

# COS 426: Computer Graphics

## Neural Rendering

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**PRINCETON  
UNIVERSITY**

.... so far so good: Computer Graphics

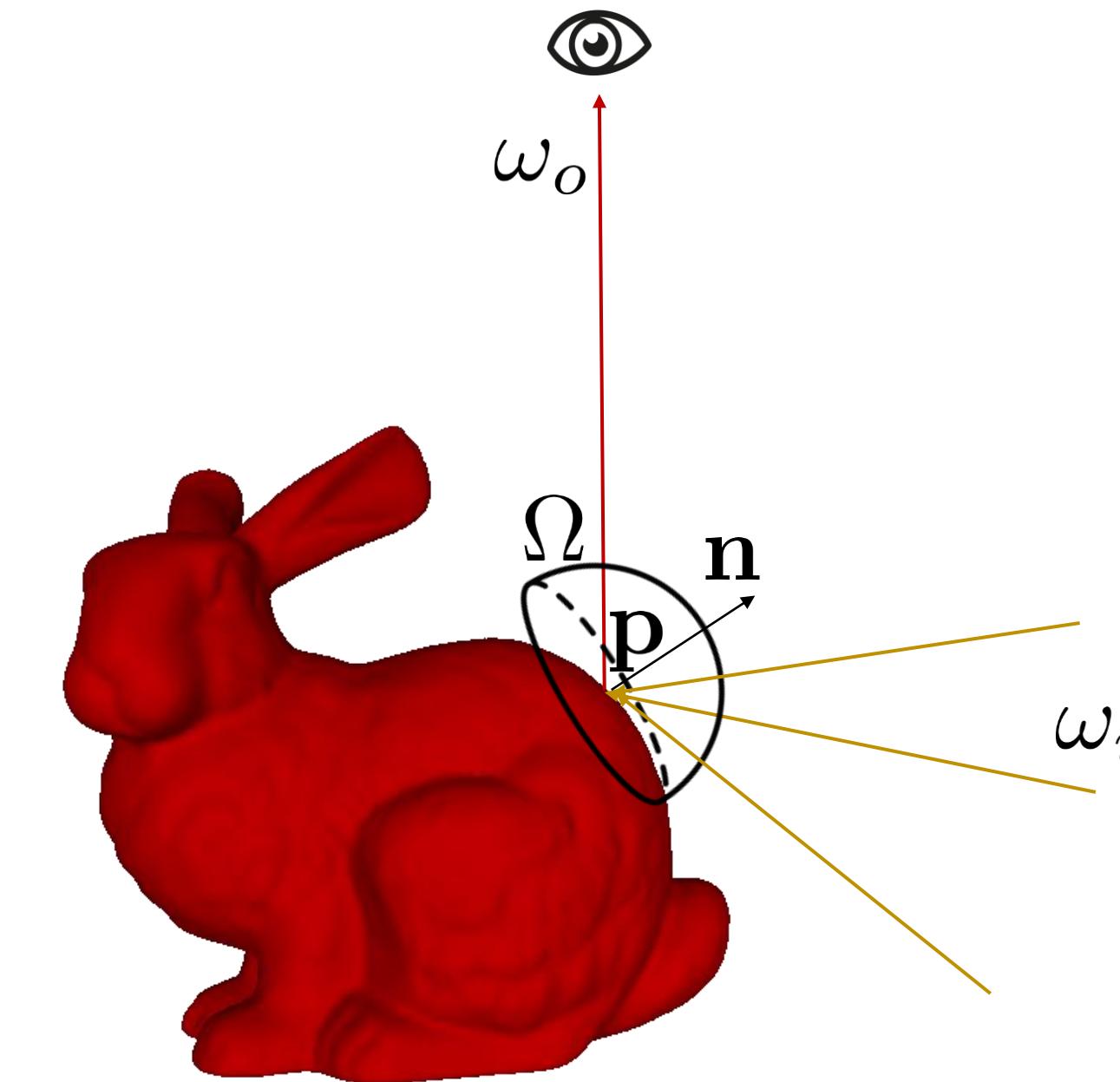


Source: (Project Sol Part 2) <https://www.youtube.com/watch?v=pNmhJx8yPLk>

# Rendering Equation

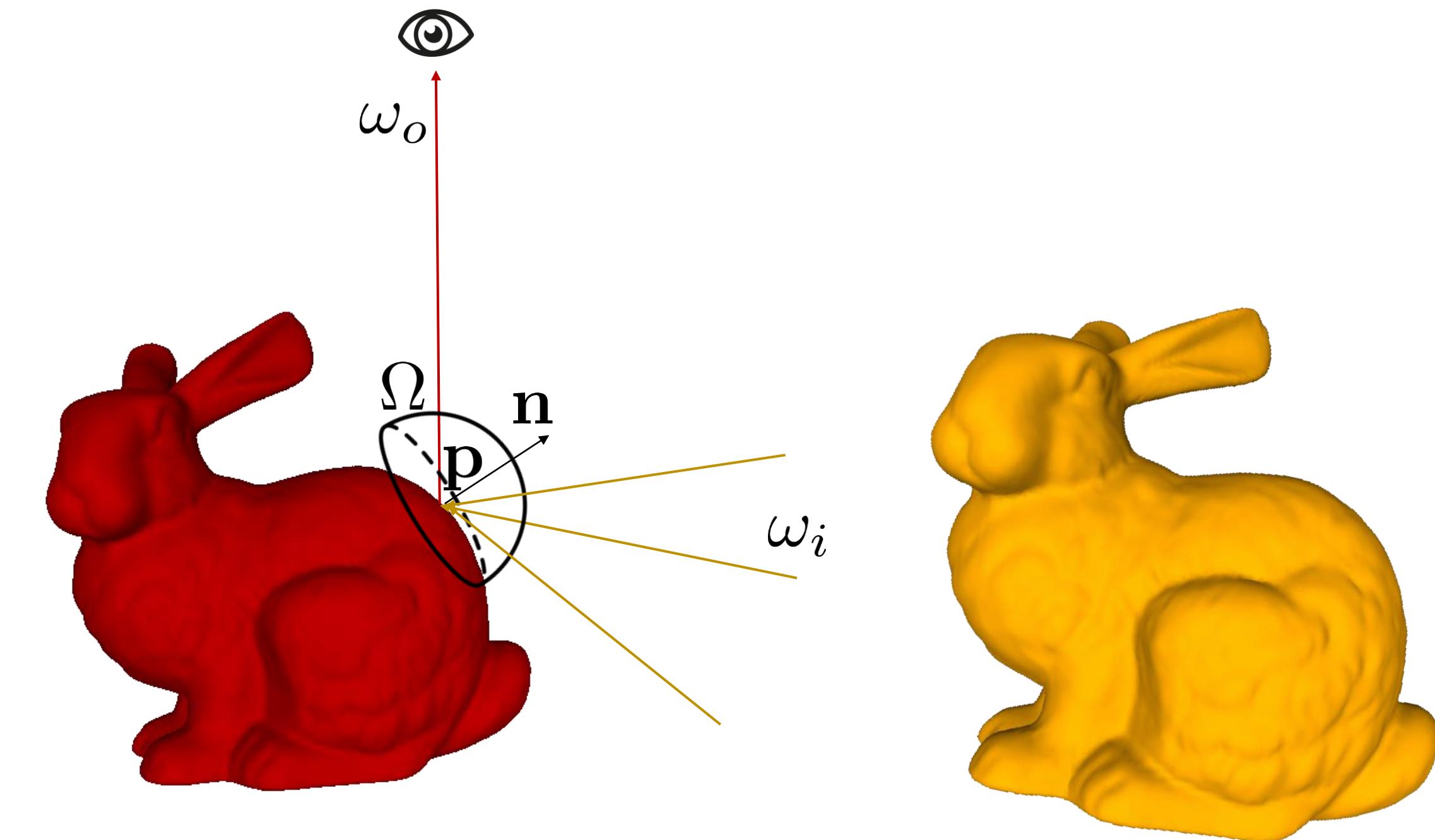
$$L_o(\mathbf{p}, \omega_o) = L_e(\mathbf{p}, \omega_o) + \int_{\Omega} [L_i(\mathbf{p}, \omega_i) f_r(\mathbf{p}, \omega_i, \omega_o) (\omega_i \cdot \mathbf{n})] d\omega_i$$

Outgoing radiance      Incident radiance      BRDF

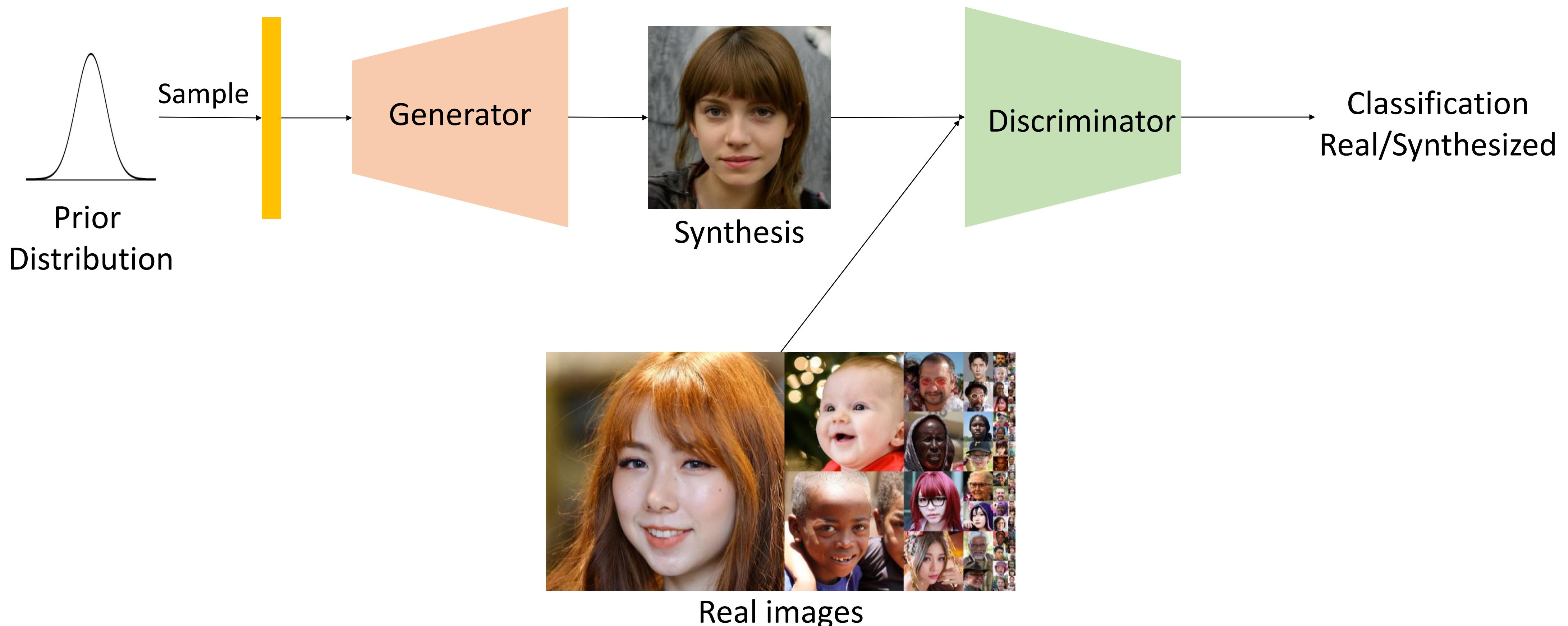


# Rendering Equation

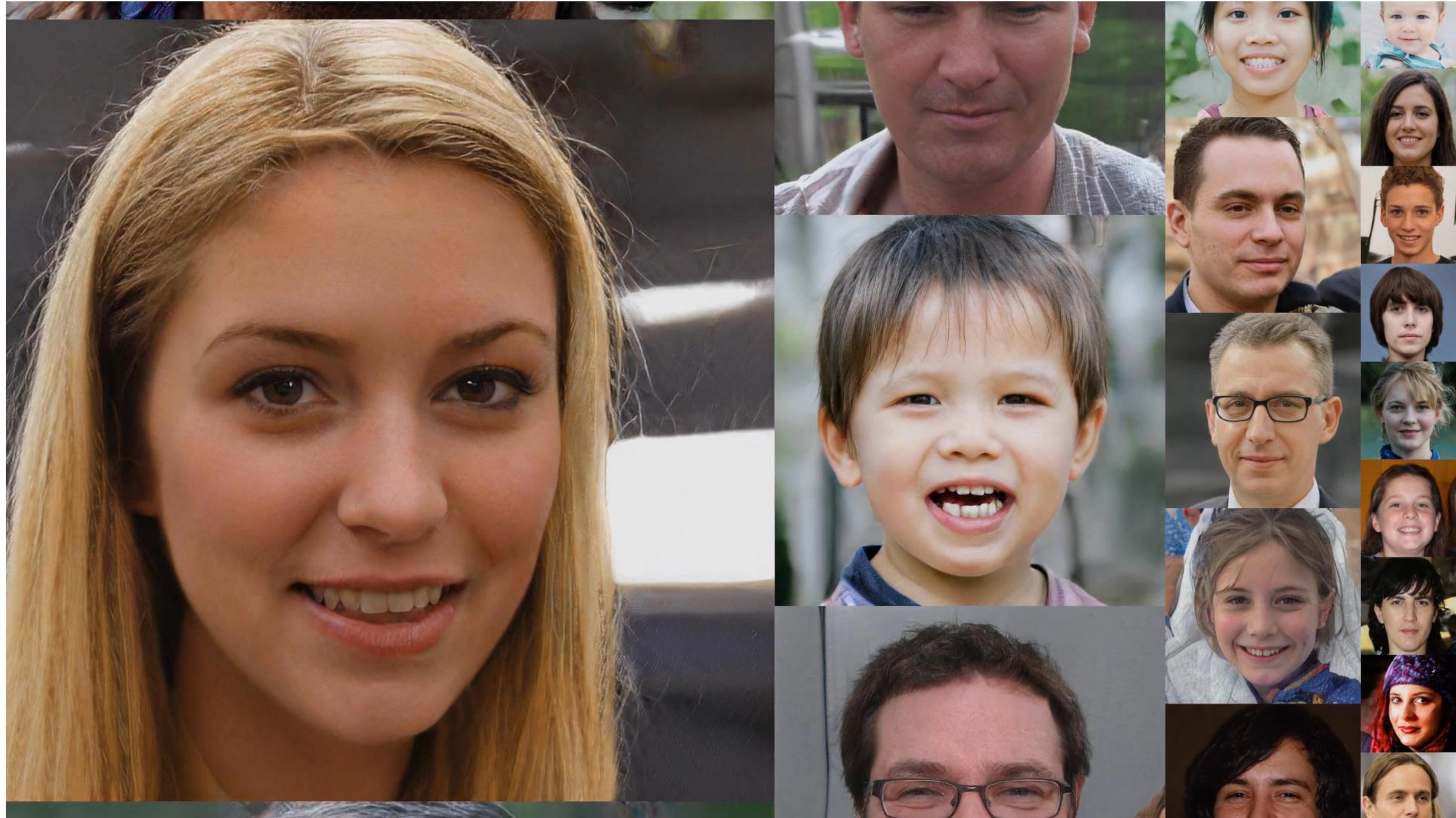
$$L_o(\mathbf{p}, \omega_o) = L_e(\mathbf{p}, \omega_o) + \int_{\Omega} [L_i(\mathbf{p}, \omega_i)] f_r(\mathbf{p}, \omega_i, \omega_o) (\omega_i \cdot \mathbf{n}) d\omega_i$$



# Generative Adversarial Networks

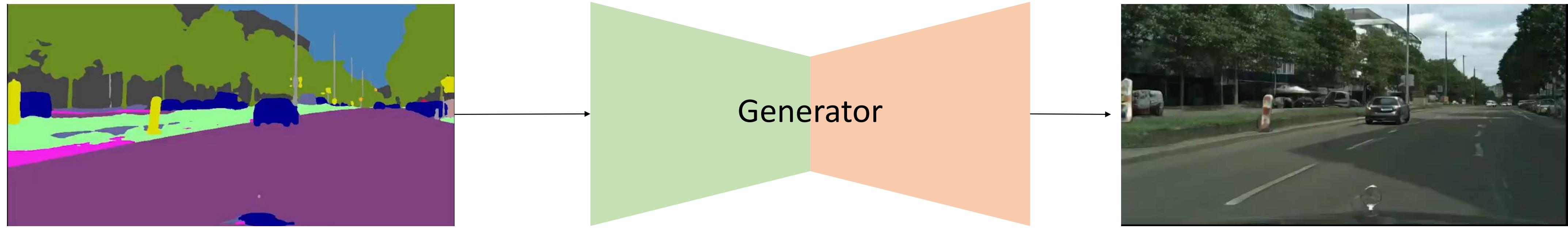


# Generative Adversarial Networks



StyleGAN [Karras et al., 2019]

# Conditional Generative Models



Vid2Vid [Wang et al., 2019]

# Two Alternatives of Realistic Image Synthesis

## Photo-realistic Rendering (CG)

### Cons:

- Requires lots of manual work
  - Building of high-quality assets
  - Setting up the scene
- Long render times

### Pros:

- Full control of scene parameter:
  - Camera, light sources, motion, geometry, appearance

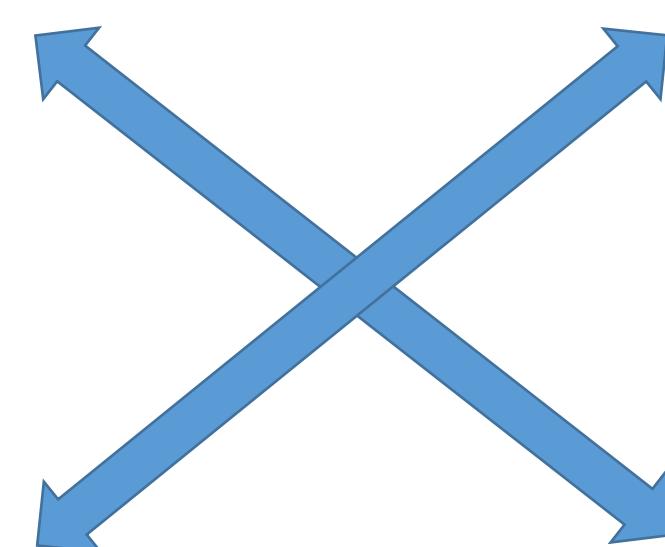
## Generative Machine Learning (ML)

### Cons:

- Requires lots of training data
- No fine-grained semantic control of the scene parameters, e.g., motion or illumination

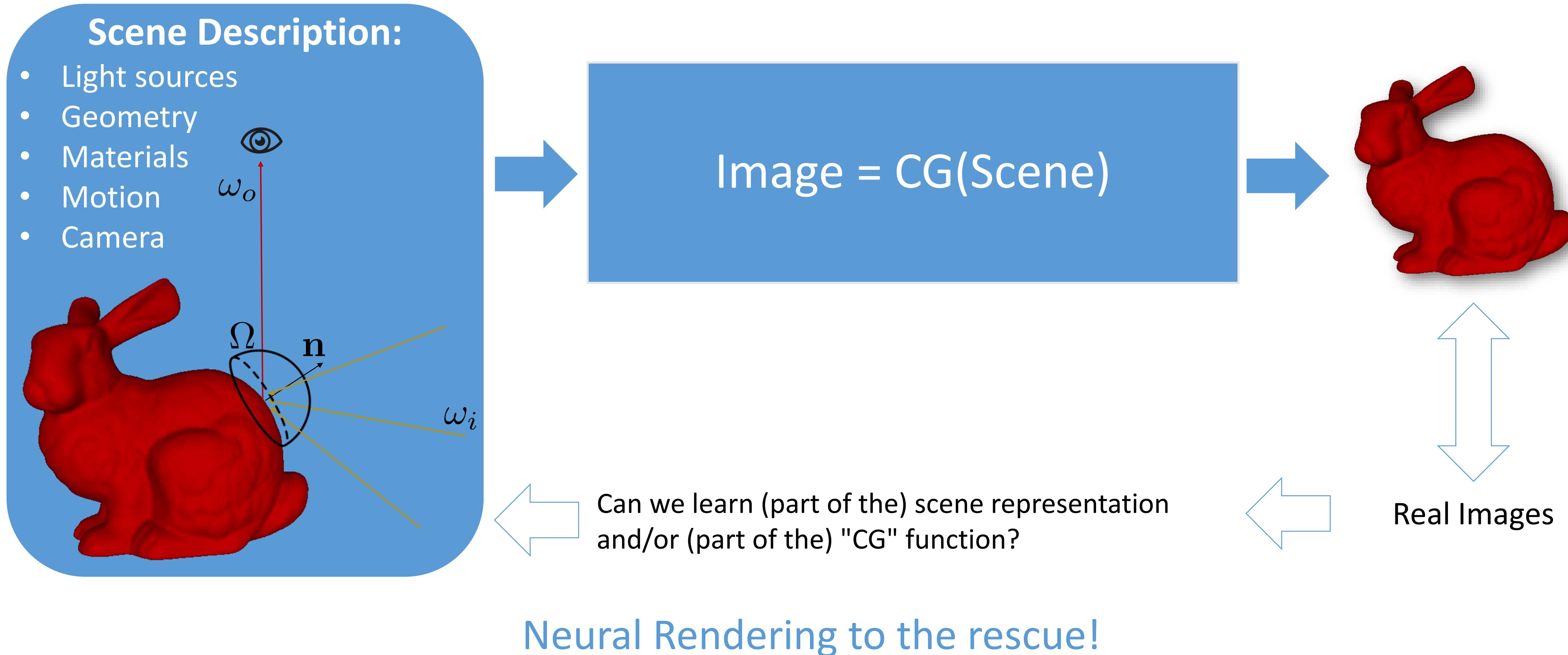
### Pros:

- Fully automatic training
- Interactive inference/rendering



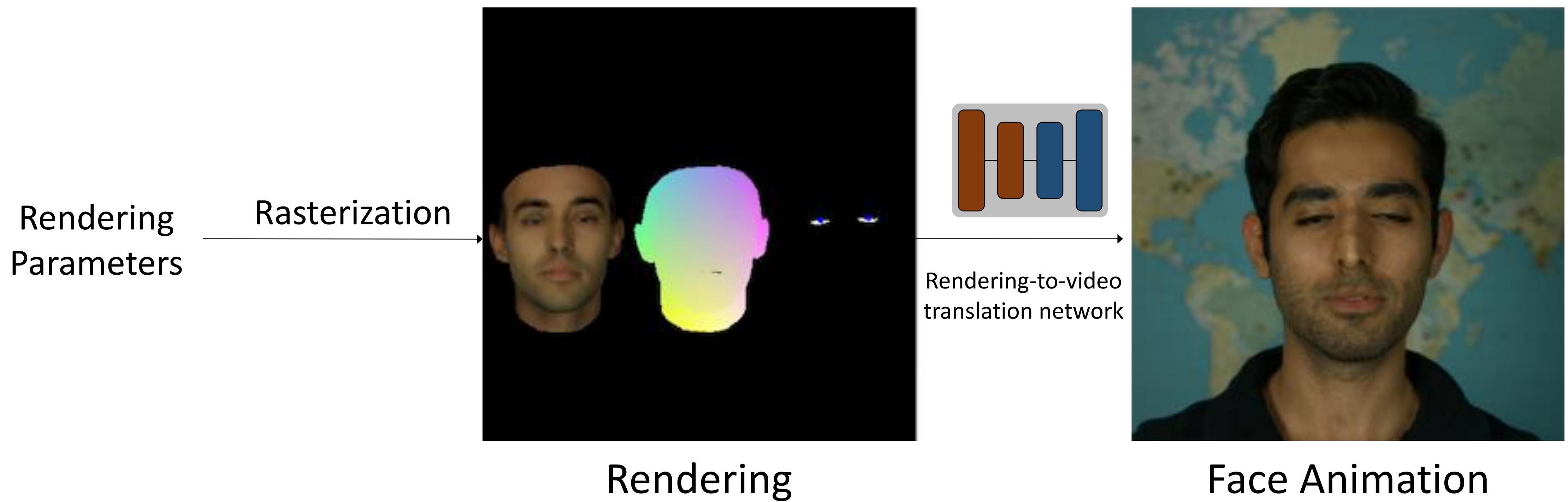
Neural Rendering to the rescue!

# Neural Rendering - Graphics vs. Learning



# CG Modules

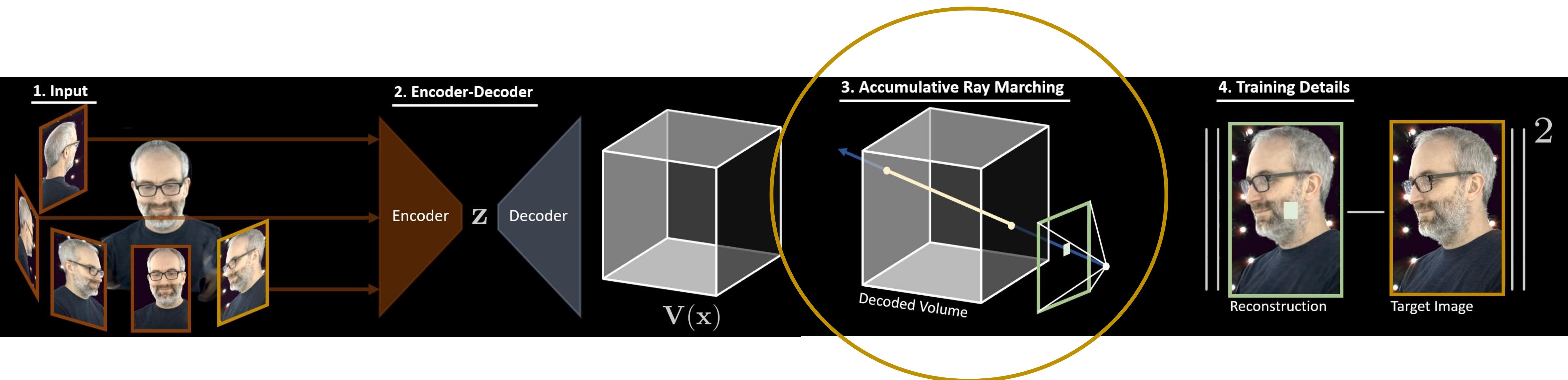
Computer Graphics Module: Rasterization is used to synthesize the input to the network.



Deep Video Portraits [Kim et al., 2018]

# CG Modules

## Computer Graphics Module: *Differentiable Volume Renderer*



Neural Volumes [Lombardi et al., 2019]

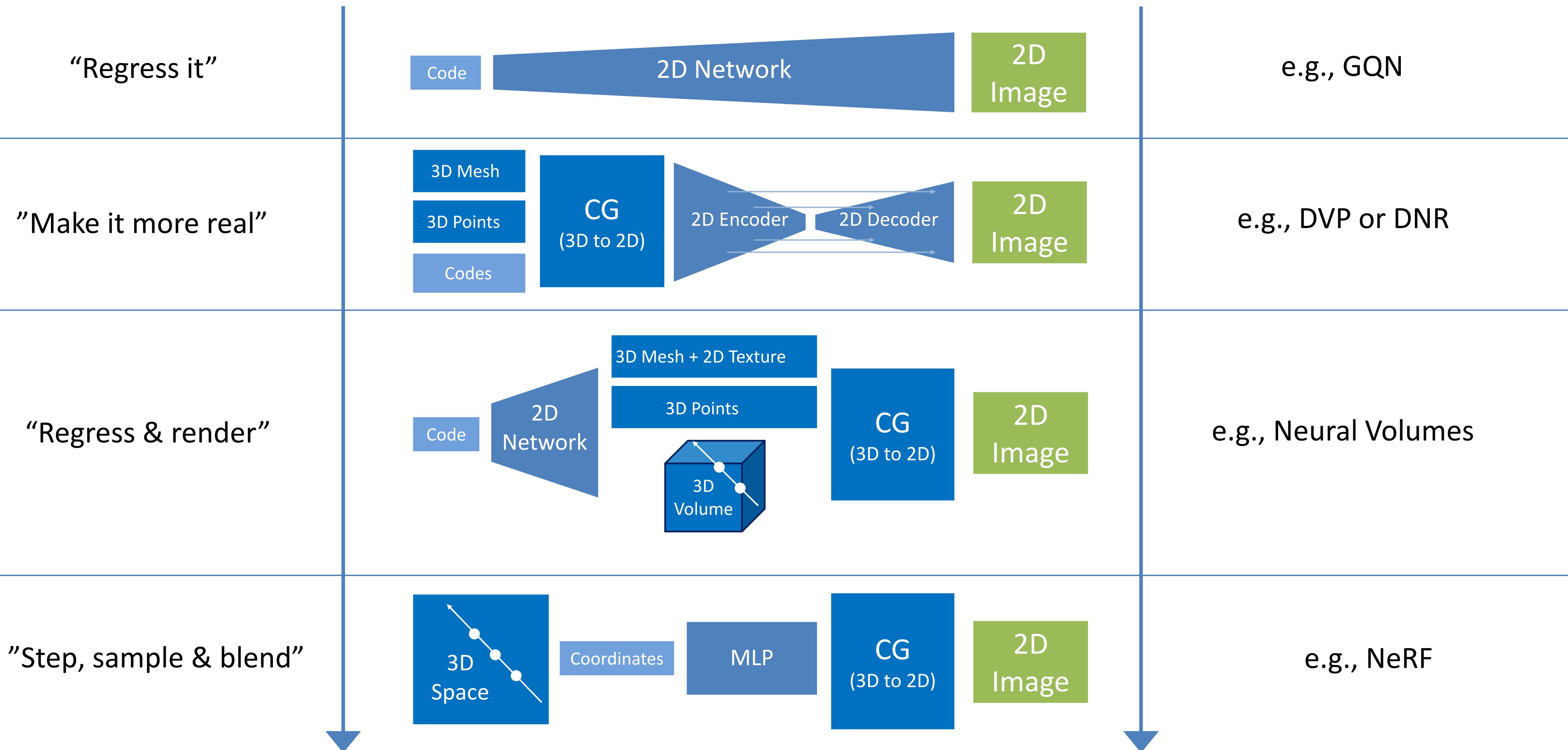
# Neural Rendering Definition:

"(Deep) neural networks for image or video generation that enable explicit or implicit control of scene properties"

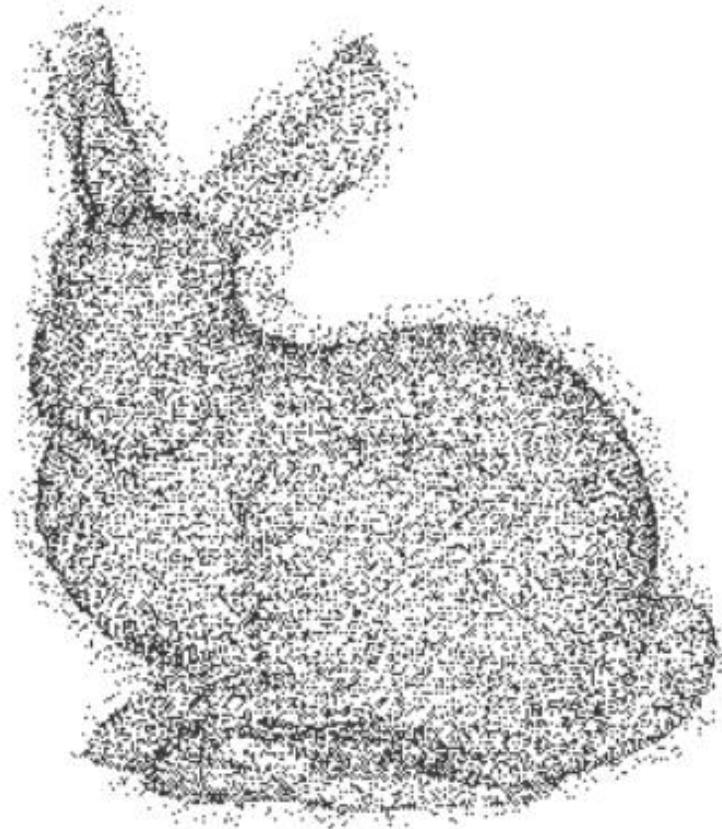


Allows us to create photorealistic assets

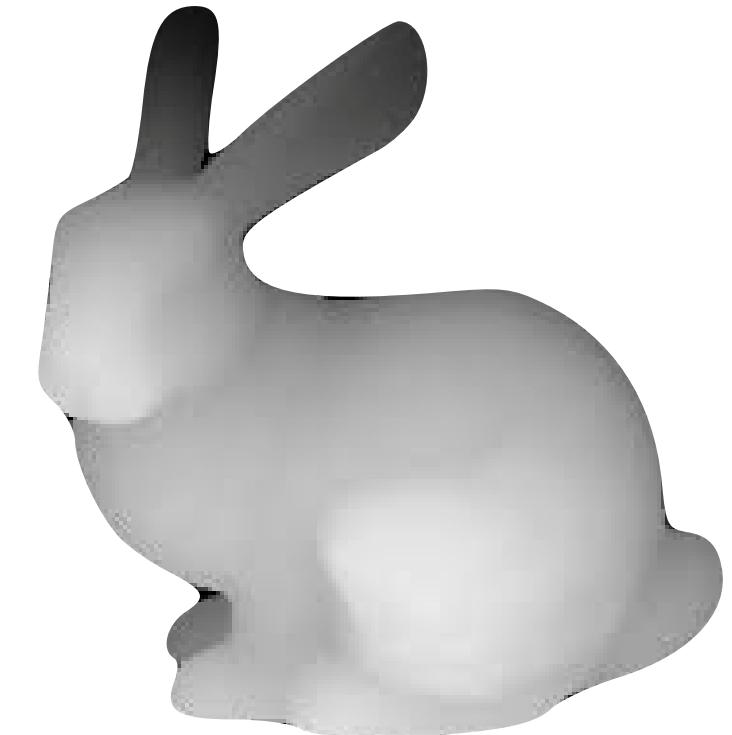
# Neural Rendering Zoo



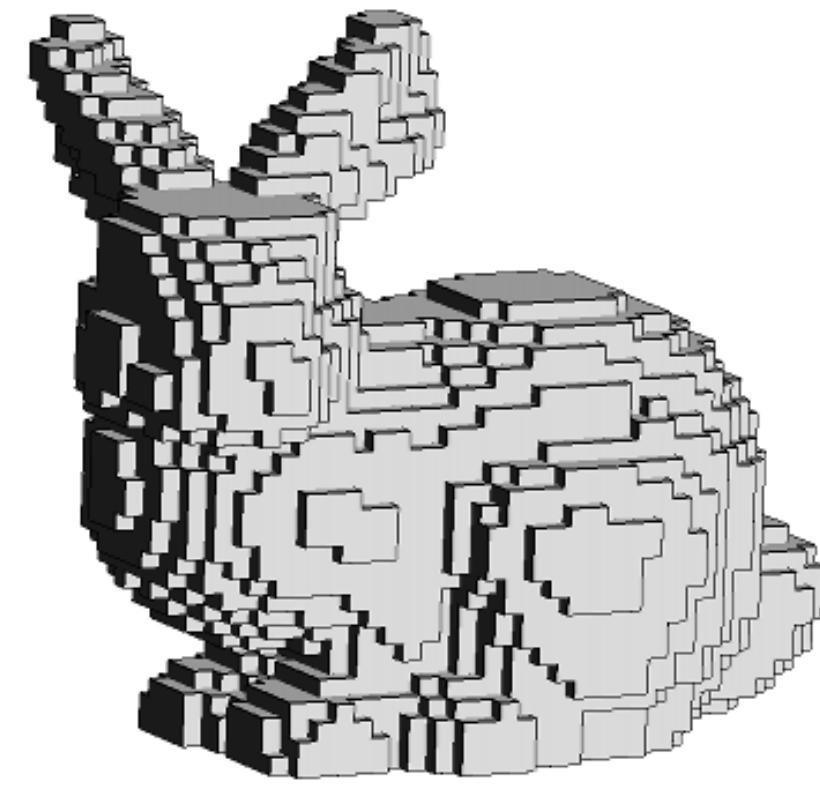
# What's the right scene representation?



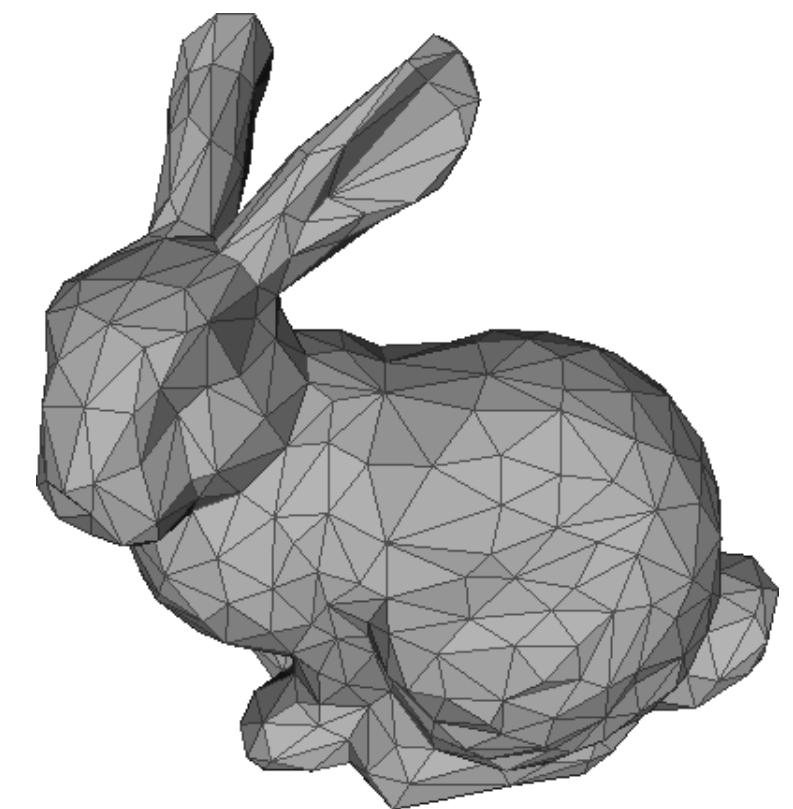
Point cloud



Depth map



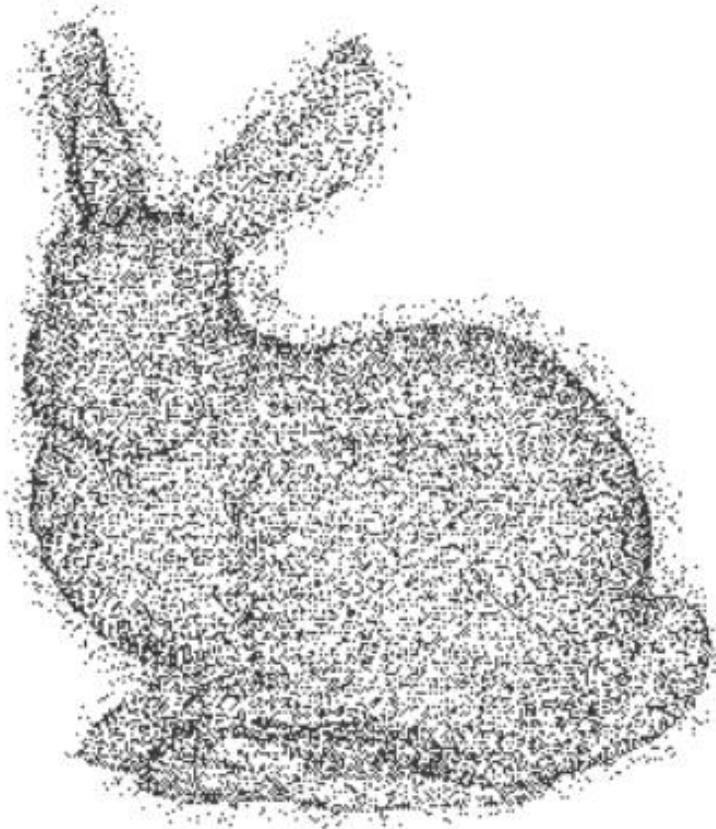
Voxel grid



Triangle mesh

# What's the right scene representation?

- ▶ **Do sensors output data in this representation?**



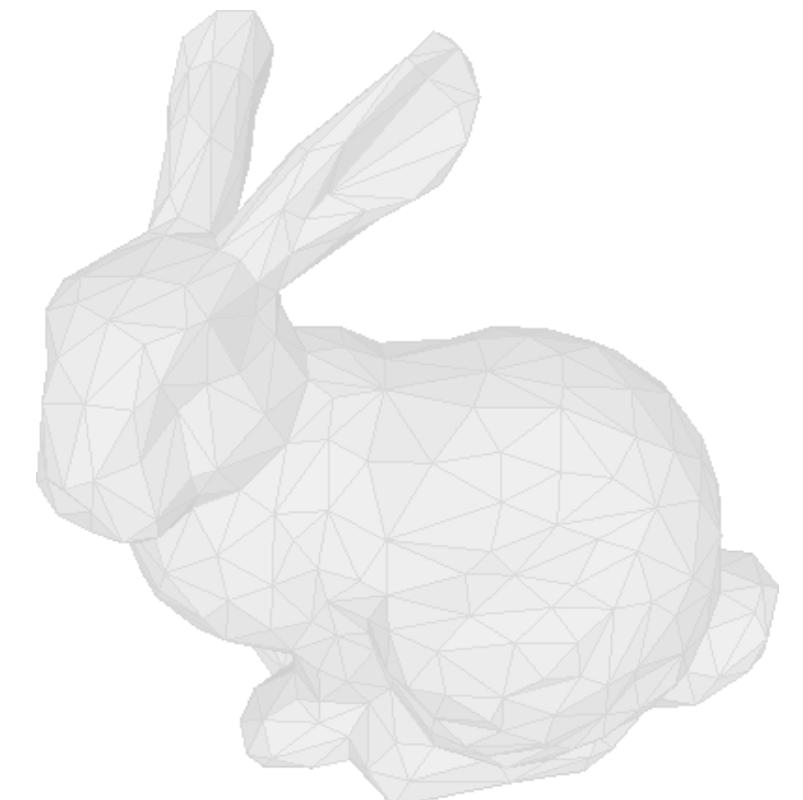
Point cloud



Depth map



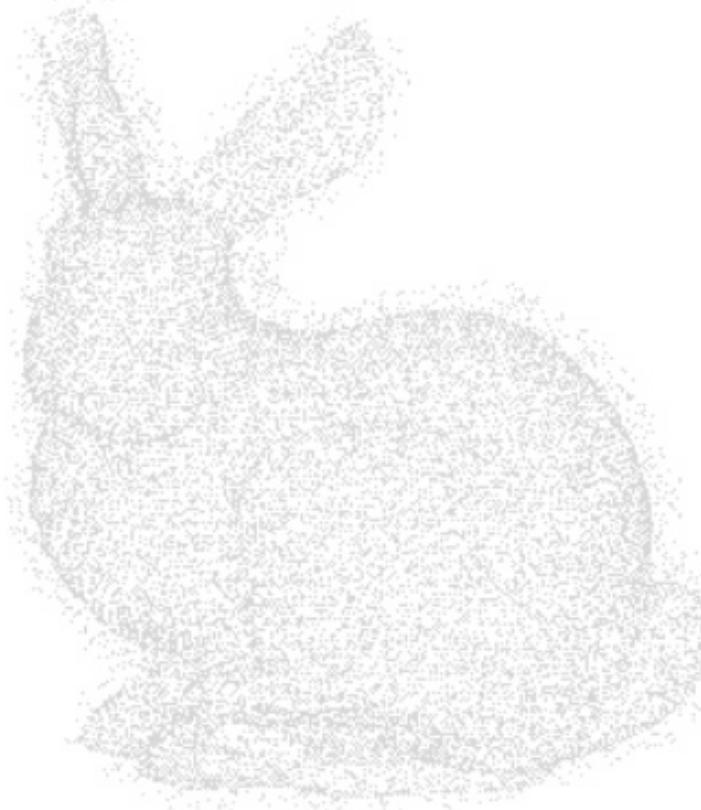
Voxel grid



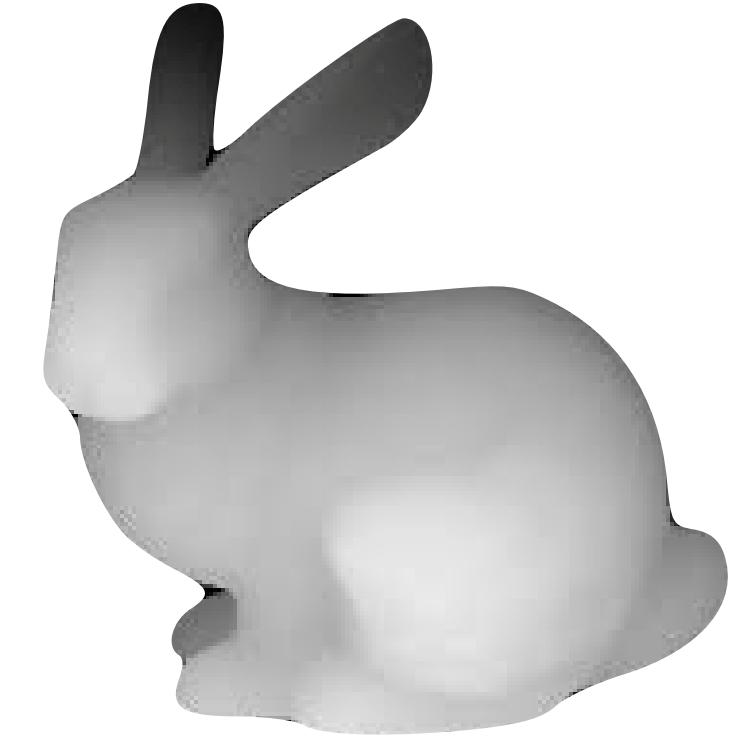
Triangle mesh

# What's the right scene representation?

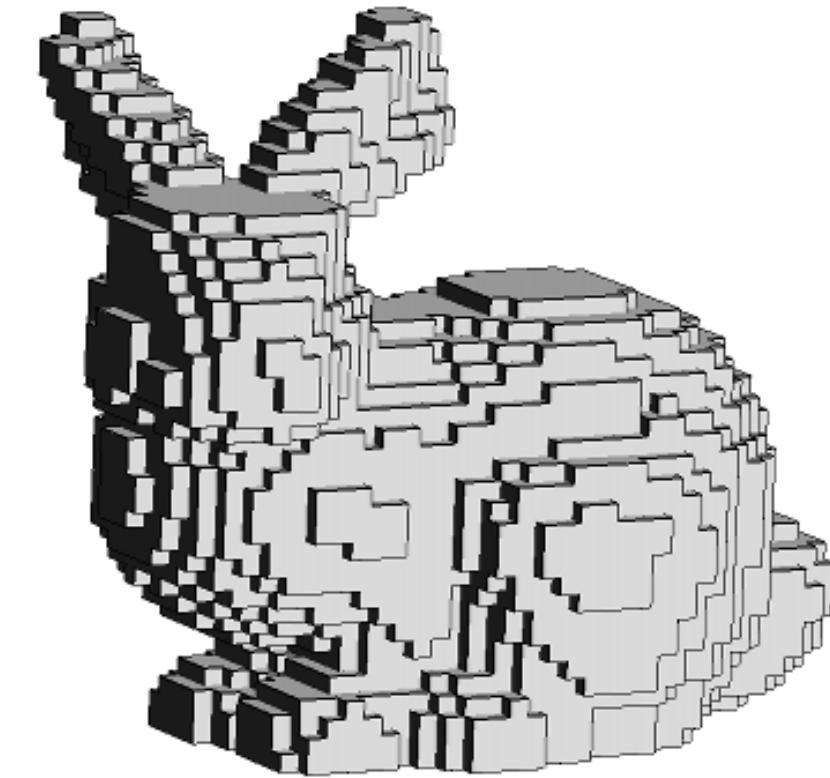
- ▶ Do sensors output data in this representation?
- ▶ Can we process/generate content in this representation?



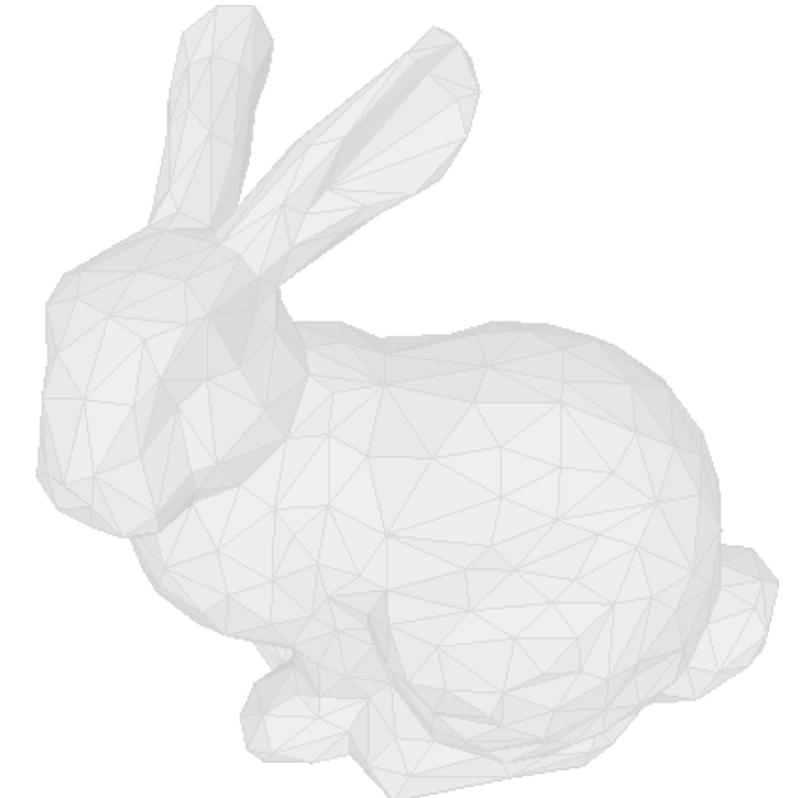
Point cloud



Depth map



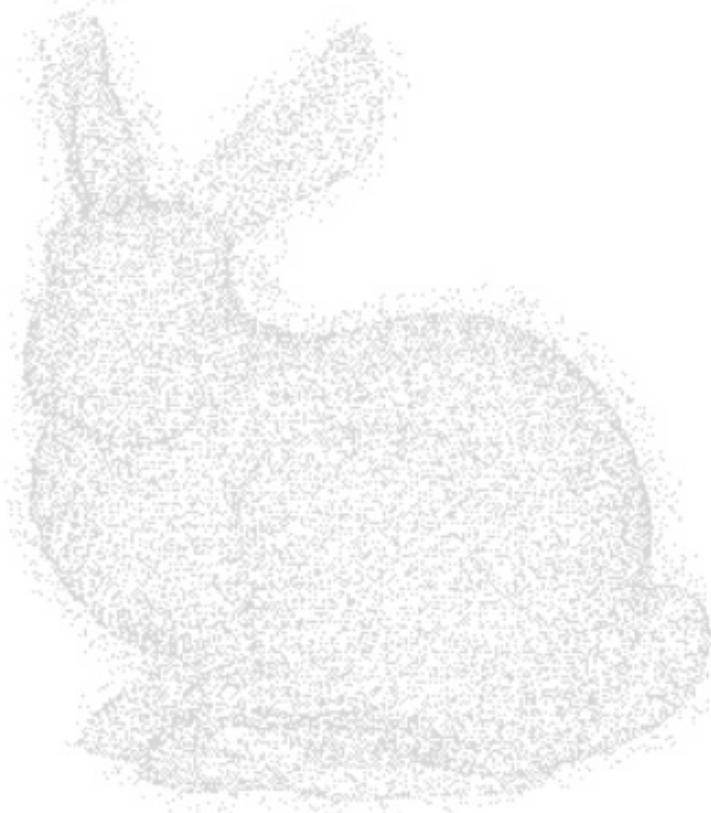
Voxel grid



Triangle mesh

# What's the right scene representation?

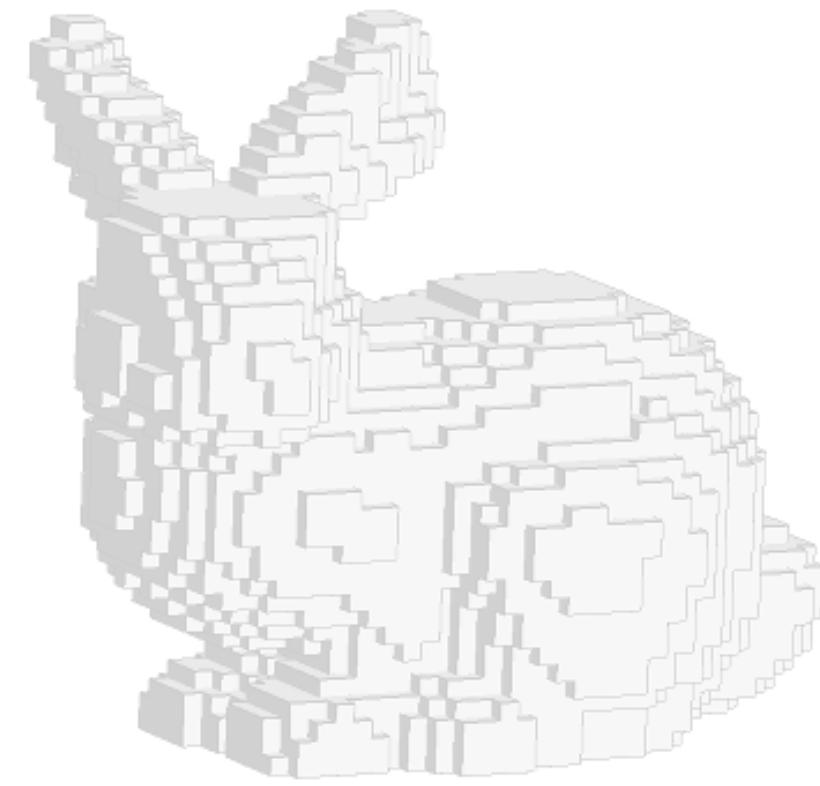
- ▶ Do sensors output data in this representation?
- ▶ Can we process/generate content in this representation?
- ▶ **Can we easily render this representation?**



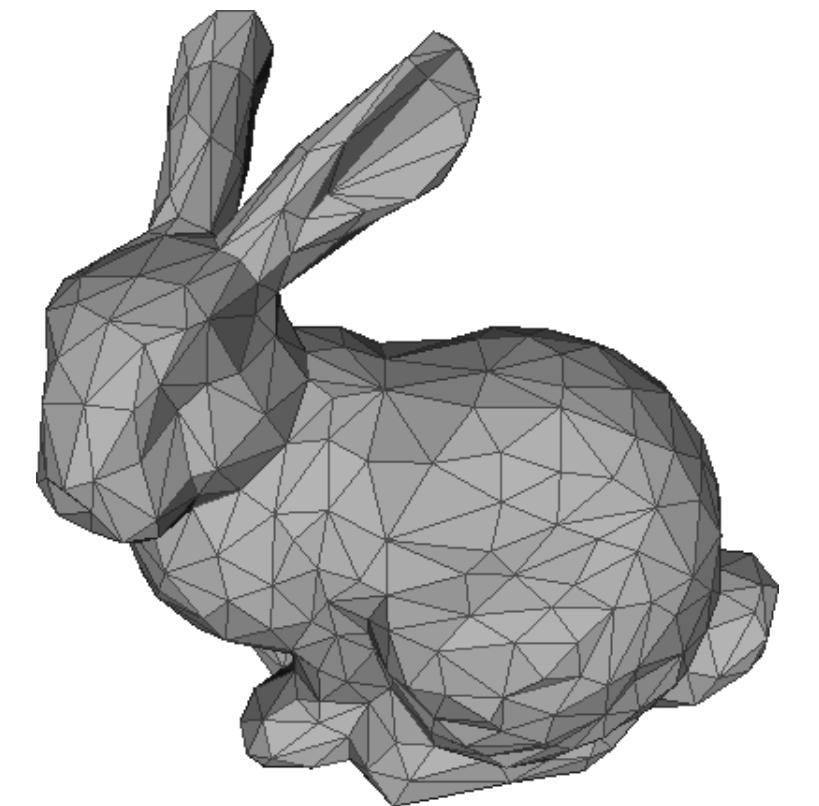
Point cloud



Depth map



Voxel grid



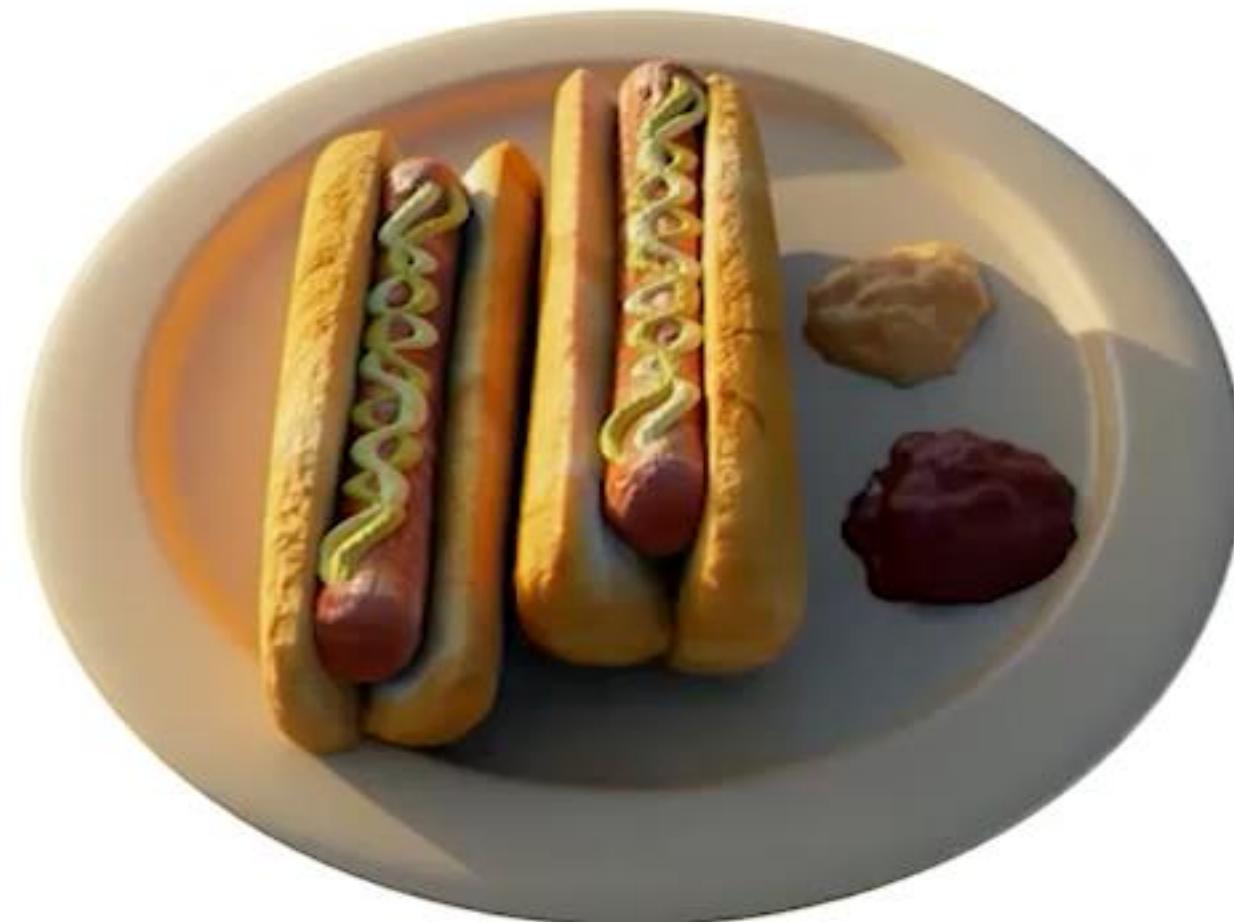
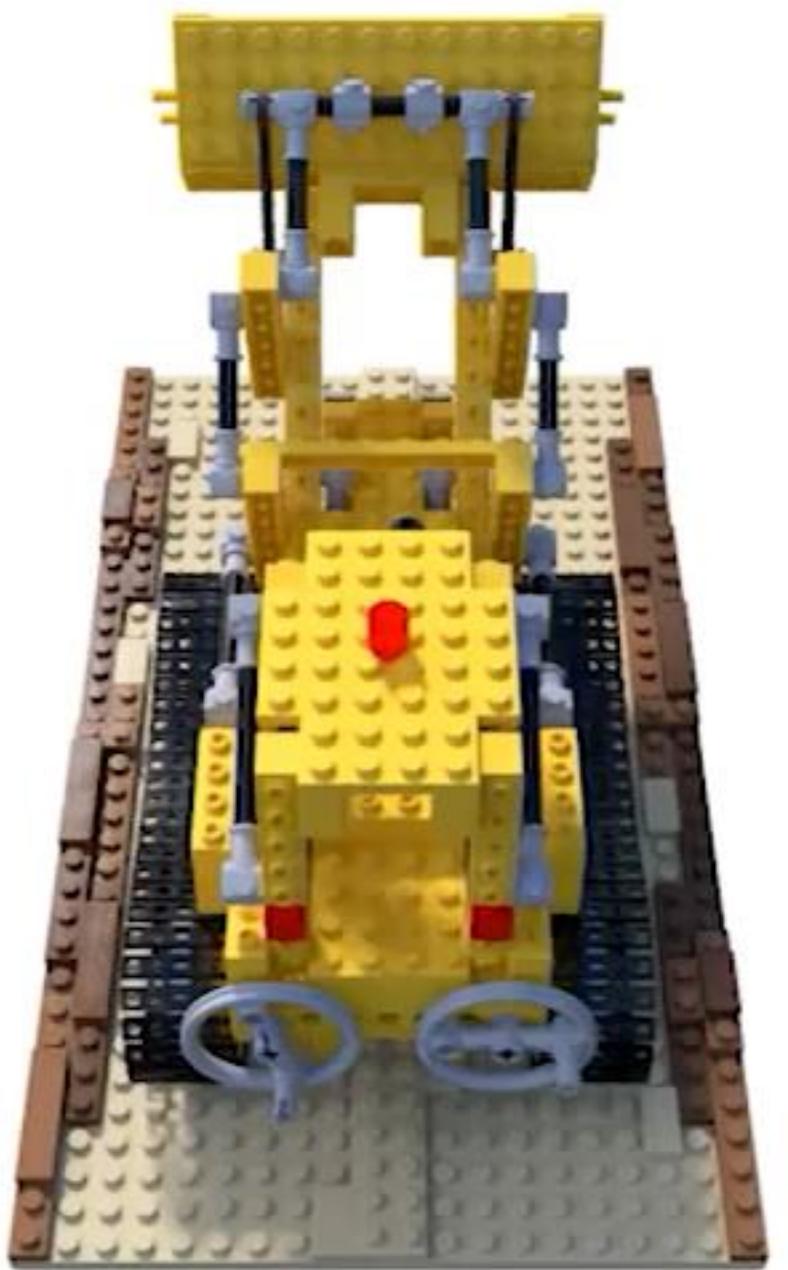
Triangle mesh

# What's the right scene representation for 3D vision?

- ▶ Sensors don't give us nice data
- ▶ World is not dense in 3D space, so maybe representation shouldn't be
- ▶ Doing computation directly on “efficient” representations is hard
- ▶ What's missing? Efficient representation that's easy to optimize with gradient-based methods!

## NeRF (neural radiance fields):

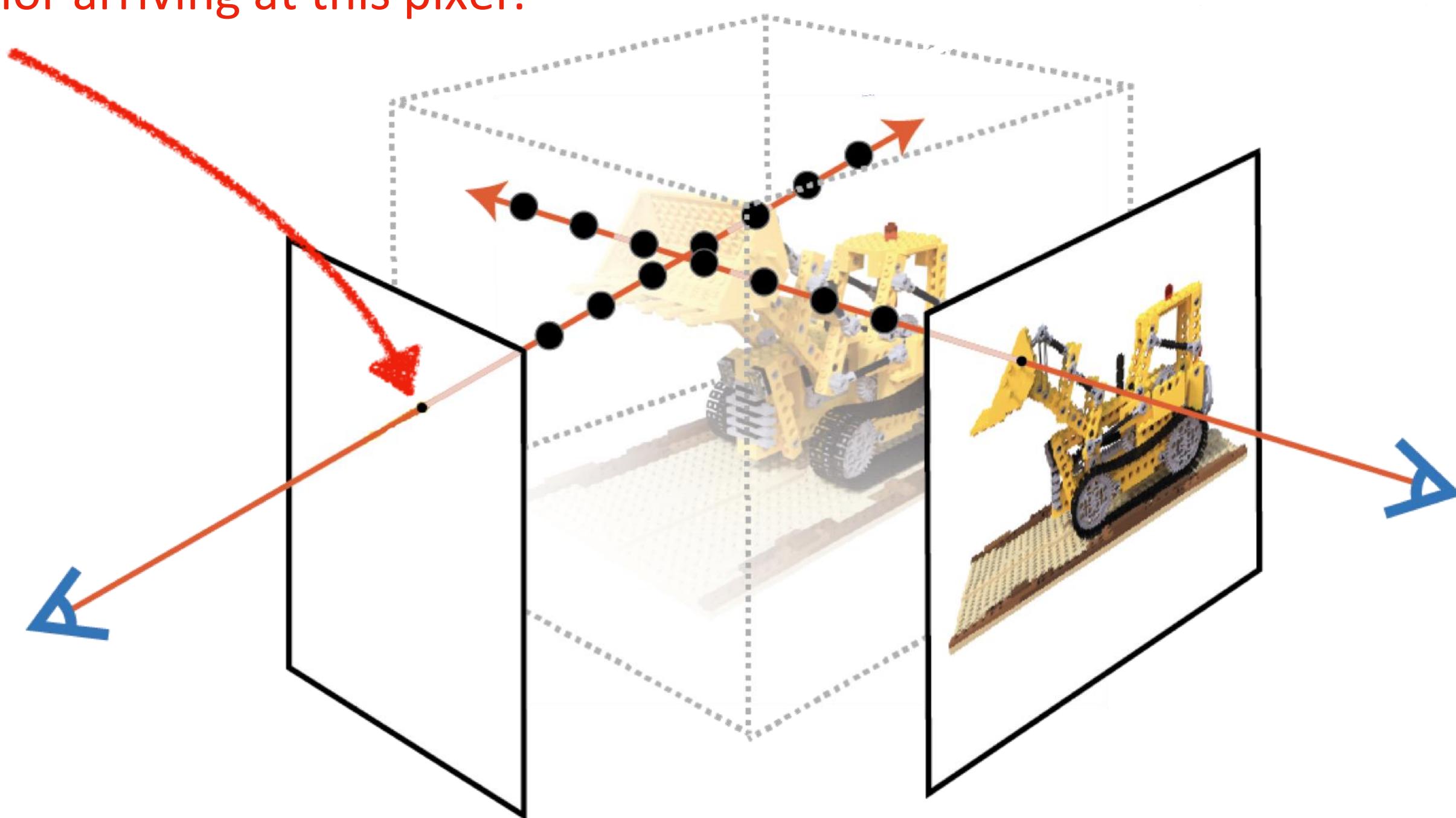
Neural networks as a volume representation,  
using volume rendering to do view  
synthesis. $(x, y, z, \theta, \phi) \rightarrow \text{color, opacity}$



# Neural Volumetric Rendering

# Neural Volumetric Rendering

What's the radiance/color arriving at this pixel?



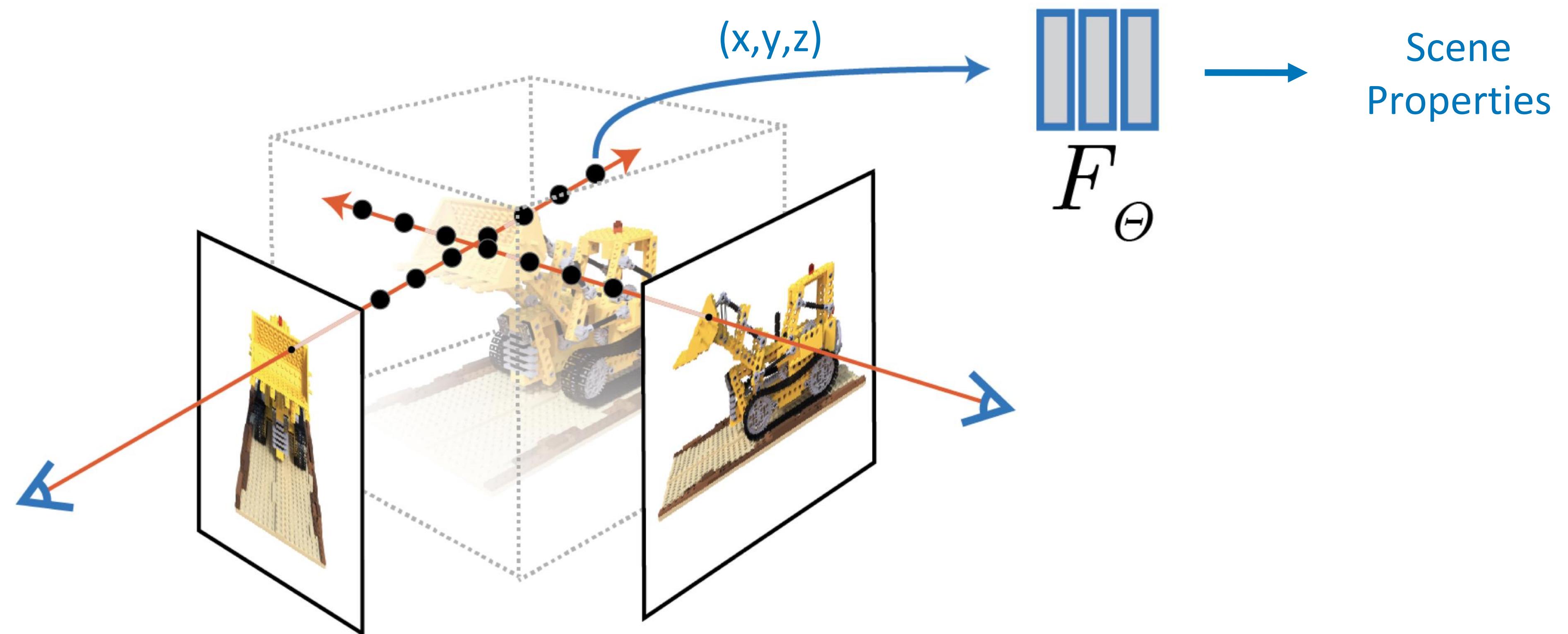
# Neural Volumetric Rendering

- ▶ “Soft” volumetric functions better suited for gradient-based optimization



# Neural Volumetric Rendering

- (Coordinate-based) neural network represents scene as continuous function

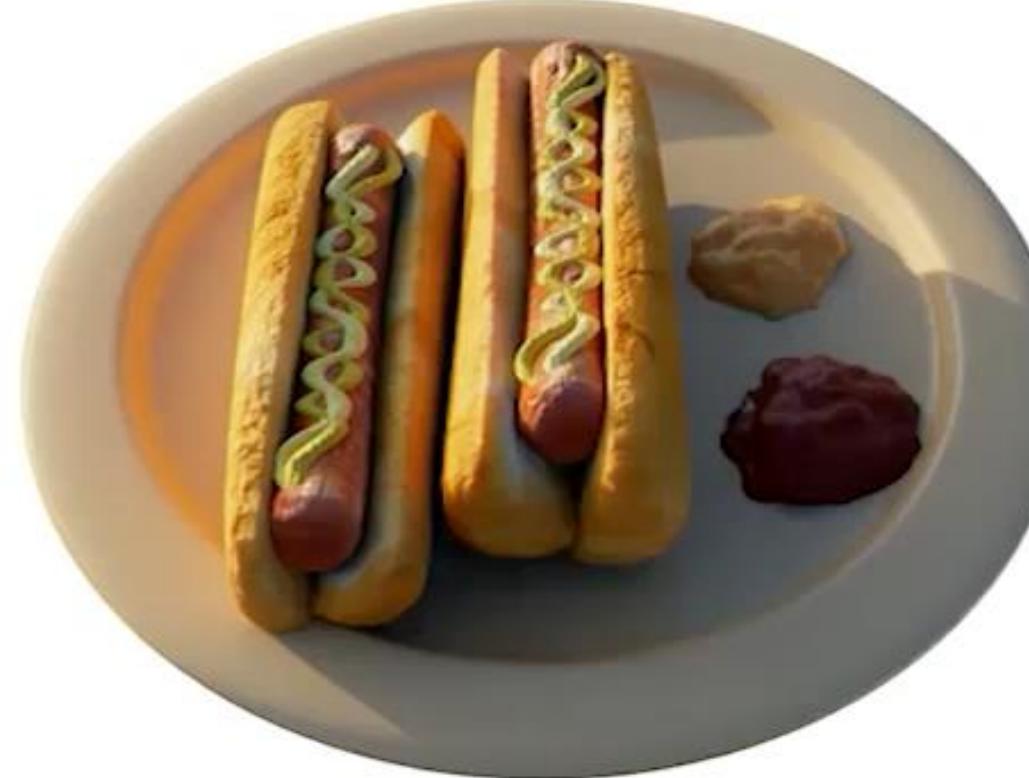
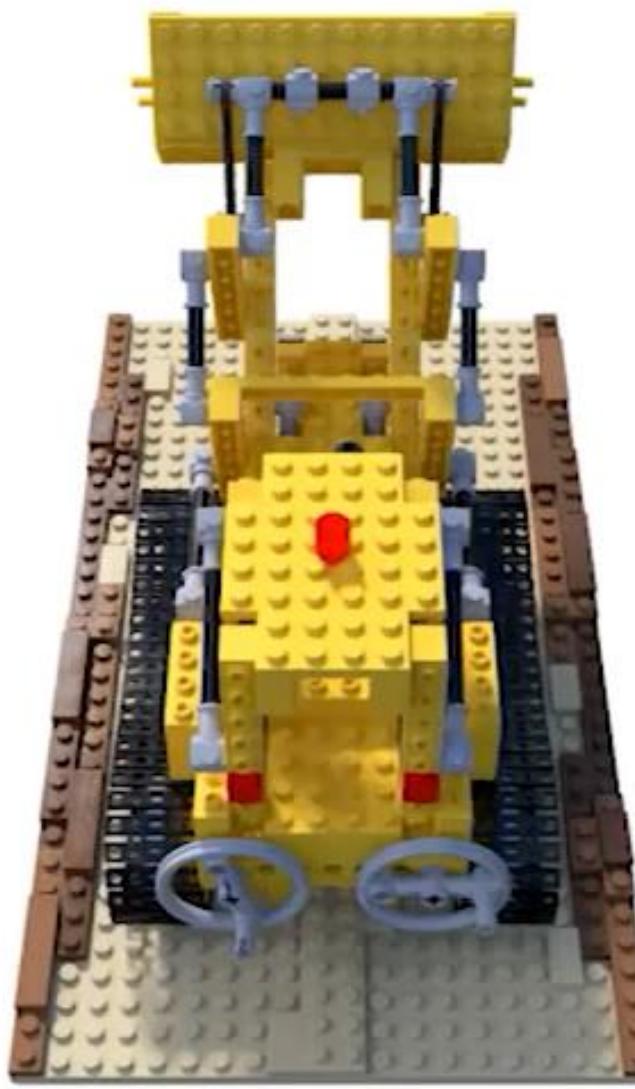


# NeRF: neural volumetric rendering for view synthesis



Inputs: sparsely sampled images of scene

Outputs: new views of same scene





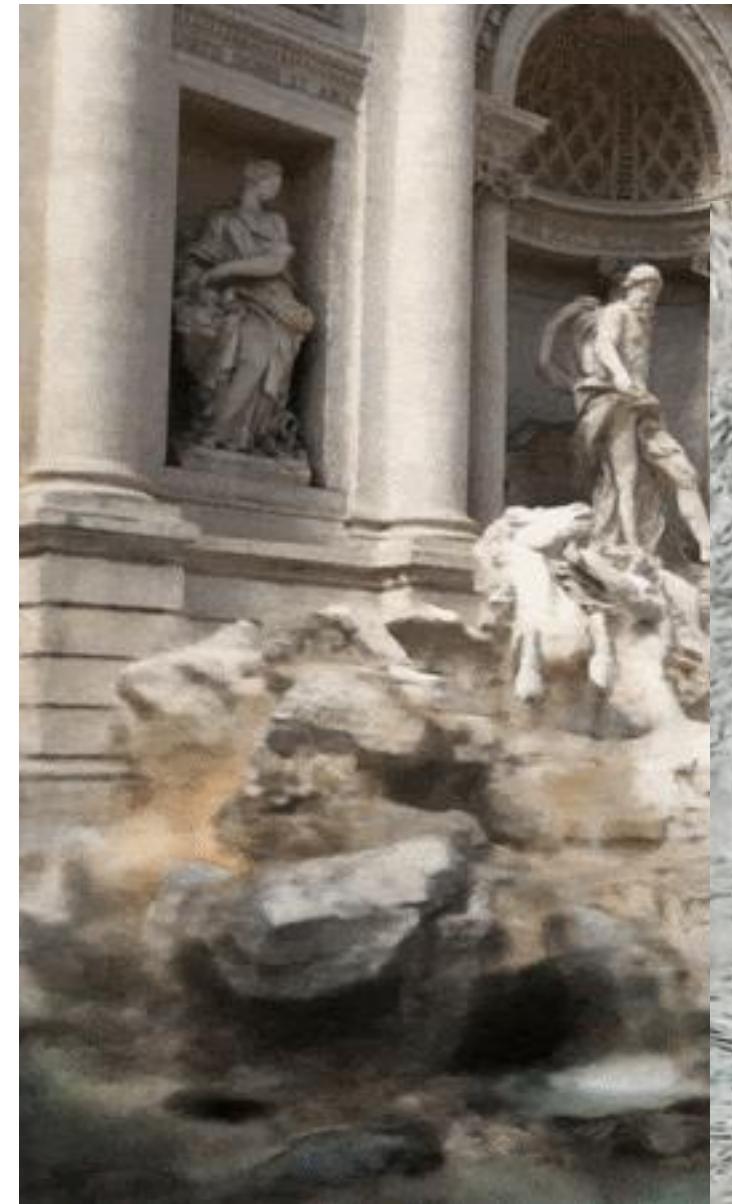
NeRF in the Wild, Martin-Brualla et al.



NeRF in the Wild, Ne



NeRFies, Park et al.



NeRF in the Wild



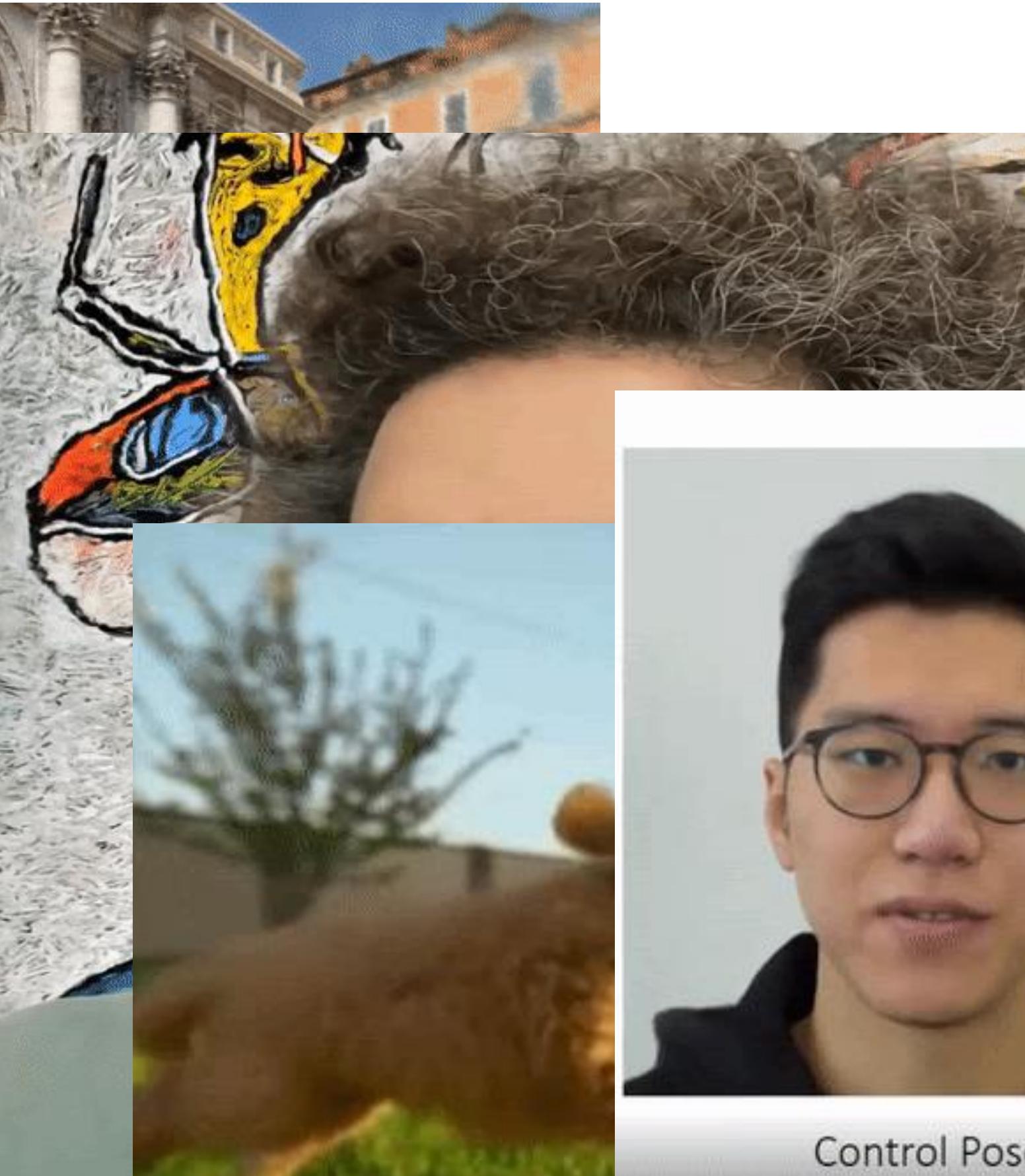
NeRF



Neural Scene Flow Fields, Li et al.



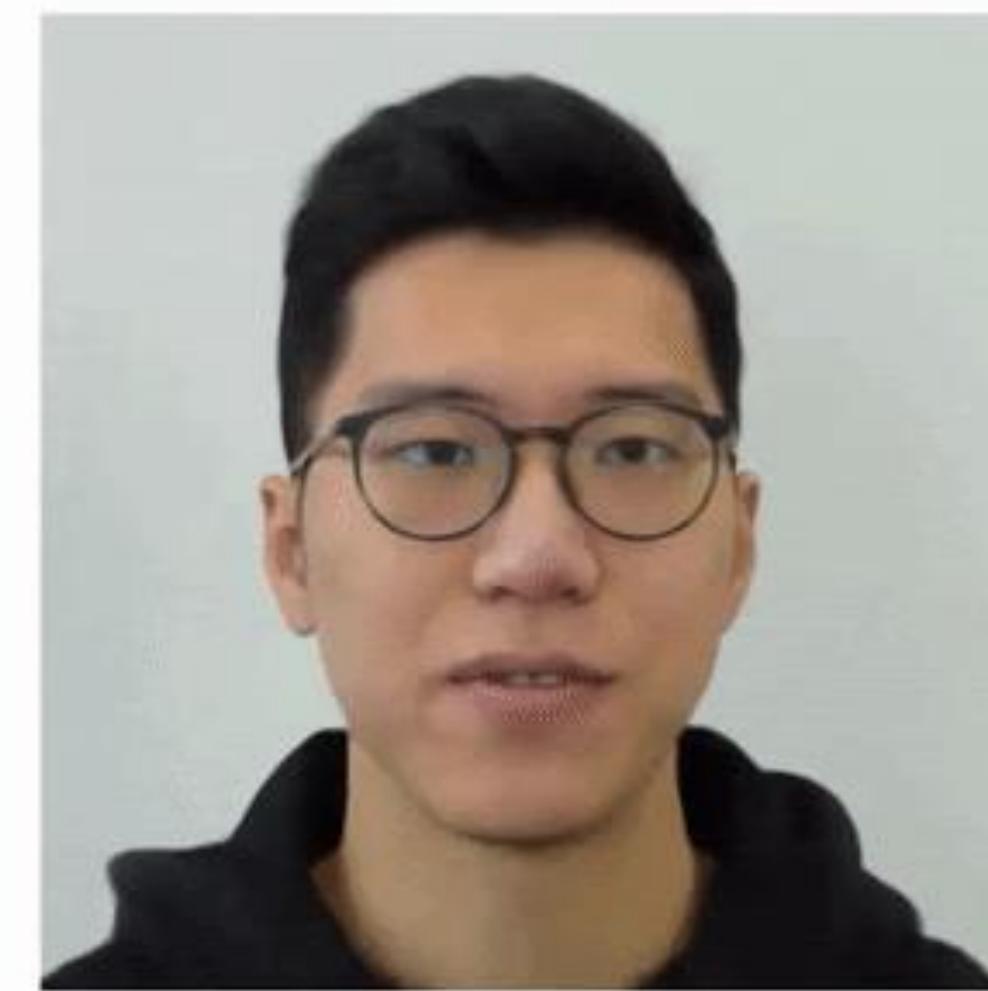
NeRF in the Wild



NeRF



Control Pose



Control Expression

Dynamic Neural Radiance Fields, Gafni et al.

Neural Scene Flow Fields, Li et al.



NeRF in the Wild



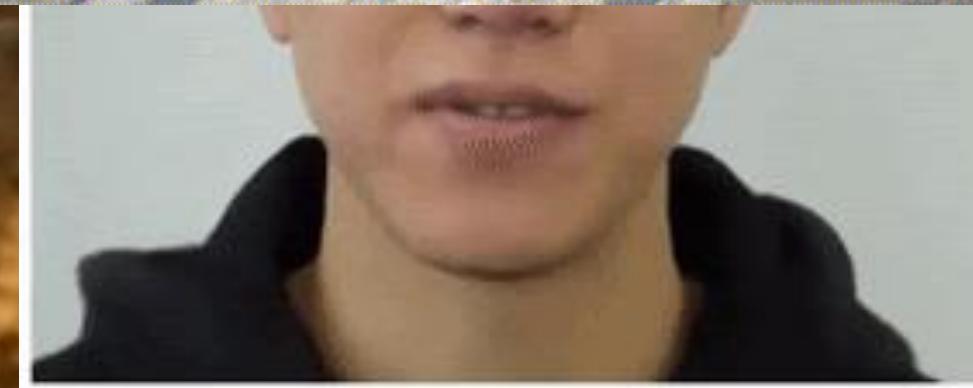
NeRF



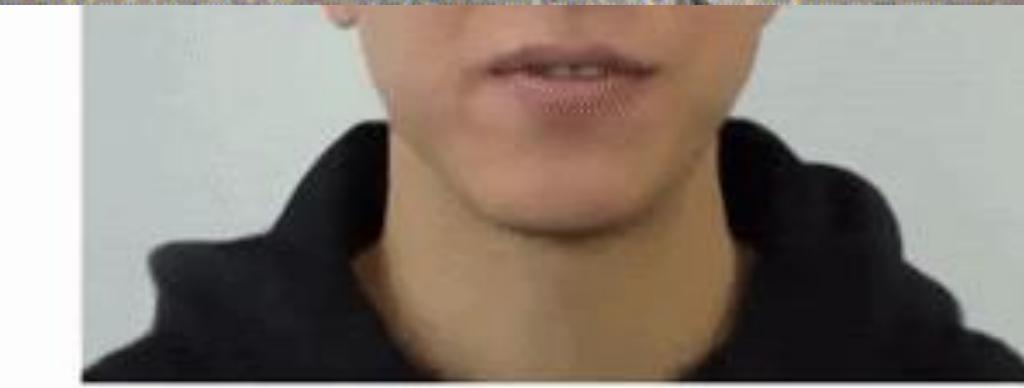
Neural Scene Flow Fields, Li et al.



Neural Scene Graphs, Ost et al.



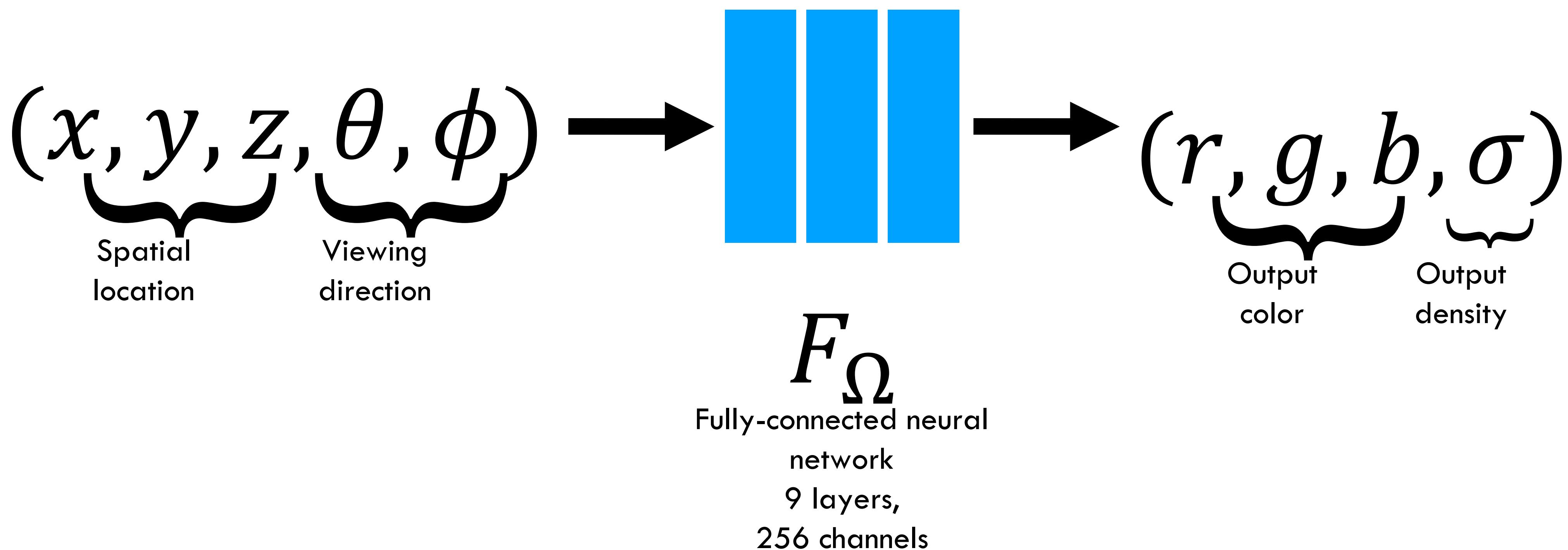
Control Pose



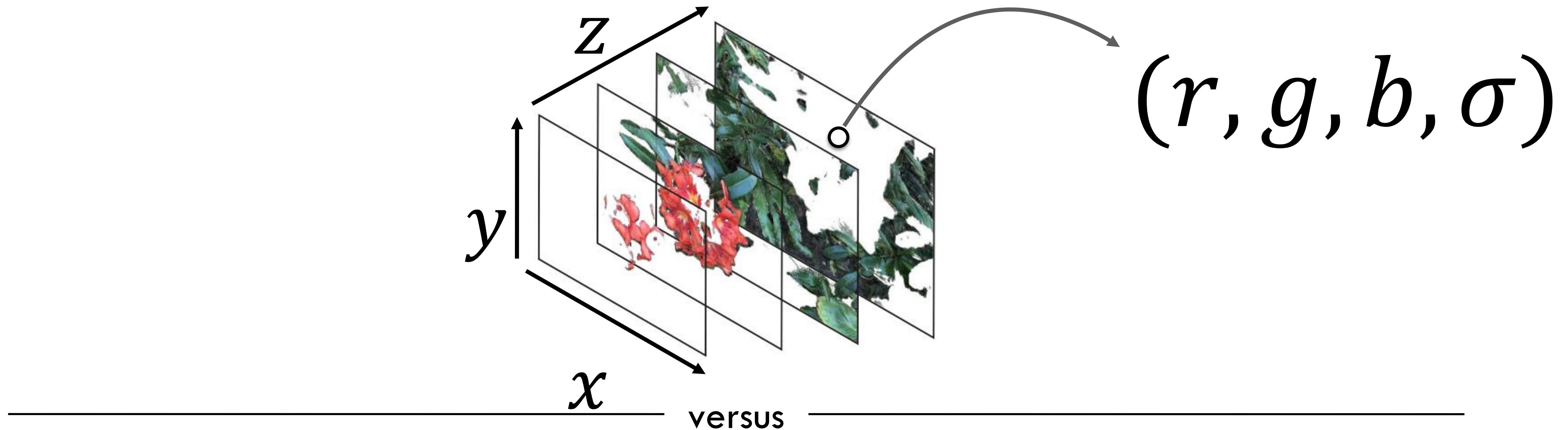
Control Expression

Dynamic Neural Radiance Fields, Gafni et al.

# Representing a scene as a continuous 5D function



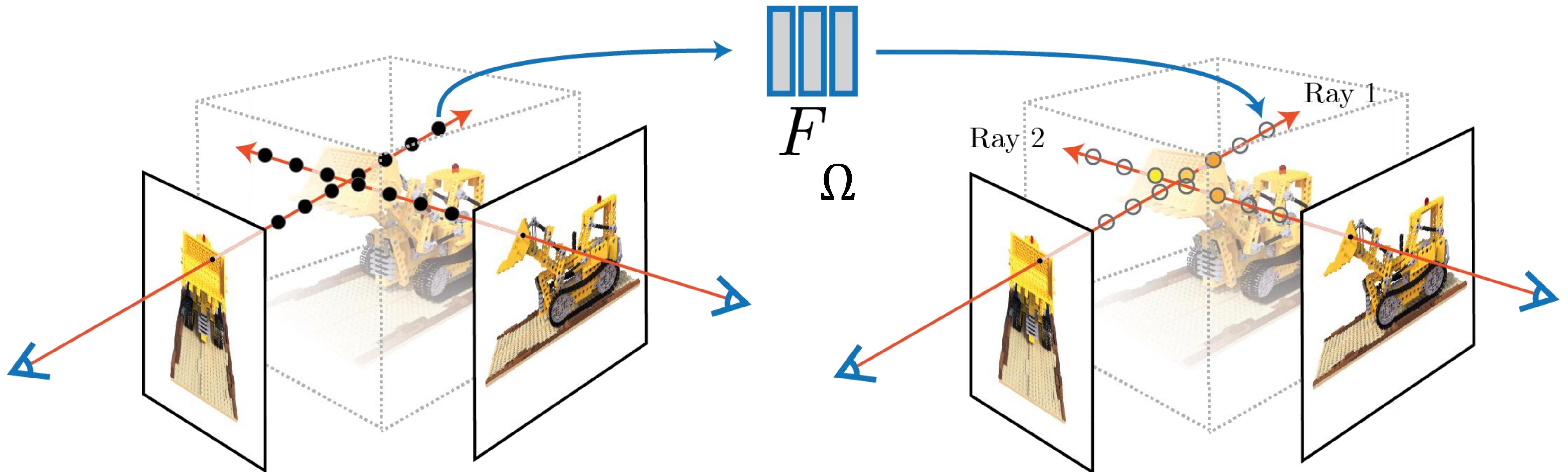
Neural network replaces large N-d array: tradeoff between storage and computation



$$(x, y, z, \theta, \phi) \rightarrow \boxed{\quad | \quad | \quad |} \rightarrow (r, g, b, \sigma)$$

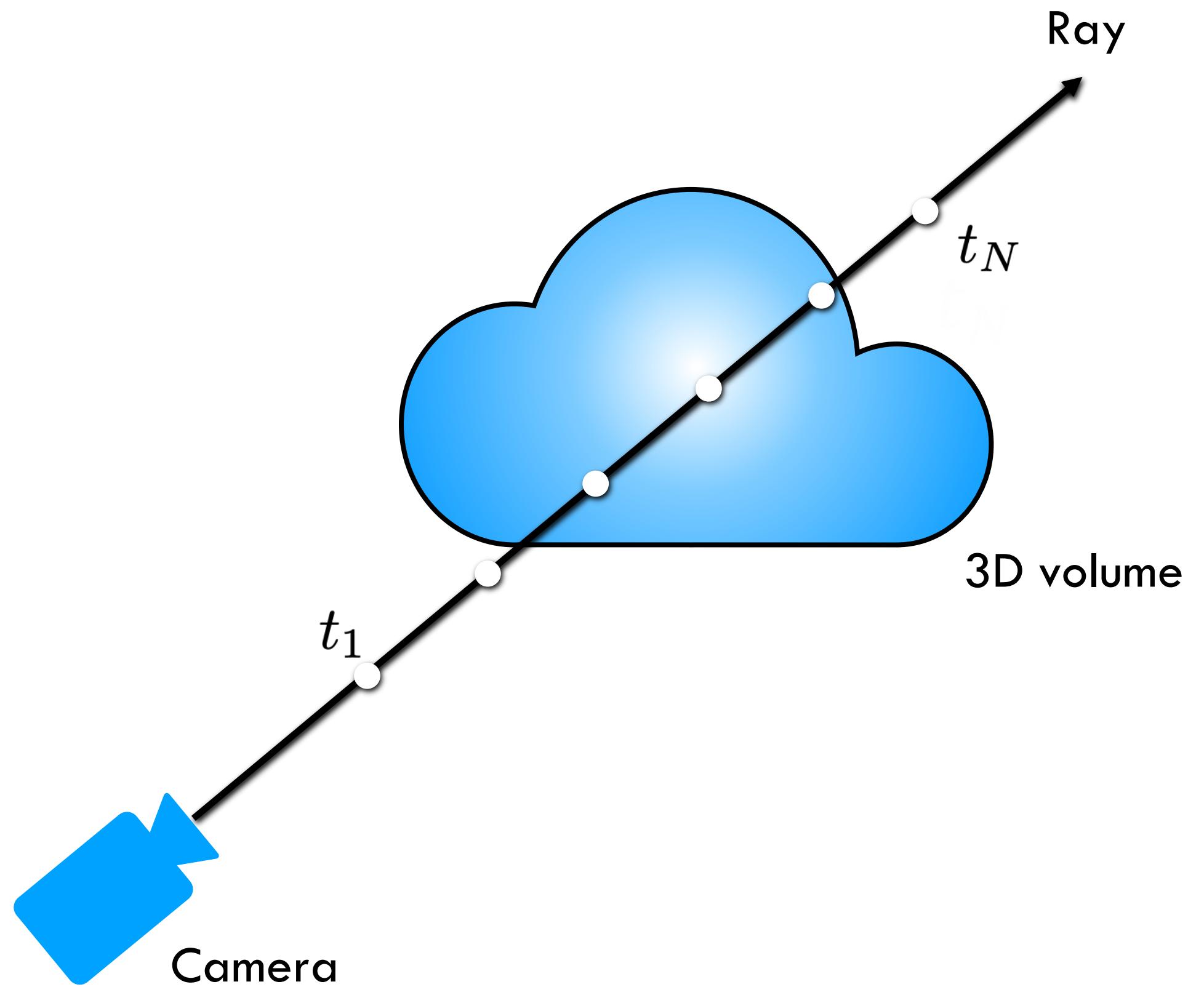
$$F_{\Omega}$$

# Generate views with traditional volume rendering



# Generate views with traditional volume rendering

Rendering model for ray  $r(t) = o + td$ :



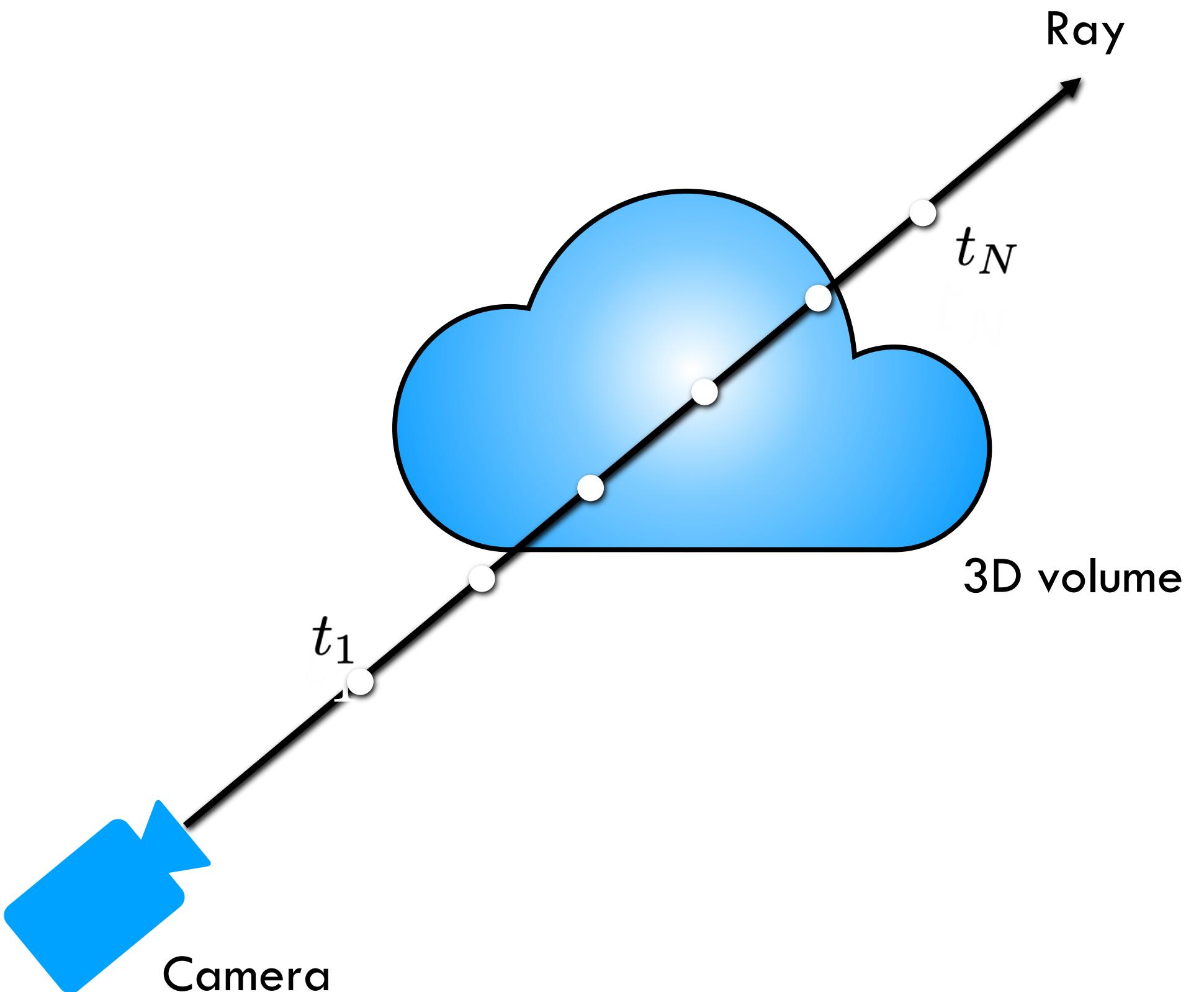
# Generate views with traditional volume rendering

Rendering model for ray  $r(t) = o + td$ :

$$C \approx \sum_{i=1}^N T_i \alpha_i c_i$$

weights

colors



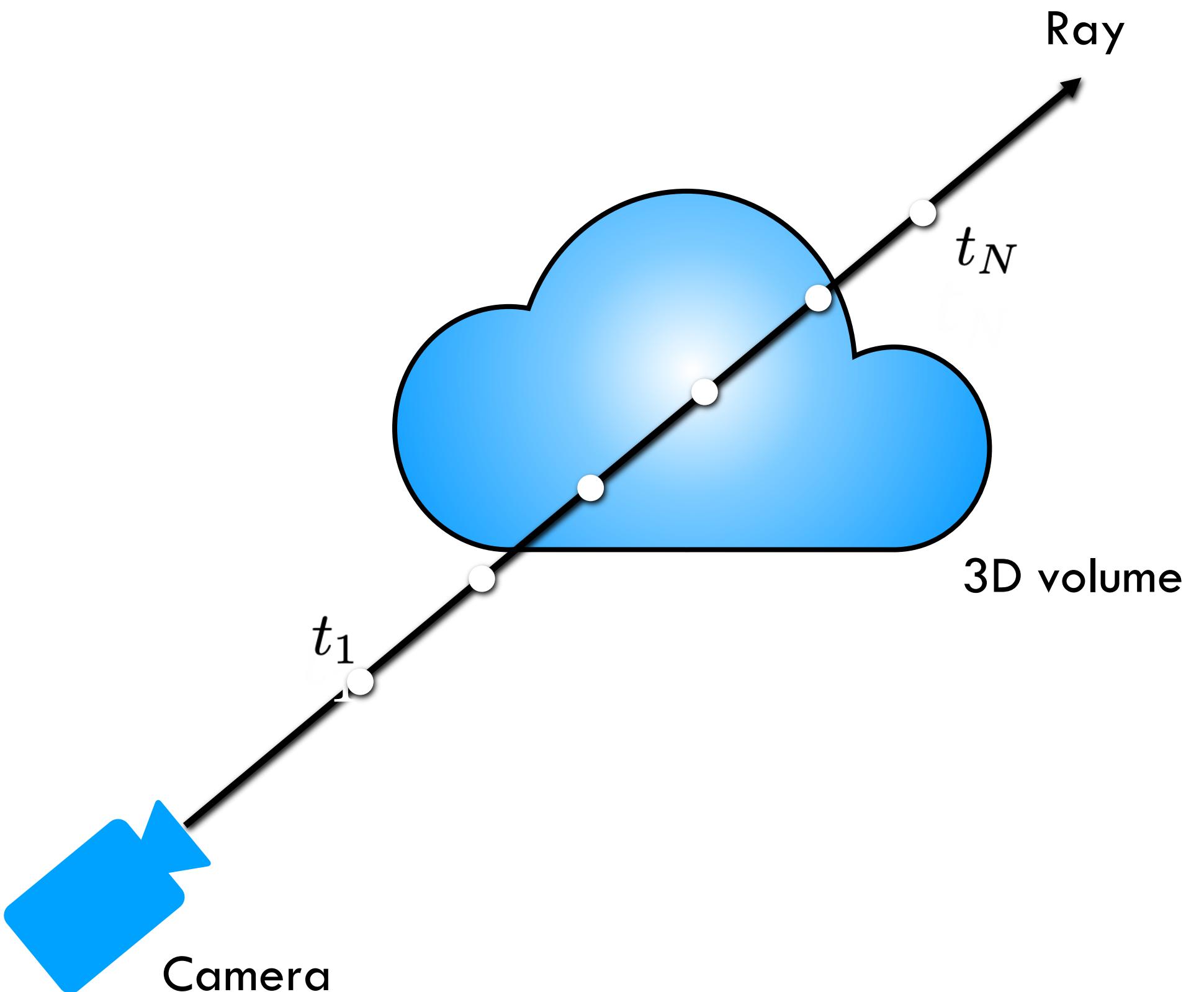
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# Generate views with traditional volume rendering

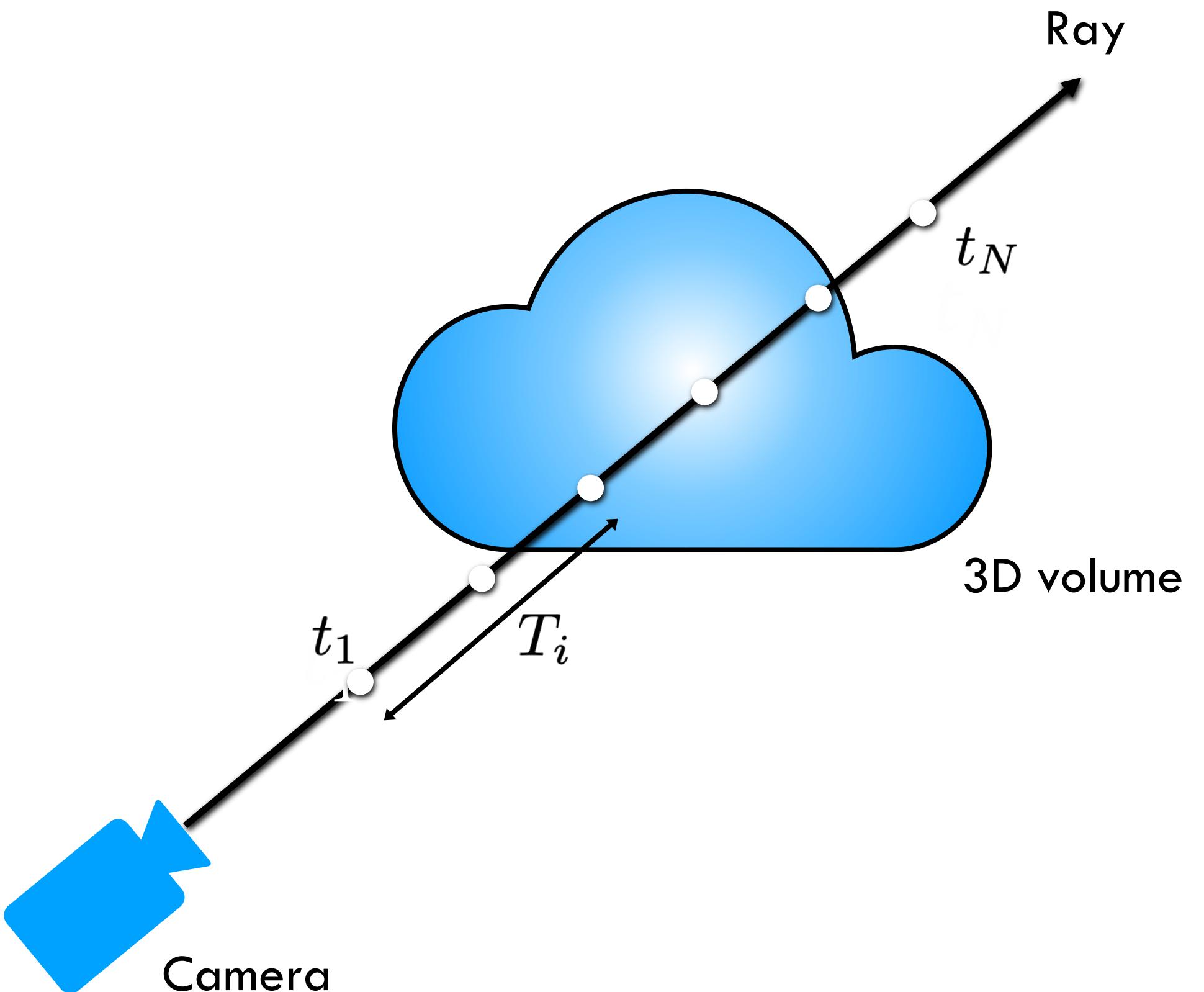
Rendering model for ray  $r(t) = o + td$ :

$$C \approx \sum_{i=1}^N T_i \alpha_i c_i$$

weights      colors

How much light is blocked earlier along ray:

$$T_i = \prod_{j=1}^{i-1} (1 - \alpha_j)$$



# Generate views with traditional volume rendering

Rendering model for ray  $r(t) = o + td$ :

$$C \approx \sum_{i=1}^N T_i \alpha_i c_i$$

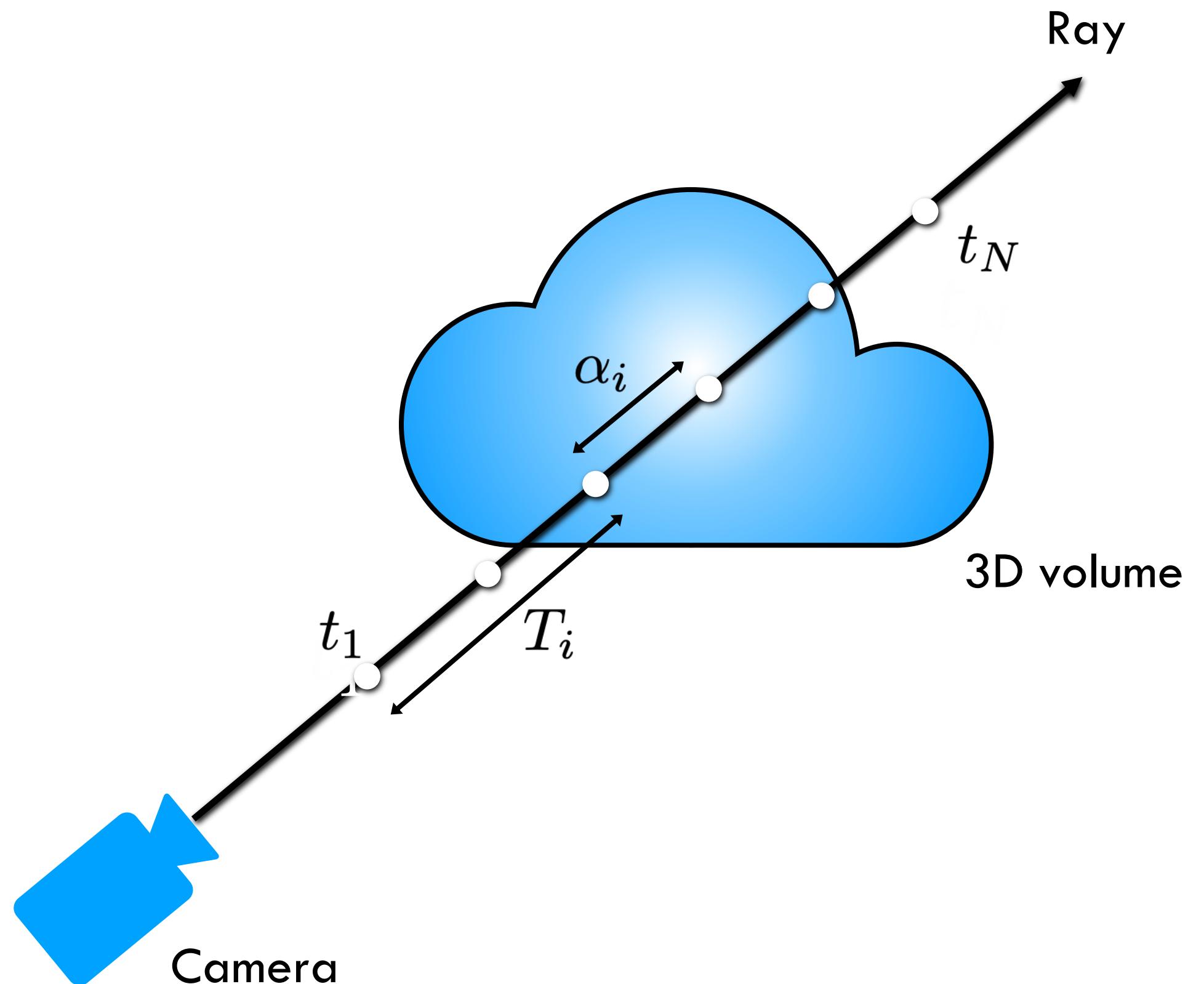
weights                      colors

How much light is blocked earlier along ray:

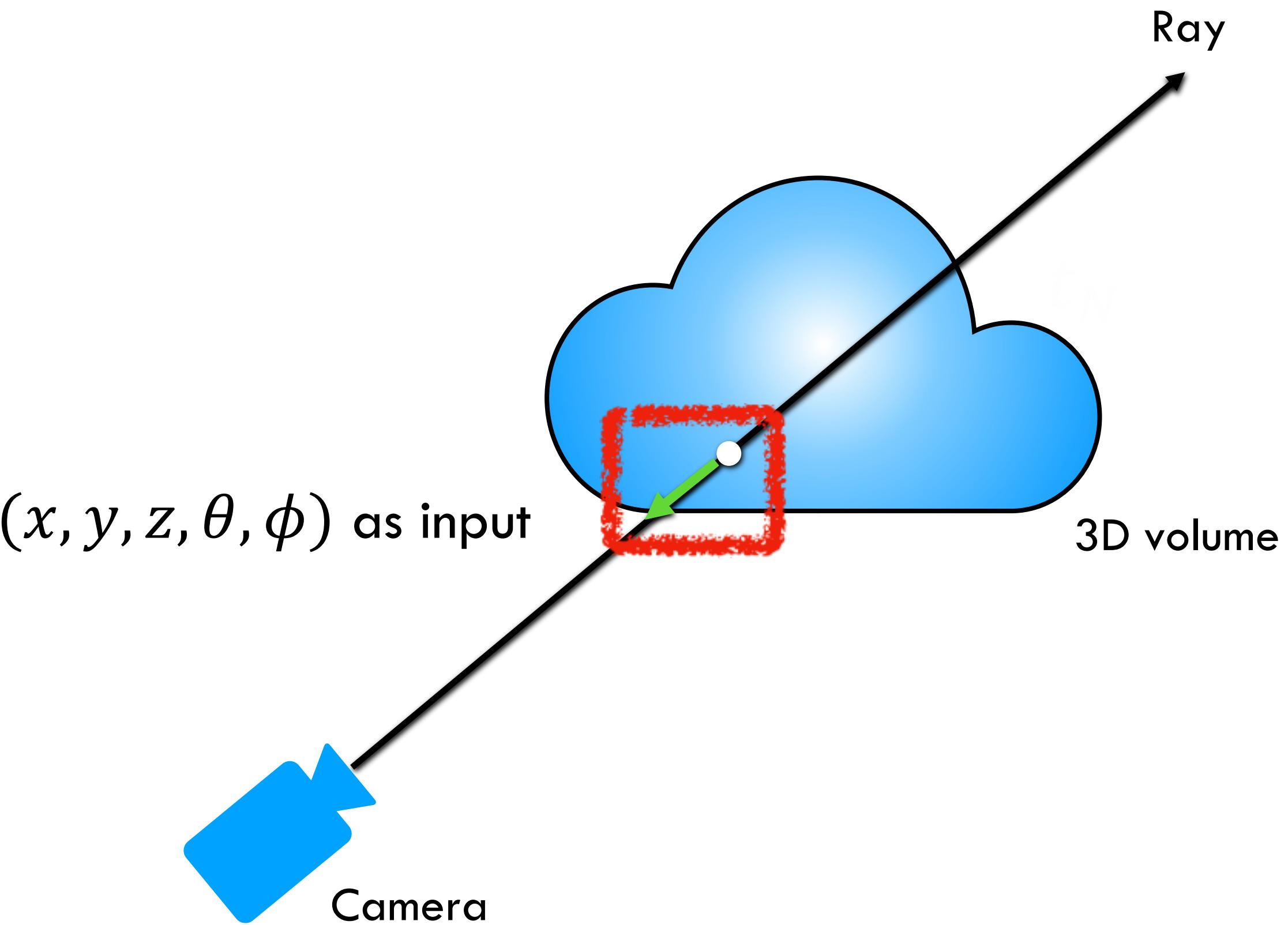
$$T_i = \prod_{j=1}^{i-1} (1 - \alpha_j)$$

How much light is contributed by ray segment  $i$ :

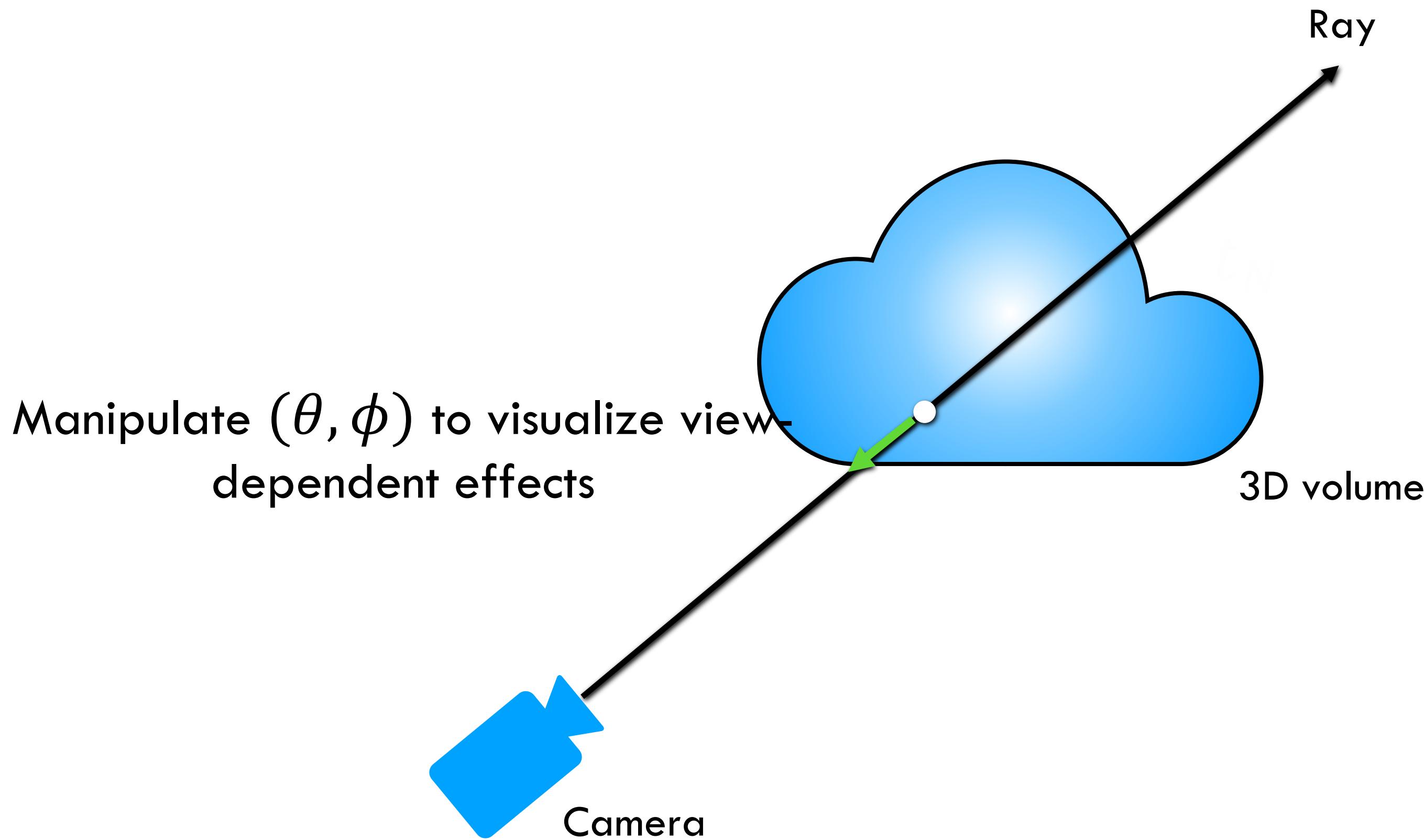
$$\alpha_i = 1 - e^{-\sigma_i \delta t_i}$$



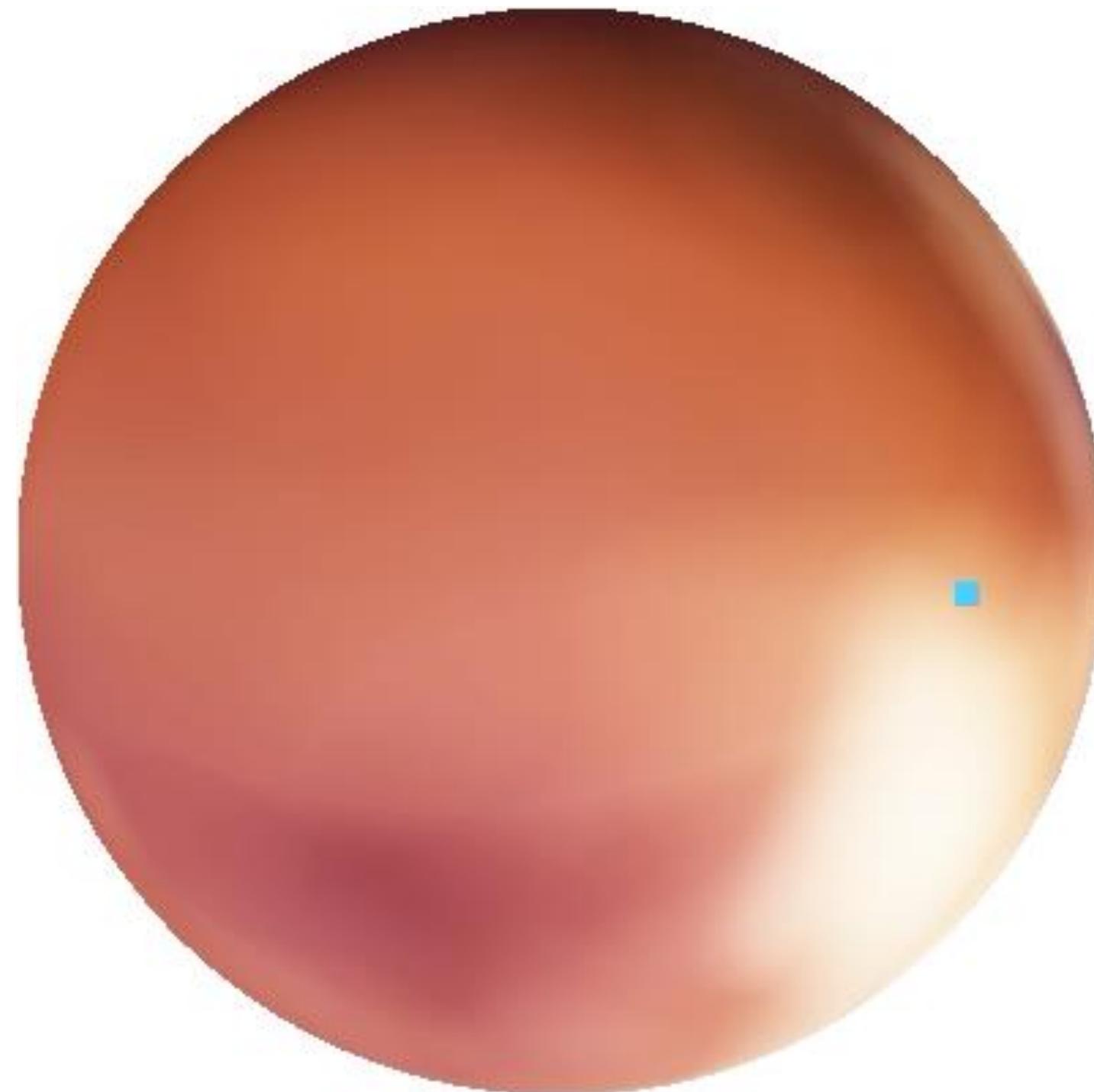
# Viewing directions as input



# Viewing directions as input



# Viewing directions as input



Radiance distribution for  
point on side of ship



Radiance distribution for  
point on water's surface

# Volume rendering is trivially differentiable

Rendering model for ray  $r(t) = o + td$ :

$$C \approx \sum_{i=1}^N T_i \alpha_i c_i$$

weights

colors

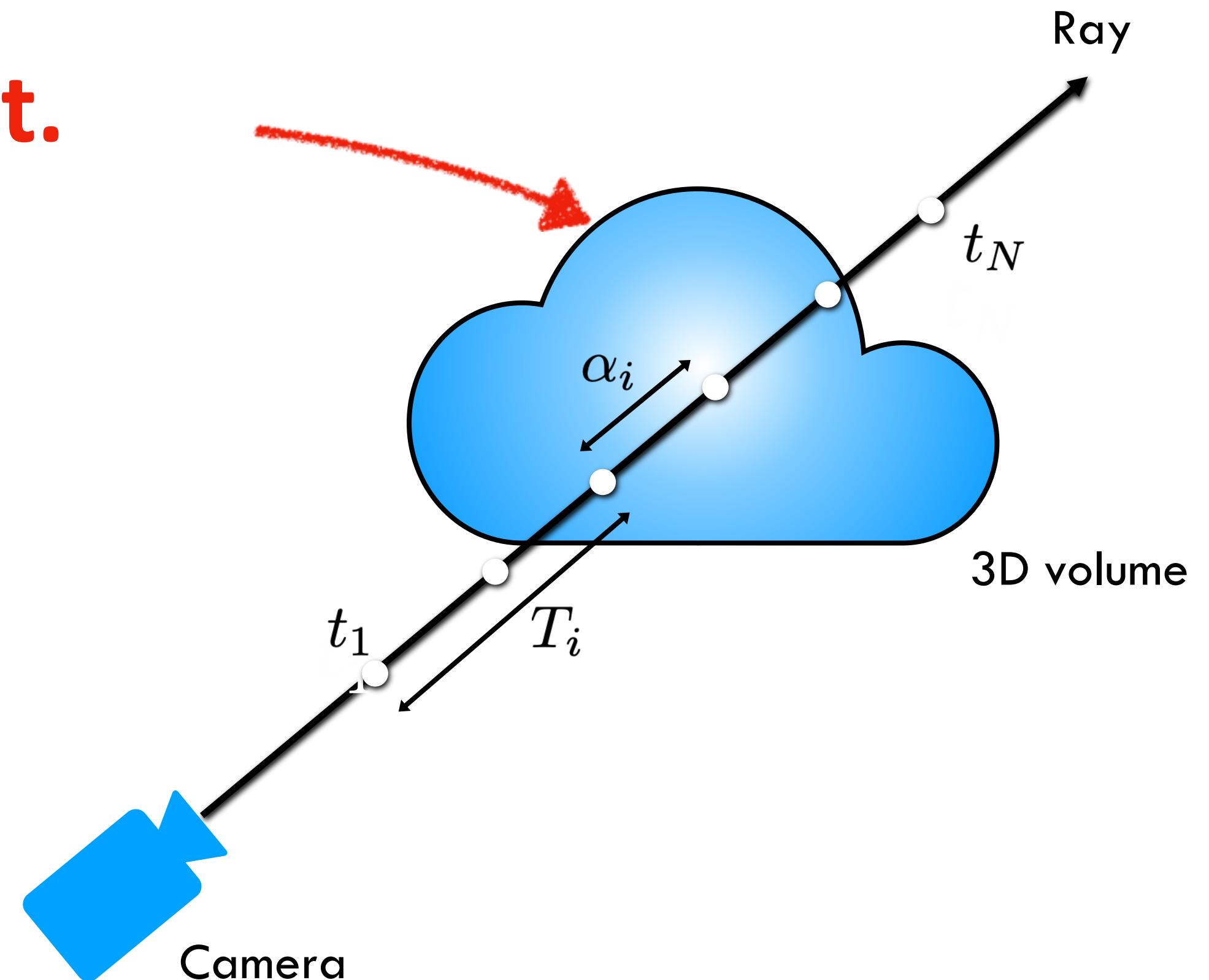
**differentiable w.r.t.**

How much light is blocked earlier along ray:

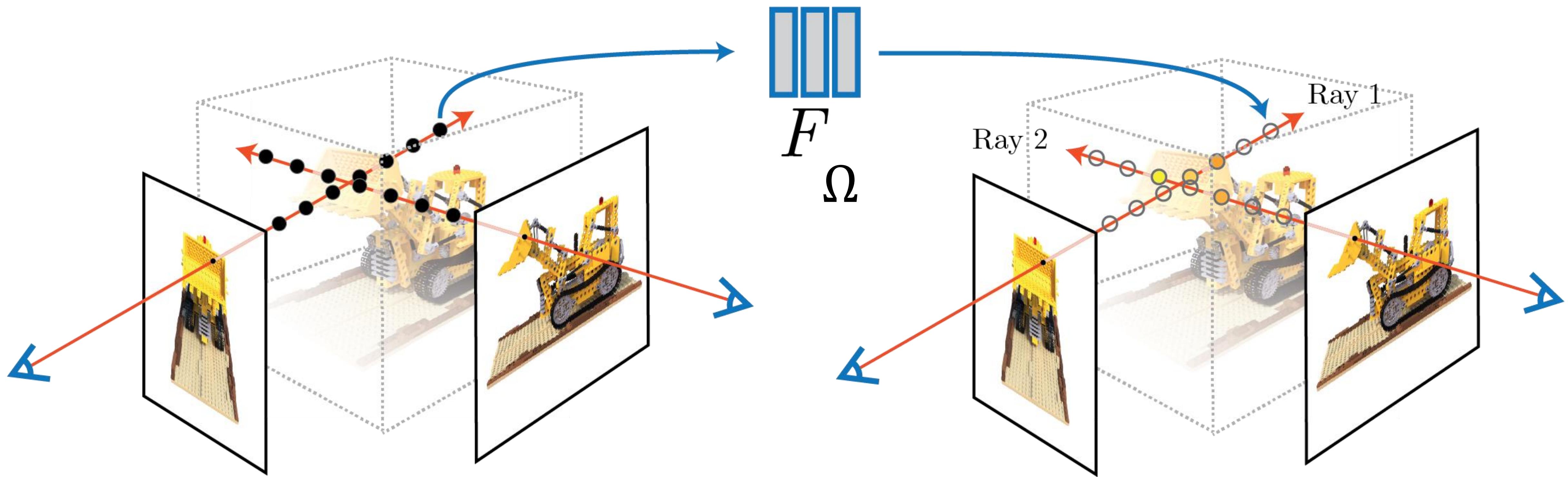
$$T_i = \prod_{j=1}^{i-1} (1 - \alpha_j)$$

How much light is contributed by ray segment  $i$ :

$$\alpha_i = 1 - e^{-\sigma_i \delta t_i}$$



# Optimize with gradient descent on rendering loss



$$\min_{\Omega} \sum_i \| \text{render}^{(i)}(F_\Omega) - I_{\text{gt}}^{(i)} \|^2$$

# Optimize with gradient descent on rendering loss

Any differentiable scene representation  $F_\Omega$   
could be used here

$$\min_{\Omega} \sum_i \| \text{render}^{(i)}(F_\Omega) - I_{\text{gt}}^{(i)} \|^2$$

# Training network to reproduce all input views of the scene



# Naive implementation produces blurry results



NeRF (Naive)

# Naive implementation produces blurry results



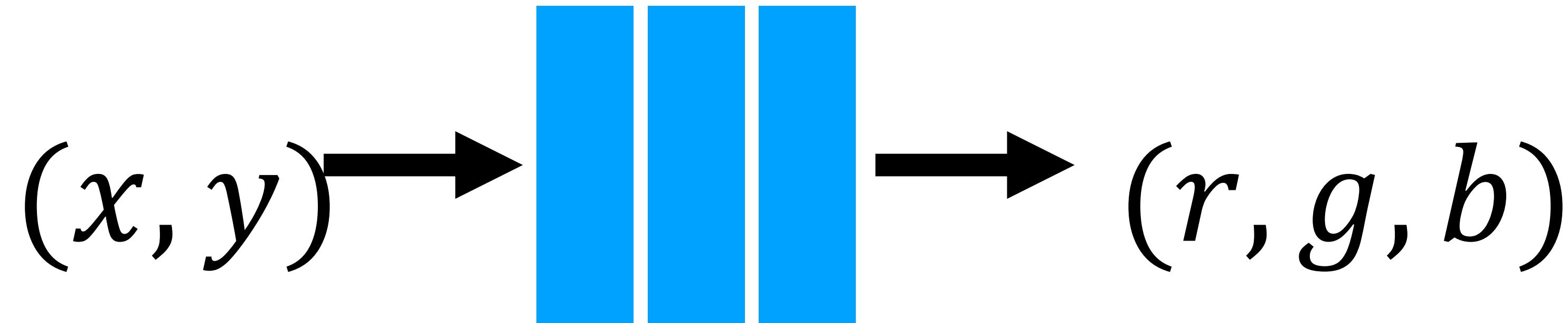
NeRF (Naive)



NeRF (with positional encoding)

**Challenge:**  
How to get MLPs to represent higher frequency functions?

# Simpler toy problem: memorizing a 2D image

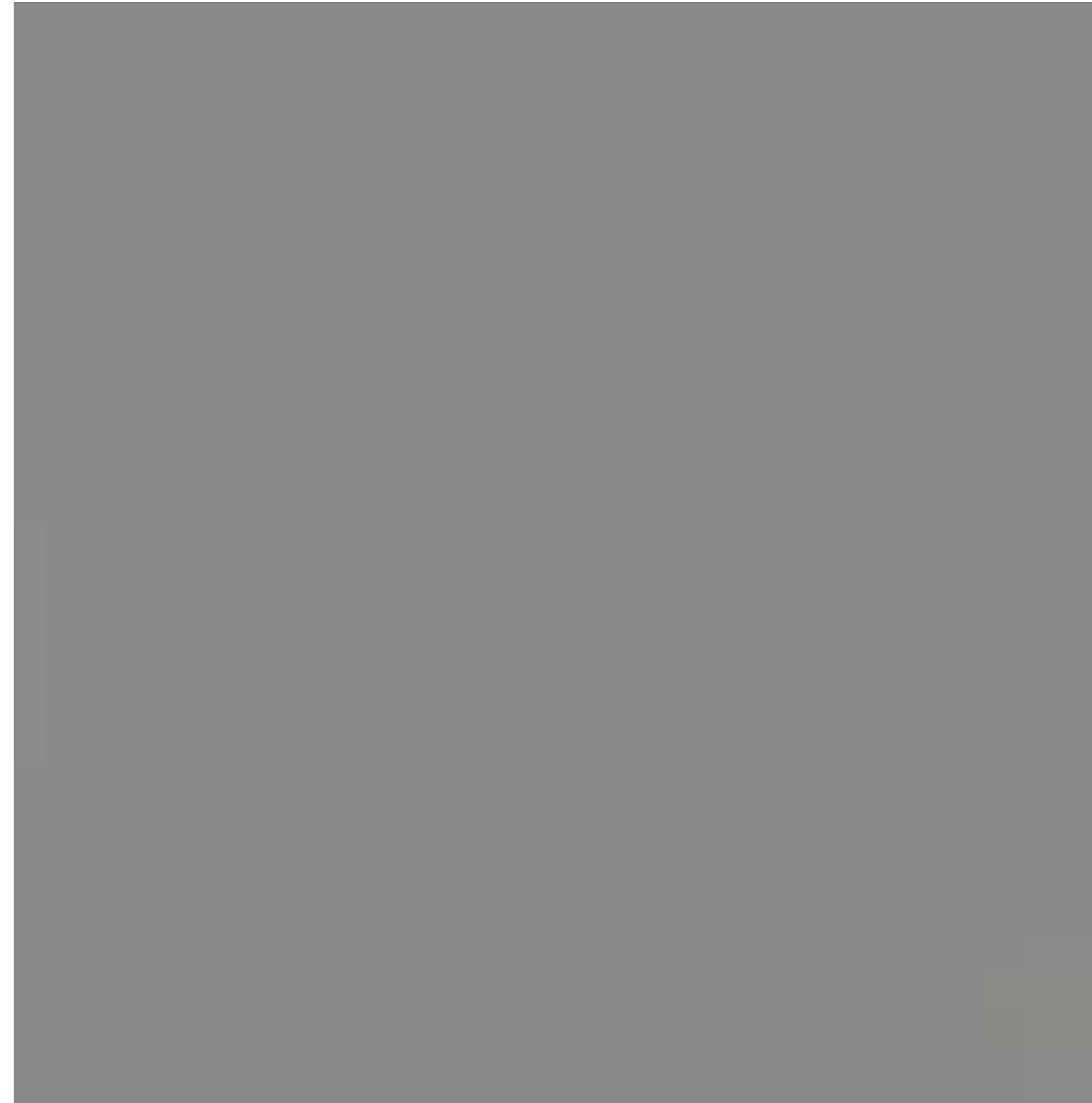


# Simple trick enables network to memorize images

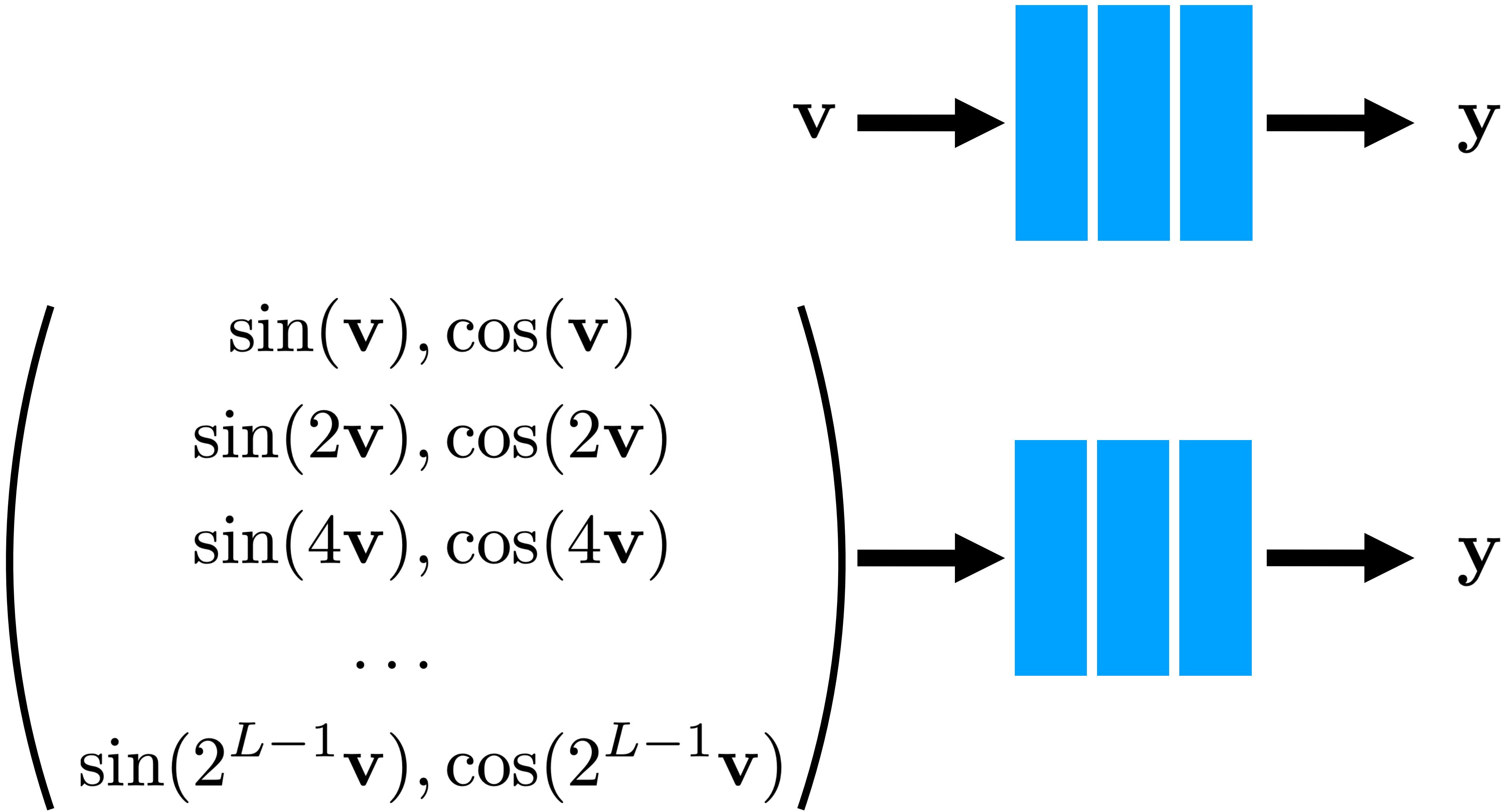
Ground truth image



Standard fully-connected net



# Positional encoding



# Training networks $\approx$ kernel regression

---

- ▶ Recent ML theory work shows that training neural network with gradient descent becomes the same as performing kernel regression as the width of each layer goes to infinity
- ▶ Can examine corresponding kernel function (the neural tangent kernel) to see why adding Fourier feature mapping allows MLPs to represent high frequency functions

# Kernel regression

- ▶ Method for fitting a continuous function to a set of data points  $\{(x_i, y_i)\}$
- ▶ High level: add up a set of blobs (kernel functions), one centered at each input point, each with its own weight
- ▶ Weights are optimal in a least-squares sense:  $\min_w \sum_i \|y_i - \hat{f}_w(x_i)\|^2$

$$\hat{f}_w(x) = \sum_{i=1}^n w_i k(x - x_i)$$

Estimated function

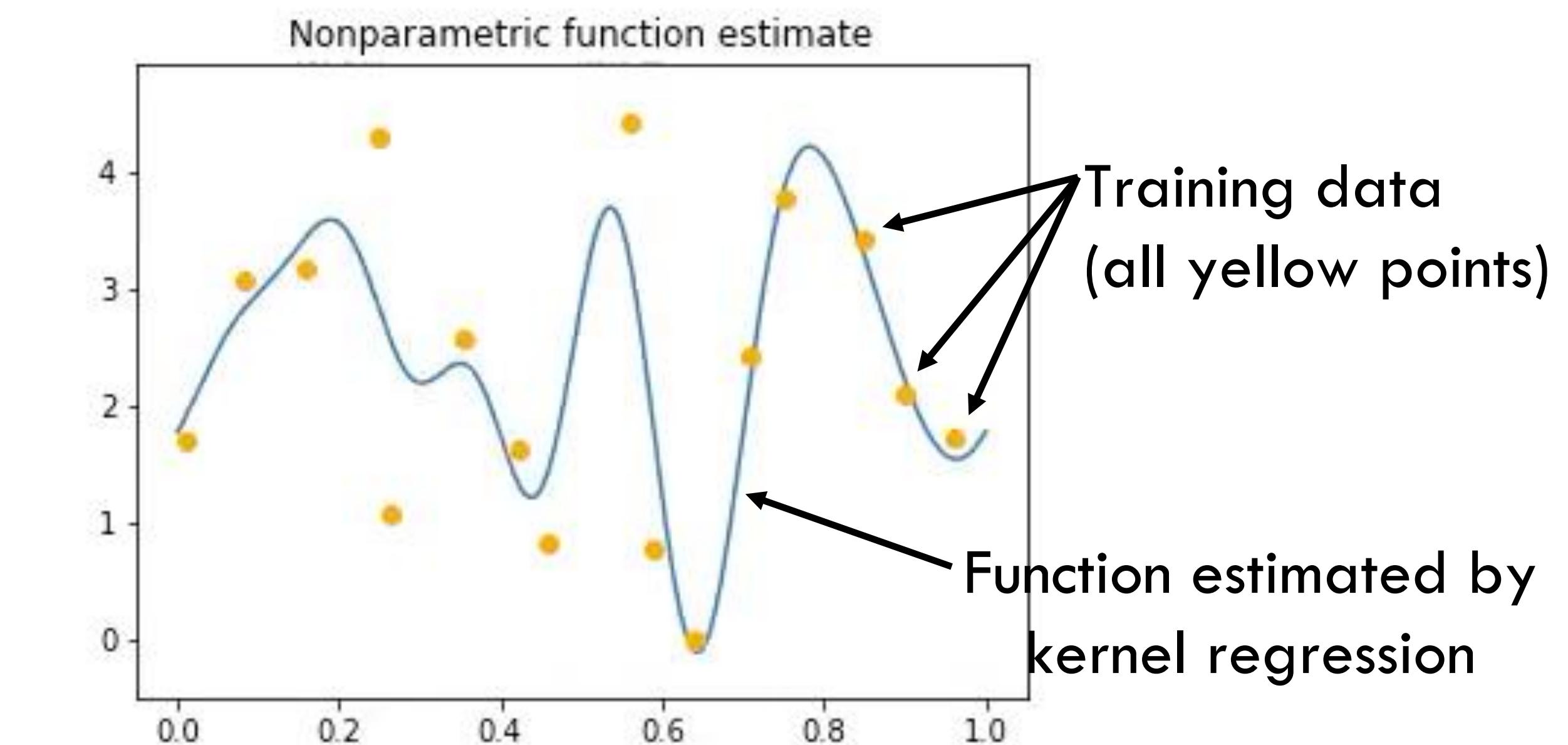
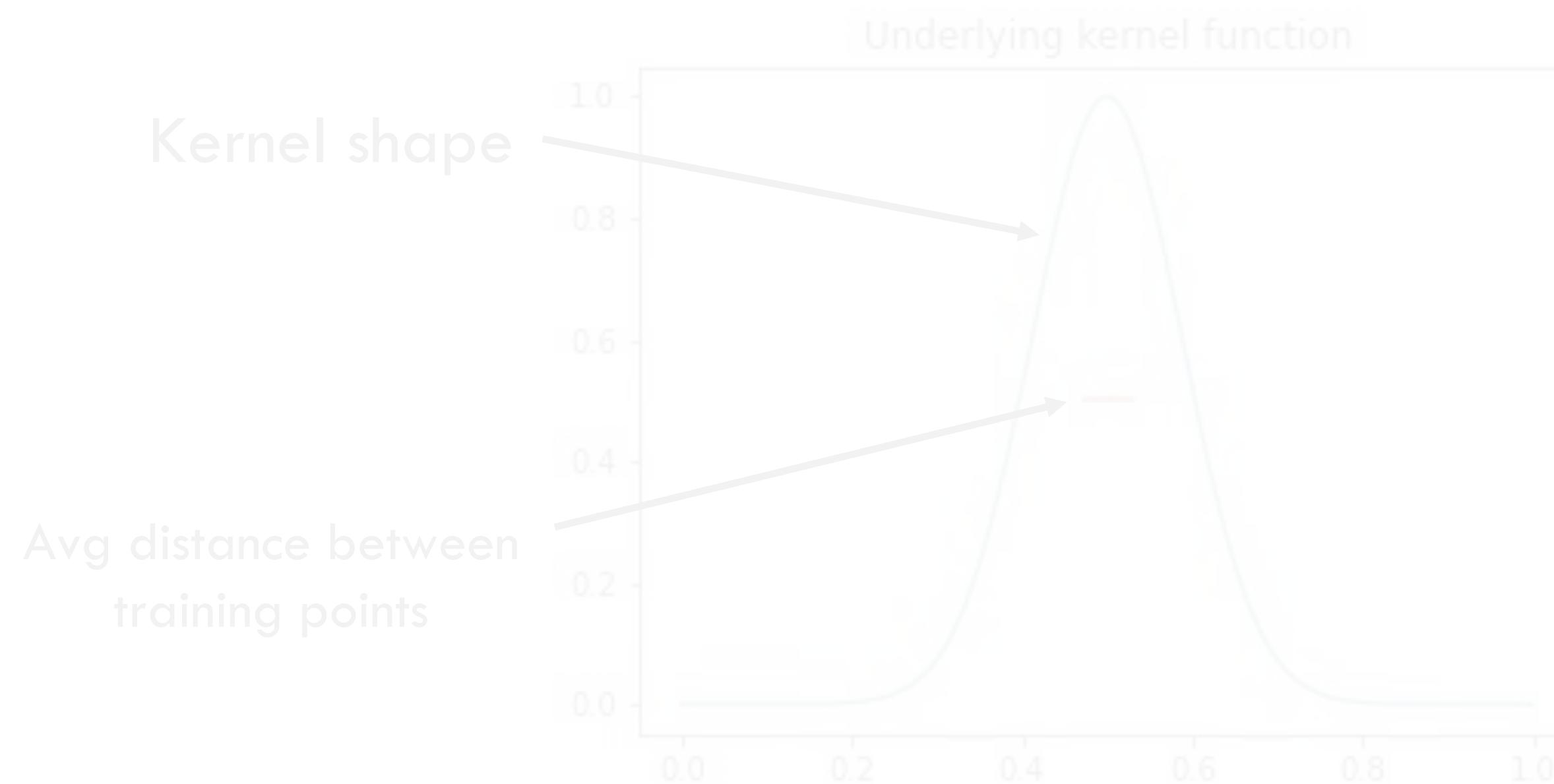
Weight corresponding to blob centered at  $x_i$

Blob centered at training input point  $x_i$

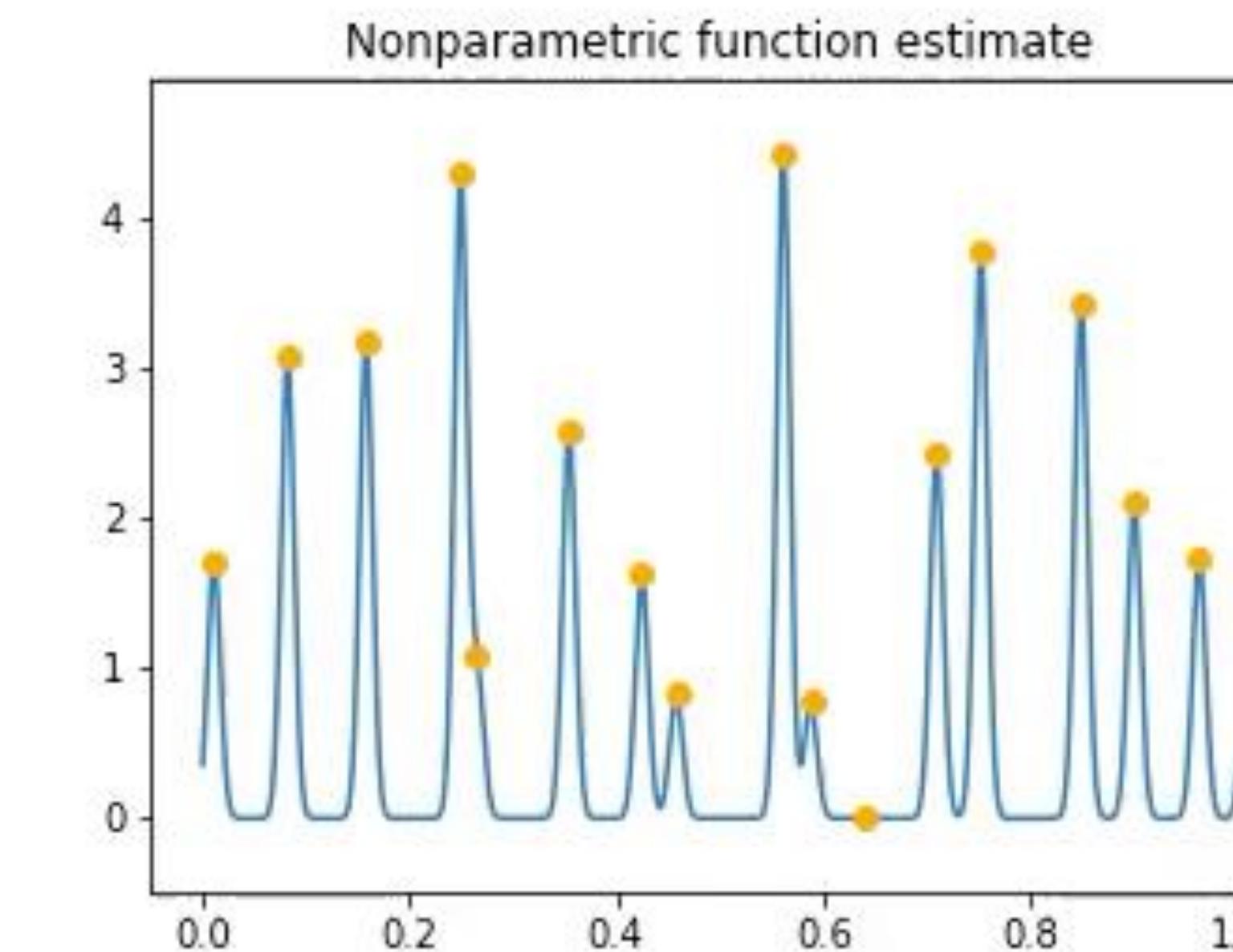
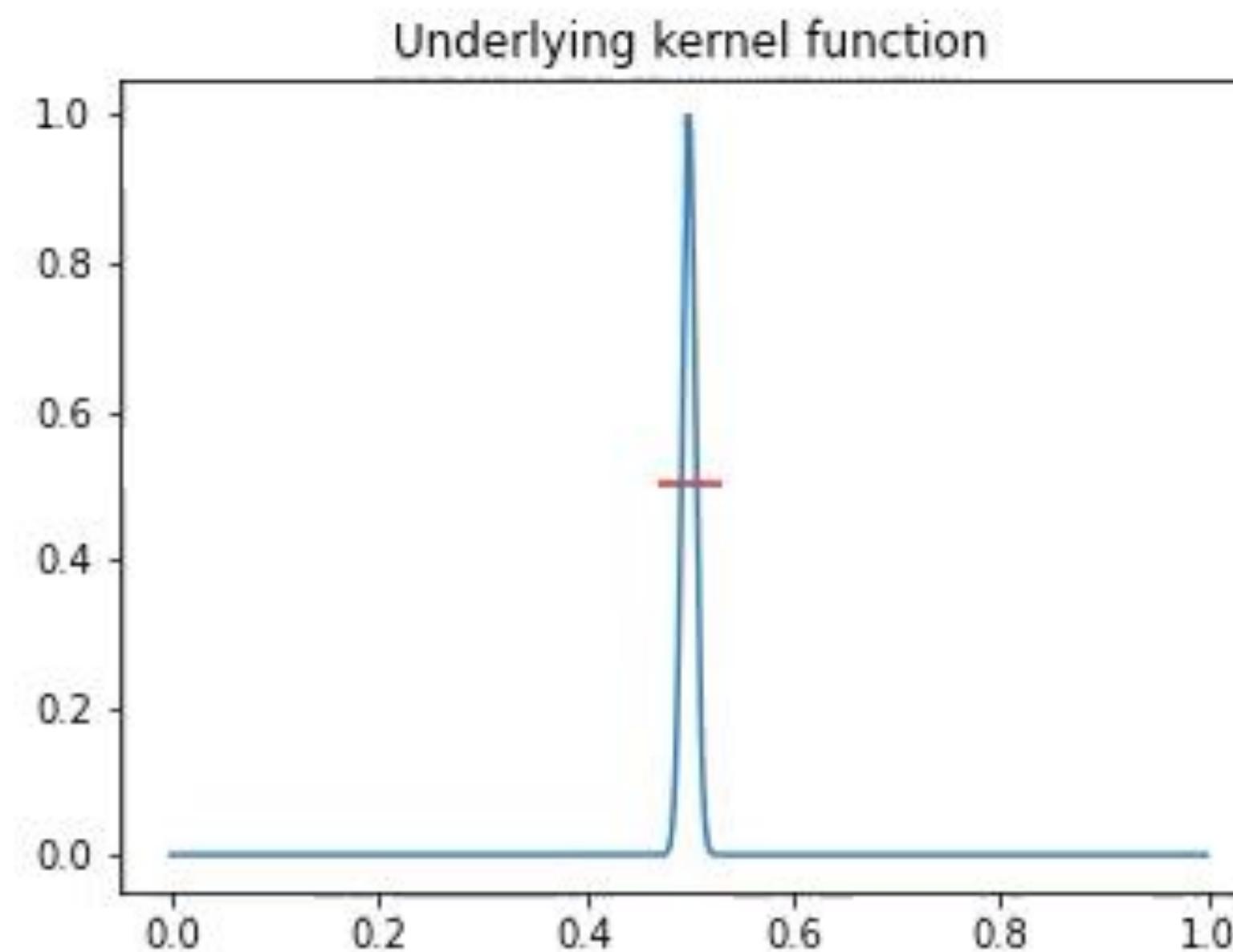
# “Width” of kernel function is critical

- ▶ If the kernel function is too wide, reconstruction is too smooth. If it's too skinny, reconstruction does not interpolate correctly.
- ▶ Similar to picking the right reconstruction filter bandwidth in signal processing to avoid either blurring or aliasing.

# “Width” of kernel function is critical



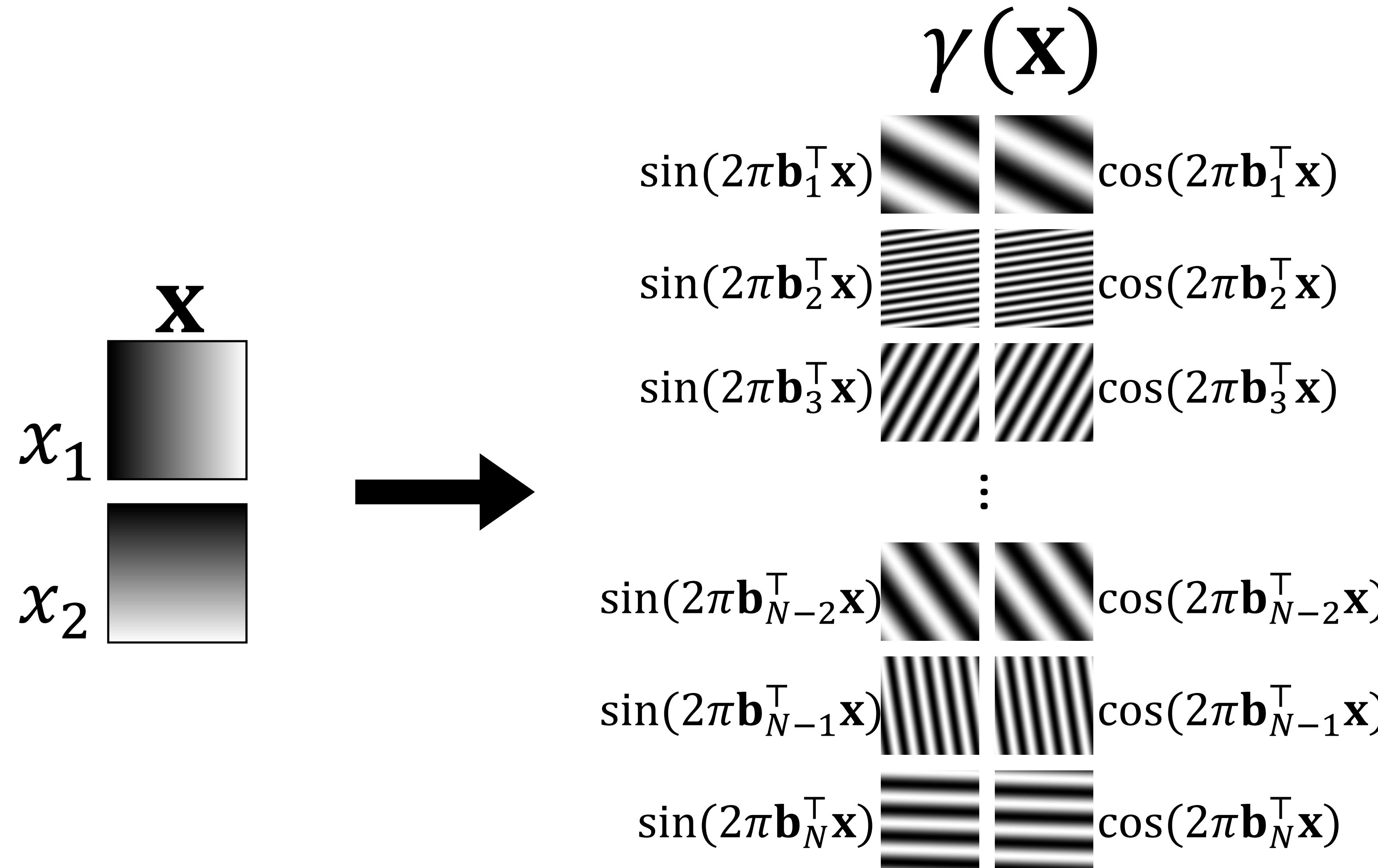
# “Width” of kernel function is critical



# Training networks $\approx$ kernel regression

- ▶ Recent ML theory work shows that training neural network with gradient descent becomes the same as performing kernel regression as the width of each layer goes to infinity
- ▶ Using a Fourier feature mapping changes the corresponding kernel function (the neural tangent kernel), allowing MLPs to represent higher frequency functions

# Fourier feature mapping: simple 2D example



# Simple trick enables network to memorize images

Ground truth image



Standard fully-connected net



With “encoding”



Positional encoding also directly improves our scene representation!



NeRF (Naive)



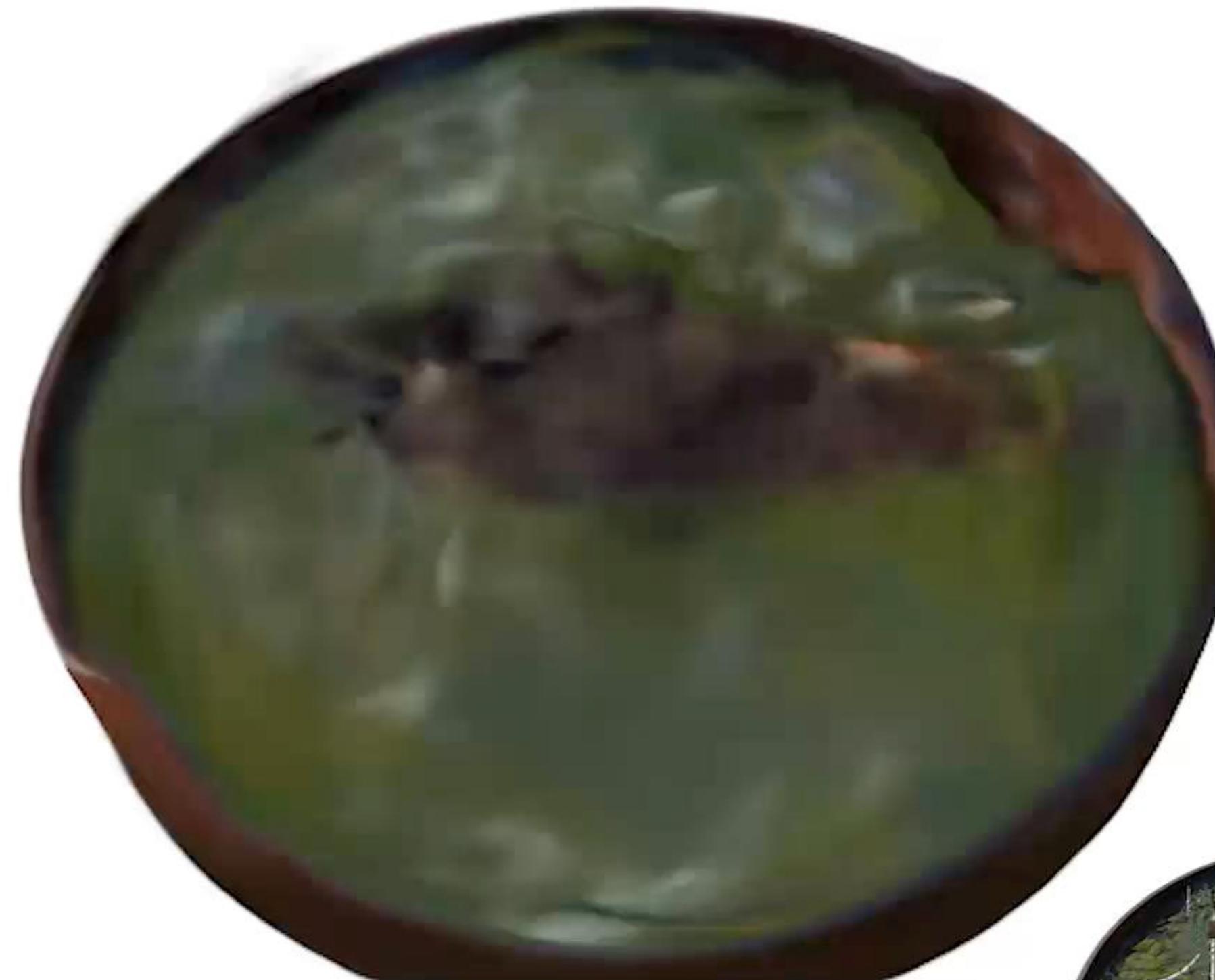
NeRF (with positional encoding)

Check out <https://bmild.github.io/fourfeat/> for more details



More detailed and consistent than prior work that represents scene as function encoded by MLP

SRN [Sitzmann et al. 2019]



NeRF



Nearest Input

# NeRF encodes convincing view-dependent effects using directional dependence



NeRF encodes convincing view-dependent effects using directional dependence



NeRF encodes detailed scene geometry with occlusion effects



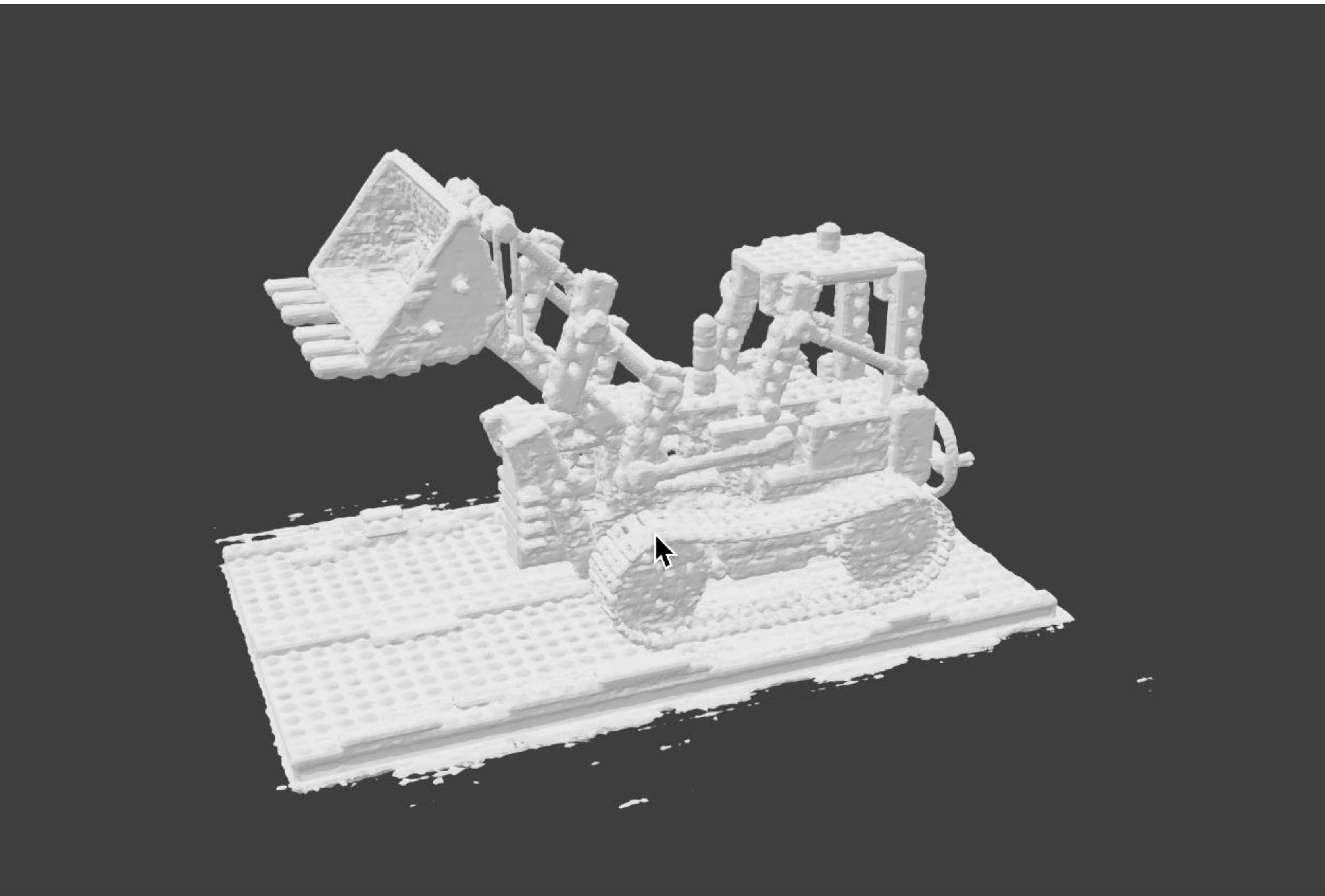
NeRF encodes detailed scene geometry with occlusion effects



# NeRF encodes detailed scene geometry with occlusion effects



# NeRF encodes detailed scene geometry



# NeRF: Key points

- ▶ Continuous neural network as a volumetric scene representation ( $5D = xyz + \text{direction}$ )
- ▶ Use volume rendering model to synthesize new views
- ▶ Optimize using rendering loss for one scene (no prior training)
- ▶ Apply positional encoding before passing coordinates into network to recover high frequency details