

1:

recursive:

```
def Fib(arg) :
```

```
    if (arg == 0 or arg == 1) :
```

```
        return arg
```

-constant time(1)

```
    else :
```

```
        return Fib(arg - 1) + Fib(arg - 2)
```

- $O(2^{n-1}) + O(2^{n-2})$

complexity: $O(2^{n-1}) + O(2^{n-2}) + O(1) = O(2^n)$

memosation:

```
memo = {}
```

```
def Fib(arg) :
```

```
    if (arg == 0 or arg == 1) :
```

```
        return arg
```

-constant time(1)

```
    if arg in memo :
```

```
        return memo[arg]
```

-constant time(1)

```
    else :
```

```
        memo[arg] = Fib(arg - 1) + Fib(arg - 2)
```

- $O(n)$

```
        return memo[arg]
```

complexity: $O(n) + O(1) + O(1) = O(n)$

Because the recursive method call the function two times for each argument, but the memosation method only call the function once because the previous result is stored in the memory.

2: The storing time will change. Still $O(n)$.

3.1: a: M, N, J, K, L

b: A

c: A

d: F, G, H

e: A, B

f: I, M, N

g: F, G, H

h: left: J, right: K

i: 1

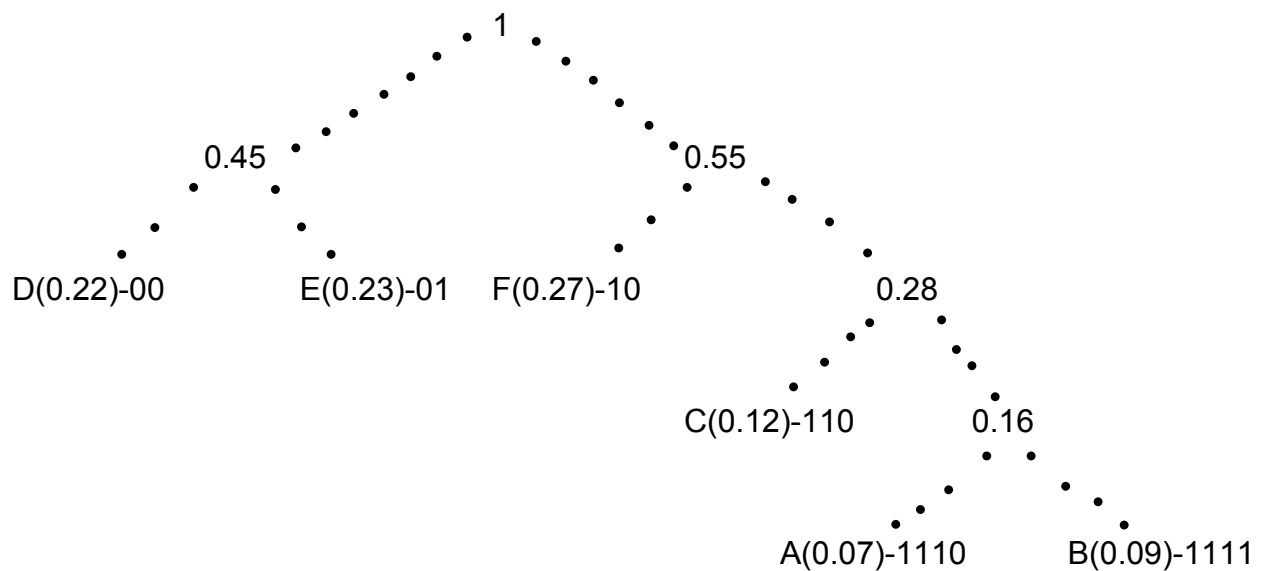
j: 2

3.2: ABEI, ACGJ, ACGK, ACHL, BEIM, BEIN. Therefore, 5 paths.

3.6:

	preorder(n) < preorder(m)	inorder(n) < inorder(m)	postorder(n) < postorder(m)
n is to the left of m	✓	✓	✓
n is to the right of m	✓		✓
n is a proper ancestor of m	✓	✓	
n is a proper descendant of m		✓	✓

3.20:



So: $0.07 * 4 + 0.09 * 4 + 0.12 * 3 + 0.22 * 2 + 0.23 * 2 + 0.27 * 2 = 2.44$

3.21: $\text{depth}(a) > \text{depth}(b)$,

So $\text{length}(a) > \text{length}(b)$ and $\text{probability}(b) = \text{probability}(a) + \text{probability}(\text{others})$.

Therefore, $\text{probability}(a) \leq \text{probability}(b)$.