ALGEBRA 2 HONORS PROBLEM SET 03

DUE DATE: JANUARY 29, 2024

Question 1. Use partial fraction decomposition to decompose the fractions

$$\frac{4x-2}{x^2+2x-8}$$
, and $\frac{7x-5}{x^2-4x-5}$

Definition. A function f is called

- even if f(-x) = f(x) for every x in Dom(f)
- odd if f(-x) = -f(x) for every x in Dom(f).

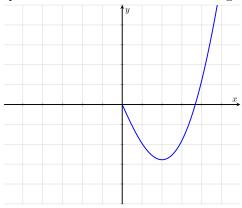
Odd functions are "symmetric about the origin" while even functions are "symmetric about the y-axis.

Question 2. Let f be an odd function and that 0 is in the domain of f. Prove that f(0) = 0. Hint: use the definition of odd function.

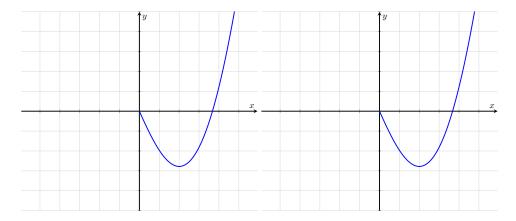
Question 3. Identify which of the functions are even, odd, or neither.

function	Even? Odd? Neither?
f(x) = 3	
g(x) = 5x + 3	
$h(x) = \sqrt{x}$	
$k(x) = x^2$	
$j(x) = x^2 + 2x + 1$	
$p(x) = x^3$	
$q(x) = \frac{1}{x}$	

Question 4. Consider the following function which is drawn below:



- (1) Complete the drawing assuming that f(x) is an even function.
- (2) Complete the drawing assuming that f(x) is an odd function.



Question 5. Let
$$f(x) = \frac{x+1}{x-1}$$
.

- (a) Find the inverse of f(x), i.e. find formula for $f^{-1}(x)$ (b) Compute the composition $(f\circ f^{-1})(x)$

Question 6. Identify which of the functions have inverses, and compute the inverse.

function	invertible?	(Y/N)	inverse, if any
f(x) = 3			
g(x) = 5x + 3			
$h(x) = \sqrt{2x+1}$			
$k(x) = x^2$			
$p(x) = (x-1)^3$			

3

Question 7. Let f(x) = 2x + 5.

- (a) Find the inverse of f(x), i.e. find formula for $f^{-1}(x)$
- (b) Compute the composition $(f \circ f)(x)$
- (c) Compute the composition $(f \circ f^{-1})(x)$

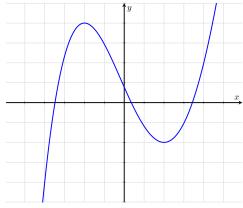
Question 8. Let f be the function given by the table

$$\begin{array}{c|cc} x & f(x) \\ \hline 1 & 3 \\ 2 & 1 \\ 3 & 4 \\ 4 & 2 \\ \end{array}$$

- (a) Is f invertible? If so, write a table for the inverse of f(x) (reverse your inputs with your outputs)
- (b) Compute the compositions

$$(f \circ f)(1), \quad (f \circ f \circ f)(1) \quad (f \circ f \circ f \circ f)(1)$$

Question 9. Consider the following function which is drawn below:



Does this function have an inverse? Why or why not?