\} \cdot \mathbb{P}\{\text{CB}^{t^*}\} \cdot \frac{1}{W_1}, & \text{if } 2 \leq i \leq B_{max}, 1 \leq j \leq T_{max} \\ \sum_{t^* \in \Omega_{ij}^t} \sum_{i'=1}^{B_{max}} \mathbb{P}\{\text{CCA}_{i'j-1}^{t^*}\} \cdot (1 - \mathbb{P}\{\text{CB}^{t^*}\}) \cdot \mathbb{P}\{F^{t^*}\} \cdot \frac{1}{W_1}, & \text{if } i = 1, 2 \leq j \leq T_{max} \end{cases} \quad (7)$$

Proof: See Appendix A. \square

Claim 3. *The probability that a sensor node performs a CCA at a certain time t can be calculated as:*

$$\mathbb{P}\{\text{CCA}^t\} = \sum_{i=1}^{B_{max}} \sum_{j=1}^{T_{max}} \mathbb{P}\{\text{CCA}_{ij}^t\} \quad (8)$$

Proof: $\mathbb{P}\{\text{CCA}^t\}$ is equal to the probability that a sensor node performs a CCA at time t in any state B_{ij} . Therefore, Equation 8 calculates $\mathbb{P}\{\text{CCA}^t\}$ as the sum of $\mathbb{P}\{\text{CCA}_{ij}^t\}, 1 \leq i \leq B_{max}, 1 \leq j \leq T_{max}$. Since events "performing a CCA at time t while in state B_{ab} " and "performing a CCA at time t while in state B_{cd} ", $a \neq c \mid b \neq d$, are always mutually exclusive, it is possible to sum probabilities $\mathbb{P}\{\text{CCA}_{ij}^t\}$. \square

6.2 ECC Initialization

As shown in Figure 4, the first step of the ECC algorithm consists in initializing the set L_c with chains derived from events occurring immediately after $t = 0$. In this section, we will refer to e_{s_i} (e_{f_i}) as the success (failure) event starting at time $i \cdot D_{bp}$, $i \in \mathbb{N}$. Also, we denote by $\mathbb{P}\{e_{s_i}\}$ ($\mathbb{P}\{e_{f_i}\}$) the probability that event e_{s_i} (e_{f_i}) occurs.

According to the CSMA/CA algorithm, at $t = 0$ each sensor node waits for a random number $w \in [0, W_1 - 1]$ of backoff periods and, then, it performs a CCA. Therefore, the first event occurring in the network can be either a success or a failure with starting time in the set $\{0, D_{bp}, 2D_{bp}, \dots, (W_1 - 1) \cdot D_{bp}\}$.

A successful transmission occurs at time $i \cdot D_{bp}$ ($i = 0, \dots, W_1 - 1$) when one node generates a backoff time equal to $i \cdot D_{bp}$, and all the other $N - 1$ nodes extract a backoff time larger than $i \cdot D_{bp}$. Therefore,

$$\mathbb{P}\{e_{s_i}\} = N \cdot \frac{1}{W_1} \cdot \left(\frac{W_1 - i - 1}{W_1} \right)^{N-1} \quad (9)$$

In Equation (9), the term $1/W_1$ is the probability that one node picks up a backoff time equal to $i \cdot D_{bp}$, while the third term gives the probability that all the remaining $N - 1$ nodes generate a backoff time larger than $i \cdot D_{bp}$. Conversely, a failure occurs at time $i \cdot D_{bp}$ when two or more nodes generate the same backoff time $i \cdot D_{bp}$ and, thus, experience a collision. Hence,

$$\mathbb{P}\{e_{f_i}\} = \sum_{k=2}^N \binom{N}{k} \left(\frac{1}{W_1} \right)^k \cdot \left(\frac{W_1 - i - 1}{W_1} \right)^{N-k} \quad (10)$$

The sum in Equation (10) takes into account that more than two nodes may collide. The term inside the sum gives the probability that exactly k nodes randomly pick up a backoff time of $i \cdot D_{bp}$, while $N - k$ nodes choose a backoff value larger than $i \cdot D_{bp}$.

Using Equations (9) and (10), ECC initializes L_c by adding chains c : $s_c = \{e_{s_i}\}$ ($s_c = \{e_{f_i}\}$) and $p_c = \mathbb{P}\{e_{s_i}\}$ ($p_c = \mathbb{P}\{e_{f_i}\}$). Note that a chain is added to L_c iff $p_c \geq \theta$. Then, ECC enters the *chains examination* phase.

6.3 Chains examination

In the chains examination phase, ECC executes a loop during which, at each step, a chain $c \in L_c$ with $s_c : \{e_1, \dots, e_m\}$ is examined. The goal of the examination is twofold. First, the algorithm checks if c represents a possible outcome of the CSMA/CA execution by computing $\mathbb{P}\{no_txs \mid c\}$ and, if so (i.e. $\mathbb{P}\{no_txs \mid c\} > 0$), it adds c to F_c . If $\mathbb{P}\{no_txs \mid c\} \neq 1$ it means that new events may occur after c . Hence, as a second step, all the events that may occur after e_m (i.e. after the last event in c) are derived. Hereafter, for simplicity, we will indicate as e_{s_i} (e_{f_i}) a success (failure) event occurring at time $t_i = f_m + i \cdot D_{bp}$, $i \in \mathbb{N}$, where f_m is the finish time of event e_m and as $\mathbb{P}\{e_{s_i} \mid c\}$ ($\mathbb{P}\{e_{f_i} \mid c\}$) its corresponding probability. For any e_{s_i} (e_{f_i}) a new chain $c_x : s_{c_x} = \{e_1, \dots, e_m, e_{s_i}\}$ ($s_{c_x} = \{e_1, \dots, e_m, e_{f_i}\}$) is added to L_c by the ECC algorithm iff $p_{c_x} = p_c \cdot \mathbb{P}\{e_{s_i} \mid c\}$ ($p_c \cdot \mathbb{P}\{e_{f_i} \mid c\}$) $\geq \theta$.

In the following we will show the computation of both $\mathbb{P}\{no_txs \mid c\}$ and $\mathbb{P}\{e_{s_i} \mid c\}$ ($\mathbb{P}\{e_{f_i} \mid c\}$). However, before deriving them, we perform two preliminary steps. First, we derive $\mathbb{P}\{\text{CCA}^t \mid c\}$, i.e. the probability that a node, that has not experienced a success until f_m , will perform (has performed) a CCA at a certain time $t \geq f_m$ ($t < f_m$), given that the events in c occurred. Second, we compute the exact number of nodes that are still active in the network at time $t = f_m$ (i.e. that have not yet terminated the CSMA/CA execution).

Derivation of $\mathbb{P}\{CCA^t | c\}$

Hereafter, we take into consideration a generic chain $c : s_c = \{e_1, \dots, e_m\}$ and denote by N_s the number of successful transmissions occurred in chain c ($N_s = |\{e_i \in s_c : T_i = S\}|$). Since each sensor node has to transmit just one data packet, at most $N_r = N - N_s$ nodes may be still active in the network after time f_m . Our goal is to derive the probability $\mathbb{P}\{CCA^t | c\}$ that any of the N_r nodes will perform (has performed) a CCA at time t , given that the sequence of events in c occurred.

First of all, we denote by $N_{P_{ij}}, 1 \leq i \leq B_{max}, 1 \leq j \leq T_{max}$, the set of all time instants $t < f_m$ at which it is not possible, for any of the N_r sensor nodes, to have performed a CCA while in state B_{ij} , if the events in c occurred. The derivation of $N_{P_{ij}}$ is shown in Appendix B, due to the sake of space.

Second, we derive, for time instants $t < f_m^1$, the probability $\mathbb{P}\{CB^t | c\}$ for any of the N_r to have found the channel busy during a CCA started at time t . We also derive $\mathbb{P}\{F^t | c\}$, i.e. the probability for any of the same nodes to have experienced a failure for a transmission whose CCA started at time t . Equations 11 and 12 hold.

$$\mathbb{P}\{CB^t | c\} = \begin{cases} 1 & \text{if } \exists e_i \in s_c : t \in [t_i + D_{bp}, f_i) \\ 0 & \text{otherwise} \end{cases} \quad (11)$$

$$\mathbb{P}\{F^t | c\} = \begin{cases} 1 & \text{if } \exists e_i \in s_c : t_i = t \wedge T_i = F \\ 0 & \text{otherwise} \end{cases} \quad (12)$$

The probability that a generic node has found the channel busy during a CCA started at time t only depends on the specific events in chain c . Specifically, $\mathbb{P}\{CB^t | c\} = 1$ if a success or failure event has occurred at time t , and zero otherwise. Similarly, $\mathbb{P}\{F^t | c\} = 1$ if a failure occurred at time $t_i = t$, and zero otherwise.

Finally, we indicate as S_{max} ($S_{max} > f_m$), the largest time instant at which any of the N_r nodes can perform a CCA, given that all the events in c occurred. S_{max} represents the largest instant at which a new event can occur after e_m . The following claim holds.

Claim 4. $S_{max} = f_m + M_w \cdot D_{bp}$, where

$$M_w = \begin{cases} W_{B_{max}} - 1 & T_m = S \\ \max\{W_{B_{max}} - 1, 2 + (W_1 - 1)\} & T_m = F \end{cases} \quad (13)$$

Proof: If $T_m = S$, S_{max} is derived by considering the worst case shown in fig. 6a where a node (node A) performs a CCA at time $t = f_m - D_{bp}$ during its $(B_{max} - 1)$ -th backoff stage, finds the channel busy, and extracts a value for the backoff time equal to $(W_{B_{max}} - 1) \cdot D_{bp}$. Hence, S_{max} is given by $f_m + (W_{B_{max}} - 1) \cdot D_{bp}$. Conversely, if $T_m = F$, two cases must be considered. A node (node A in fig. 6b) may perform a CCA at time $t = f_m - D_{bp}$ during the $(B_{max} - 1)$ -th backoff stage, and extract a backoff time value equal to $(W_{B_{max}} - 1) \cdot D_{bp}$. At the same time, another node (node B in fig. 6b),

1. We assume that both $\mathbb{P}\{CB^t | c\}$ and $\mathbb{P}\{F^t | c\}$ are equal to 0 $\forall t \geq f_m$. This allows to calculate the probability that a node will directly perform a CCA at a time $t \geq f_m$.

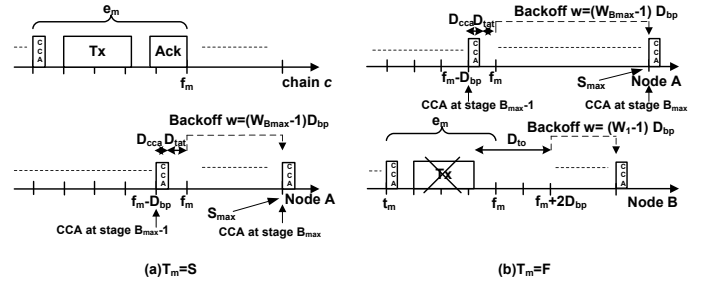


Fig. 6: Derivation of S_{max}

which has experienced the collision represented by e_m , waits for the retransmission timeout D_{to} and extracts a backoff time equal to $(W_1 - 1) \cdot D_{bp}$. Hence, we need to consider the largest value for S_{max} in the two cases, i.e. $S_{max} = f_m + \max((W_{B_{max}} - 1), 2 + (W_1 - 1)) \cdot D_{bp}$. \square

Now, we can show the computation of $\mathbb{P}\{CCA^t | c\}$ for time instants $t \in [0, S_{max}]$. The following claim holds.

Claim 5. The probability $\mathbb{P}\{CCA_{ij}^t | c\}$ that any of the N_r nodes has performed a CCA at time $t \in [0, f_m]$ or will perform a CCA at a time $t \in [f_m, S_{max}]$, while in state B_{ij} , provided that all the events in chain c have occurred, is

$$\begin{cases} 0 & \text{if } t \notin \Lambda_{ij} \vee t \in N_{P_{ij}} \\ \frac{1}{|\Lambda_{11} \setminus N_{P_{11}}|}, & \text{if } i = 1, j = 1 \\ \sum_{t^* \in (\Omega_{ij}^t \setminus N_{P_{i-1,j}})} \mathbb{P}\{CCA_{i-1,j}^{t^*} | c\} \cdot \mathbb{P}\{CB^{t^*} | c\} \cdot \frac{1}{|h_{ij}^{t^*}|}, & \text{if } 1 < i \leq B_{max}, 1 \leq j \leq T_{max} \\ \sum_{i'=1}^{B_{max}} \sum_{t^* \in (\Omega_{i'j}^t \setminus N_{P_{i',j-1}})} \mathbb{P}\{CCA_{i',j-1}^{t^*} | c\} \cdot (1 - \mathbb{P}\{CB^{t^*} | c\}) \cdot \mathbb{P}\{F^{t^*} | c\} \cdot \frac{1}{|h_{i'j}^{t^*}|}, & \text{if } i = 1, 2 \leq j \leq T_{max} \end{cases} \quad (14)$$

Proof: See Appendix C. \square

Finally, we can derive $\mathbb{P}\{CCA^t | c\}$ as follows

$$\mathbb{P}\{CCA^t | c\} = \sum_{i=1}^{B_{max}} \sum_{j=1}^{T_{max}} \mathbb{P}\{CCA_{ij}^t | c\} \quad (15)$$

Estimating the number of active nodes at time $t = f_m$

Since N_s nodes experienced a success during the chain c , at most $N_r = N - N_s$ nodes can be potentially active at time $t = f_m$. Each of these N_r nodes can be in one of the following states at time $t = f_m$: (i) the node has reached the maximum number B_{max} of consecutive CCAs for a data packet transmission; or (ii) the node has reached the maximum number T_{max} of retransmissions for a data packet; (iii) the node is really active, i.e. it has not yet finished the CSMA/CA execution. Indeed, in the first two cases the sensor node drops its data packet, according to the CSMA/CA algorithm and, thus, it is no longer active at time $t = f_m$. To derive the number of sensor nodes that are really active at time $t = f_m$, we need to calculate the probability, for each of the N_r nodes, to be in state (i), (ii) or (iii), respectively. The following claims hold.

Claim 6. Let $\mathbb{P}\{F_{CCA} | c\}$ denote the probability that any of the N_r sensor nodes has exceeded the maximum number

B_{max} of consecutive CCAs allowed for the transmission of a data packet before time $t = f_m$. It is

$$\mathbb{P}\{F_{CCA} | c\} = \sum_{t=0}^{f_m - D_{bp}} \sum_{j=1}^{T_{max}} \mathbb{P}\{CCA_{B_{max}j}^t | c\} \cdot \mathbb{P}\{CB^t | c\} \quad (16)$$

Proof: See Appendix D. \square

Claim 7. Let $\mathbb{P}\{F_{Rtx} | c\}$ denote the probability that any of the N_r sensor nodes has exceeded the number of retransmissions allowed for a data packet before time $t = f_m$. It is

$$\mathbb{P}\{F_{Rtx} | c\} = \sum_{t=0}^{f_m - D_{bp}} \sum_{i=1}^{B_{max}} \mathbb{P}\{CCA_{iT_{max}}^t | c\} \cdot \mathbb{P}\{F^t | c\} \quad (17)$$

Proof: See Appendix E. \square

Claim 8. Let $\mathbb{P}\{A_p | c\}$ denote the probability that any of the N_r nodes: (i) is still active at $t = f_m$ and (ii) it has participated to the last event e_m in chain c , i.e. it has performed a CCA at time $t = t_m$. It is

$$\mathbb{P}\{A_p | c\} = \begin{cases} 0 & T_m = S \\ \sum_{i=1}^{B_{max}} \sum_{j=1}^{T_{max}-1} \mathbb{P}\{CCA_{ij}^{t_m} | c\} & T_m = F \end{cases} \quad (18)$$

Proof: See Appendix F. \square

Claim 9. Let $\mathbb{P}\{A_{np} | c\}$ denote the probability that any of the N_r sensor nodes: (i) is still active at time $t = f_m$, and (ii) it has not participated to the last event e_m in chain c , i.e. it has not performed a CCA at time $t = t_m$. Hence,

$$\mathbb{P}\{A_{np} | c\} = \sum_{t=f_m}^{S_{max}} \mathbb{P}\{CCA^t | c\} - \mathbb{P}\{A_p | c\} \quad (19)$$

Proof: See Appendix G. \square

Let us denote by $\bar{N} = [N_p, N_{np}, N_d]$ a composition of sensor nodes, where (i) N_p indicates the number of nodes that are still active at f_m and have participated to event e_m (i.e. have performed a CCA at time $t = t_m$), (ii) N_{np} is the number of nodes that are still active at f_m but have not participated to e_m (i.e. have not performed a CCA at time $t = t_m$), and (iii) N_d is the number of sensor nodes that have dropped their packet and, hence, are no more active at f_m . By definition, $\forall \bar{N}, \forall c, N_p + N_{np} + N_d = N_r$. We now compute the probability of \bar{N} , $\mathbb{P}\{\bar{N} | c\}$, both when e_m is a success and when it is a failure.

If e_m is a success $T_m = S$, then $\mathbb{P}\{A_p | c\} = 0$. This is because it is not possible for a node to be still active after experiencing a success (each node has a single packet to transmit). Hence, $N_p = 0$, $\forall \bar{N}$, and $\mathbb{P}\{\bar{N} | c\}$ is equal to:

$$\mathbb{P}\{\bar{N} | c\} = \binom{N_r}{N_{np}} \cdot \mathbb{P}\{A_{np} | c\}^{N_{np}} \cdot \mathbb{P}\{D\}^{N_d} \quad (20)$$

In Equation 20 $\mathbb{P}\{D\} = \mathbb{P}\{F_{CCA} | c\} + \mathbb{P}\{F_{Rtx} | c\}$ is the probability that a sensor node has dropped its data packet due to either exceeded number of backoff stages or exceeded number of retransmissions, before f_m . In addition, the second and third terms provide the

probability that exactly N_{np} nodes are still active in the network, and the probability that N_d nodes are no more active, respectively. Obviously, all possible combinations are taken into consideration.

The calculation of \bar{N} for the case $T_m = F$ follows the same line of reasoning and is shown in Appendix H.

Claim 10. The probability $\mathbb{P}\{no_txs | c\}$ that no other events occur in the network after e_m is:

$$\mathbb{P}\{no_txs | c\} = \mathbb{P}\{\bar{N} = [0, 0, N_r] | c\} \quad (21)$$

Proof: The probability $\mathbb{P}\{no_txs | c\}$ that no events occur after e_m , is equal to the probability that all nodes have finished their CSMA/CA execution before f_m , i.e. $\mathbb{P}\{\bar{N} = [0, 0, N_r] | c\}$. \square

Derivation of new events after e_m

When $\mathbb{P}\{no_txs | c\} \neq 1$, it means that there are cases when at least one node is still active at time f_m and, hence, other events may occur in the network. We consider all the events that may occur after e_m and calculate the corresponding probability. To this end, we first derive the probability for an active sensor node to perform a CCA at a time $t \in [f_m, S_{max}]$. We need to discriminate between active nodes that have participated to event e_m , and active nodes that have not participated.

In the former case, after participating to e_m , sensor nodes are in one of the states $B_{1j}, 2 \leq j \leq T_{max}$, i.e. the first backoff stage of a retransmission attempt. Hence, according to CSMA/CA, they will perform a CCA after waiting for both the retransmission timeout D_{to} and a random number $w \in [0, W_1 - 1]$ of backoff periods. Since w is uniformly distributed in $[0, W_1 - 1]$, the probability $\mathbb{P}\{CCA_{1j}^t | c\}$ that any of the considered sensor nodes will perform a CCA at time $t \in [f_m, S_{max}]$ is equal to $\frac{1}{W_1}$ for $t \in [f_m + 2D_{bp}, f_m + 2D_{bp} + (W_1 - 1)D_{bp}]$, and zero otherwise (see also figure 6b).

In the second case, we consider nodes that have not participated to e_m . First, we correct the computation of $\mathbb{P}\{CCA_{1j}^t | c\}$, $2 \leq j \leq T_{max}$, for time instants $t \in [f_m + 2 \cdot D_{bp}, f_m + 2 \cdot D_{bp} + (W_1 - 1) \cdot D_{bp}]$, in equation 14 as

$$\mathbb{P}\{CCA_{1j}^t | c\} = \mathbb{P}\{CCA_{1j}^t | c\} - \sum_{i=1}^{B_{max}} \mathbb{P}\{CCA_{ij-1}^{t_m} | c\} \cdot \frac{1}{W_1} \quad (22)$$

This is to exclude those cases that lead the sensor node to perform a CCA at time t after performing a CCA at time t_m . Thus, $\mathbb{P}\{CCA_{np}^t | c\}$, for $t \in [f_m, S_{max}]$, is:

$$\mathbb{P}\{CCA_{np}^t | c\} = \frac{\mathbb{P}\{CCA^t | c\}}{\mathbb{P}\{A_{np}\}} \quad (23)$$

Equation 23 can be explained as follows. Since we are considering an active sensor node, it will surely perform a CCA at a time $t \geq f_m$. Hence, for such a node, the probability to perform a CCA at a specific time $t \in [f_m, S_{max}]$ can be calculated by normalizing $\mathbb{P}\{CCA^t | c\}$ with probability $\mathbb{P}\{A_{np}\}$, i.e., the probability that the node will perform a CCA at any instant $t \geq f_m$.

Now, we derive both $\mathbb{P}\{e_{s_i} | \bar{N}\}$ and $\mathbb{P}\{e_{f_i} | \bar{N}\}$, $i \in \{0, 1, \dots, M_w\}$ where $\mathbb{P}\{e_{s_i} | \bar{N}\}$ ($\mathbb{P}\{e_{f_i} | \bar{N}\}$) denotes the probability that the first event that occurs after e_m , given the composition of nodes \bar{N} , is a success (failure) occurring at time $t_i = f_m + i \cdot D_{bp}$. Claim 11 holds.

Claim 11.

$$\begin{aligned} \mathbb{P}\{e_{s_i} | \bar{N}\} &= N_{np} \cdot \mathbb{P}\{CCA_{np}^{f_m+i \cdot D_{bp}} | c\} \\ &\cdot \left(\sum_{j=i+1}^{M_w} \mathbb{P}\{CCA_{np}^{f_m+j \cdot D_{bp}} | c\} \right)^{N_{np}-1} \\ &\cdot \left(\sum_{j=i+1}^{M_w} \mathbb{P}\{CCA_p^{f_m+j \cdot D_{bp}} | c\} \right)^{N_p} \\ &+ N_p \cdot \mathbb{P}\{CCA_p^{f_m+i \cdot D_{bp}} | c\} \cdot \\ &\cdot \left(\sum_{j=i+1}^{M_w} \mathbb{P}\{CCA_p^{f_m+j \cdot D_{bp}} | c\} \right)^{N_p-1} \\ &\cdot \left(\sum_{j=i+1}^{M_w} \mathbb{P}\{CCA_{np}^{f_m+j \cdot D_{bp}} | c\} \right)^{N_{np}} \end{aligned}$$

Proof: See Appendix I. \square

Let us focus now on probability $\mathbb{P}\{e_{f_i} | \bar{N}\}$. Since a failure can occur only if $N_{np} + N_p \geq 2$ it follows that $\mathbb{P}\{e_{f_i} | \bar{N}\} = 0$, $\forall i \in [0, M_w]$ if $N_p + N_{np} < 2$. Below, we will focus on cases where $N_p + N_{np} \geq 2$. We denote by $comp(m)$ the set of compositions (m_1, m_2) of an integer m in two distinct parts m_1 and m_2 with $m_1 + m_2 = m$.

Claim 12.

$$\begin{aligned} \mathbb{P}\{e_{f_i} | \bar{N}\} &= \sum_{m=2}^{N_p+N_{np}} \sum_{(m_1, m_2) \in comp(m): m_1 \leq N_p \wedge m_2 \leq N_{np}} \\ &\binom{N_p}{m_1} \cdot \mathbb{P}\{CCA_p^{f_m+i \cdot D_{bp}} | c\}^{m_1} \\ &\cdot \left(\sum_{j=i+1}^{M_w} \mathbb{P}\{CCA_p^{f_m+j \cdot D_{bp}} | c\} \right)^{N_p-m_1} \\ &\cdot \binom{N_{np}}{m_2} \mathbb{P}\{CCA_{np}^{f_m+i \cdot D_{bp}} | c\}^{m_2} \\ &\cdot \left(\sum_{j=i+1}^{M_w} \mathbb{P}\{CCA_{np}^{f_m+j \cdot D_{bp}} | c\} \right)^{N_{np}-m_2} \end{aligned}$$

Proof: See Appendix J. \square

Finally, using the law of total probability, we derive both $\mathbb{P}\{e_{s_i} | c\}$ and $\mathbb{P}\{e_{f_i} | c\}$, $i \in [0, M_w]$ as follows.

$$\mathbb{P}\{e_{s_i} | c\} = \sum_{\bar{N}} \mathbb{P}\{\bar{N} | c\} \cdot \mathbb{P}\{e_{s_i} | \bar{N}\} \quad (24)$$

$$\mathbb{P}\{e_{f_i} | c\} = \sum_{\bar{N}} \mathbb{P}\{\bar{N} | c\} \cdot \mathbb{P}\{e_{f_i} | \bar{N}\} \quad (25)$$

6.4 Parallelization of ECC algorithm

As shown in Figure 4, ECC continuously performs the following steps:

- 1) extracts a chain $c: s_c = \{e_1, e_2, \dots, e_m\}$ from L_c ;
- 2) generates all the events e_x that can occur after e_m .
- 3) $\forall e_x$, adds $c_x: s_{c_x} = \{e_1, e_2, \dots, e_m, e_x\}$ to L_c .

During the execution of the three steps above only information associated with chain c is used by the algorithm. Hence, it is possible to speed-up the execution by allowing more threads to manage different chains in parallel. In section 7 we show, through experimental measurements, that the execution time of the ECC algorithm decreases almost *linearly* with the number of used threads. This drastically reduces the computation time needed to generate all the possible outcomes and makes the analysis of large networks computationally feasible.

6.5 Derivation of performance metrics

When L_c becomes empty, F_c contains all chains c representing possible outcomes of the CSMA/CA execution with a probability to occur greater than, or equal to, θ . By using chains $c \in F_c$, we derive the following metrics:

- **Coverage (C):** portion of event space covered by chains in F_c ; it characterizes the ECC accuracy.
- **Packet delivery ratio (R):** fraction of data packet successfully transmitted to the coordinator node; it measures the reliability provided by CSMA/CA.
- **Packet latency (L):** delay experienced by a sensor node to successfully transmit its data packet to the coordinator node; it indicates the timeliness allowed by CSMA/CA in reporting an event.
- **Energy consumption (E):** average total energy consumed by all sensor nodes in the network to report an event to the coordinator node; it measures the energy efficiency of CSMA/CA.

Let $c_i: s_{c_i} = \{e_1, e_2, \dots, e_m\}$ be a specific chain in set F_c , and p_{c_i} its associated probability. Then, the coverage C can be calculated as follows:

$$C = \sum_{c_i \in F_c} p_{c_i} \quad (26)$$

To derive the delivery ratio R we compute, for each chain c_i , the fraction of successful transmissions R_i occurred in c_i . Since there are N nodes in the network and each node transmits one data packet, R_i can be easily calculated as $R_i = N_s^i / N$ where N_s^i is the number of successful transmissions in c_i . Since each chain c_i has probability p_{c_i} to occur, the delivery ratio R is given by

$$R = \sum_{c_i \in F_c} \frac{p_{c_i}}{C} \cdot R_i \quad (27)$$

To calculate the average latency L we first derive the probability density function (PDF) of packet latency. Specifically, the probability $P(t)$ to successfully receive a data packet with a delay equal to t is

$$P(t) = \sum_{c_i \in F_c: \exists e_j \in s_{c_i} | T_j = S \wedge f_j = t} p_{c_i} \quad (28)$$

$P(t)$ is the sum of the probabilities of all chains c_i containing a successful transmission at t . Then, by denoting as t_{max} the largest instant at which a successful transmission can occur, we compute L as:

$$L = \frac{\sum_{t=0}^{t_{max}} t \cdot P(t)}{\sum_{t=0}^{t_{max}} P(t)} \quad (29)$$

Finally, we calculate the average total energy consumption E . Let en_{c_i} be the total energy consumed by all sensor nodes when the events of chain c_i occur. Hence,

$$E = \sum_{c_i \in F_c} \frac{p_{c_i}}{C} \cdot en_{c_i} \quad (30)$$

The derivation of en_{c_i} is reported in [28].

7 RESULTS

In this section, we evaluate the accuracy and tractability of our analytical model. We also use the model to investigate the performance of CSMA/CA in the considered event-driven scenario. Furthermore, we compare the results obtained using the ECC algorithm with those of the following two analytical models:

- *Tagged node model* [16]. It focuses on a single node of the network (*tagged-node*), and provides delivery ratio, average packet latency and delay distribution. The effects of acknowledgments and retransmissions are not considered.
- *SAN model* [18]. It makes use of stochastic automata networks (SANs) and considers the entire WSNs (i.e. all nodes altogether). It provides delivery ratio, average packet latency and delay distribution but not energy consumption.

These models are the state-of-the-art models for event-driven WSNs using the unslotted 802.15.4 CSMA/CA.

7.1 Model validation

We validate our analytical model through simulations implemented on the ns2 simulation tool [23], which includes the 802.15.4 module. In our simulations we consider a star network topology with sensor nodes located in a circle of radius $10m$ centered at the coordinator node. The transmission range was set to $15m$, while the carrier sensing range was set to $30m$. In all the simulations we assume that the 802.15.4 MAC protocol is operating in NBE mode with a 250 Kbps bit rate. Power consumption values are derived from the Chipcon CC2420 radio transceiver [24]. Unless stated otherwise, we use the following set of CSMA/CA parameter values: $macMinBE = 3$, $macMaxBE = 4$, $macMaxBackoffs = 2$, $macMaxFrameRetries = 1$.

For each simulation experiment, we performed 10 independent replications, each of which consists of 10000 cycles. In each cycle, it is assumed that all sensor nodes have to transmit one packet. We derived confidence intervals by using the independent replications method and a 95% confidence level. However, they are typically very small and cannot be appreciated in the plots below.

Figures 7-9 compare simulation results with the analytical results provided by the ECC algorithm, and the models in [16] and [18], in terms of delivery ratio, average latency and average energy consumption, respectively, for different network sizes (i.e., number of sensor nodes). We anticipate that the graphs also show the results related to the experimental evaluation described in Section 7.4 (*Testbed* label). Finally, Figures 10-12 compare the probability density function (PDF) of packet latency for three different network sizes (i.e. with 5, 30, and 50 sensor nodes). Figure 9 reports the analytical results of ECC only since the other two considered models do not provide the energy consumption. Also, in all the presented graphs, results related to SAN model are only available for networks composed of at most 5 nodes. This is due to the very high complexity of this model (that increases exponentially with the network size) that prevented us to run the analysis with higher network sizes. Finally, we want to point out that the analytical results of ECC have been obtained using $\theta = 0$.

In general, we observe that ECC results and simulation results almost overlap in all the considered scenarios. We studied additional scenarios, with different parameter values, and observed a similar agreement. Some of these results are presented in section 7.3.

Focusing on the Tagged node model [16], we observe a good match between analysis and simulations for small network sizes. Conversely, the gap between analysis and simulations becomes significant with high network sizes. This is because the impact of retransmissions, which was not considered in [16], becomes more apparent as the number of nodes increases (i.e. when the collision probability is high). Specifically, by looking at Figures 10-12 we can observe that the percentage of packets with high delays significantly increases with higher network sizes. However, the Tagged node model is not able to capture at all the contribution of such long-latency packets (since it neglects retransmissions). Finally, we can observe a perfect match between the SAN model results and simulations. However, we remark that the high complexity of the model allows to study only very small networks. Also, we recall that, unlike ECC, the considered models do not provide the energy consumption of nodes, that is a fundamental metric for WSNs.

Figure 7 shows that the delivery ratio drastically reduces with the number of sensor nodes and it is very low even with a limited number of sensor nodes. This is because the 802.15.4 CSMA/CA is not able to manage contention efficiently even when the number of contending nodes is relatively low, due to its random nature. In the considered *event-driven* scenario this limitation is more apparent as *all* sensor nodes in the network start reporting data *simultaneously*, upon detecting an event.

Figures 8 and 9 show that both the average latency and energy consumption increase with the network size, as expected. This is because when the number of sensor nodes contending for channel access increases, the collision probability increases as well. Hence, sensor nodes

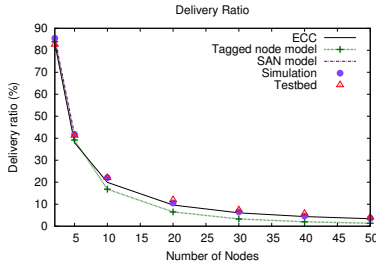


Fig. 7: Delivery Ratio.

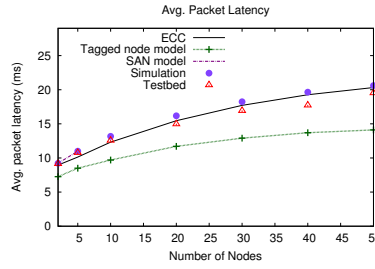


Fig. 8: Average Packet Latency.

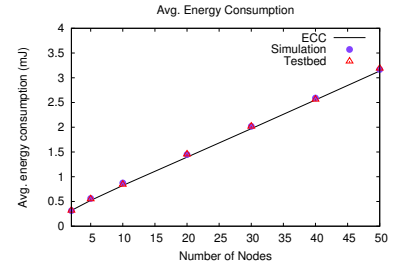


Fig. 9: Average Energy Consumption.

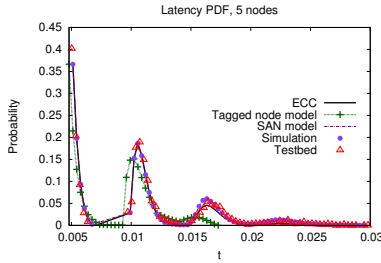


Fig. 10: Latency PDF, 5 nodes.

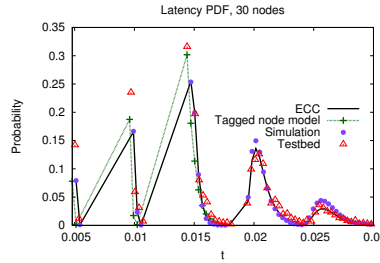


Fig. 11: Latency PDF, 30 nodes.

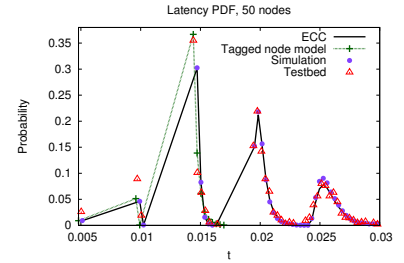


Fig. 12: Latency PDF, 50 nodes.

TABLE 1: Analytical results, R(%), L (ms), E (mJ), Time (s), with different values of θ .

| N | $\theta = 0$ | | | | | | $\theta = 10^{-7}$ | | | | | | $\theta = 10^{-5}$ | | | | | |
|----|--------------|---------|-------|-------|-------|---------|--------------------|--------|-------|-------|-------|---------|--------------------|--------|-------|-------|-------|---------|
| | C | Chains | R | L(ms) | E(mJ) | Time(s) | C | Chains | R | L(ms) | E(mJ) | Time(s) | C | Chains | R | L(ms) | E(mJ) | Time(s) |
| 10 | 1 | 1842355 | 19.94 | 12.33 | 0.822 | 14407 | 0.999 | 27590 | 19.94 | 12.32 | 0.822 | 398 | 0.970 | 3814 | 19.88 | 12.17 | 0.811 | 93 |
| 30 | 1 | 1842355 | 6.07 | 17.81 | 1.970 | 24768 | 0.999 | 19536 | 6.07 | 17.81 | 1.970 | 922 | 0.978 | 3224 | 6.04 | 17.75 | 1.966 | 267 |
| 50 | 1 | 1842355 | 3.40 | 20.36 | 3.130 | 33264 | 0.999 | 11509 | 3.40 | 20.36 | 3.130 | 875 | 0.987 | 2253 | 3.39 | 20.34 | 3.136 | 316 |

consume more energy. In addition, they take more time to transmit their packets. Specifically, successful transmissions tend to occur some time after the beginning, when the level of contention is lower because some nodes have already given up, due to exceeded number of backoff stages or retransmissions (see Section 3). This behavior is confirmed by Figures 10-12, where the highest spikes in the latency PDF shift to the right side of the graphs as the number of sensor nodes increases.

7.2 Impact of θ and multithreading

In order to evaluate the trade-off between *tractability* and *accuracy* of our model, Table 1 summarizes the analytical results obtained with different values of θ (the network parameter values are the same as in Section 7.1). Specifically, Table 1 shows the number of chains generated by the ECC algorithm, the coverage of the event space (C), the performance metrics defined in Section 6.5 (i.e., R , L and E) and, finally, the computation time (in seconds) required to compute the same performance metrics. When using $\theta = 0$, a coverage of 100% and, hence, the maximum accuracy of results is obtained. However, the number of generated chains is very large (more than 1800000), which requires a high computation time (33264s in the case of 50 sensor nodes, i.e. 9 hours).

As expected, the coverage of the event space decreases as the value of θ increases. With $\theta = 10^{-5}$, it reduces to 97 – 98%, however the model still obtains nearly the same accuracy as with $\theta = 0$. Moreover, the computation

time reduces by a factor larger than 100, and the number of generated chains reduces by a factor larger than 500, with respect to $\theta = 0$, when $N = 50$. These results can be explained as follows. As mentioned in Section 6, ECC analyzes only events that are most likely to occur in the network, which are the events that will influence most the performance metrics. This way, ECC achieves approximately the same accuracy as when $\theta = 0$ while analyzing a much lower number of events. Therefore, it saves a tremendous amount of computation time.

Surprisingly, Table 1 shows that, when $\theta > 0$, the number of chains generated by ECC *decreases* as the network size increases. In addition, the coverage *increases* although the number of chains decreases. This apparently counterintuitive behavior can be explained as follows. When the number of sensor nodes increases, some events become significantly more likely to occur than others. For instance, if $N = 50$, collisions are more likely to occur than successful transmissions. Therefore, when $N = 50$, ECC will select, at each step, fewer (yet very likely) events with respect to the case $N = 5$. Hence, the number of considered chains decreases (and the coverage increases), as the number of nodes increases. This property of ECC reduces the computation needed to calculate the metrics of interest when the network size increases, making the analysis of large networks easier.

Finally, to further assess the model tractability, we measured the average computation time of the analytical model as a function of the number of threads that are activated. Figure 13 shows that the computation time

decreases almost *linearly* with the number of threads. This is because the algorithm is implemented in such a way to assign the computation of the various chains to different threads. Since threads synchronize only to modify a global data structure (i.e. the list of chains L_c), each thread is almost independent from the others. Hence, the almost linear decrease of computation time.

7.3 Impact of CSMA/CA parameters

In this section we evaluate the impact of each single CSMA/CA parameter on the overall performance. To this end, we focus on a network with 30 sensor nodes. For the sake of space, we only show the delivery ratio, however, we also derived the average latency and energy consumption (see [28] for the complete set of results). We also report the analytical results obtained by Tagged node model. We do not consider the SAN model due to its high complexity with the considered network size.

In general, we can observe a quite good match between ECC results and simulation results. Conversely, there is a significant gap between simulation results and the Tagged node model results. This is due to the simplifications introduced by this model.

Figure 14 shows that increasing the maximum allowed number of retransmissions (i.e. *macMaxFrameRetries*) does not provide any significant effect on the delivery ratio, for values larger than one. This is because the majority of packets are dropped by the MAC protocol because of exceeded number of backoff stages (i.e., consecutive CCAs). Indeed, increasing the maximum number of backoff stages (i.e. the *macMaxBackoffs*) results in an increase of the delivery ratio, as shown in Figure 15. Furthermore, we also observed an increase in both the average latency and energy consumption. This is because a larger number of packets is successfully transmitted, which takes more time and more energy. Finally, Figure 16 shows that increasing the minimum backoff window size (i.e. *macMinBE*) also causes an increase of the delivery ratio. The motivation is that a larger initial backoff window size reduces the collision probability at the first backoff stage, thus increasing the probability of successful transmission. Again, we observed an increase in the average latency. Instead, the energy consumption decreases since less collisions occur.

The above results show that increasing the CSMA/CA parameter values is beneficial in terms of increased communication reliability. However, it also increases the energy consumption and packet latency, which may not be good for time-critical applications. Hence, the most appropriate parameter setting depends on the specific application scenario.

7.4 Experimental evaluation

To verify the ability of our analytical model to predict the performance of the WSN in a real environment, we implemented the 802.15.4 unslotted CSMA/CA algorithm in the Contiki OS [26]. For experimental measurements

we used a testbed composed of Tmote-sky motes [25]. As in the analysis, all nodes simultaneously start transmitting a data packet to a common coordinator node. We repeat this experiment 1000 times.

We performed different sets of experiments varying the number of nodes in the network (from 2 up to 50) as well as the MAC parameter values. The obtained results are reported in Figures 7-12 and Figures 14-16 (*Testbed* label). In general, we can observe that experimental and ECC results are very close in all the considered scenarios. In some cases we noticed that the performance of the real WSN is slightly better than what predicted by the analysis (e.g. lower latency in experiments with respect to analysis (Figure 8) and higher spikes of PDF in experiments with respect to analysis (Figures 10-12)). We found that this apparently counterintuitive behavior is due to the *capture effect* that occurs in the real testbed, i.e. the ability of the radio to correctly receive a strong signal from one transmitter, despite significant interference from other transmitters [27].

8 CONCLUSIONS

In this paper, we have presented an analytical model of the unslotted CSMA/CA algorithm used in 802.15.4 WSNs operating in NBE mode. The proposed model is both accurate and efficient. It leverages an approach called *Event Chains Computation* (ECC), that reduces complexity, with a limited loss of accuracy, by removing event sequences whose probability to occur is below a given threshold. We have shown that the computation time required for deriving the performance metrics of interest can be reduced by a factor larger than 100, or more, with a negligible impact on the accuracy of the obtained results. Also, our model can exploit a multi-threading approach, thus taking advantage of a parallel execution. Our model allows an accurate analysis of 802.15.4 WSNs in NBE mode, even when there is a large number of sensor nodes. As a matter of fact, we have used our model to investigate the impact of different CSMA/CA parameters on the WSN performance. We have observed that, in the considered scenario, the delivery ratio is very low even when the number of contending nodes is relatively low. It can be improved by increasing the initial backoff-window size and/or the maximum number of backoff stages allowed for each packet. However, this also increases the energy consumption and packet latency.

9 ACKNOWLEDGMENTS

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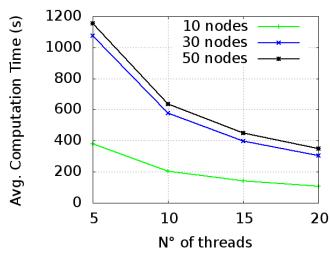


Fig. 13: Avg. computation time vs. number of threads.

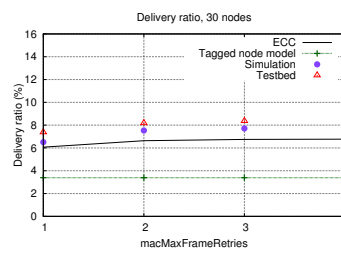


Fig. 14: Delivery ratio vs. *macMaxFrameRetries*

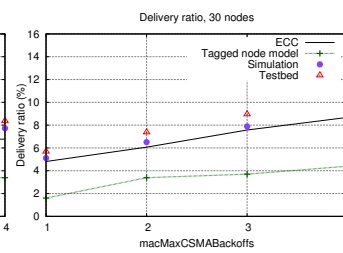


Fig. 15: Delivery ratio vs. *macMaxCSMABackoffs*

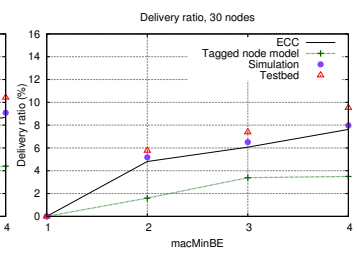


Fig. 16: Delivery ratio vs. *macMinBE*

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