

$\Sigma = \{a, b, c, \dots, z, _ \}$ 27 letters
 \updownarrow
 $I = \{0, 1, 2, \dots, 25, 26\}$

SHIFT CIPHER

0 1 2 3 4 5 6
 a b c d e f
 c d e f a b
 2 3 4 5 0 1

$$k = C = 2$$

$m =$ deadbeef
 Cipher = f a c f d a a b

$m \in \Sigma^n$
 $k \in \Sigma$

ENCRYPT: $C[i] = (m[i] + k) \bmod \ell$

DECRYPT: $m[i] = (c[i] - k) \bmod \ell$

\uparrow
 by

\uparrow
 length of alphabet (27)

Vigenère cipher

\rightarrow a b c d e f

key = bed (bed bed bed...)

$\begin{array}{cccccc} \text{a} & \text{b} & \text{c} & \text{d} & \text{e} & \text{f} \\ \text{b} & \text{c} & \text{d} & \text{e} & \text{f} & \text{a} \\ \text{c} & \text{d} & \text{e} & \text{f} & \text{a} & \text{b} \\ \text{d} & \text{e} & \text{f} & \text{a} & \text{b} & \text{c} \end{array}$

$\text{key} = \text{bed} (\text{bed bed bed} \dots)$
 143

$m = \text{deadbeef}$

$c = \text{ecdefafd}$

$\begin{array}{cccccc} 0 & 1 & 2 & 3 & 4 & 5 \\ 1 & 2 & 3 & 4 & 5 & 0 \end{array}$

450123

345012

$m \in \sum^n, k \in \sum^p$

ENCRYPT

DECRYPT

$k = 143$

$m = 311325$

$c = 454402$

$$c[i] = (m[i] + k[i \bmod p]) \bmod q$$

$$m[i] = (c[i] - k[i \bmod p]) \bmod p$$