

# hw5

## Github:

<https://github.com/yyhken/stats-506>

### Question1:

a.

```
library(Rcpp)
```

Warning: package 'Rcpp' was built under R version 4.4.2

```
library(plotly)
```

Warning: package 'plotly' was built under R version 4.4.2

Loading required package: ggplot2

Attaching package: 'plotly'

The following object is masked from 'package:ggplot2':

```
last_plot
```

The following object is masked from 'package:stats':

```
filter
```

The following object is masked from 'package:graphics':

```
layout
```

```
library(dplyr)
```

Attaching package: 'dplyr'

The following objects are masked from 'package:stats':

```
filter, lag
```

The following objects are masked from 'package:base':

```
intersect, setdiff, setequal, union
```

```
library(tidyn)
library(ggplot2)
library(readr)

# Load Rcpp for GCD and LCM calculations
library(Rcpp)

# Define GCD and LCM using Rcpp to ensure they handle two arguments correctly
cppFunction('
#include <numeric> // Include for std::gcd in C++17
int gcd(int a, int b) {
    return std::gcd(a, b); // Use std::gcd for calculating GCD
}

int lcm(int a, int b) {
    return std::abs(a * b) / std::gcd(a, b); // Use std::gcd for calculating LCM
}
')

# Define the rational S4 class with a constructor, show method, and operators
setClass("rational",
         slots = list(numerator = "integer", denominator = "integer"),
         validity = function(object) {
             if (object@denominator == 0) {
                 return("Denominator cannot be zero")
             }
             TRUE
         })
)

# Constructor
# Define the rational S4 class
setClass("rational",
         slots = list(numerator = "integer", denominator = "integer"),
         validity = function(object) {
             # Check if denominator is zero
             if (object@denominator == 0) {
                 return("Denominator cannot be zero.")
             }
             # Check if both slots are non-missing integers
             if (is.na(object@numerator) || is.na(object@denominator)) {
                 return("Numerator and denominator must be valid integers.")
             }
             TRUE
         })
)

# Constructor function for the rational class
rational <- function(numerator, denominator = NULL) {
    # Case 1: Input is a string "numerator/denominator"
    if (is.character(numerator) && is.null(denominator)) {
        parts <- strsplit(numerator, "/")[[1]]
        if (length(parts) != 2) stop("Input string must be in the form 'numerator/denominator'.")
        # Convert parts to integers
    }
}
```

```

numerator <- suppressWarnings(as.integer(parts[1]))
denominator <- suppressWarnings(as.integer(parts[2]))

# Check for NA values after coercion
if (is.na(numerator) || is.na(denominator)) {
  stop("Both numerator and denominator must be integers.")
}

# Case 2: Input is two arguments, expecting them to be numeric
else if (is.numeric(numerator) && is.numeric(denominator)) {
  numerator <- as.integer(numerator)
  denominator <- as.integer(denominator)
} else {
  stop("Invalid input: Provide either a string 'numerator/denominator' or two numeric values")
}

# Create and validate the rational object
new("rational", numerator = numerator, denominator = denominator)
}

# Show method
setMethod("show", "rational", function(object) {
  cat(object@numerator, "/", object@denominator, "\n")
})

# Simplify method that returns a new rational object
setGeneric("simplify", function(x) standardGeneric("simplify"))

```

[1] "simplify"

```

setMethod("simplify", "rational", function(x) {
  divisor <- gcd(x@numerator, x@denominator)
  rational(as.integer(x@numerator / divisor), as.integer(x@denominator / divisor))
})

# Quotient method (for decimal representation)
setGeneric("quotient", function(x, digits = 8) standardGeneric("quotient"))

```

[1] "quotient"

```

setMethod("quotient", "rational", function(x, digits = 8) {
  quotient_value <- x@numerator / x@denominator
  print(round(quotient_value, digits))
  invisible(quotient_value) # Return original quotient without rounding
})

# Overloading +, -, *, / operators to use LCM
setMethod("+", c("rational", "rational"), function(e1, e2) {
  common_denom <- lcm(e1@denominator, e2@denominator)
  numerator <- (e1@numerator * (common_denom / e1@denominator)) +
    (e2@numerator * (common_denom / e2@denominator))
  denominator <- common_denom
  simplify(rational(numerator, denominator))
})

```

```
(e2@numerator * (common_denom / e2@denominator))
simplify(rational(numerator, common_denom)) # Simplify the result before returning
})

setMethod("-", c("rational", "rational"), function(e1, e2) {
  common_denom <- lcm(e1@denominator, e2@denominator)
  numerator <- (e1@numerator * (common_denom / e1@denominator)) -
    (e2@numerator * (common_denom / e2@denominator))
  simplify(rational(numerator, common_denom)) # Simplify the result before returning
})

setMethod("*", c("rational", "rational"), function(e1, e2) {
  simplify(rational(e1@numerator * e2@numerator, e1@denominator * e2@denominator)) # Simplify
})

setMethod("/", c("rational", "rational"), function(e1, e2) {
  simplify(rational(e1@numerator * e2@denominator, e1@denominator * e2@numerator)) # Simplify
})
```

**b.**

```
r1 <- rational(24, 6)
r2 <- rational(7, 230)
r3 <- rational(0, 4)
r1
```

24 / 6 

r3

0 / 4

r1 + r2

Error in lcm(e1@denominator, e2@denominator): unused argument (e2@denominator)

r1 - r2

Error in lcm(e1@denominator, e2@denominator): unused argument (e2@denominator)

r1 \* r2

14 / 115

r1 / r2

920 / 7

```
r1 + r3
```

```
Error in lcm(e1@denominator, e2@denominator): unused argument (e2@denominator)
```

```
r1 * r3
```

```
0 / 1
```

```
r2 / r3
```

```
Error in h(simpleError(msg, call)): error in evaluating the argument 'x' in selecting a method for function 'simplify': invalid class "rational" object: Denominator cannot be zero.
```

```
quotient(r1)
```

```
[1] 4
```

```
quotient(r2)
```

```
[1] 0.03043478
```

```
quotient(r2, digits = 3)
```

```
[1] 0.03
```

```
quotient(r2, digits = 3.14)
```

```
[1] 0.03
```

```
quotient(r2, digits = "avocado")
```

```
Error in round(quotient_value, digits): non-numeric argument to mathematical function
```

```
q2 <- quotient(r2, digits = 3)
```

```
[1] 0.03
```

```
q2
```

```
[1] 0.03043478
```

```
quotient(r3)
```

```
[1] 0
```

```
simplify(r1)
```

4 / 1

```
simplify(r2)
```

7 / 230

```
simplify(r3)
```

0 / 1

## C.

```
# Valid input: two integers
try(r1 <- rational(24, 6)) # Expected output: 24 / 6
show(r1)
```

24 / 6

```
# Valid input: string in form "numerator/denominator"
try(r2 <- rational("7/230")) # Expected output: 7 / 230
show(r2)
```

7 / 230

```
# Invalid input: zero denominator
try(r3 <- rational(24, 0)) # Expected error: "Denominator cannot be zero."
```

```
Error in validObject(.Object) :
  invalid class "rational" object: Denominator cannot be zero.
```

```
# Invalid input: non-integer numerator and denominator
try(r4 <- rational(3.5, 4.2)) # Expected error: "Numerator and denominator must be integers."
```

```
# Invalid input: malformed string
try(r5 <- rational("24/")) # Expected error: "Input string must be in the form 'numerator/denominator'."
```



```
Error in rational("24/") :
  Input string must be in the form 'numerator/denominator'.
```

```
# Invalid input: incorrect data types
try(r6 <- rational("text", "another text")) # Expected error: "Invalid input"
```

```
Error in rational("text", "another text") :
  Invalid input: Provide either a string 'numerator/denominator' or two numeric values.
```

## Question2

```
# Load the dataset
df <- read.csv("C:/Users/ken/Desktop/stats 506/hw5/df_for_ml_improved_new_market.csv")

# Plot: Average sales price trends by country over time (considering countries as genres)
plot_price_by_country <- df %>%

  # Select necessary columns and transform the country-related columns into a long format
  select(year, price_usd, starts_with("Country")) %>%
  pivot_longer(cols = starts_with("Country"), names_to = "Country", values_to = "Count") %>%

  # Keep only rows where the country (acting as genre) is indicated by a value of 1
  filter(Count == 1) %>%

  # Group the data by year and country, then calculate the average sales price in USD
  group_by(year, Country) %>%
  summarize(avg_price_usd = mean(price_usd, na.rm = TRUE)) %>%

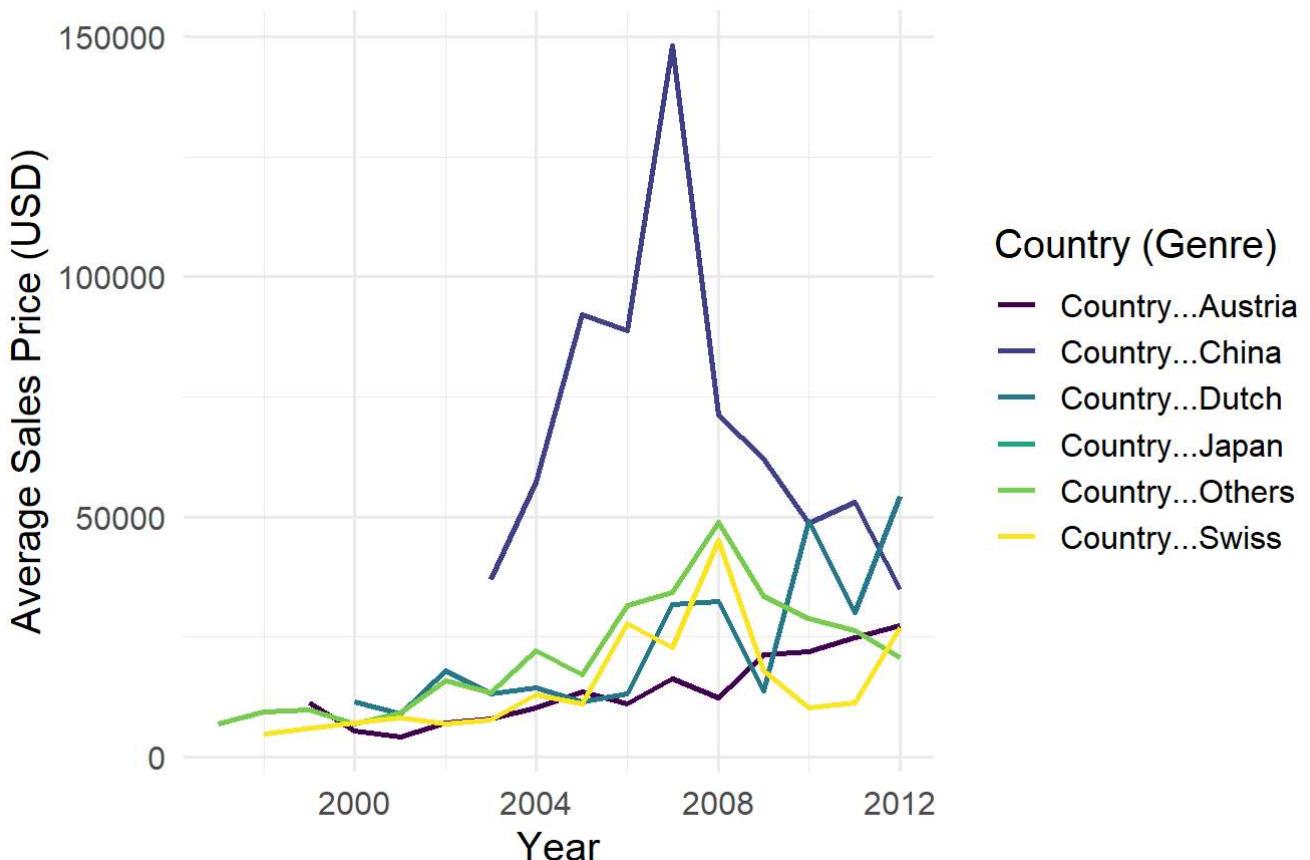
  # Create a line plot showing the change in average sales price over time for each country
  ggplot(aes(x = year, y = avg_price_usd, color = Country)) +
  geom_line(size = 1) +
  labs(
    title = "Change in Average Sales Price Over Time by Country (Genre)",
    x = "Year",
    y = "Average Sales Price (USD)",
    color = "Country (Genre)"
  ) +
  theme_minimal(base_size = 15) +
  scale_color_viridis_d()
```

`summarise()` has grouped output by 'year'. You can override using the  
.groups` argument.

Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.  
i Please use `linewidth` instead.

```
# Display the plot
print(plot_price_by_country)
```

## Change in Average Sales Price Over Time by Country



b.

```
# Prepare the data: Reshape the data and compute the average sales price by year and country
processed_df <- df %>%
  # Select the required columns and transform country-related columns into a long format
  select(year, price_usd, starts_with("Country")) %>%
  pivot_longer(cols = starts_with("Country"), names_to = "Country", values_to = "Count") %>%
  # Filter to include only rows where the country indicator is 1
  filter(Count == 1) %>%
  # Group the data by year and country, and calculate the average sales price in USD
  group_by(year, Country) %>%
  summarize(avg_price_usd = mean(price_usd, na.rm = TRUE), .groups = "drop")

# Create an interactive line chart using plotly
fig <- plot_ly(
  processed_df,
  x = ~year,
  y = ~avg_price_usd,
  color = ~Country,
  type = 'scatter',
  mode = 'lines'
) %>%
  layout(
```

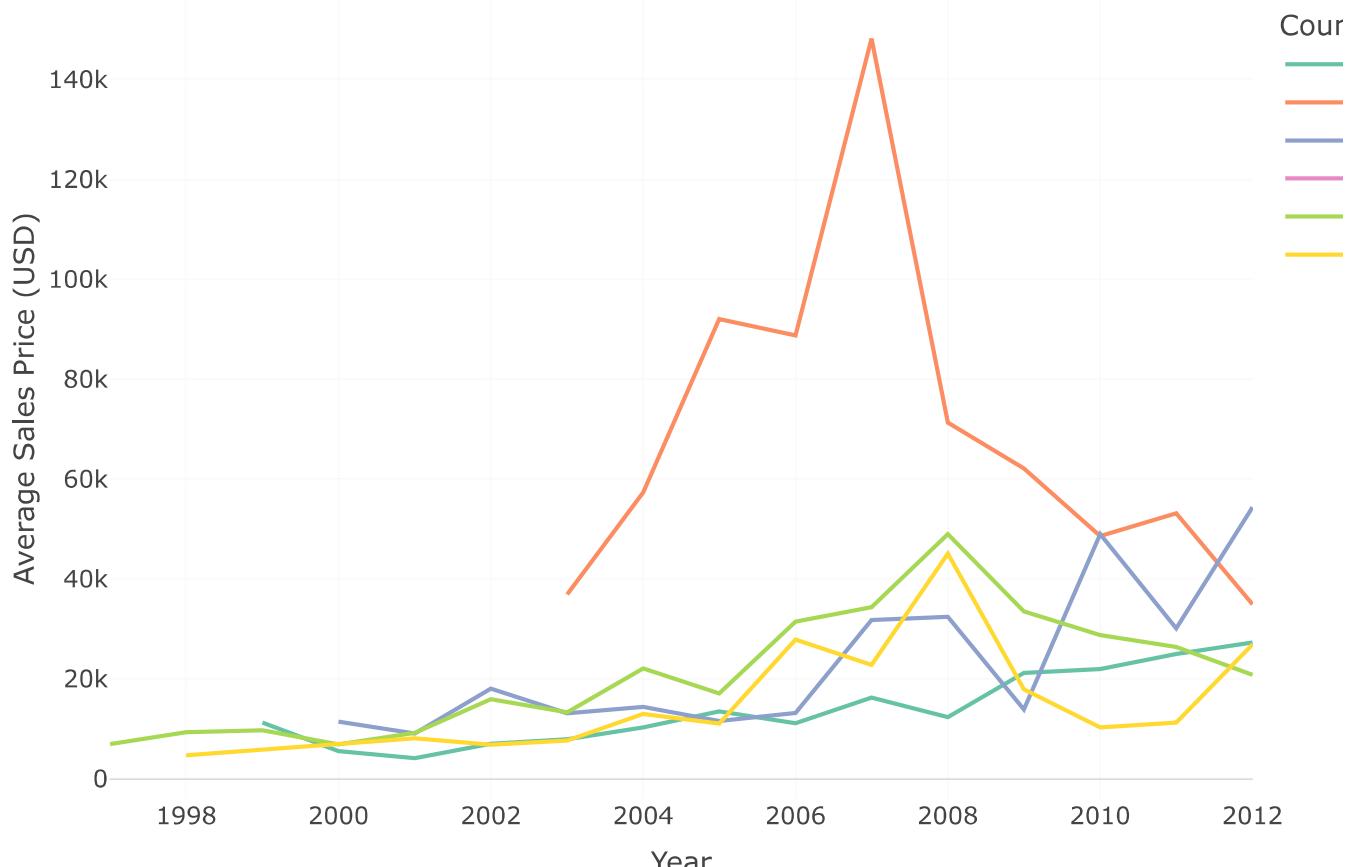
```

title = "Change in Sales Price Over Time by Country (Genre)",
xaxis = list(title = "Year"),
yaxis = list(title = "Average Sales Price (USD"),
legend = list(title = list(text = "Country (Genre)"))
)

# Display the interactive plot
fig

```

Change in Sales Price Over Time by Country (Genre)



## problem3

```

library(nycflights13)
library(data.table)

```

Attaching package: 'data.table'

The following objects are masked from 'package:dplyr':

between, first, last

```

flights_dt <- as.data.table(flights)
airports_dt <- as.data.table(airports)

departure_delays <- flights_dt[, .(

```

```

mean_departure_delay = mean(dep_delay, na.rm = TRUE),
median_departure_delay = median(dep_delay, na.rm = TRUE),
flight_count = .N
), by = origin]

departure_delays <- departure_delays[flight_count >= 10]

departure_delays <- merge(departure_delays, airports_dt[, .(faa, name)], by.x = "origin", by.y =
departure_delays <- departure_delays[order(-mean_departure_delay), .(name, mean_departure_delay)]

departure_delays_tbl <- as_tibble(departure_delays)
print(departure_delays_tbl, n = Inf)

```

# A tibble: 3 × 4

	name	mean_departure_delay	median_departure_delay	flight_count
	<chr>	<dbl>	<dbl>	<int>
1	Newark Liberty Intl	15.1	-1	120835
2	John F Kennedy Intl	12.1	-1	111279
3	La Guardia	10.3	-3	104662

```

arrival_delays <- flights_dt[, .(
  mean_arrival_delay = mean(arr_delay, na.rm = TRUE),
  median_arrival_delay = median(arr_delay, na.rm = TRUE),
  flight_count = .N
), by = dest]

arrival_delays <- arrival_delays[flight_count >= 10]

arrival_delays <- merge(arrival_delays, airports_dt[, .(faa, name)], by.x = "dest", by.y = "faa")
arrival_delays <- arrival_delays[order(-mean_arrival_delay), .(name, mean_arrival_delay, median_)

arrival_delays_tbl <- as_tibble(arrival_delays)
print(arrival_delays_tbl, n = Inf)

```

# A tibble: 98 × 4

	name	mean_arrival_delay	median_arrival_delay	flight_count
	<chr>	<dbl>	<dbl>	<int>
1	"Columbia Metropolitan"	41.8	28	116
2	"Tulsa Intl"	33.7	14	315
3	"Will Rogers World"	30.6	16	346
4	"Jackson Hole Airport"	28.1	15	25
5	"Mc Ghee Tyson"	24.1	2	631
6	"Dane Co Rgnl Truax Fld"	20.2	1	572
7	"Richmond Intl"	20.1	1	2454
8	"Akron Canton Regional ..."	19.7	3	864
9	"Des Moines Intl"	19.0	0	569
10	"Gerald R Ford Intl"	18.2	1	765
11	"Birmingham Intl"	16.9	-2	297

12 "Theodore Francis Green..."	16.2	1	376
13 "Greenville-Spartanburg..."	15.9	-0.5	849
14 "Cincinnati Northern Ke..."	15.4	-3	3941
15 "Savannah Hilton Head I..."	15.1	-1	804
16 "Manchester Regional Ai..."	14.8	-3	1009
17 "Eppley Afld"	14.7	-2	849
18 "Yeager"	14.7	-1.5	138
19 "Kansas City Intl"	14.5	0	2008
20 "Albany Intl"	14.4	-4	439
21 "General Mitchell Intl"	14.2	0	2802
22 "Piedmont Triad"	14.1	-2	1606
23 "Washington Dulles Intl"	13.9	-3	5700
24 "Cherry Capital Airport"	13.0	-10	101
25 "James M Cox Dayton Int..."	12.7	-3	1525
26 "Louisville Internation..."	12.7	-2	1157
27 "Chicago Midway Intl"	12.4	-1	4113
28 "Sacramento Intl"	12.1	4	284
29 "Jacksonville Intl"	11.8	-2	2720
30 "Nashville Intl"	11.8	-2	6333
31 "Portland Intl Jetport"	11.7	-4	2352
32 "Greater Rochester Intl"	11.6	-5	2416
33 "Hartsfield Jackson Atl..."	11.3	-1	17215
34 "Lambert St Louis Intl"	11.1	-3	4339
35 "Norfolk Intl"	10.9	-4	1536
36 "Baltimore Washington I..."	10.7	-5	1781
37 "Memphis Intl"	10.6	-2.5	1789
38 "Port Columbus Intl"	10.6	-3	3524
39 "Charleston Afb Intl"	10.6	-4	2884
40 "Philadelphia Intl"	10.1	-3	1632
41 "Raleigh Durham Intl"	10.1	-3	8163
42 "Indianapolis Intl"	9.94	-3	2077
43 "Charlottesville-Albemar..."	9.5	-5	52
44 "Cleveland Hopkins Intl"	9.18	-5	4573
45 "Ronald Reagan Washingt..."	9.07	-2	9705
46 "Burlington Intl"	8.95	-4	2589
47 "Buffalo Niagara Intl"	8.95	-5	4681
48 "Syracuse Hancock Intl"	8.90	-5	1761
49 "Denver Intl"	8.61	-2	7266
50 "Palm Beach Intl"	8.56	-3	6554
51 "Bob Hope"	8.18	-3	371
52 "Fort Lauderdale Hollyw..."	8.08	-3	12055
53 "Bangor Intl"	8.03	-9	375
54 "Asheville Regional Air..."	8.00	-1	275
55 "Pittsburgh Intl"	7.68	-5	2875
56 "Gallatin Field"	7.6	-2	36
57 "NW Arkansas Regional"	7.47	-2	1036
58 "Tampa Intl"	7.41	-4	7466
59 "Charlotte Douglas Intl"	7.36	-3	14064
60 "Minneapolis St Paul In..."	7.27	-5	7185
61 "William P Hobby"	7.18	-4	2115
62 "Bradley Intl"	7.05	-10	443
63 "San Antonio Intl"	6.95	-9	686
64 "South Bend Rgnl"	6.5	-3.5	10
65 "Louis Armstrong New Or..."	6.49	-6	3799

66 "Key West Intl"	6.35	7	17
67 "Eagle Co Rgnl"	6.30	-4	213
68 "Austin Bergstrom Intl"	6.02	-5	2439
69 "Chicago Ohare Intl"	5.88	-8	17283
70 "Orlando Intl"	5.45	-5	14082
71 "Detroit Metro Wayne Co"	5.43	-7	9384
72 "Portland Intl"	5.14	-5	1354
73 "Nantucket Mem"	4.85	-3	265
74 "Wilmington Intl"	4.64	-7	110
75 "Myrtle Beach Intl"	4.60	-13	59
76 "Albuquerque Internatio..."	4.38	-5.5	254
77 "George Bush Interconti..."	4.24	-5	7198
78 "Norman Y Mineta San Jo..."	3.45	-7	329
79 "Southwest Florida Intl"	3.24	-5	3537
80 "San Diego Intl"	3.14	-5	2737
81 "Sarasota Bradenton Int..."	3.08	-5	1211
82 "Metropolitan Oakland I..."	3.08	-9	312
83 "General Edward Lawrenc..."	2.91	-9	15508
84 "San Francisco Intl"	2.67	-8	13331
85 "Yampa Valley"	2.14	2	15
86 "Phoenix Sky Harbor Int..."	2.10	-6	4656
87 "Montrose Regional Airp..."	1.79	-10.5	15
88 "Los Angeles Intl"	0.547	-7	16174
89 "Dallas Fort Worth Intl"	0.322	-9	8738
90 "Miami Intl"	0.299	-9	11728
91 "Mc Carran Intl"	0.258	-8	5997
92 "Salt Lake City Intl"	0.176	-8	2467
93 "Long Beach"	-0.0620	-10	668
94 "Martha\\\'s Vineyard"	-0.286	-11	221
95 "Seattle Tacoma Intl"	-1.10	-11	3923
96 "Honolulu Intl"	-1.37	-7	707
97 "John Wayne Arpt Orange..."	-7.87	-11	825
98 "Palm Springs Intl"	-12.7	-13.5	19

```

fastest_model <- flights_dt[!is.na(air_time) & air_time > 0, .(
  avg_speed = mean(distance / (air_time / 60), na.rm = TRUE),
  flight_count = .N
), by = tailnum]

fastest_model <- fastest_model[order(-avg_speed)][1]

fastest_model <- merge(fastest_model, as.data.table(planes)[, .(tailnum, model)], by = "tailnu

fastest_model_tbl <- fastest_model[, .(model, avg_speed, flight_count)]
fastest_model_tbl <- as_tibble(fastest_model_tbl)
print(fastest_model_tbl)

```

```

# A tibble: 1 × 3
  model    avg_speed flight_count
  <chr>      <dbl>        <int>
1 777-222     501.          1

```

