

ALGEBRA 2 HONORS
PROBLEM SET #10

DUE DATE: SEPTEMBER 28, 2023

Question 1. Compute the resulting matrix:

$$(a) \begin{bmatrix} 1 & 2 & 3 \\ 3 & -1 & 7 \end{bmatrix} + 2 \begin{bmatrix} 0 & -1 & 3 \\ 2 & 3 & 1 \end{bmatrix} =$$

$$(b) \begin{bmatrix} 2 \\ 0 \end{bmatrix} \begin{bmatrix} 2 & 3 \end{bmatrix} =$$

$$(c) \begin{bmatrix} 2 & 0 \end{bmatrix} \begin{bmatrix} 2 \\ 3 \end{bmatrix} =$$

$$(d) \begin{bmatrix} 1 & 2 & 3 \\ 4 & 0 & -1 \end{bmatrix} \begin{bmatrix} 3 & -1 \\ 2 & 0 \\ 0 & 1 \end{bmatrix} =$$

Question 2. Solve for the solutions of x, y, z, w from the equations

$$\begin{cases} x + y + z + w = 13 \\ 2x + y + z + w = 18 \\ x + 2y + z + w = 16 \\ w = 4 \end{cases}$$

(use the three rules to get to $\left[\begin{array}{cccc|c} 1 & 0 & 0 & 0 & a \\ 0 & 1 & 0 & 0 & b \\ 0 & 0 & 1 & 0 & c \\ 0 & 0 & 0 & 1 & d \end{array} \right]$.)

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Question 3. Use **Cramer's rule** to solve the system of equations

$$12x - 3y = 5$$

$$15x + 2y = 10$$

Question 4. Let $A = \begin{bmatrix} 1 & 2023 \\ 0 & 1 \end{bmatrix}$ and let $B = \begin{bmatrix} 1 & -2023 \\ 0 & 1 \end{bmatrix}$.

- (a) Compute AB .
- (b) Compute BA .
- (c) What can you conclude about B ?