

HW due today!

Sequence: list of #'s!

Alfred: 1, 4, 3, 14, 5.9 \leftarrow no pattern

Jay: 2, 5, 7, 13, 15 \leftarrow

Italian dude: 1, 1, 2, 3, 5, 8, 13, 21, 34

recursive formula

init. values

$a_1 = 1$
 $a_2 = 1$

2 things needed

- (1) the formula itself.
- (2) a starting pt.

\uparrow
"initial value"

next #

=

current #

+

previous #

recursive
formula

$$a_{n+1} = a_n + a_{n-1}$$

Example -

Create a seq by

$$x_{n+1} = (1 + x_n^2)(1 - x_{n-1}^2)$$

where $x_1 = 0$ Find x_3, x_4, x_5

$$x_2 = 1$$

$$\begin{aligned} x_3 &= (1 + x_2^2)(1 - x_1^2) \\ &= 2 \cdot 1 = 2 \\ x_4 &= (1 + x_3^2)(1 - x_2^2) \\ &= 0 \\ x_5 &= (1 + x_4^2)(1 - x_3^2) \\ &= 1(-3) = -3 \end{aligned}$$

Lucas #'s

$$L_1 = 2 \quad L_{n+1} = L_n + L_{n-1}$$

$$L_2 = 1 \quad 2, 1, 3, 4, 7, 11, 18, 29,$$

Fibonacci
#'s : 1, 1, 2, 3, 5, 8, 13, 21, ...

$$f_1 = 1$$

$$f_2 = 1$$

← init
values

$$f_{n+1} = f_n + f_{n-1}$$

$$(Q_n) = \frac{f_{n+1}}{f_n}$$

What is

$$Q_1 = \frac{f_{1+1}}{f_1} = \frac{f_2}{f_1} = \left(\frac{1}{1} \right)$$

$$Q_2 = \frac{f_3}{f_2} = \left(\frac{2}{1} \right)$$

$$q_3 = \left(\frac{3}{2} \right)$$

$$q_4 =$$

$$q_5 =$$

