

Project Proposal

Alexey Yermakov
Logan Barnhart
Tyler Jensen

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Introductory Material

We have decided to work on Project 3: Regularization in Least Squares. The introductory material for this project includes matrices, unitary matrices, matrix operations, data fitting, and least squares. We will also elaborate on why least squares is useful in the context of noise and data.

Distribution of Work

For the independent part of the project we plan to extend the notion of discrete least squares regularization to regularized continuous least squares.

In order to meet the project's requirements of having everyone work on each of:

- Researching
- Writing
- Coding
- Presentation

we will assign work in the following way:

Ridge Regression

- 2.1.1: Deriving the Ridge Estimator - Alexey (Research)
- 2.1.2: Exploring the Ridge Estimator - Tyler (Coding)

Tikhonov Regularization

- 2.2.1: Show that \mathbf{D} is unitary - Tyler (Research)
- 2.2.2: Tikhonov regularization - Logan (Research)
- 2.2.3: Tikhonov modeling - Logan (Coding)
- 2.2.4: Other finite difference method - Alexey (Coding)

Independent Extension

For the independent extension we'll explore LASSO and elastic net for the least squares regularization. Whereas we traditionally we can write the least squares problem as:

$$\|y - X\beta\|_2^2 + \lambda_2 \|\beta\|_2^2$$

The LASSO method is similar, except the regularization term has an L1 norm:

$$\|y - X\beta\|_2^2 + \lambda_1 \|\beta\|_1$$

The elastic net method combines the previous two methods by having both regularization terms in summation:

$$\|y - X\beta\|_2^2 + \lambda_1 \|\beta\|_1 + \lambda_2 \|\beta\|_2^2$$

We'll explore these methods by doing the following:

- 3.1
- 3.2
- 3.3

Seeing as how this is a group project, the above assignments aren't strict and group members are encouraged to collaborate with one another.

Milestones

Given the distribution of work above, we have set the following milestones for our project:

- Finish **Ridge Regression**: November 5
- Finish **Tikhonov Regularization**: November 15
- Finish **Independent Extension** December 14

Deadlines

The various deadlines we have are:

- 2-page proposal (October 29)
- Rough draft (November 15)
- Final draft (December 14)
- Presentation (December 14)