## **Data Structures**

CSCI 2270-202: REC 11

Sanskar Katiyar

### Logistics

#### Office Hours (This week)

Today: 5 pm - 7 pm

Friday: 3 pm - 5 pm

#### **Assignment 7 Concerns**

Interview grading opportunity

#### No notes on Assignment 8, 9

Most stuff covered in recitation, Check Github

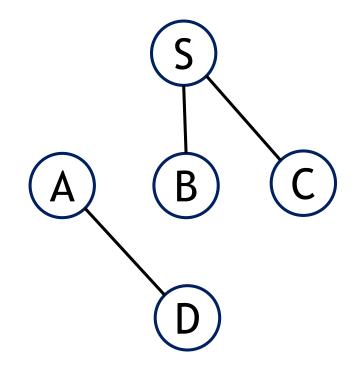
#### **Recitation Outline**

- 1. Implementing Graph: Add/Remove, Display
- 2. BFS, DFS: Review
- 3. Dijkstra's Shortest Path Algorithm
- 4. Exercise

# BFS, DFS: Review

## **DFS:** Pseudocode (Recursive)

```
DFS(G, u) {
    u.visited = true
    for each v \in G.Adj[u]
        if v.visited == false
             DFS(G, v)
for each u \in G
    u.visited = false
for each u \in G
    if u.visited == false
        DFS(G, u)
```



Initialize all nodes as unvisited

Loop: If there is more than one component

#### **BFS**: Pseudocode (Iterative)

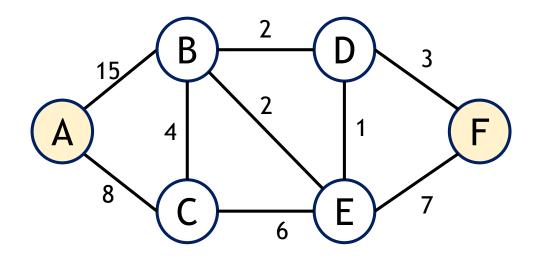
```
BFS(G, u) {
  Q = Queue()
 Q.enqueue(u)
  u.visited = true
  while !Q.isEmpty()
    v = Q.peek(); Q.dequeue();
    for each w \in G[v]
      if w.visited == false
        Q.enqueue(w)
        w.visited = true
```

### **DFS:** Finding Number of Components

```
DFS(G, u) {
     u.visited = true
    for each v \in G.Adj[u]
         if v.visited == false
              DFS(G, v)
                                         #components++;
for each u \in G
                                           Initialize all nodes as unvisited
     u.visited = false
for each u \in G
     if u.visited == false
                                           Loop: If there is more than one component
         DFS(G, u)
```

## Dijkstra's Shortest Path

#### Breadth First Search: Shortest Path



#### **BFS: Shortest Path**

Path with the smallest number of edges (agnostic to edge weight)

Assume Edge weights are distances between two vertices

#### Shortest Path from A->F

### Dijkstra's Shortest Path Algorithm

Edsger W. Dijkstra (in 1956)

**Greedy Algorithm** 

Single-source shortest paths to all reachable vertices

Applicable to Weighted Graphs

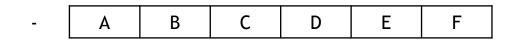
Applications: Network Routing Protocols, Path Planning (Potential Field Methods), Al

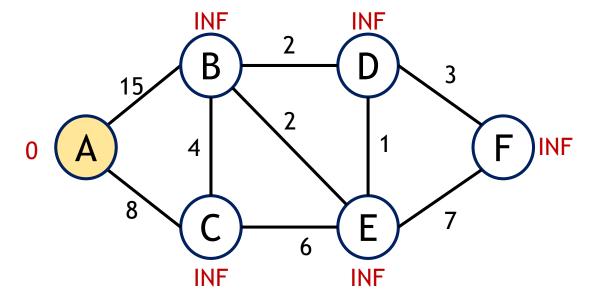
### Dijkstra's Shortest Path: Steps

- 1. From the source vertex, visit the vertex u with the least known distance
- 2. Once at the vertex u, check each of u's neighbors
- 3. Calculate the distance for the neighbors by summing the cost of the edges leading from the source vertex
- 4. If the distance is less than a known distance, update the shortest distance for that vertex; mark the node from which the edge emanates as the predecessor

|      | Α | В   | С   | D   | E   | F   |
|------|---|-----|-----|-----|-----|-----|
| DIST | 0 | INF | INF | INF | INF | INF |
| PREV | ı | -   | -   | ı   | ı   | -   |

Initialize the distance of all nodes from A as INF; Populate Queue/Array with all vertices





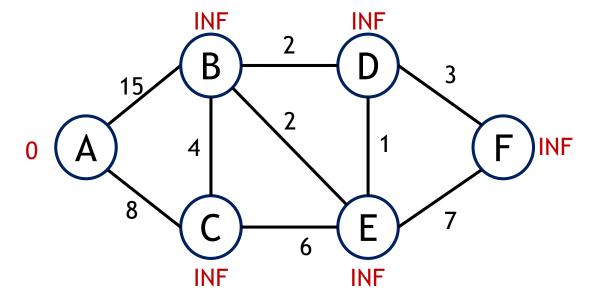
Source's distance to itself is 0

Why INF?

Think about non-reachable nodes, and comparison limits

|      | Α | В   | С   | D   | E   | F   |
|------|---|-----|-----|-----|-----|-----|
| DIST | 0 | INF | INF | INF | INF | INF |
| PREV | - | -   | -   | -   | •   | 1   |

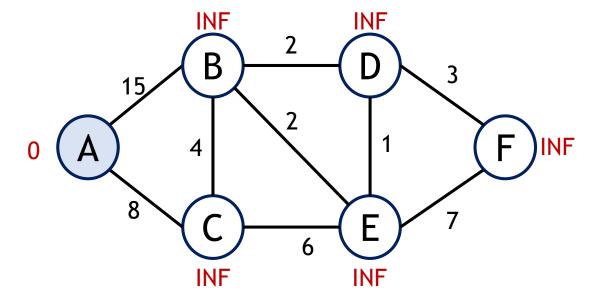




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | Α | В   | С   | D   | E   | F   |
|------|---|-----|-----|-----|-----|-----|
| DIST | 0 | INF | INF | INF | INF | INF |
| PREV | - | -   | -   | -   | •   | 1   |

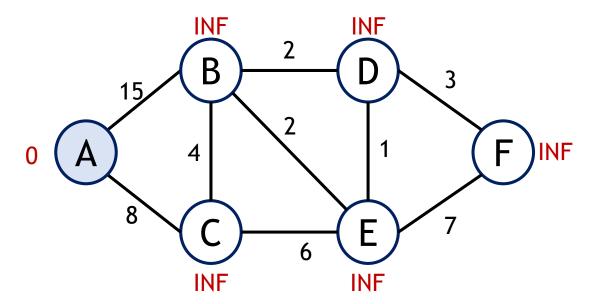




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST) 
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | В   | С   | D   | E   | F   |
|------|----|-----|-----|-----|-----|-----|
| DIST | 0  | INF | INF | INF | INF | INF |
| PREV | -  | -   | -   | -   | -   | -   |

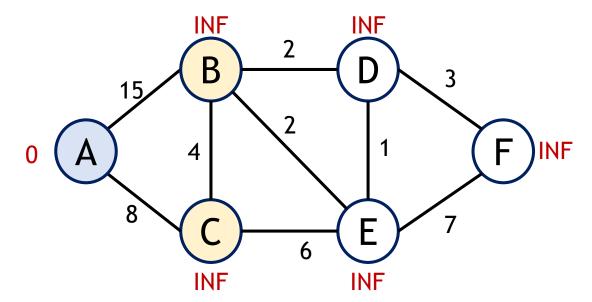
| A B C | D | Е | F |  |
|-------|---|---|---|--|
|-------|---|---|---|--|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | В   | С   | D   | E   | F   |
|------|----|-----|-----|-----|-----|-----|
| DIST | 0  | INF | INF | INF | INF | INF |
| PREV | -  | -   | -   | 1   | -   | -   |

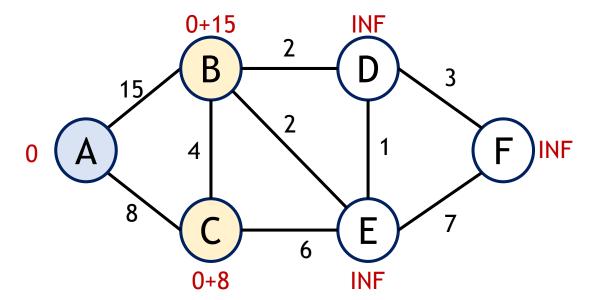
| A B C D E F |  |
|-------------|--|
|-------------|--|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
            DIST[v] = T
            PREV[v] = u</pre>
```

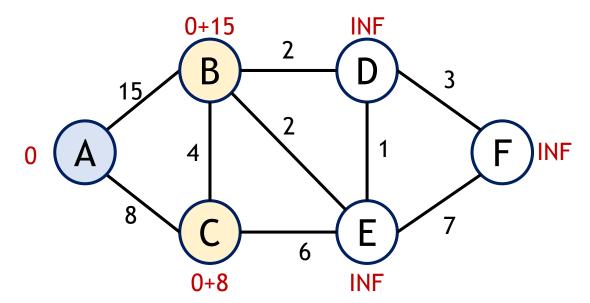
|      | A* | В   | С   | D   | E   | F   |
|------|----|-----|-----|-----|-----|-----|
| DIST | 0  | INF | INF | INF | INF | INF |
| PREV | -  | -   | -   | -   | -   | -   |

| Α | В | С | D | Е | F |  |
|---|---|---|---|---|---|--|
|   |   |   |   |   |   |  |



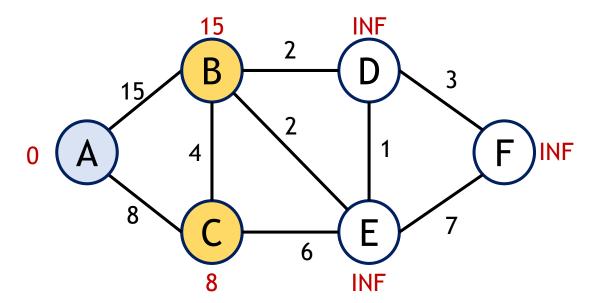
|      | A* | В   | С   | D   | E   | F   |
|------|----|-----|-----|-----|-----|-----|
| DIST | 0  | INF | INF | INF | INF | INF |
| PREV | -  | -   | -   | -   | -   | -   |

| A B C | D | Е | F |  |
|-------|---|---|---|--|
|-------|---|---|---|--|



|      | A* | В  | С | D   | E   | F   |
|------|----|----|---|-----|-----|-----|
| DIST | 0  | 15 | 8 | INF | INF | INF |
| PREV | -  | Α  | Α | -   | -   | -   |

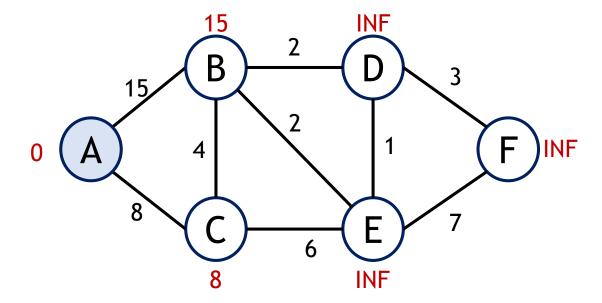
| A B C | D | Е | F |  |
|-------|---|---|---|--|
|-------|---|---|---|--|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | В  | С | D   | E   | F   |
|------|----|----|---|-----|-----|-----|
| DIST | 0  | 15 | 8 | INF | INF | INF |
| PREV | -  | Α  | Α | -   | -   | -   |

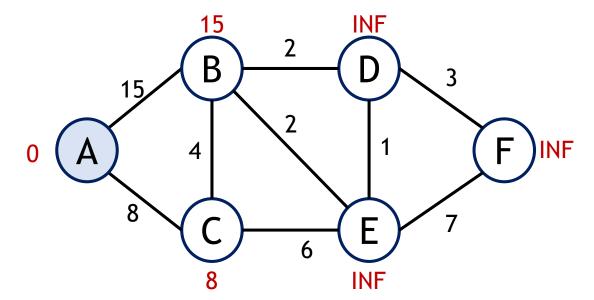
| Α | В | С | D | Е | F |  |
|---|---|---|---|---|---|--|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | В  | С | D   | E   | F   |
|------|----|----|---|-----|-----|-----|
| DIST | 0  | 15 | 8 | INF | INF | INF |
| PREV | -  | Α  | Α | -   | -   | -   |

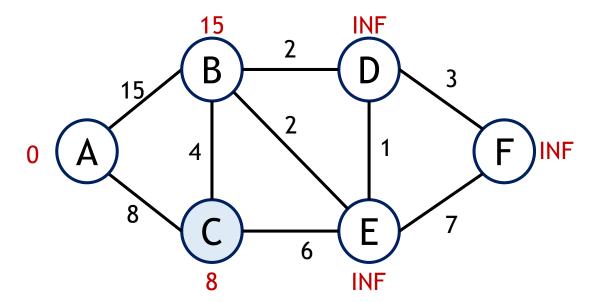
| Α | В | С | D | Е | F |  |
|---|---|---|---|---|---|--|
|   |   |   |   |   |   |  |



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST) 
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | В  | C* | D   | E   | F   |
|------|----|----|----|-----|-----|-----|
| DIST | 0  | 15 | 8  | INF | INF | INF |
| PREV | -  | Α  | Α  | -   | ı   | -   |

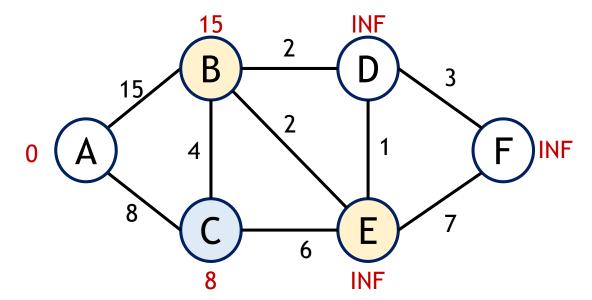
| С | В | D | Е | F |  |
|---|---|---|---|---|--|
|   |   |   |   |   |  |



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | В  | C* | D   | E   | F   |
|------|----|----|----|-----|-----|-----|
| DIST | 0  | 15 | 8  | INF | INF | INF |
| PREV | -  | Α  | Α  | 1   | -   | -   |

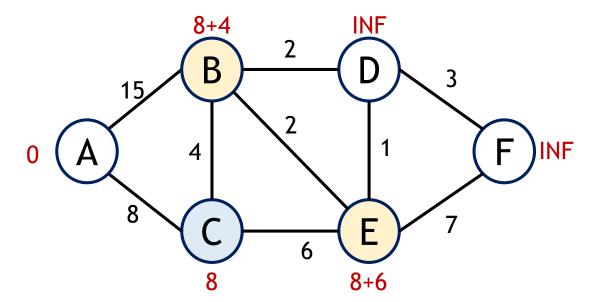
| С | В | D | Е | F |  |  |
|---|---|---|---|---|--|--|
|---|---|---|---|---|--|--|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

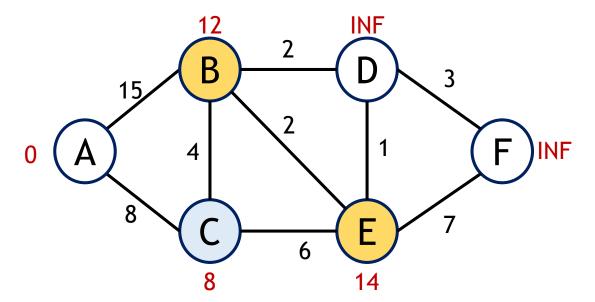
|      | A* | В  | C* | D   | E   | F   |
|------|----|----|----|-----|-----|-----|
| DIST | 0  | 15 | 8  | INF | INF | INF |
| PREV | -  | Α  | Α  | 1   | -   | -   |

| С | В | D | Е | F |  |
|---|---|---|---|---|--|
|   |   |   |   |   |  |



|      | A* | В  | C* | D   | E  | F   |
|------|----|----|----|-----|----|-----|
| DIST | 0  | 12 | 8  | INF | 14 | INF |
| PREV | -  | С  | Α  | 1   | С  | -   |

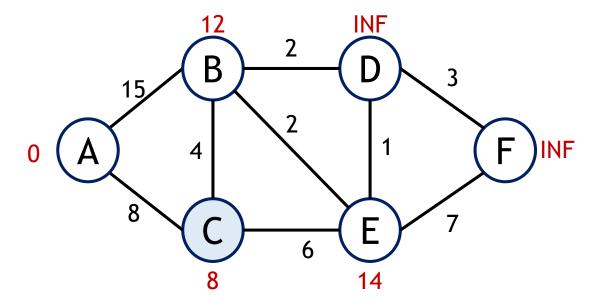
| C B D E F |
|-----------|
|-----------|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | В  | C* | D   | E  | F   |
|------|----|----|----|-----|----|-----|
| DIST | 0  | 12 | 8  | INF | 14 | INF |
| PREV | -  | С  | Α  | -   | С  | -   |

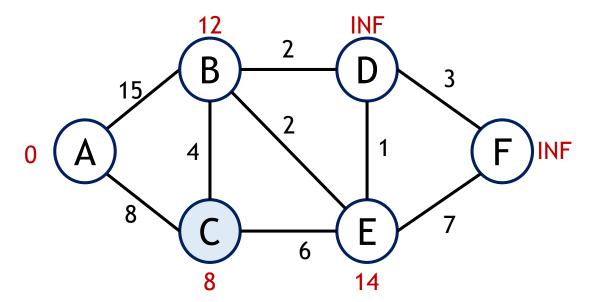
| c | R   | ח | F | F |  |
|---|-----|---|---|---|--|
| C | ן ט |   | _ |   |  |



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
            DIST[v] = T
            PREV[v] = u</pre>
```

|      | A* | B* | C* | D   | E  | F   |
|------|----|----|----|-----|----|-----|
| DIST | 0  | 12 | 8  | INF | 14 | INF |
| PREV | -  | С  | A  | -   | С  | -   |

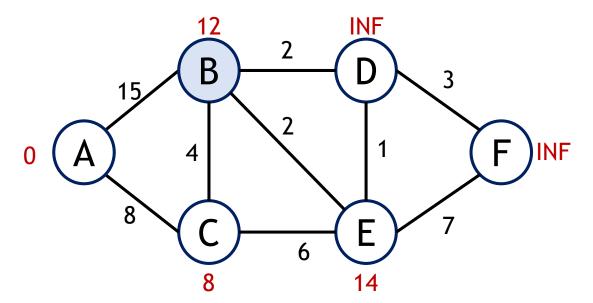
|  | С | В | D | Е | F |  |  |
|--|---|---|---|---|---|--|--|
|--|---|---|---|---|---|--|--|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST) 
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D   | E  | F   |
|------|----|----|----|-----|----|-----|
| DIST | 0  | 12 | 8  | INF | 14 | INF |
| PREV | -  | С  | Α  | -   | С  | -   |

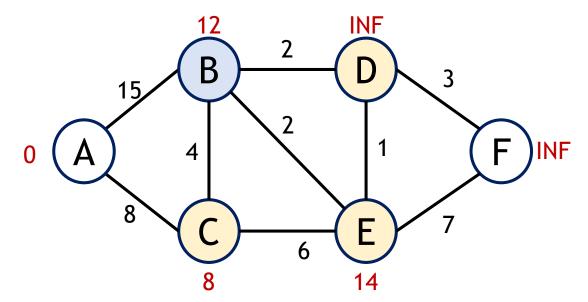
|--|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D   | E  | F   |
|------|----|----|----|-----|----|-----|
| DIST | 0  | 12 | 8  | INF | 14 | INF |
| PREV | -  | С  | Α  | -   | С  | -   |

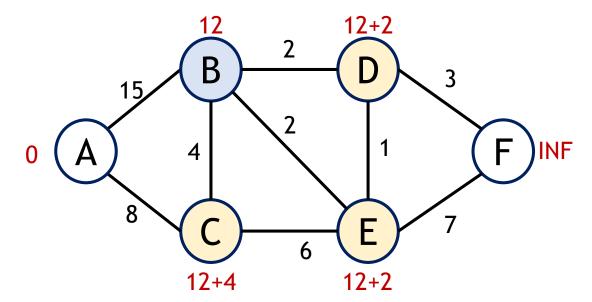
|--|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

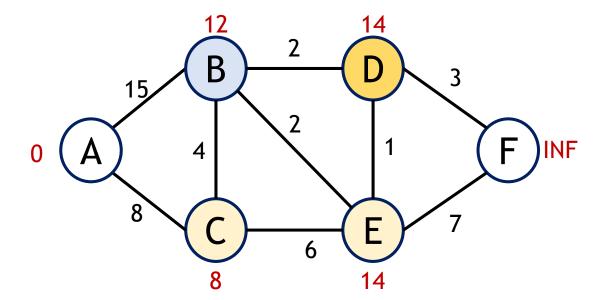
|      | A* | B* | C* | D   | E  | F   |
|------|----|----|----|-----|----|-----|
| DIST | 0  | 12 | 8  | INF | 14 | INF |
| PREV | -  | С  | Α  | -   | С  | -   |

|--|



|      | A* | B* | C* | D  | E  | F   |
|------|----|----|----|----|----|-----|
| DIST | 0  | 12 | 8  | 14 | 14 | INF |
| PREV | -  | С  | Α  | В  | С  | -   |

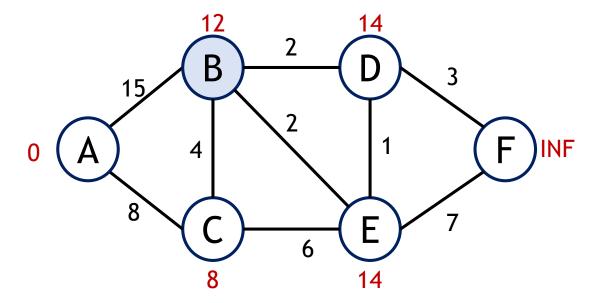
| В | D | Ε | F |  |  |
|---|---|---|---|--|--|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D  | E  | F   |
|------|----|----|----|----|----|-----|
| DIST | 0  | 12 | 8  | 14 | 14 | INF |
| PREV | -  | С  | Α  | В  | С  | -   |

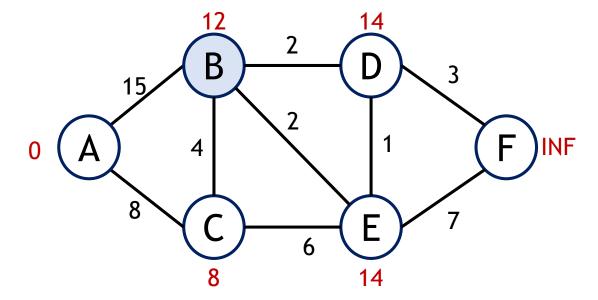
| B D E F |
|---------|
|---------|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D  | E  | F   |
|------|----|----|----|----|----|-----|
| DIST | 0  | 12 | 8  | 14 | 14 | INF |
| PREV | -  | С  | Α  | В  | С  | -   |

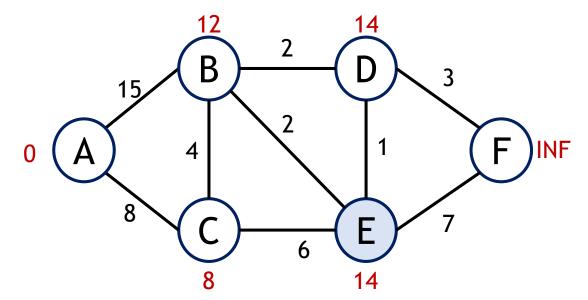
| B D E F |
|---------|
|---------|



```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST) 
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D  | E* | F   |
|------|----|----|----|----|----|-----|
| DIST | 0  | 12 | 8  | 14 | 14 | INF |
| PREV | -  | С  | Α  | В  | С  | ı   |

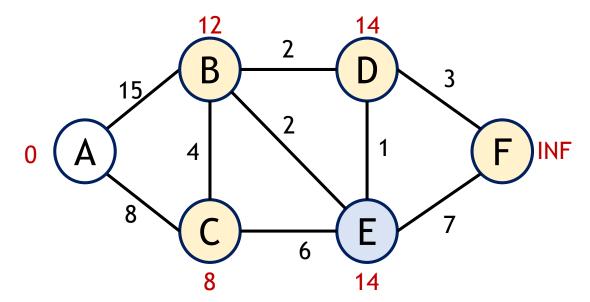




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D  | E* | F   |
|------|----|----|----|----|----|-----|
| DIST | 0  | 12 | 8  | 14 | 14 | INF |
| PREV | -  | С  | Α  | В  | С  | -   |

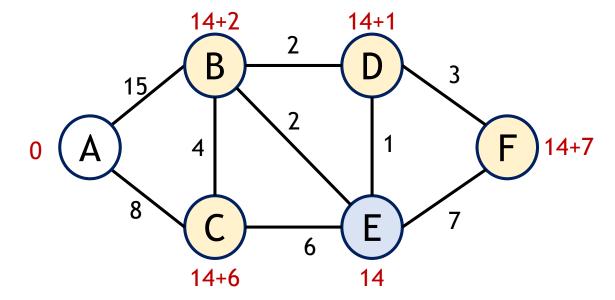




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

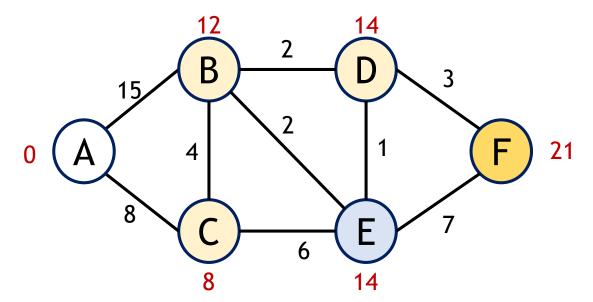
|      | A* | B* | C* | D  | E* | F   |
|------|----|----|----|----|----|-----|
| DIST | 0  | 12 | 8  | 14 | 14 | INF |
| PREV | -  | С  | Α  | В  | С  | -   |





|      | A* | B* | C* | D  | E* | F  |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 21 |
| PREV | -  | С  | Α  | В  | С  | E  |

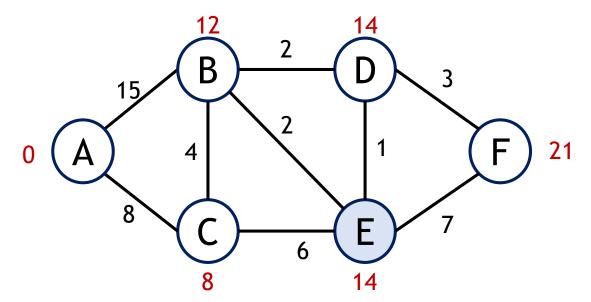




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D  | E* | F  |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 21 |
| PREV | -  | С  | Α  | В  | С  | E  |

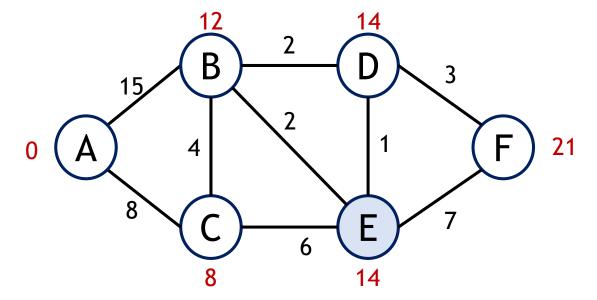




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D  | E* | F  |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 21 |
| PREV | -  | С  | Α  | В  | С  | Ε  |

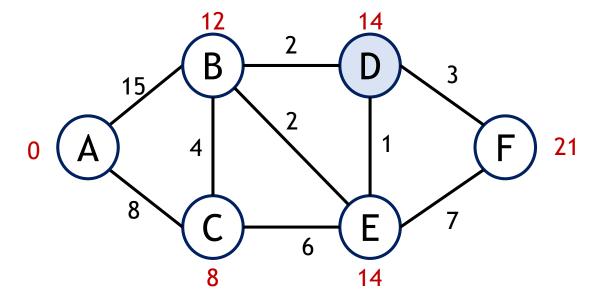




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST) 
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D* | E* | F  |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 21 |
| PREV | -  | С  | Α  | В  | С  | E  |

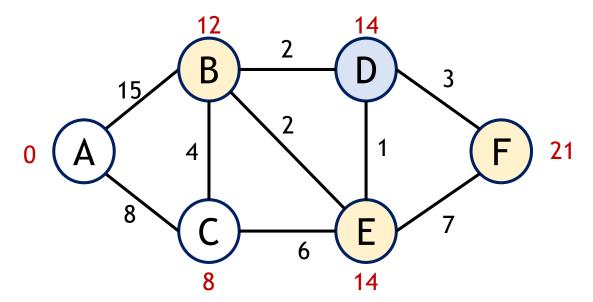




```
while !Q.isEmpty()
  u = vertex in Q w. min(DIST)
  remove u from Q
  for each v in G[u]
    T = DIST[u] + DIST[u,v]
    if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D* | E* | F  |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 21 |
| PREV | -  | С  | Α  | В  | С  | E  |

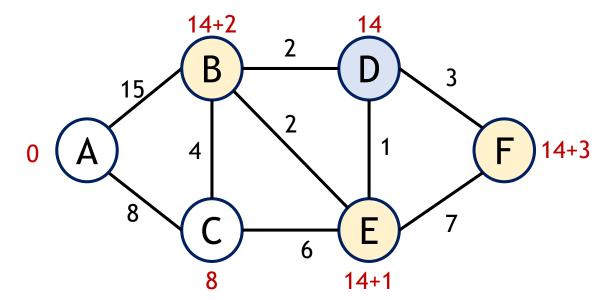




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D* | E* | F  |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 21 |
| PREV | -  | С  | Α  | В  | С  | E  |

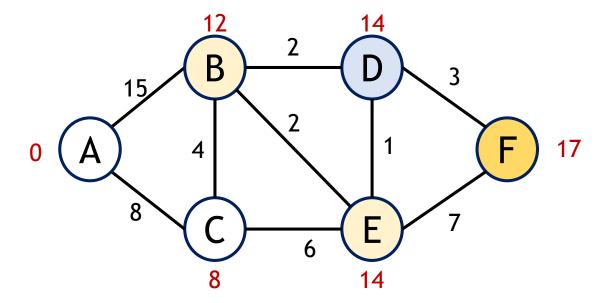




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D* | E* | F  |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 17 |
| PREV | -  | С  | Α  | В  | С  | D  |

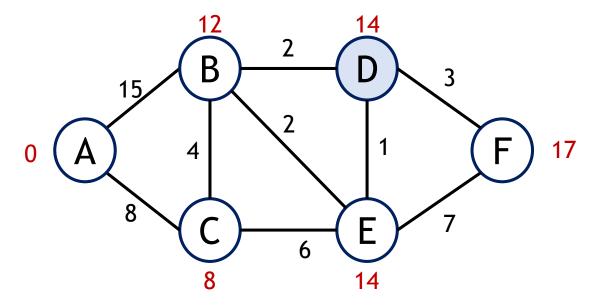




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D* | E* | F  |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 17 |
| PREV | -  | С  | Α  | В  | С  | D  |

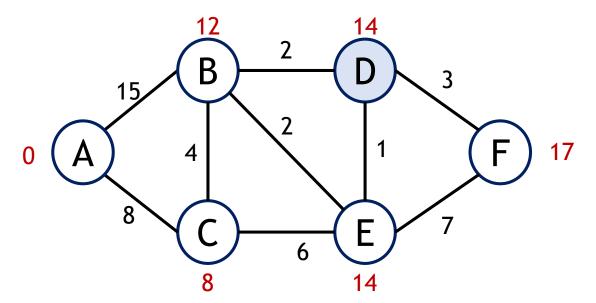




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D* | E* | F  |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 17 |
| PREV | -  | С  | Α  | В  | С  | D  |

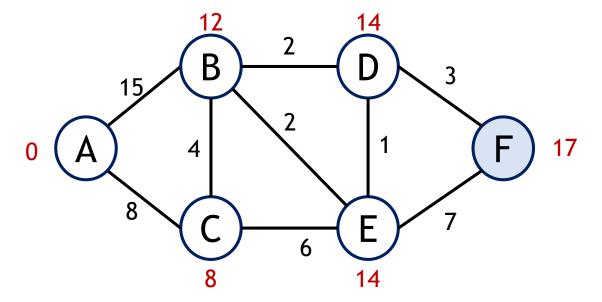




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST) 
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D* | E* | F* |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 17 |
| PREV | -  | С  | Α  | В  | С  | D  |

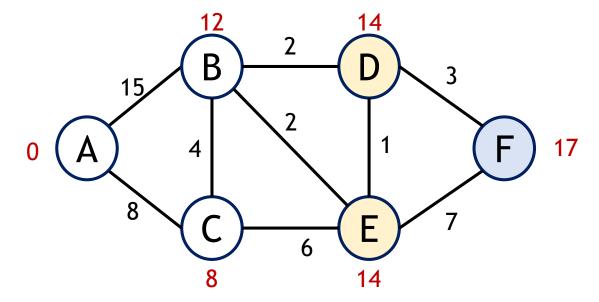




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D* | E* | F* |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 17 |
| PREV | -  | С  | A  | В  | С  | D  |

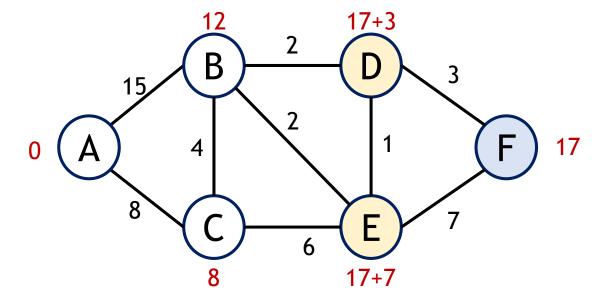




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

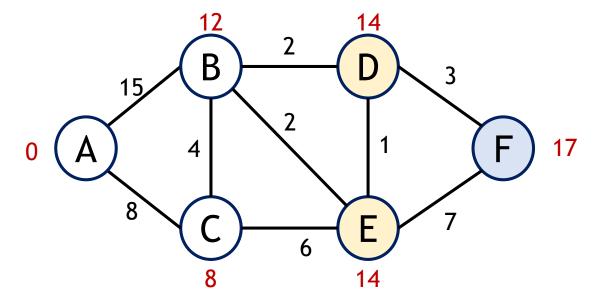
|      | A* | B* | C* | D* | E* | F* |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 17 |
| PREV | -  | С  | Α  | В  | С  | D  |





|      | A* | B* | C* | D* | E* | F* |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 17 |
| PREV | -  | С  | Α  | В  | С  | D  |

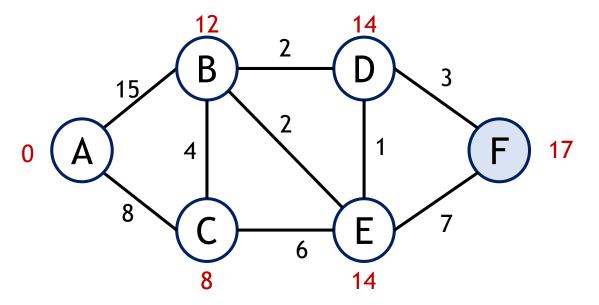




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D* | E* | F* |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 17 |
| PREV | -  | С  | Α  | В  | С  | D  |

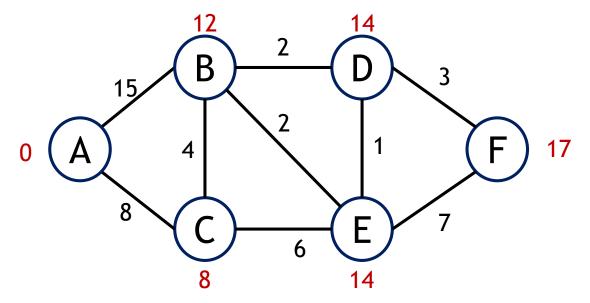




```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

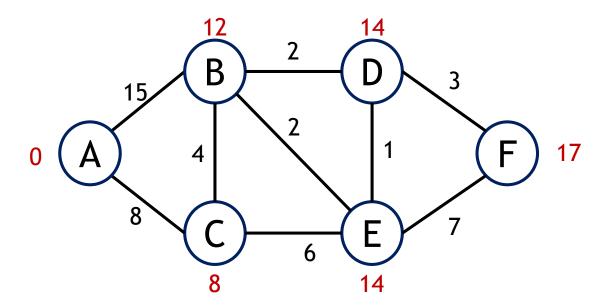
|      | A* | B* | C* | D* | E* | F* |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 17 |
| PREV | -  | С  | Α  | В  | С  | D  |





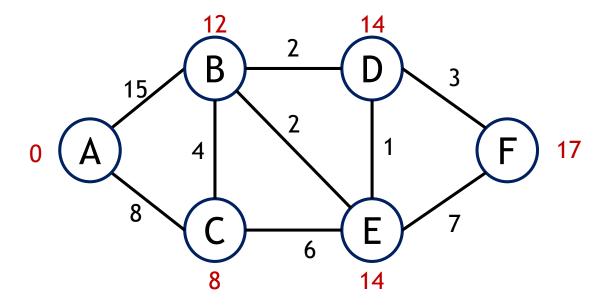
```
while !Q.isEmpty()
    u = vertex in Q w. min(DIST)
    remove u from Q
    for each v in G[u]
        T = DIST[u] + DIST[u,v]
        if T < DIST[v]
        DIST[v] = T
        PREV[v] = u</pre>
```

|      | A* | B* | C* | D* | E* | F* |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 17 |
| PREV | -  | С  | Α  | В  | С  | D  |



| То | Path                  | d  |
|----|-----------------------|----|
| Α  | -                     | 0  |
| В  | A -> C -> B           | 12 |
| С  | A -> C                | 8  |
| D  | A -> C -> B -> D      | 14 |
| E  | A -> C -> E           | 14 |
| F  | A -> C -> B -> D -> F | 17 |

|      | A* | B* | C* | D* | E* | F* |
|------|----|----|----|----|----|----|
| DIST | 0  | 12 | 8  | 14 | 14 | 17 |
| PREV | -  | С  | Α  | В  | С  | D  |



#### Trace Path from A -> F

Start at F

PREV(F) = D

PREV(D) = B

PREV(B) = C

PREV(C) = A

A, C, B, D, F

### Dijkstra's Shortest Path: Implementation

return DIST, PREV

 $O(|Q|) \approx O(|V|)$ 

# Dijkstra's Shortest Path: Complexity

#### iter #:findmin(), neighbors

```
1: |V| reps, |V|-1 nbrs
2: |V| - 1 reps, |V|-1 nbrs
3: |V| - 2 reps, |V|-1 nbrs
.
i: |V| - i - 1 reps, |V|-1 nbrs
.
|V|: 1 reps, |V|-1 nbrs
```

$$O(\sum_{i=1}^{i=|V|}[|V|-i-1]+[|V|-1])$$

$$O\left(\sum_{i=1}^{i=|V|} 2|V| - i - 2\right)$$

$$= O\left(2\sum_{i=1}^{i=|V|} |V| - 2\sum_{i=1}^{i=|V|} 1 - \sum_{i=1}^{i=|V|} i\right)$$

$$= O\left(2|V|^2 - 2|V| - \frac{|V|(|V|+1)}{2}\right)$$

$$= O(|V|^2)$$

### Dijkstra's Shortest Path: Implementation

```
while !Q.isEmpty()
u = vertex in Q w. min(DIST)
remove u from Q
for each v in G[u]
T = DIST[u] + DIST[u,v]
if T < DIST[v]
DIST[v] = T
PREV[v] = u</pre>
Utilize Priority Queue,
which is implemented
using a Binary Heap
(Min-Heap)

O(log(|V|))
```

#### References

https://medium.com/basecs/finding-the-shortest-path-with-a-little-help-from-dijkstra-613149fbdc8e

https://www.hackerearth.com/practice/notes/dijkstrasalgorithm/

# Exercise: Identify if an edge is a bridge

#### What is a bridge?

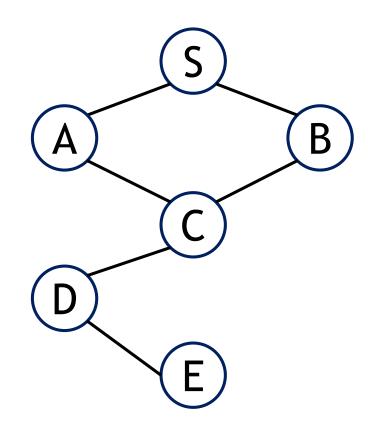
If removing an edge increases the number of components of the graph, then that edge is a bridge.

Implement following subroutines:

removeEdge

**DFTraversal** 

isBridge



# Exercise: Identify if an edge is a bridge

- 1. Pick Edge e you wish to check
- 2. Perform DFS/BFS, count components ci
- 3. tmp\_edge = e;
- 4. Remove edge e
- 5. Perform BFS/DFS, count components cf
- 6. Restore Edge tmp\_edge
- 7. if cf > ci: return True
- 8. return False

