Graph Contrastive Learning Automated

Yuning You¹, Tianlong Chen², Yang Shen¹, Zhangyang Wang²

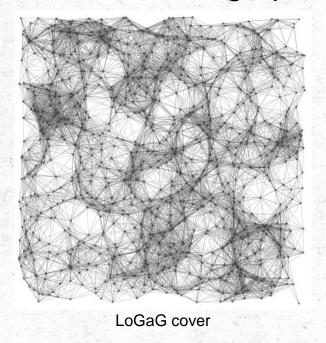
¹Texas A&M University, ²University of Texas at Austin



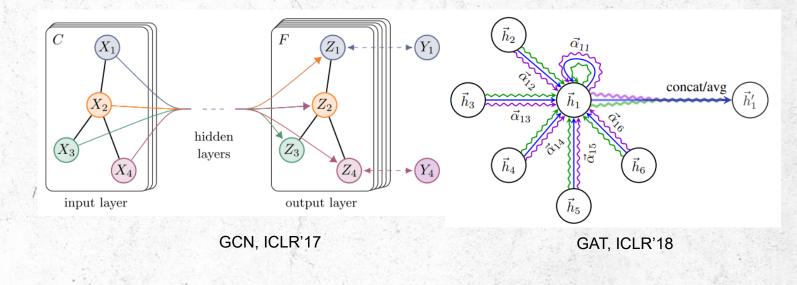
The Learning on Graphs and Geometry Reading Group (LoGaG) Presentation August 17, 2021



Data-structure of graphs



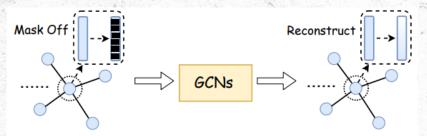
Graph networks



> Self-supervised learning: Warming-up models with unlabeled data



- > Self-supervision on graphs
 - Predictive task

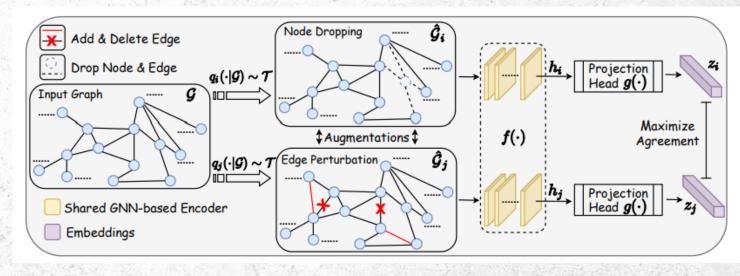


E.g. Graph completion, ICML'20 AutoSSL, arXiv'21

- Contrastive learning
 - GraphCL, NeurIPS'20
 - Augmentations + perturbation invariance

Self-Supervised Learning of Graph Neural Networks: A Unified Review

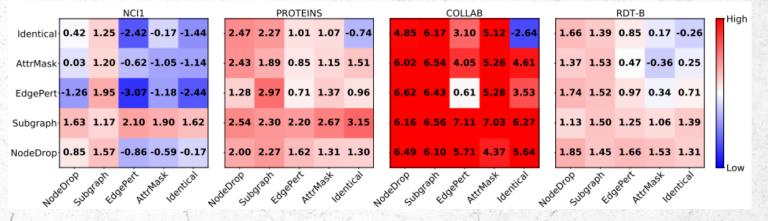
Yaochen Xie, Zhao Xu, Jingtun Zhang, Zhengyang Wang, Shuiwang Ji, Senior Member, IEEE





> Augmentation is crucial in GraphCL

| Data augmentation | Type | Underlying Prior |
|-------------------|--------------|--|
| Node dropping | Nodes, edges | Vertex missing does not alter semantics. |
| Edge perturbation | Edges | Semantic robustness against connectivity variations. |
| Attribute masking | Nodes | Semantic robustness against losing partial attributes. |
| Subgraph | Nodes, edges | Local structure can hint the full semantics. |



> Reason: challenge of heterogeneous nature of graph data



Fig 2. Polymers

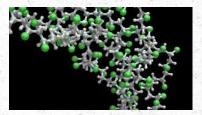


Fig 3. Power grids



Data heterogeneity







> Ad-hoc choices of augmentations in GraphCL

| | Data augmentation | Type | Underlying Prior | | | | | |
|----|----------------------------|--------------|--|--|--|--|--|--|
| | Node dropping Nodes, edges | | Vertex missing does not alter semantics. | | | | | |
| 1 | Edge perturbation | Edges | Semantic robustness against connectivity variations. | | | | | |
| 1 | Attribute masking | Nodes | Semantic robustness against losing partial attributes. | | | | | |
| Ĭ. | Subgraph | Nodes, edges | Local structure can hint the full semantics. | | | | | |

> Rules derived from tedious tuning

| | | | NCI1 | | | | | PF | ROTEIN | IS | | | | (| COLLAE | 3 | | | | | RDT-B | | | | ligh |
|-----------|------------|------------|---------------|-----------|---------|------|------------|-----------|-----------|------|--------|------|--------------|-----------|------------|------|--------|------|-----------|-----------|------------|-------|--------|-----|------|
| Identical | 0.42 | 1.25 | -2.42 | -0.17 | -1.44 | | 2.47 | 2.27 | 1.01 | 1.07 | -0.74 | | 4.85 | 6.17 | 3.10 | 5.12 | -2.64 | | 1.66 | 1.39 | 0.85 | 0.17 | -0.26 | | igii |
| AttrMask | 0.03 | 1.20 | -0.62 | -1.05 | -1.14 | | 2.43 | 1.89 | 0.85 | 1.15 | 1.51 | | 6.02 | 6.54 | 4.05 | 5.26 | 4.61 | | 1.37 | 1.53 | 0.47 | -0.36 | 0.25 | | |
| EdgePert | -1.26 | 1.95 | -3.07 | -1.18 | -2.44 | | 1.28 | 2.97 | 0.71 | 1.37 | 0.96 | | 6.62 | 6.43 | 0.61 | 5.28 | 3.53 | | 1.74 | 1.52 | 0.97 | 0.34 | 0.71 | | |
| Subgraph | 1.63 | 1.17 | 2.10 | 1.90 | 1.62 | | 2.54 | 2.30 | 2.20 | 2.67 | 3.15 | | 6.16 | 6.56 | 7.11 | 7.03 | 6.27 | | 1.13 | 1.50 | 1.25 | 1.06 | 1.39 | | |
| NodeDrop | 0.85 | 1.57 | -0.86 | -0.59 | -0.17 | | 2.00 | 2.27 | 1.62 | 1.31 | 1.30 | | 6.49 | 6.10 | 5.71 | 4.37 | 5.64 | | 1.85 | 1.45 | 1.66 | 1.53 | 1.31 | L., | |
| 406 | seDrop Sub | diable Eq. | gePerk Att | SMask Ide | intical | Mode | EDrop Subf | alaby Equ | ePerk Att | Mast | ntical | Mog. | eDrop Sub | graph Edi | gePerk Att | Mask | ntical | Hode | EDrop Sub | alaby Equ | gePerk Att | Mast | ntical | -10 | ow |

Question: Can we be more principled and automated?

Contributions



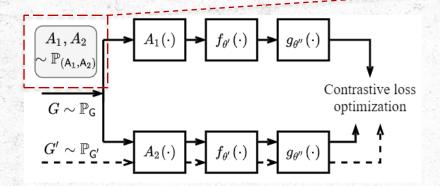
➤ Given a new and unseen graph dataset, can GraphCL automatically select augmentations, avoiding ad-hoc choices or tedious tuning?

- > Joint augmentation optimization (JOAO)
 - * A principled bi-level optimization framework
 - * Automatic, free of human labor of trial-and-error
 - * Adaptive, generalizing smoothly to handling diverse graph data
 - Dynamic, allowing for augmentation types varying at different steps

Method. JOAO

TEXAS
The University of Texas at Austin

- > GraphCL
 - Enforcing perturbation invariance



$$\begin{split} & \min_{\theta} \, \mathcal{L}(\mathsf{G}, \mathsf{A}_{1}, \mathsf{A}_{2}, \theta) \\ &= \min_{\theta} \, \Big\{ (-\mathbb{E}_{\mathbb{P}_{\mathsf{G}} \times \mathbb{P}_{(\mathsf{A}_{1}, \mathsf{A}_{2})}} \mathrm{sim}(\overleftarrow{\mathsf{T}_{\theta, 1}(\mathsf{G})}, \mathsf{T}_{\theta, 2}(\mathsf{G})) \\ &+ \mathbb{E}_{\mathbb{P}_{\mathsf{G}} \times \mathbb{P}_{\mathsf{A}_{1}}} \mathrm{log}(\mathbb{E}_{\mathbb{P}_{\mathsf{G}'} \times \mathbb{P}_{\mathsf{A}_{2}}} \mathrm{exp}(\mathrm{sim}(\underbrace{\mathsf{T}_{\theta, 1}(\mathsf{G})}, \mathsf{T}_{\theta, 2}(\mathsf{G}')))) \Big\}, \end{split}$$

➤ The unified framework, joint augmentation optimization (JOAO) as a bi-level optimization

$$\begin{aligned} & \min_{\theta} \ \mathcal{L}(\mathsf{G}, \mathsf{A}_1, \mathsf{A}_2, \theta), \\ & \text{s.t.} \ \boxed{\mathbb{P}_{(\mathsf{A}_1, \mathsf{A}_2)}} \in & \arg\min_{\mathbb{P}_{(\mathsf{A}_1', \mathsf{A}_2')}} \mathcal{D}(\mathsf{G}, \mathsf{A}_1', \mathsf{A}_2', \theta), \end{aligned} \tag{2}$$

Method. Instantiation of JOAO



> A min-max optimization instantiation

$$\min_{\theta} \quad \mathcal{L}(\mathsf{G}, \mathsf{A}_{1}, \mathsf{A}_{2}, \theta),$$
s.t.
$$\mathbb{P}_{(\mathsf{A}_{1}, \mathsf{A}_{2})} \in \arg\max_{\mathbb{P}_{(\mathsf{A}'_{1}, \mathsf{A}'_{2})}} \left\{ \mathcal{L}(\mathsf{G}, \mathsf{A}'_{1}, \mathsf{A}'_{2}, \theta) \right\}$$

$$-\frac{\gamma}{2} \operatorname{dist}(\mathbb{P}_{(\mathsf{A}'_{1}, \mathsf{A}'_{2})}, \mathbb{P}_{\operatorname{prior}}) ,$$
(3)

> Principles

MBRDL, arXiv'i20

- Exploiting challenging augmentations: model-based adversarial training
- * Regularization with prior
 - Uniform distribution avoiding collapse
 - Squared Euclidean distance
 Ref 5. Wang et al., arXiv'19
- \clubsuit Trade-off by γ

$$\operatorname{dist}(\mathbb{P}_{(\mathsf{A}_1,\mathsf{A}_2)},\mathbb{P}_{\operatorname{prior}}) = \sum_{i=1}^{|\mathcal{A}|} \sum_{j=1}^{|\mathcal{A}|} (p_{ij} - \frac{1}{|\mathcal{A}|^2})^2,$$
$$p_{ij} = \operatorname{Prob}(\mathsf{A}_1 = A^i, \mathsf{A}_2 = A^j)$$



- > Alternating gradient descent (AGD) Wang et al., arXiv'19
 - Upper-level minimization
 - Lower-lever maximization

$$\begin{aligned} \min_{\theta} \quad \mathcal{L}(\mathsf{G},\mathsf{A}_{1},\mathsf{A}_{2},\theta), \\ \text{s.t.} \quad & \mathbb{P}_{(\mathsf{A}_{1},\mathsf{A}_{2})} \in \arg\max_{\mathbb{P}_{(\mathsf{A}_{1}',\mathsf{A}_{2}')}} \Big\{ \mathcal{L}(\mathsf{G},\mathsf{A}_{1}',\mathsf{A}_{2}',\theta) \\ & \qquad \qquad - \frac{\gamma}{2} \operatorname{dist}(\mathbb{P}_{(\mathsf{A}_{1}',\mathsf{A}_{2}')},\mathbb{P}_{\operatorname{prior}}) \Big\}, \end{aligned} \tag{3}$$

- Upper-level minimization
 - GraphCL optimization given sampling distribution

$$\theta^{(n)} = \theta^{(n-1)} - \alpha' \nabla_{\theta} \mathcal{L}(\mathsf{G}, \mathsf{A}_1, \mathsf{A}_2, \theta), \tag{4}$$

where $\alpha' \in \mathcal{R}_{>0}$ is the learning rate.



- Lower-level maximization
 - Gradient is not intuitive
 - Analytical rewrite

$$\mathcal{L}(\mathsf{G}, \mathsf{A}_{1}, \mathsf{A}_{2}, \theta) = \sum_{i=1}^{|\mathcal{A}|} \sum_{j=1}^{|\mathcal{A}|} \underbrace{p_{ij}}^{\text{Targeted}} \left\{ -\mathbb{E}_{\mathbb{P}_{\mathsf{G}}} \mathrm{sim}(T_{\theta}^{i}(\mathsf{G}), T_{\theta}^{j}(\mathsf{G})) + \mathbb{E}_{\mathbb{P}_{\mathsf{G}}} \log(\sum_{j'=1}^{|\mathcal{A}|} \underbrace{p_{j'}}_{\text{Undesired}} \mathbb{E}_{\mathbb{P}_{\mathsf{G}'}} \exp(\mathrm{sim}(T_{\theta}^{i}(\mathsf{G}), T_{\theta}^{j'}(\mathsf{G}')))) \right\},$$
(5)

$$\begin{split} \min_{\theta} \quad & \mathcal{L}(\mathsf{G},\mathsf{A}_1,\mathsf{A}_2,\theta), \\ \text{s.t.} \quad & \mathbb{P}_{(\mathsf{A}_1,\mathsf{A}_2)} \in \arg\max_{\mathbb{P}_{(\mathsf{A}_1',\mathsf{A}_2')}} \Big\{ \mathcal{L}(\mathsf{G},\mathsf{A}_1',\mathsf{A}_2',\theta) \\ & \qquad \qquad - \frac{\gamma}{2} \operatorname{dist}(\mathbb{P}_{(\mathsf{A}_1',\mathsf{A}_2')},\mathbb{P}_{\operatorname{prior}}) \Big\}, \end{split} \tag{3}$$

Undesired marginal probability $p_{j'}$ entangled in negative term



A lower-bound approximation to decouple $p_{j'}$

$$\begin{split} &\mathbb{E}_{\mathbb{P}_{\mathsf{G}} \times \mathbb{P}_{\mathsf{A}_{1}}} \log(\mathbb{E}_{\mathbb{P}_{\mathsf{G}'} \times \mathbb{P}_{\mathsf{A}_{2}}} \exp(\sin(\mathsf{T}_{\theta,1}(\mathsf{G}),\mathsf{T}_{\theta,2}(\mathsf{G}')))) \\ & \geq \mathbb{E}_{\mathbb{P}_{\mathsf{G}} \times \mathbb{P}_{\mathsf{A}_{1}} \times \mathbb{P}_{\mathsf{A}_{2}}} \log(\mathbb{E}_{\mathbb{P}_{\mathsf{G}'}} \exp(\sin(\mathsf{T}_{\theta,1}(\mathsf{G}),\mathsf{T}_{\theta,2}(\mathsf{G}')))) \\ & \approx \mathbb{E}_{\mathbb{P}_{\mathsf{G}} \times \mathbb{P}_{(\mathsf{A}_{1},\mathsf{A}_{1})}} \log(\mathbb{E}_{\mathbb{P}_{\mathsf{G}'}} \exp(\sin(\mathsf{T}_{\theta,1}(\mathsf{G}),\mathsf{T}_{\theta,2}(\mathsf{G}')))), \end{split} \tag{6}$$

$$\begin{split} \min_{\theta} \quad \mathcal{L}(\mathsf{G},\mathsf{A}_{1},\mathsf{A}_{2},\theta), \\ \text{s.t.} \quad \mathbb{P}_{(\mathsf{A}_{1},\mathsf{A}_{2})} \in \arg\max_{\mathbb{P}_{(\mathsf{A}_{1}',\mathsf{A}_{2}')}} \Big\{ \mathcal{L}(\mathsf{G},\mathsf{A}_{1}',\mathsf{A}_{2}',\theta) \\ &\quad - \frac{\gamma}{2} \operatorname{dist}(\mathbb{P}_{(\mathsf{A}_{1}',\mathsf{A}_{2}')},\mathbb{P}_{\operatorname{prior}}) \Big\}, \end{split} \tag{3}$$

Approximated contrastive loss:

$$\mathcal{L}(\mathsf{G}, \mathsf{A}_{1}, \mathsf{A}_{2}, \theta) \approx \sum_{i=1}^{|\mathcal{A}|} \sum_{j=1}^{|\mathcal{A}|} \underbrace{p_{ij}}^{\text{Targeted}} \ell(\mathsf{G}, A^{i}, A^{j}, \theta)$$

$$= \sum_{i=1}^{|\mathcal{A}|} \sum_{j=1}^{|\mathcal{A}|} p_{ij} \Big\{ - \mathbb{E}_{\mathbb{P}_{\mathsf{G}}} \mathrm{sim}(T_{\theta}^{i}(\mathsf{G}), T_{\theta}^{j}(\mathsf{G}))$$

$$+ \mathbb{E}_{\mathbb{P}_{\mathsf{G}}} \log(\mathbb{E}_{\mathbb{P}_{\mathsf{G}'}} \exp(\mathrm{sim}(T_{\theta}^{i}(\mathsf{G}), T_{\theta}^{j}(\mathsf{G}')))) \Big\}. \tag{7}$$



Rewrote lower-level optimization

$$\mathbb{P}_{(\mathsf{A}_{1},\mathsf{A}_{2})} \in \arg\max_{\boldsymbol{p}\in\mathcal{P},\boldsymbol{p}=[p_{ij}],i,j=1,...,|\mathcal{A}|} \{\psi(\boldsymbol{p})\},$$

$$\psi(\boldsymbol{p}) = \sum_{i=1}^{|\mathcal{A}|} \sum_{j=1}^{|\mathcal{A}|} p_{ij} \ell(\mathsf{G}, A^{i}, A^{j}, \theta) - \frac{\gamma}{2} \sum_{i=1}^{|\mathcal{A}|} \sum_{j=1}^{|\mathcal{A}|} (p_{ij} - \frac{1}{|\mathcal{A}|^{2}})^{2},$$
(8)

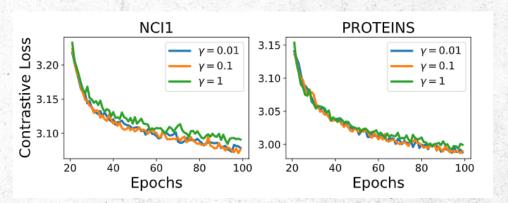
$$\begin{aligned} \min_{\theta} \quad \mathcal{L}(\mathsf{G}, \mathsf{A}_{1}, \mathsf{A}_{2}, \theta), \\ \text{s.t.} \quad \mathbb{P}_{(\mathsf{A}_{1}, \mathsf{A}_{2})} \in \arg \max_{\mathbb{P}_{(\mathsf{A}_{1}', \mathsf{A}_{2}')}} \Big\{ \mathcal{L}(\mathsf{G}, \mathsf{A}_{1}', \mathsf{A}_{2}', \theta) \\ &\quad - \frac{\gamma}{2} \operatorname{dist}(\mathbb{P}_{(\mathsf{A}_{1}', \mathsf{A}_{2}')}, \mathbb{P}_{\operatorname{prior}}) \Big\}, \end{aligned} \tag{3}$$

Projected gradient descent Boyd et al., 2004

$$b = p^{(n-1)} + \alpha'' \nabla_p \psi(p^{(n-1)}), p^{(n)} = (b - \mu \mathbf{1})_+, (9)$$

where $\alpha'' \in \mathcal{R}_{>0}$ is the learning rate, μ is the root of the equation $\mathbf{1}^{\mathsf{T}}(\boldsymbol{b} - \mu \mathbf{1}) = 1$, and $(\cdot)_+$ is the element-wise non-negative operator. μ can be efficiently found via the bi-jection method.

Empirical convergence

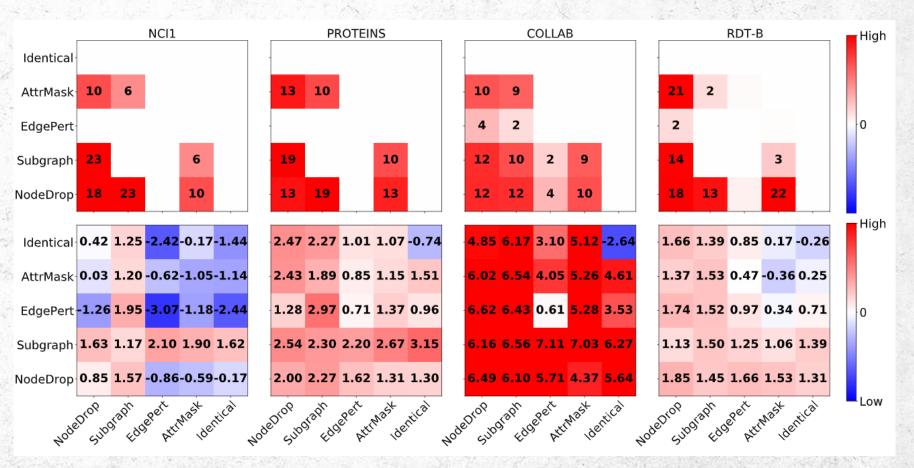


Method. JOAO Sanity Check



> Are JOAO selected augmentation reasonable?

Selections align with "best practices"



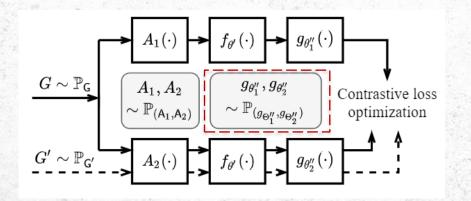
Method. JOAOv2 Addressing Distortion



- > JOAO selects automatic, adaptive and dynamic augmentations
- > However, more diverse, aggressive and challenging
- ➤ Potentially distorting training distribution SLA+AG, ICML'20 DistAug, ICML'20

| Datasets | A.S. | JOAO | JOAOv2 |
|----------|------|------------------|------------------|
| NCI1 | 0.2 | 61.77±1.61 | 62.52 ± 1.16 |
| NCII | 0.25 | 60.95 ± 0.55 | 61.67 ± 0.72 |
| PROTEINS | 0.2 | 71.45±0.89 | 71.66±1.10 |
| FROTEINS | 0.25 | 71.61 ± 1.65 | 73.01 ± 1.02 |
| | | | |

> JOAOv2 = JOAO + augmentation-aware multi-projection heads



$$\min_{\theta} \quad \mathcal{L}_{v2}(\mathsf{G}, \mathsf{A}_{1}, \mathsf{A}_{2}, \theta', \Theta_{1}'', \Theta_{2}''),$$
s.t.
$$\mathbb{P}_{(\mathsf{A}_{1}, \mathsf{A}_{2})} \in \arg\max_{\mathbb{P}_{(\mathsf{A}_{1}', \mathsf{A}_{2}')}} \left\{ \mathcal{L}_{v2}(\mathsf{G}, \mathsf{A}_{1}, \mathsf{A}_{2}, \theta', \Theta_{1}'', \Theta_{2}'') - \frac{\gamma}{2} \operatorname{dist}(\mathbb{P}_{(\mathsf{A}_{1}', \mathsf{A}_{2}')}, \mathbb{P}_{\operatorname{prior}}) \right\},$$

$$\mathbb{P}_{(g_{\Theta_{1}''}, g_{\Theta_{2}''})} = \mathbb{P}_{(\mathsf{A}_{1}, \mathsf{A}_{2})}. \tag{10}$$

Experiments & Discussions



- Settings
 - Semi-supervised
 - Unsupervised
 - Transfer

- Datasets
 - Across diverse fields
 - On bioinformatics domains

- Competitors
 - Heuristic designed pretexts
 - GraphCL with rules

Summary of JOAO performance

| | v.s. GraphCL | v.s. Heuristic methods |
|-----------------------|--------------|------------------------|
| Across diverse fields | Comparable | Better |
| On specific domains | Better | Worse |

Experiments & Discussions. Across Diverse Datasets



JOAO performs on par with ad-hoc rules

Augmentation-aware projection heads strengths JOAO

Semi-supervised learning

| L.R. | Methods | NCI1 | PROTEINS | DD | COLLAB | RDT-B | RDT-M5K | GITHUB | A.R.↓ |
|------|---------------|--------------------|--|--------------------|---------------------------|--------------------|--------------------|----------------------|-------|
| 1% | No pre-train. | 60.72±0.45 | - | - | 57.46±0.25 | - | - | 54.25±0.22 | 7.6 |
| | Augmentations | 60.49±0.46 | - | - | 58.40±0.97 | - | - | 56.36 ± 0.42 | 6.6 |
| | GAE | 61.63±0.84 | | | $63.\overline{20}\pm0.67$ | | | 59.44 ± 0.44 | 4.0 |
| | Infomax | 62.72 ±0.65 | - | - | 61.70±0.77 | - | - | 58.99 ± 0.50 | 3.3 |
| | ContextPred | 61.21±0.77 | | | 57.60±2.07 | | | 56.20 ± 0.49 | 6.6 |
| | GraphCL | 62.55 ±0.86 | | - | 64.57 ±1.15 | - | <u>-</u> | 58.56 ± 0.59 | 2.6 |
| [] | JOAO | 61.97±0.72 | - | | 63.71 ±0.84 | | - | 60.35 ± 0.24 | 3.0 |
| | JOAOv2 | 62.52 ±1.16 | - | | 64.51 ±2.21 | - | - | 61.05 ±0.31 | 2.0 |
| 10% | No pre-train. | 73.72 ± 0.24 | 70.40 ± 1.54 | 73.56 ± 0.41 | 73.71±0.27 | 86.63±0.27 | 51.33±0.44 | 60.87±0.17 | 7.0 |
| | Augmentations | 73.59 ± 0.32 | 70.29 ± 0.64 | 74.30 ± 0.81 | 74.19 ± 0.13 | 87.74 ± 0.39 | 52.01 ± 0.20 | 60.91 ± 0.32 | 6.2 |
| | GĀĒ | 74.36±0.24 | $70.\overline{5}1\pm0.\overline{17}$ | 74.54 ± 0.68 | 75.09 ± 0.19 | 87.69 ± 0.40 | 53.58 ±0.13 | $6\bar{3}.89\pm0.52$ | 4.5 |
| | Infomax | 74.86 ±0.26 | 72.27 ± 0.40 | 75.78 ± 0.34 | 73.76±0.29 | 88.66 ± 0.95 | 53.61 ± 0.31 | 65.21 ± 0.88 | 3.0 |
| | ContextPred | 73.00 ± 0.30 | 70.23 ± 0.63 | 74.66 ± 0.51 | 73.69 ± 0.37 | 84.76 ± 0.52 | 51.23 ± 0.84 | 62.35 ± 0.73 | 7.2 |
| | GraphCL | 74.63 ±0.25 | 74.17 ± 0.34 | 76.17 ± 1.37 | 74.23 ± 0.21 | 89.11 ±0.19 | 52.55 ± 0.45 | 65.81 ± 0.79 | 2.4 |
| | JOAO | 74.48 ± 0.27 | $7\overline{2}.\overline{13}\pm\overline{0}.\overline{92}$ | 75.69 ±0.67 | 75.30 ± 0.32 | 88.14±0.25 | 52.83 ± 0.54 | 65.00 ± 0.30 | 3.5 |
| | JOAOv2 | 74.86 ±0.39 | 73.31 ± 0.48 | 75.81 ± 0.73 | 75.53 ±0.18 | 88.79 ± 0.65 | 52.71 ± 0.28 | 66.66 ±0.60 | 1.8 |
| | | | | | | | | | |

Unsupervised learning

| Methods | NCI1 | PROTEINS | DD | MUTAG | COLLAB | RDT-B | RDT-M5K | IMDB-B | A.R.↓ |
|-----------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|-------|
| GL | - | - | - | 81.66±2.11 | - | 77.34 ± 0.18 | 41.01 ± 0.17 | 65.87 ± 0.98 | 7.4 |
| WL | 80.01 ±0.50 | 72.92 ± 0.56 | - | 80.72 ± 3.00 | - | 68.82 ± 0.41 | 46.06 ± 0.21 | 72.30 ± 3.44 | 5.7 |
| DGK | 80.31 ±0.46 | 73.30 ± 0.82 | - | 87.44 ± 2.72 | - | 78.04 ± 0.39 | 41.27 ± 0.18 | 66.96 ± 0.56 | 4.9 |
| node2vec | 54.89±1.61 | 57.49±3.57 | - | 72.63 ± 10.20 | - | - | - | - | 8.6 |
| sub2vec | 52.84 ± 1.47 | 53.03 ± 5.55 | - | 61.05 ± 15.80 | - | 71.48 ± 0.41 | 36.68 ± 0.42 | 55.26 ± 1.54 | 9.5 |
| graph2vec | 73.22 ± 1.81 | 73.30 ± 2.05 | - | 83.15 ± 9.25 | - | 75.78 ± 1.03 | 47.86 ± 0.26 | 71.10 ± 0.54 | 5.7 |
| MVGRL | - | - | - | 75.40 ± 7.80 | - | 82.00 ± 1.10 | - | 63.60 ± 4.20 | 7.2 |
| InfoGraph | 76.20 ± 1.06 | 74.44 ±0.31 | 72.85 ± 1.78 | 89.01 ±1.13 | 70.65±1.13 | 82.50 ± 1.42 | 53.46 ± 1.03 | 73.03 ±0.87 | 3.0 |
| GraphCL | 77.87 ± 0.41 | 74.39 ± 0.45 | 78.62 ±0.40 | 86.80 ± 1.34 | 71.36±1.15 | 89.53 ±0.84 | 55.99±0.28 | 71.14 ±0.44 | 2.6 |
| JOAO | 78.07 ±0.47 | 74.55 ±0.41 | 77.32 ±0.54 | 87.35 ±1.02 | 69.50 ±0.36 | 85.29 ±1.35 | 55.74 ±0.63 | 70.21±3.08 | 3.3 |
| JOAOv2 | 78.36 ± 0.53 | 74.07 ± 1.10 | 77.40 ±1.15 | 87.67 ±0.79 | 69.33±0.34 | 86.42±1.45 | 56.03 ±0.27 | 70.83 ± 0.25 | 2.8 |

Experiments & Discussions. Across Diverse Datasets



Semi-supervised learning

| L.R. | Methods | NCI1 | PROTEINS | DD | COLLAB | RDT-B | RDT-M5K | GITHUB | A.R.↓ |
|------|---------------|--------------------|----------------------------|--------------------|--------------------|--------------------|------------------|--------------------|-------|
| 1% | No pre-train. | 60.72±0.45 | - | - | 57.46±0.25 | - | - | 54.25 ± 0.22 | 7.6 |
| | Augmentations | 60.49±0.46 | - | - | 58.40±0.97 | - | - | 56.36 ± 0.42 | 6.6 |
| | GAE | 61.63 ± 0.84 | - | - | 63.20±0.67 | - | - | 59.44 ± 0.44 | 4.0 |
| 1 | Infomax | 62.72 ±0.65 | - | - | 61.70±0.77 | - | - | 58.99 ± 0.50 | 3.3 |
| L | ContextPred | 61.21 ± 0.77 | | | 57.60±2.07 | | | 56.20 ± 0.49 | 6.6 |
| | GraphCL | 62.55 ± 0.86 | - | | 64.57 ±1.15 | | - | 58.56 ± 0.59 | 2.6 |
| | JOAO | 61.97 ± 0.72 | | | 63.71 ±0.84 | - | - | 60.35 ± 0.24 | 3.0 |
| | JOAOv2 | 62.52 ±1.16 | - | - | 64.51 ±2.21 | - | - | 61.05 ± 0.31 | 2.0 |
| 10% | No pre-train. | 73.72 ± 0.24 | 70.40 ± 1.54 | 73.56 ± 0.41 | 73.71 ± 0.27 | 86.63 ± 0.27 | 51.33 ± 0.44 | 60.87 ± 0.17 | 7.0 |
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| | GAE | 74.36 ± 0.24 | 70.51 ± 0.17 | 74.54 ± 0.68 | 75.09±0.19 | 87.69 ± 0.40 | 53.58 ± 0.13 | 63.89 ± 0.52 | 4.5 |
| 1 | Infomax | 74.86 ±0.26 | 72.27 ± 0.40 | 75.78 ± 0.34 | 73.76±0.29 | 88.66 ± 0.95 | 53.61 ± 0.31 | 65.21 ± 0.88 | 3.0 |
| L. | ContextPred | 73.00 ± 0.30 | 70.23 ± 0.63 | 74.66 ± 0.51 | 73.69 ± 0.37 | 84.76 ± 0.52 | 51.23 ± 0.84 | 62.35 ± 0.73 | 7.2 |
| | GraphCL | 74.63 ± 0.25 | 74.17 ± 0.34 | 76.17 ± 1.37 | 74.23 ± 0.21 | 89.11 ±0.19 | 52.55 ± 0.45 | 65.81 ± 0.79 | 2.4 |
| | JOAO | 74.48 ± 0.27 | $72.\overline{13}\pm 0.92$ | 75.69 ±0.67 | 75.30 ± 0.32 | 88.14 ± 0.25 | 52.83 ± 0.54 | 65.00 ± 0.30 | 3.5 |
| | JOAOv2 | 74.86 ±0.39 | 73.31 ± 0.48 | 75.81 ±0.73 | 75.53 ±0.18 | 88.79±0.65 | 52.71 ± 0.28 | 66.66 ±0.60 | 1.8 |

Unsupervised learning

| Methods | NCI1 | PROTEINS | DD | MUTAG | COLLAB | RDT-B | RDT-M5K | IMDB-B | A.R.↓ |
|------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|-------|
| GL | - | - | - | 81.66±2.11 | - | 77.34 ± 0.18 | 41.01 ± 0.17 | 65.87 ± 0.98 | 7.4 |
| WL | 80.01 ±0.50 | 72.92 ± 0.56 | - | 80.72 ± 3.00 | - | 68.82 ± 0.41 | 46.06 ± 0.21 | 72.30 ± 3.44 | 5.7 |
| DGK | 80.31 ±0.46 | 73.30 ± 0.82 | - | 87.44 ± 2.72 | - | 78.04 ± 0.39 | 41.27 ± 0.18 | 66.96 ± 0.56 | 4.9 |
| node2vec | 54.89±1.61 | 57.49±3.57 | - | 72.63 ± 10.20 | - | | | - | 8.6 |
| sub2vec | 52.84±1.47 | 53.03 ± 5.55 | - | 61.05 ± 15.80 | - | 71.48 ± 0.41 | 36.68 ± 0.42 | 55.26 ± 1.54 | 9.5 |
| graph2vec | 73.22±1.81 | 73.30 ± 2.05 | - | 83.15 ± 9.25 | - | 75.78 ± 1.03 | 47.86 ± 0.26 | 71.10 ± 0.54 | 5.7 |
| MVGRL | - | - | - | 75.40 ± 7.80 | - | 82.00 ± 1.10 | - | 63.60 ± 4.20 | 7.2 |
| InfoGraph_ | 76.20±1.06 | 74.44 ±0.31 | 72.85 ± 1.78 | 89.01±1.13 | 70.65±1.13 | 82.50 ± 1.42 | 53.46 ± 1.03 | 73.03 ±0.87 | 3.0 |
| GraphCL | 77.87 ± 0.41 | 74.39 ±0.45 | 78.62 ±0.40 | 86.80 ± 1.34 | 71.36 ±1.15 | 89.53 ±0.84 | 55.99 ±0.28 | 71.14 ±0.44 | 2.6 |
| JOAO | 78.07 ±0.47 | 74.55 ±0.41 | 77.32 ±0.54 | 87.35 ±1.02 | 69.50 ±0.36 | 85.29 ±1.35 | 55.74 ±0.63 | 70.21 ± 3.08 | 3.3 |
| JOAOv2 | 78.36±0.53 | 74.07 ± 1.10 | 77.40 ±1.15 | 87.67 ±0.79 | 69.33±0.34 | 86.42 ±1.45 | 56.03 ±0.27 | $70.83 {\pm} 0.25$ | 2.8 |
| | | | | | | | | | |

JOAOv2 generally outperforms heuristic self-supervised pretext tasks

Experiments & Discussions. On Bioinformatics Datasets



- ➤ JOAOv2 underperforms heuristic self-supervised pretext tasks, without incorporating domain expertise
- ➤ JOAOv2 generalizes better than GraphCL on unseen / domain specific datasets

Transfer learning

| Methods | BBBP | Tox21 | ToxCast | SIDER | ClinTox | MUV | HIV | BACE | PPI | A.R.↓ |
|---------------|--------------------|------------------|------------------|------------------|--------------------|-----------------------|--------------------|------------------|--------------------|-------|
| No pre-train. | 65.8±4.5 | 74.0 ± 0.8 | 63.4±0.6 | 57.3±1.6 | 58.0±4.4 | 71.8 ± 2.5 | 75.3±1.9 | 70.1 ± 5.4 | 64.8±1.0 | 6.6 |
| Infomax | 68.8 ± 0.8 | 75.3 ± 0.5 | 62.7 ± 0.4 | 58.4 ± 0.8 | 69.9±3.0 | 75.3±2.5 | 76.0 ± 0.7 | 75.9 ± 1.6 | 64.1±1.5 | 5.3 |
| EdgePred | 67.3 ± 2.4 | 76.0 ± 0.6 | 64.1 ± 0.6 | 60.4 ± 0.7 | 64.1 ± 3.7 | 74.1 ± 2.1 | 76.3 ± 1.0 | 79.9 ±0.9 | 65.7 ±1.3 | 3.8 |
| AttrMasking | 64.3 ± 2.8 | 76.7 ± 0.4 | 64.2 ± 0.5 | 61.0 ± 0.7 | 71.8 ± 4.1 | 74.7 ± 1.4 | 77.2 ± 1.1 | 79.3 ±1.6 | 65.2 ±1.6 | 3.1 |
| ContextPred | 68.0 ± 2.0 | 75.7 ± 0.7 | 63.9 ± 0.6 | 60.9 ± 0.6 | 65.9 ± 3.8 | 75.8 \pm 1.7 | 77.3 ± 1.0 | 79.6 ±1.2 | 64.4±1.3 | 3.4 |
| GraphCL | 69.68 ±0.67 | 73.87 ± 0.66 | 62.40 ± 0.57 | 60.53 ± 0.88 | 75.99 ±2.65 | 69.80 ± 2.66 | 78.47 ± 1.22 | 75.38 ± 1.44 | 67.88 ±0.85 | 4.6 |
| JOAO | 70.22 ±0.98 | 74.98 ± 0.29 | 62.94 ± 0.48 | 59.97±0.79 | 81.32±2.49 | 71.66 ± 1.43 | 76.73 ± 1.23 | 77.34 ± 0.48 | 64.43±1.38 | 4.5 |
| JOAOv2 | 71.39 ±0.92 | 74.27 ± 0.62 | 63.16 ± 0.45 | 60.49 ± 0.74 | 80.97 ±1.64 | 73.67 ± 1.00 | 77.51 ±1.17 | 75.49 ± 1.27 | 63.94±1.59 | 4.3 |

Experiments & Discussions. On Large-Scale Datasets

JOAOv2 achieves a better generalizability and scalability, outperforms on large-scale datasets



Semi-supervised learning on large-scale datasets

| L.R. | Methods | ogbg-ppa | ogbg-code |
|------|---------------|--------------------|----------------------|
| 1% | No pre-train. | 16.04 ± 0.74 | 6.06 ± 0.01 |
| | GraphCL | 40.81±1.33 | 7.66 ± 0.25 |
| | JŌĀŌ - | 47.19 ±1.30 | 6.84±0.31 |
| | JOAOv2 | 44.30 ±1.67 | 7.74 ± 0.24 |
| 10% | No pre-train. | 56.01±1.05 | 17.85 ± 0.60 |
| | GraphCL | 57.77±1.25 | 22.45 ± 0.17 |
| | JŌĀŌ - | 60.91 ±0.83 | $\bar{2}2.06\pm0.30$ |
| | JOAOv2 | 59.32 ±1.11 | 22.65 ± 0.22 |

Conclusions



> Problem: Handling heterogenous graph data with less manual efforts

- > Contributions:
 - ❖ JOAO, a unified automatic framework
 - An instantiation as min-max optimization, with AGD for solution
 - JOAOv2, addressing distortion with multi-projection heads
 - Thorough experiments verifying the rationale and performance advantage

Further Discussions



> Limitation:

Automating augmentation selection, while requiring human to construct & config augmentation pool: "full" automation is still desired

> Potential:

In parallel to the principled formulation of bi-level optimization, a metalearning formulation can also be pursued

References & Figures



References

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- > Wang et al: Towards A Unified Min-Max Framework for Adversarial Exploration and Robustness
- Boyd et al: Convex Optimization
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- DistAug: Distribution Augmentation for Generative Modeling

> Figures

- ➤ 1. https://www.euroscientist.com/imagine-a-social-network-like-facebook-with-no-facebook/
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- > 3. https://www.e-education.psu.edu/ebf483/node/643



Thank you for listening!

Paper: https://arxiv.org/abs/2106.07594

Code: https://github.com/Shen-Lab/GraphCL_Automated