

# Atmospheric Neutrino Oscillation in Super-K

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## I. Neutrino Oscillation

Four types of neutrino sources are classified as solar neutrino, atmospheric neutrino, accelerator neutrino, and reactor neutrino. Besides, these neutrino sources are investigated in different experimental facilities. As the aforementioned, the first affiliated neutrino observatory is SNO (Sudbury Neutrino Observatory) in Canada; the second representative neutrino observatory is Super-K (Super Kamiokande) in Japan; the third corresponding observatories are KEK-SuperK (Japan), T2K(Japan), etc; the last observatories representing are KamLAND, Daya bay (China), etc. In this final report, we are going to present and elaborate on atmospheric neutrino oscillation in Super-K.

### i. Neutrino Oscillation

Neutrino oscillation is a phenomenon that describes the flavor of neutrino oscillating among three different flavors. In general, the “flavor eigenstates” are related to the “mass eigenstates” of the” with  $3 \times 3$  unitary mixing matrix:

$$|\nu_\alpha\rangle = \sum_i U_{\alpha i} |\nu_i\rangle$$

The matrix  $U$  is the PMNS matrix (Pontecorvo-Maki-Nakagawa-Sakata matrix: mixing flavor eigenstates of leptons);  $\nu_\alpha$  is the mass eigenstate and  $\nu_i$  is the flavor eigenstate. Thus, we need the PMNS matrix in order to find the relation be-

tween eigenspaces. The PMNS matrix is [1] [2]:

$$U_{\alpha i} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

where  $\alpha = e, \mu, \tau; i = 1, 2, 3$ ;  $c_{ab}$  and  $s_{ab}$  means  $\sin$  and  $\cos$  with mixing angle  $\theta_{ab}$ ;  $\delta$  means CP-violating phase (s.t. second term of the matrix is small). The first term of the matrix is corresponding to “solar mixing”, the second term of the matrix is known to be small, and the third term of the matrix describes “atmospheric mixing”.

The experiment of testing the neutrino oscillation needs a distance  $L$  to investigate. We, thence, need to consider the state propagating. For mass eigenstate

$$|\nu_j(t)\rangle = e^{-i(E_j t - \vec{p}_j \cdot \vec{x})} |\nu_j(0)\rangle$$

take ultrarelativistic limit  $|\vec{p}_j| \gg m_j$  and also drop out the relative phase. When  $t \approx L$ : [2]

$$|\nu_j(L)\rangle = e^{-i(\frac{m_j^2 L}{2E})} |\nu_j(0)\rangle$$

In the wake of knowing the propagation of the mass eigenstate, we want to know the “interference” between the flavor eigenstate. Therefore, suppose the initial lepton with the flavor eigenstate  $\alpha$  and what is the probability if we observe

$\beta$  when  $t \approx L$  [1]

$$\begin{aligned}
 P_{\alpha \rightarrow \beta} &= |\langle \nu_{\beta} | \nu_{\alpha} \rangle|^2 \\
 &= \left| \sum_j U_{\alpha j}^* U_{\beta j} e^{-i(\frac{m_j^2 L}{2E})} \right|^2 \\
 &\quad \text{drop out } \mathbb{I}m \\
 &\Rightarrow \delta_{\alpha\beta} - 4 \sum_{j>i} \mathbb{R}e \left\{ U_{\alpha i}^* U_{\beta j} U_{\alpha k} U_{\beta k}^* \right\} \\
 &\quad \times \sin^2 \left( \frac{\Delta_{jk} m^2 L}{4E} \right)
 \end{aligned}$$

ii. *One mass scale domination approximation*

## II. Super Kamiokonde

## III. Results

In reality, the source usage rate depends on distance, constructed a concentric structure, for ex-

ample, Beijing (Figure), Chicago, etc. Here, our artificially built city will likewise develop around the center of sources; thus, we adopt the concentric zone model to discuss the hierarchy distribution.

## IV. Outlook

### References

- [1] J. Hosaka et al. Physical Review D (2006)
- [2] Wikipedia Contributors, Neutrino oscillation, Wikipedia (2022).