



## Week10\_Course

# Database System-Schema+Design part4

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## Schema Design and Refinement

- How do we obtain a good design?
- Functional dependencies & keys
- ➔ • Desirable properties of schema refinement
- Boyce Codd Normal Form (BCNF)
- Third Normal Form (3NF)
- Fourth Normal Form (4NF)

Persons with several phones:

Name	SSN	Phone
Fred	123-321-99	(201) 555-1234
Fred	123-321-99	(206) 572-4312
Joe	909-438-44	(908) 464-0028
Joe	909-438-44	(212) 555-4000

		SSN	Phone
123-321-99	Fred	123-321-99	(201) 555-1234
909-438-44	Joe	123-321-99	(206) 572-4312
		909-438-44	(908) 464-0028
		909-438-44	(212) 555-4000

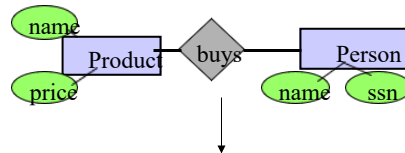
(SSN,Name) (Name,Phone) ?

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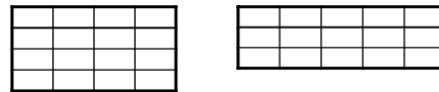
## Relational Schema Design (or Logical Design)

Conceptual Model:



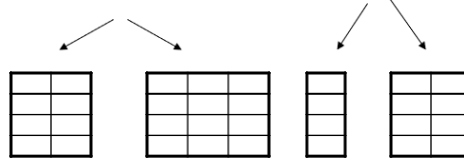
Relational Model:

- create tables
- specify FD's
- find keys



Normalization

- use FDs to **decompose** tables to achieve better design



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## Desirable Properties of Schema Refinement

- 1) minimize redundancy
- 2) avoid info loss
- 3) preserve dependency
- 4) ensure good query performance

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## Recall: Relation Decomposition

Break the relation into two:

The original relation schema

Name	SSN	Phone
Fred	123-321-99	(201) 555-1234
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Joe	909-438-44	(212) 555-4000

SSN	Name
123-321-99	Fred
909-438-44	Joe

SSN	Phone
123-321-99	(201) 555-1234
123-321-99	(206) 572-4312
909-438-44	(908) 464-0028
909-438-44	(212) 555-4000

**Desirable Property #1: Minimize redundancy**

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## Decompositions in General

Let  $R$  be a relation with attributes  $A_1, A_2, \dots, A_n$

Create two relations  $R_1$  and  $R_2$  with attributes

$$B_1, B_2, \dots, B_m \quad C_1, C_2, \dots, C_t$$

Such that:

$$B_1, B_2, \dots, B_m \cup C_1, C_2, \dots, C_t = A_1, A_2, \dots, A_n$$

And

- $R_1$  is the projection of  $R$  on  $B_1, B_2, \dots, B_m$
- $R_2$  is the projection of  $R$  on  $C_1, C_2, \dots, C_t$

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## Certain Decomposition May Cause Problems

Name	Price	Category
Gizmo	19.99	Gadget
OneClick	24.99	Camera
DoubleClick	29.99	Camera

Decompose on : Name, Category and Price, Category

Name	Category
Gizmo	Gadget
OneClick	Camera
DoubleClick	Camera



Price	Category
19.99	Gadget
24.99	Camera
29.99	Camera

When we put it back:  
Cannot recover information

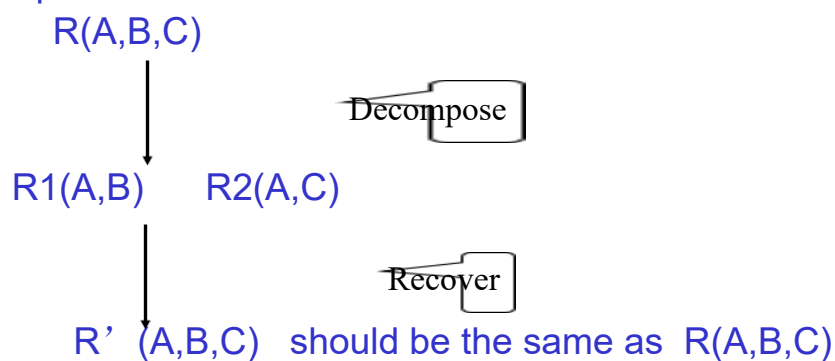
Name	Price	Category
Gizmo	19.99	Gadget
OneClick	24.99	Camera
<b>OneClick</b>	<b>29.99</b>	<b>Camera</b>
<b>DoubleClick</b>	<b>24.99</b>	<b>Camera</b>
DoubleClick	29.99	Camera

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## Lossless Decomposition (无损分解)

A decomposition is **lossless** if we can recover:



$R'$  is in general larger than  $R$ . Must ensure  $R' = R$

**Desirable Property #2: Lossless decomposition**

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## Put Another Way: "Lossless" Joins

- The main idea: if you decompose a relation schema, then join the parts of an instance via a natural join, you might get more rows than you started with, i.e., spurious tuples
  - This is bad!
  - Called a "lossy join".
- Goal: decompositions which produce only "lossless" joins
  - "non-additive" join is more descriptive

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## Dependency Preserving

(保持函数依赖)

- Given a relation R and a set of FDs S
- Suppose we decompose R into R1 and R2
- Suppose
  - R1 has a set of FDs S1
  - R2 has a set of FDs S2
  - S1 and S2 are computed from S
- We say the decomposition is dependency preserving if by enforcing S1 over R1 and S2 over R2, we can enforce S over R
- $(S1 \cup S2)^+ = S^+$

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## An Example

Unit	Company	Product
------	---------	---------

FD's: Unit  $\rightarrow$  Company; Company, Product  $\rightarrow$  Unit

So, there is a BCNF violation, and we decompose.

Unit	Company
Galaga99	UI
Bingo	UI

Unit  $\rightarrow$  Company

Unit	Product
Galaga99	databases
Bingo	databases

No FDs

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## So What' s the Problem?

Unit	Company	Unit	Product
Galaga99	UI	Galaga99	databases
Bingo	UI	Bingo	databases

No problem so far. All *local* FD' s are satisfied.

Let' s put all the data back into a single table again:

Unit	Company	Product
Galaga99	UI	databases
Bingo	UI	databases

**Violates the dependency: company, product  $\rightarrow$  unit!**

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## Preserving FDs

- What if, when a relation is decomposed, the X of an  $X \rightarrow Y$  ends up only in one of the new relations and the Y ends up only in another?
- Such a decomposition is not “dependency-preserving.”
- **Desirable Property #3: always have FD-preserving decompositions**
- We will talk about "Desirable Property #4: Ensure Good Query Performance" later

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## Review

- When decomposing a relation R, we want to decomposition to
  - minimize redundancy
  - avoid info loss
  - preserve dependencies (i.e., constraints)
  - ensure good query performance
- These objectives can be conflicting
- Various normal forms achieve parts of the objectives

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多选题 1分



## 互动交流一

已知关系模式：学生（身份证号，学号，姓名）  
将其分解为两个关系模式：学生身份（身份证号，姓名）  
学生信息（学号，姓名）  
下面哪个描述是正确的？（多选题）

- ☐ A 这个分解是无损分解
- ☐ B 这个分解不是无损分解
- ☐ C 这是保持无损连接的分解
- ☐ D 这不是保持无损连接的分解

提交

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单选题 1分



## 互动交流二

已知关系模式：学生（身份证号，学号，姓名）  
将其分解为两个关系模式：学生身份（身份证号，姓名）  
学生信息（学号，姓名）  
下面哪个描述是正确的？

- ☐ A 这个分解是保持函数依赖的分解
- ☐ B 这个分解是丢失函数依赖的分解

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多选题 1分



### 互动交流三

已知关系模式：学生（身份证号，学号，姓名）  
将其分解为两个关系模式：学生身份（身份证号，姓名）  
学生信息（学号，姓名）  
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- ☐ D 这不是保持无损连接的分解

提交

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多选题 1分



### 互动交流四

已知关系模式：学生（身份证号，学号，姓名）  
将其分解为两个关系模式：学生身份（身份证号，姓名）  
学生信息（学号，姓名）  
下面哪个描述是正确的？

- ☐ A 这个分解是保持函数依赖的分解
- ☐ B 这个分解是丢失函数依赖的分解

提交

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## 互动交流五

Consider a relation  $R = (A, B, C, D, E)$  with FD' s  $A \rightarrow C$ ,  
 $CD \rightarrow B$ ,  $B \rightarrow E$  and  $E \rightarrow D$ .

We decompose  $R$  into  $R_1(B, C, D)$  and  $R_2(A, C, E)$ .

What are the FD' s that hold in  $R_1$  and  $R_2$ ?

What are the keys of  $R_1$  and  $R_2$ ?

请用弹幕回答

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## Week10\_Course

## Database System-Schema+Design part5

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# Schema Design and Refinement

- How do we obtain a good design?
- Functional dependencies & keys
- Desirable properties of schema refinement
- ➔ • Boyce Codd Normal Form (BCNF)
- Third Normal Form (3NF) and 3NF Decomposition
- Fourth Normal Form (4NF)

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## Normal Forms

**First Normal Form** = all attributes are atomic

**Second Normal Form (2NF)** = old and obsolete

**Boyce Codd Normal Form (BCNF)**

**Third Normal Form (3NF)**

**Fourth Normal Form (4NF)**

Others...



$R \in 4NF \gg R \in BCNF \gg R \in 3NF \gg R \in 2NF \gg R \in 1NF$

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# What We Want to Do with Normal Forms

- Take a relation schema...
- Test it against a normalization criterion...
- If it passes, fine!
  - Maybe test again with a higher criterion
- If it fails, decompose into smaller relations
  - Each of them will pass the test
  - Each can then be tested with a higher criterion

Persons with several phones:

Name	SSN	Phone
Fred	123-321-99	(201) 555-1234
Fred	123-321-99	(206) 572-4312
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Joe	909-438-44	(212) 555-4000



SSN	Name	SSN	Phone
123-321-99	Fred	123-321-99	(201) 555-1234
123-321-99	Fred	123-321-99	(206) 572-4312
909-438-44	Joe	909-438-44	(908) 464-0028
909-438-44	Joe	909-438-44	(212) 555-4000

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## Boyce-Codd Normal Form

A relation R is in BCNF if and only if:

Whenever there is a nontrivial FD  $A_1, A_2, \dots, A_n \rightarrow B$

for R, it is the case that  $\{A_1, A_2, \dots, A_n\}$  is a super-key for R.

Remember: *nontrivial* means  $A$  is not a member of set  $X$ . ( $X \rightarrow A$ )

Remember, a *superkey* is any superset of a key (not necessarily a proper superset).

In English (though a bit vague):

Whenever a set of attributes of R is determining another attribute, it should determine all attributes of R.

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## Example

Name	SSN	Phone
Fred	123-321-99	(201) 555-1234
Fred	123-321-99	(206) 572-4312
Joe	909-438-44	(908) 464-0028
Joe	909-438-44	(212) 555-4000

Person(Name, SSN, Phone)

FDs: {SSN  $\rightarrow$  Name}

What are the dependencies?

SSN  $\rightarrow$  Name

What are the keys?

Is it in BCNF?

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## Decompose it into BCNF

SSN	Name
123-321-99	Fred
909-438-44	Joe

FDs: SSN  $\rightarrow$  Name

如果一个关系模式只含有两个属性，它是不是BCNF范式？

SSN	Phone
123-321-99	(201) 555-1234
123-321-99	(206) 572-4312
909-438-44	(908) 464-0028
909-438-44	(212) 555-4000

FDs: No

如果一个关系模式没有函数依赖，它是不是BCNF范式？

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## Decomposition into BCNF

- Given: relation  $R$  with FD' s  $F$ .
- Look among the given FD' s for a BCNF violation  $X \rightarrow B$ .
  - If any FD following from  $F$  violates BCNF, then there will surely be an FD in  $F$  itself that violates BCNF.
- Compute  $X^+$ .
  - Not all attributes, or else  $X$  is a superkey.

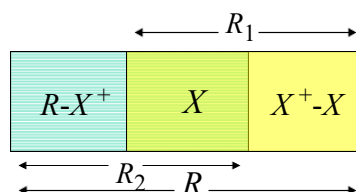
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## Decompose $R$ Using $X \rightarrow B$

- Replace  $R$  by relations with schemas:
    1.  $R_1 = X^+$ .
    2.  $R_2 = R - (X^+ - X)$ .
- Project* given FD' s  $F$  onto the two new relations.
3. Compute the *closure* of  $F$  = all nontrivial FD' s that follow from  $F$ .
  4. Use only those FD' s whose attributes are all in  $R_1$  or all in  $R_2$ .

Decomposition Picture



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## BCNF Decomposition

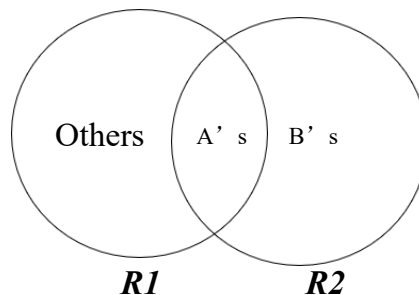
Find a dependency that violates the BCNF condition:

$$A_1, A_2, \dots, A_n \rightarrow B_1, B_2, \dots, B_m$$

Heuristics: choose  $B_1, B_2, \dots, B_m$  “as large as possible”

Decompose:

Any  
2-attribute  
relation is  
in BCNF.



Continue until  
there are no  
BCNF violations  
left.

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## Example

Drinkers(name, addr, beersLiked, manf, favBeer)

$F = \text{name} \rightarrow \text{addr}, \text{name} \rightarrow \text{favBeer}, \text{beersLiked} \rightarrow \text{manf}$

- Pick BCNF violation  $\text{name} \rightarrow \text{addr}$ .
- Close the left side:  $\{\text{name}\}^+ = \{\text{name}, \text{addr}, \text{favBeer}\}$ .
- Decomposed relations:
  1. Drinkers1(name, addr, favBeer)
  2. Drinkers2(name, beersLiked, manf)

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## Example, Continued

- We are not done; we need to check Drinkers1 and Drinkers2 for BCNF.
- Projecting FD' s is complex in general, easy here.
- For Drinkers1(name, addr, favBeer), relevant FD' s are  $\text{name} \rightarrow \text{addr}$  and  $\text{name} \rightarrow \text{favBeer}$ .
  - Thus, {name} is the only key and Drinkers1 is in BCNF.

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## Example, Continued

- For Drinkers2(name, beersLiked, manf), the only FD is  $\text{beersLiked} \rightarrow \text{manf}$ , and the only key is {name, beersLiked}.
  - Violation of BCNF.
- $\text{beersLiked}^+ = \{\text{beersLiked}, \text{manf}\}$ , so we decompose *Drinkers2* into:
  1. Drinkers3(beersLiked, manf)
  2. Drinkers4(name, beersLiked)

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## Example, Concluded

- The resulting decomposition of *Drinkers* :
    1. *Drinkers1*(name, addr, favBeer)
    2. *Drinkers3*(beersLiked, manf)
    3. *Drinkers4*(name, beersLiked)
- WNotice: *Drinkers1* tells us about drinkers, *Drinkers3* tells us about beers, and *Drinkers4* tells us the relationship between drinkers and the beers they like.

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## Thus,

- BCNF removes certain types of redundancy
- For examples of redundancy that it cannot remove, see "multivalued redundancy" later
- BCNF avoids info loss

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## However

- BCNF is not always dependency preserving
- In fact, some times we cannot find a BCNF decomposition that is dependency preserving
- Can handle this situation using 3NF
- See next few slides for example

**Summary: Boyce Codd Normal Form (BCNF)**

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单选题 1分



## 互动交流一

已知关系模式：学生（学号、姓名、系、系主任）  
它存在的函数依赖是：{学号  $\rightarrow$  姓名，学号  $\rightarrow$  系，  
请确定它是否属于BCNF范式？

- ☐ A 它属于BCNF范式
- ☐ B 它不属于BCNF范式

提交

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多选题 1分



## 互动交流二

已知关系模式：学生（学号、姓名、系、系主任）  
它存在的函数依赖是：学号  $\rightarrow$  姓名，学号  $\rightarrow$  系，  
如果将它分解为：R1（学号、姓名、系主任），  
R2（学号、系），R1和R2中存在的函数依赖分别为：

☐ A R1: {学号  $\rightarrow$  姓名}

☐ C R2: {学号  $\rightarrow$  系，系  $\rightarrow$  系主任}

☐ B R1: {学号  $\rightarrow$  姓名，学号  $\rightarrow$  系主任}

☐ D R2: {学号  $\rightarrow$  系主任，学号  $\rightarrow$  系}

提交

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多选题 1分



## 互动交流三

已知关系模式：学生（学号、姓名、系、系主任）  
它存在的函数依赖是：学号  $\rightarrow$  姓名，学号  $\rightarrow$  系，  
如果将它分解为：R1（学号、姓名、系主任），  
R2（学号、系），R1和R2的keys分别为：

☐ A R1的keys: 学号

☐ C R2的keys: 学号

☐ B R1的keys: (学号，系主任)

☐ D R2的keys: (学号，系)

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多选题 1分



## 互动交流四

已知关系模式：学生（学号、姓名、系、系主任）  
它存在的函数依赖是：学号  $\rightarrow$  姓名，学号  $\rightarrow$  系，  
如果将它分解为：R1（学号、姓名、系主任），R2（学号、系、系主任），  
请判断分解后的R1和R2是否属于BCNF范式？

A

R1  $\in$  BCNF 成立

C

R2  $\in$  BCNF 成立

B

R1  $\in$  BCNF 不成立

D

R2  $\in$  BCNF 不成立

提交

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单选题 1分



## 互动交流五

The following three questions refer to a relation R(A, B, C, D, E) with functional dependencies  $A \rightarrow B$ ,  $BC \rightarrow D$ , and  $E \rightarrow C$ .

If we project R onto S(B, C, D, E), which of the following functional dependencies holds in S and also does not violate the BCNF condition for S?

A

$BC \rightarrow D$

B

$BE \rightarrow D$

C

$B \rightarrow E$

D

$E \rightarrow C$

提交

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主观题 10分



## 互动交流六

已知关系模式：学生（学号、姓名、系、系主任）

它存在的函数依赖是：学号  $\rightarrow$  姓名，学号  $\rightarrow$  系，系  $\rightarrow$  系主任

请按照课堂讲授的方法，将其分解为一组满足BCNF范式的关系模式。

提交

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## 往年的期末考题

Consider a relation  $R = (A, B, C, D)$  with FD's  $AB \rightarrow C$ ,  $C \rightarrow D$ , and  $D \rightarrow B$

- List all keys for  $R$ .
- Is  $R$  in BCNF? If yes, briefly explain why. Otherwise,
- Write down two functional dependencies that causes this relation to violate BCNF.
- decompose further until all decomposed relations are in BCNF, and then show your final results.

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