Implementation of SPA

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Chapter 1

Advanced cryptography

Blind signature The blind signature [1] is an extension of the digital signature. It permits to sign a message without revealing the message to the signer. The concept can be hard to understand because it is difficult to guess why a signer would sign a message without knowing it. Let's consider this simple example. Imagine a political party which wants to hold an election. The party wants to authenticate each vote but each elector does not want his vote to be known. The blind signature is a solution to this problem.
In this project, we use a blind signature based on RSA: (N, e) is the public key and (d) is the private key. The idea is to enclose the message using a blind factor r. Since the signer does not know r, he is unable to read the message.
The original message is represented as $m \in \mathbb{Z}_n$ and the signature as s.
First, we add the blind factor $r \in \mathbb{Z}_n^*$ to the message.

$$m' = r^e m \mod N$$

Then, the signer signs the message using its private key.

$$s' = (m')^d \mod N = r^{ed} m^d \mod N = r m^d \mod N$$

Finally, we remove the blind factor using the inverse.

$$s = r^{-1} s' \mod N = r^{-1} r m^d \mod N = m^d \mod N$$

Blinding attack: Nevertheless, the RSA blind signature is not perfect because it is vulnerable to blinding attack. This comes from the fact that RSA uses the same key to sign or to decrypt a message. Let's consider an example where Alice is a server. She has a single private key to sign and to exchange messages. Imagine that Bob sends a message m to Alice using Alice's public key.

$$m' = m^d \mod N$$

Now, imagine that Oscar wants to read this message. If Oscar can intercept the message from Bob, he can send it to Alice by asking to sign it. Since Alice is using her private key to sign a message, Oscar gets the original message of Bob.

$$m = m'^d \mod N = m^{ed} \mod N$$

In other words, Alice decrypt the message when she signs it. The solution to this problem is to use a different key pair for signing and exchanging messages. In this project, we do not use RSA encryption. Therefore, the blinding attack does not concern us.

Oblivious transfer The oblivious transfer is a protocol which permits to exchange data between a client and a server. Let's imagine that the server has n tuples of the form (w_i, c_i), w_i is an index and c_i is the corresponding data. The particularity of this protocol is that the client can retrieve the data c_j from the index w_j without revealing the value w_j to the server and without learning any value c_i with $i \neq j$
We use the oblivious transfer protocol from [2]. Let H be a hash function and G be a random generator. We assume that the server and the client share an RSA key pair (N, e) and (d). The server starts by creating n keys using the indexes w_i.

$$K_i = (H(w_i))^d \mod N$$

Then it uses these keys to encrypt each data c_i in the following way :

$$E_i = G(w_i \| K_i \| i) \oplus (0^l \| c_i)$$

To execute the xor, each part must have the same length. Hence, we add zeros in front of c_i to respect this property. Concretly, l is the length of c_i. Then, the server sends every E_i to the client. Now, let's consider that the client wants to retrieve data for index w_j. Using blind signature, the client is able to reconstruct the key K_j corresponding to w_j. So, using a blind factor r, the client generates:

$$Y = r^e H(w_j) \mod N$$

Then, the client asks the server for a blind signature. This way, the server cannot learn the value w_j choosen. At the end, the client received the value:

$$K_j = r^{ed} H(w_j)^d \mod N = H(w_j)^d \mod N$$

Finally, he can find the corresponding data using:

$$(a_i \| b_i) = E_i \oplus G(w_j \| K_j \| i)$$

If $a_i = 0^l$, b_i corresponds to the data wanted by the client. Since, the client has only one K_j, he can only decrypt the data c_j corresponding to w_j. So, he cannot learn any other value of c_i with $i \neq j$.

Chapter 2

Protocol description

The single password authentication protocol permits a client (Alice) to connect to any website (Bob) using a unique password. The password is used to encrypt a secret stored in an untrusted storage or a trusted mobile device (Carol).

Registration: First, Alice generates a username and a password. When she registers to Bob, she generates a secret key sk. She sends her username and sk to Bob. Then, Alice registers to Carol. She generates an id and she uses her password to encrypt sk. Finally, she sends her id and sk encrypted to Carol. At that point, Alice can only remember her username and her password.

Connection: When Alice wants to connect to Bob, she first needs her username and her password. She uses the username to obtain a challenge from Bob. Then, Alice generates id again and sends it to Carol to recover sk encrypted. Now, Alice can decrypt sk and calculate the response to the challenge. Then Alice sends it to Bob. Finally, Bob verifies the response and accepts the connection if it is correct.

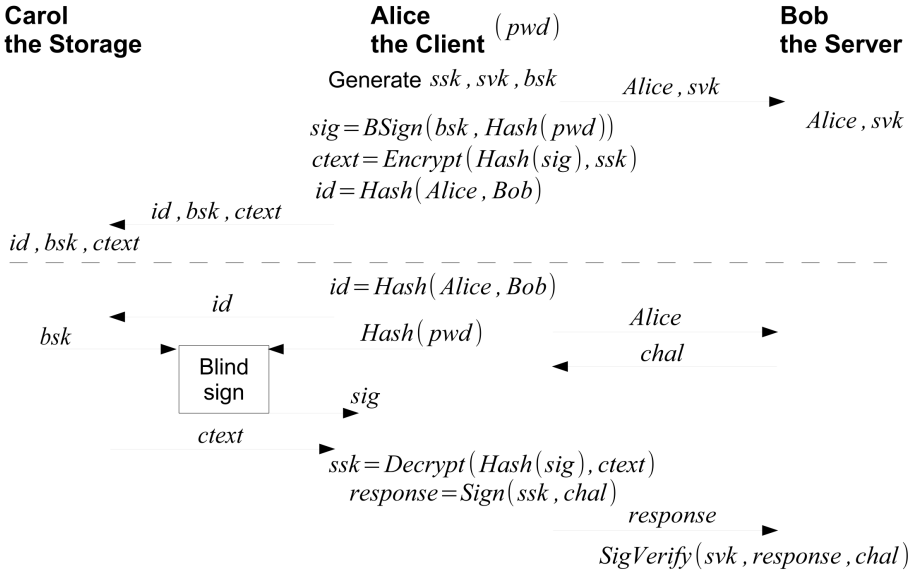
SPA describes four different protocols: server optimal cloud SPA, storage optimal cloud SPA, privacy optimal cloud SPA and mobile SPA.

2.1 Server optimal cloud SPA

Registration: First, Alice generates two RSA key pairs. (ssk, svk) for digital signature used with Bob and (bsk, bvk) for blind signature used with Carol. To register to Bob, Alice sends him her username and svk. Then, to register to Carol, Alice starts by signing her password with bsk to get $sig = BSign(bsk, Hash(password)$. Then, she uses sig to encrypt ssk and to obtain $ctext = Encrypt(Hash(sig), ssk)$. Then, Alice generates an

$id = Hash(Alice, Bob)$. Finally, Alice sends to Carol id, bsk and $ctext$. Now, she can forget everything except her username and her password.

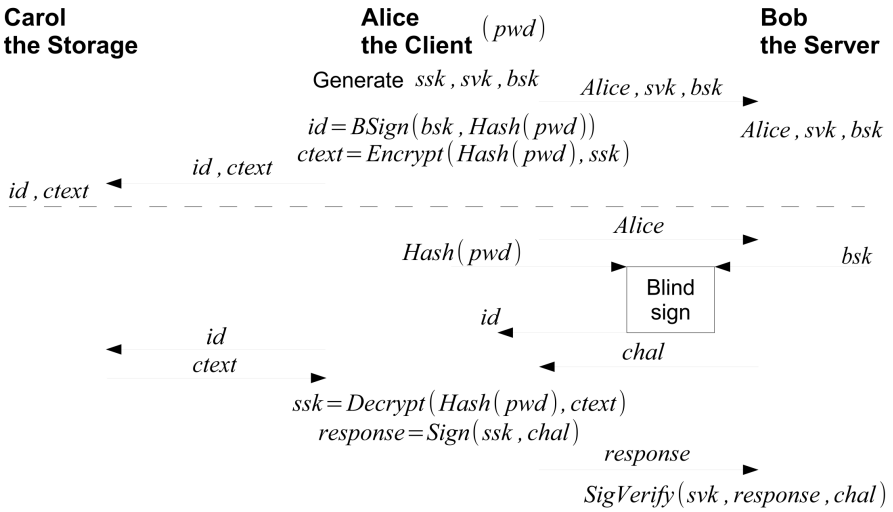
Connection: When Alice wants to connect to Bob, she only sends him her username and gets a challenge. Then, Alice must recover ssk to compute a response. She begins by recovering her id $= Hash(Alice, Bob)$ and sends it to Carol. She asks Carol to sign her password: $sig = BSign(bsk, Hash(password)$. Finally, Carol sends Alice $ctext$. Now that Alice has sig and $ctext$, she can compute $ssk = Decrypt(Hash(sig), ctext)$. Then she can computes the response and sends it to Bob which accepts if it is correct.
This version of the protocol is the most efficient for the server. Unfortunately, Alice is not anonymous to Carol. Alice's username is calculated using $Hash(Alice, Bob)$. So Carol can launch a dictionary attack to find it. Furthermore, Alice is linkable by linking the found username with the id provided.



2.2 Storage optimal cloud SPA

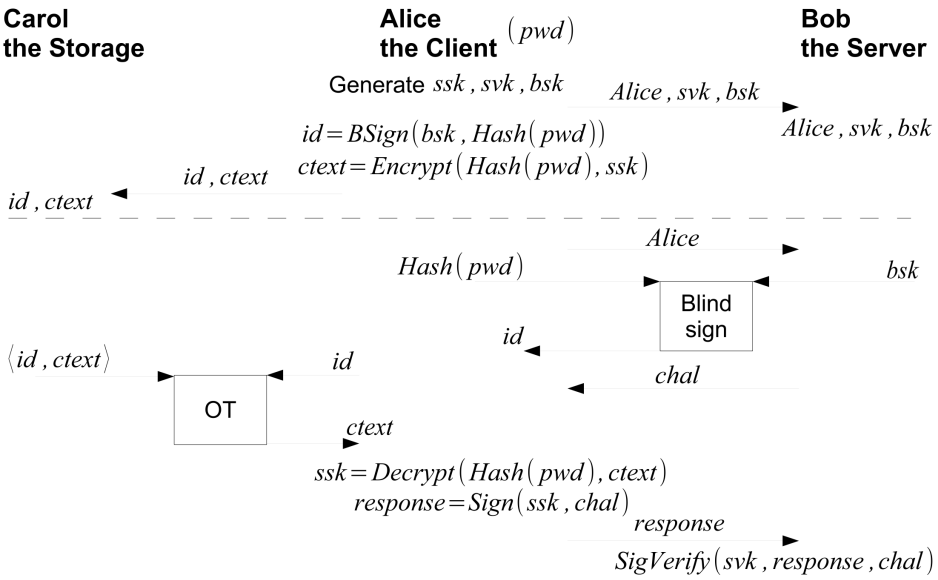
Registration: As Server optimal cloud SPA, Alice first generates two RSA key pairs (ssk, svk) and (bsk, bvk). To register to Bob, Alice sends him the username, svk and bsk. Then, to register to Carol, Alice begins by generating her $id = BSign(bsk, Hash(password))$. Then, she encrypts ssk with her password to get $ctext = Encrypt(Hash(password), ssk)$. Finally, Alice sends id and $ctext$ to Carol.

Connection: When Alice wants to connect to Bob, she first sends him her username. Then she asks Bob to sign her password: $id = BSign(bsk, Hash(password)$. Finally Bob sends Alice a challenge. Then Alice needs ssk to compute the response. Now that she has recovered her id, she sends it to Carol and Carol sends her the corresponding $ctext$. Then, Alice can recover $ssk = Decrypt(Hash(password), ctext)$ and compute $response = Sign(ssk, challenge)$. At the end, Alice sends the response to Bob which accept if it is correct.
This protocol is the most efficient for storage. But this time, Alice's username is a signature, so Alice is anonymous. Unfortunately, Carol still has access to the id, so Alice is still linkable.



2.3 Privacy optimal cloud SPA

Privacy optimal protocol is the same has storage optimal. The only difference is made during the connection. When Alice retrieves $ctext$ from Carol. They use oblivious transfer. This provides unlinkability in addition to anonymity. This protocol provides anonymity to Alice, like storage optimal. Furthermore, Carol never learns the id during a connection. So, Alice is unlinkable.

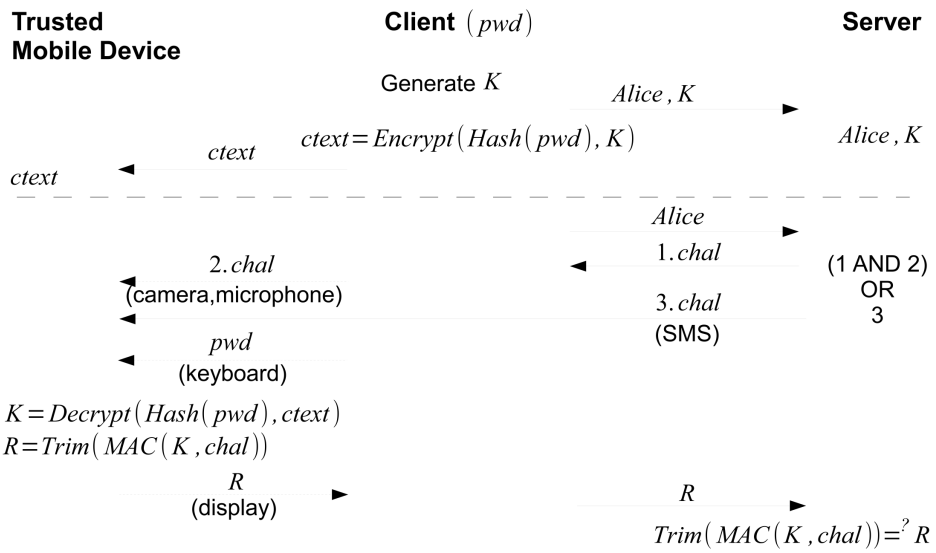


2.4 Mobile SPA

Mobile SPA does not require a cloud storage. It uses a trusted mobile device instead. The name of Carol is kept to describe the mobile device. This protocol requires a connection between Alice and Carol. It can be a direct internet connection (SSL) or an indirect internet connection (Bluetooth, Wi-Fi, USB). Carol must also be able to display and analyze a human-readable information, like a QR code or a sound.

Registration: Alice starts by generating a symmetric key K. To register to Bob, she sends him her username and K. Then, to register to Carol, Alice encrypts K using her password:
$ctext = Encrypt(Hash(password), K)$. Now, Alice can forget everything except her username and her password.

Connection: When Alice wants to connect to Bob, she first sends him her username to get a challenge. This challenge can be send to Alice (QR code or audio file) or directly to Carol (SMS). If the challenge is sent to Alice, she uses her mobile device to read it. Then, Alice provides her password to Carol. Now, Carol can recover
$K = Decrypt(Hash(password), ctext)$ and computes the response
$R = MAC(K, challenge)$). Carol shortens the response using a $TRIM$ function and displays it to Alice. Now, Alice can provide R to Bob which verifies it and accept the connection if it is correct.


Trusted Mobile Device
Client (pwd)
Server
Generate K
Alice, K
ctext = Encrypt(Hash(pwd), K)
Alice, K
ctext
ctext
Alice
1. chal
(1 AND 2) OR 3
2. chal
(camera,microphone)
3. chal
(SMS)
pwd
(keyboard)
K = Decrypt(Hash(pwd), ctext)
R = Trim(MAC(K, chal))
R
(display)
R
Trim(MAC(K, chal)) =? R

Chapter 3

Implementation

3.1 Cryptography library

Symmetric algorithms The first type of algorithms implemented is contained in the SymmetricEncryption.java class. It implements functions to encrypt, decrypt or MAC a given message using a symmetric key. The first implemented algorithm is AES256, this implementation is made using a java library [3]. Nevertheless, AES256 requires many calculations. Therefore, the second implemented algorithm is one time padding encryption. It is very fast since it uses one xor operation. It also gives perfect security because:
-We use uniformly ditributed random key
-Every message in SPA protocol is encrypted with a new key
-The key size and the message size are the same.
Note that we could use AES256 for the encryption but in terms of efficiency, we preferred to use one-time padding. Regarding MAC, the implemented algorithm is HMacSHA256. It generates MAC efficiently and in a very secured way.

Asymmetric algorithms The second type of algorithms implemented are contained in AsymmetricEncryption.java class. This class only implements RSA. The choice of this algorithm comes from the fact that blind signature can be based on it. So, the class contains functions to encrypt, decrypt, sign and verify the signature of a message. It also implements functions for blind signature: generating a random blind factor, blind and unblind a message. Like, SymmetricEncryption.java, there exist libraries [3] to implement these functions. Nevertheless, I prefer to make my own implementation. It makes the code more readable and it permits to understand in details how blind signature is implemented.

Key generation: Encryption can be relatively easy to implement, but key generation is more sophisticated. Therefore, I decided to generate keys using the existing java libraries [3] in MyKeyGenerator.java class. So, the generation is secured and efficient. Concretly, AES, RSA and HMacSHA256 keys are generated using theses libraries. One time padding key is generated using a secure random generator [4]. Each key can be generated in three ways: from random, from a password or into a file. Note that RSA key generation from a password is not necessary in this project. Hence, it is not implemented.

Hash The class Hash.java implements SHA256 using java libraries [3]. SHA256 provides the right balance between security and performance.

Oblivious transfer Since oblivious tranfer is used by a server and a client. I did not choose to create a static library. I created two objects OTSender and OTReceiver which can be instantiated by a server and a client to execute the oblivious transfer protocol. OTSender needs a Map with w_i the keys and c_i the corresponding data. It also requires an RSAPrivateKey. OTSender automatically generates the keys K_i. Then it provides two functions. One to encrypt the data using K_i by generating E_i and one to generate K_j from the index Y received from the client. OTReceiver needs an index w_j and an RSAPublicKey to be instantiated. Then it provides four additional functions. The first one blinds the index using a given blind factor r to generate Y. The second one unblind the value K_j received by the server. The third one is used to decrypt the data E_i received by server using K_j. And finally, the last one checks the data generated during the decryption to find and return the corresponding value.

3.2 Database

Database connection After implementing the necessary cryptographic components, the next step was to find an efficient database for the storage. This database must have many properties. It must be free, fast and it must offer a performance report. I chose to use the SQL database of the Microsoft Azure plateform [5]. It is free for academic purposes [6]. It is fast because their servers are available in Europe. Furthermore, their platform automatically provides many statistics about the database. The only disadvantage is the storage size since there is only 35 MB available. In the concern of this project, it is enough, since any user store only a small amount of data.

The implementation has two parts: SQL and java. The SQL part means tables creation and testing queries. I created two tables.

Storage_server_optimal for the server optimal protocol. It contains three columns (id, bsk and ctext), each one has type varbinary(256) to store 2048 bits:

id	bsk	ctext
0x582A749BFF...	0x80128461BB...	0x4816B4F323...
0x769398B3F3...	0x68154A3FF1...	0x729BA5BB72...

Storage_storage_optimal for storage optimal and privacy optimal protocols. It contains two columns (id, ctext), each one is also of type varbinary(256):

id	ctext
0x549748104A...	0x6381036A24...
0x32F38BA233...	0x67C7471B31...

The SQL code can be found in the SQLCommands.txt file.
The java implementation is done using the JDBC library [7] created by Oracle and modified by Microsoft for their database. I provide database connection with an object written in the DatabaseConnector.java class. When the object is instantiated, the user provides which protocol he uses and then the corresponding connection is automatically created with the database. Then, I provide functions to execute SQL queries: insertion, search and deletion. For privacy optimal protocol, I also provide a function to fetch every elements of the table in a random order.

Chapter 4

References

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