

11/13/2023:

Polynomials

• constants

x^0

• lines

x^1

• quadratics

$x^2 \leftarrow \text{deg } 2$

• cubic

$x^3 \leftarrow \text{deg } 3$

• quartic

x^4

• quintic

x^5

• sextic

x^6

x^7

\vdots

x^n

$a \neq$

"degree"

$a \geq 0$

✓

$$(2)x^{2023} - \pi x^7 + 2$$

degree = 2023

BIGGEST exponent on x 's

$n = \text{degree}$

if n is even



both up or
both down

if n is odd

one up
one down

"leading coefficient"

$a < 0$

$a > 0$

$$f(x) = \underline{3x^{15}} - 7x^{10} + 23$$

deg
15

leading
coeff
3

$$g(x) = -20x + 17x^2 - \underline{1x^3}$$

~~not a polynomial if~~

x in

denominator

in the exponent

$$3 + \sqrt{x^3}$$

$\frac{1}{x}$
 2^x
not a poly

FAILURES

$$x^2 + \sqrt{x^3}$$

← not a poly

$$f(x) = 2 + 3x^2 - 5x^4$$

$$g(x) = 1 - 2x^2 + x^3 - 10x^4$$

Find $f(x) + g(x)$

$$= \boxed{3 + 1x^2 + 1x^3 - 15x^4}$$

$f(x) - g(x)$

$$\begin{array}{r} 2 + 3x^2 - 5x^4 \\ - [1 - 2x^2 + x^3 - 10x^4] \end{array}$$

$$1 + 5x^2 - 1x^3 + 5x^4$$