ASTR2013_ass1

August 1, 2019

1 Q1 2/2

From chain rule we get:

$$f_{\nu} = \frac{df}{d\nu} = \frac{df}{d\lambda} \frac{d\lambda}{d\nu} = -\frac{d\lambda}{d\nu} f_{\lambda}$$

where we use the minus sign for correcting for making f_{λ} positive.

As

$$\lambda = \frac{c}{v} \quad \frac{d\lambda}{dv} = -\frac{c}{v^2}$$

We get the conversion formula:

$$f_{\nu} = \frac{c}{\nu^2} f_{\lambda} = \frac{\lambda^2}{c} f_{\lambda}$$

2 Q2

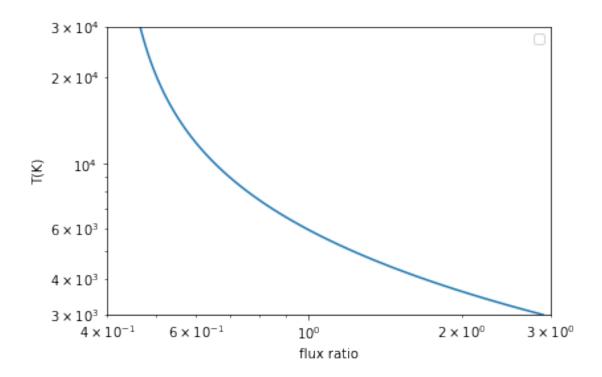
(a) 1.5/2 - The flux equation is missing a factor of pi

```
In [1]: import astropy.constants as c, astropy.units as u
    import numpy as np, matplotlib.pyplot as plt
```

In [3]:
$$F = lambda \ lambd$$
, $T: 2*c.h*c.c**2/lambd**5/(np.exp(c.h*c.c/lambd/c.k_B/T)-1)$
 $F_1 = F(lambd_1, T)$
 $F_2 = F(lambd_2, T)$

Log-log plot of temperature vs measured flux ratio with temperature varying between 3000 and 30000K.

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1.5/2 - Missed out some steps in the algebra to get to the final equation

(b)
In Wien's limit, flux ratio writes:

$$f_{\lambda} = \frac{2hc^2}{\lambda^5} e^{-\frac{hc}{\lambda kT}}$$

For two wavelength, we get:

$$f_1 = \frac{2hc^2}{\lambda_1^5} e^{-\frac{hc}{\lambda_1 kT}}$$

$$f_2 = \frac{2hc^2}{\lambda_2^5} e^{-\frac{hc}{\lambda_2 kT}}$$

Hence the flux ratio writes:

$$\frac{f_2}{f_1} = \frac{\lambda_1^5}{\lambda_2^5} e^{\frac{hc}{kT}(\frac{1}{\lambda_1} - \frac{1}{\lambda_2})}$$

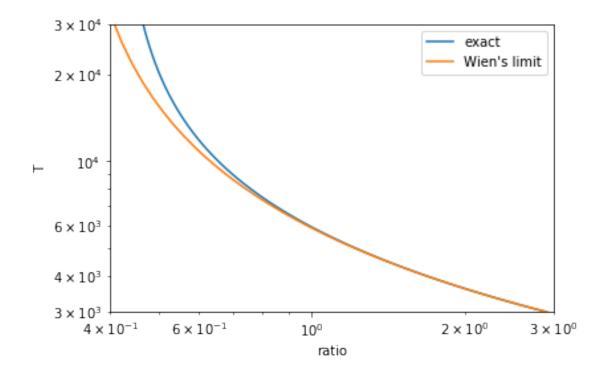
After a few algebra, we can get the temperature is given by:

$$T = \frac{hc}{k_B} \left(\frac{1}{\lambda_1} - \frac{1}{\lambda_2} \right) \frac{1}{\ln(f_2/f_1) + 5\ln(\lambda_2/\lambda_1)}$$

Plot of approximation formula and exact formula

In [5]: T_wien = lambda lambd_1, lambd_2, f_r:
$$(c.h*c.c/c.k_B*(1/lambd_1-1/lambd_2) / (np.log(f_r)+5*np.log(lambd_2/lambd_1))).to(u.K)$$

Out[7]: [0.4, 3.0, 3000, 30000]



we can see that when temperature is high or the flux ratio is low, wien's limit is not very good. **(c)**

From Poisson statistics, the uncertainty of measurement is $\sqrt{N} = \sqrt{10000}$ 100

$$\sqrt{N} \approx \sqrt{10000} = 100$$

Then precision of measurement $\approx 100/10000 = 0.01$

precision of flux ratio is approximately $\sqrt{0.01^2 + 0.01^2} \approx 0.01414$

we use the following code to illustate the accuracy of temperature measurement using flux ratio.

At low temperature, we use the wien approximation as it gives a good approximation to the exact case.

At high temperature, we use intepolation module to calculate the temperature.

```
In [8]: from scipy import interpolate
    err=np.sqrt(0.01**2+0.01**2)

T_ex = interpolate.interp1d(F_2/F_1,T)

T_1 = 4000*u.K
```

Temperature measurement of 4000K fall in range between 3963.14 K to 4032.26 K: Temperature measurement of 20000K fall in range between 18896.47 K to 21285.47 K:

3/3 - Good job!

We can see that the precision of measurement of 4000K is about 30/4000=0.75%, whereas for 20000K, the precision is about 1200/20000=6%. The measurement of 4000K is more precise.

3 Q3

(a) 2/2

We use interpolation to calculate the temperature of star

The temperature of star is:5019.73 K

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(b) 1/1
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The distance to the star is:52.63 pc
The distance to the star is:1624040832351153.50 km

(c)

Using inverse square law:

$$f_{earth} = \frac{f_{\lambda} R_{sun}^2}{D^2}$$

we get:

$$R_{sun} = D\sqrt{rac{f_{earth}}{f_{\lambda}}}$$

We perform this calculation for two filters. 1.5/2 - The method is almost right but the factor of pi missing becomes important here; the

The radius of the star is: 1.58 solRad

```
In [12]: lambd = 797*u.nm
    F_earth = 4.8e-13*u.erg/u.s/u.cm**2/u.Angstrom
    ratio = F_earth/F(lambd, T_star)
    R_star = D*np.sqrt(ratio)
    print('The radius of the star is: {:.2f}'.format(R_star.to(u.R_sun)))
```

The radius of the star is: 1.58 solRad

We can see that they give approximately the same answer.

(d)

We calculate Luminosity using Stefan-Boltzmann law:

The Luminosity of the star is: 1.43 solLum

From the temperature and luminosity of the star, we see that it lies in the main sequence in the HR-diagram. They are main sequence star.

1/2 - The luminosity is incorrect, but you correctly identified that a star with a larger radius and luminosity than the sun by about 1.5 times would be a main sequence star.