#### Geophysical Fluid Dynamics – MATH-GA.3001-001

Fall 2025

## Course Description

Geophysical Fluid Dynamics (GFD) applies fluid dynamics to stratified fluids in a rotating reference frame. Rotation and stratification shape the atmosphere and ocean, giving rise to the jet stream, hurricanes, the Gulf Stream, and even the bands on Jupiter.

In this course we will study the equations describing these motions, but just as importantly, we will build the physical intuition that makes GFD one of the most fascinating areas of fluid dynamics. Among these ideas are the shallow water model, which captures the essence of large-scale motion; potential vorticity, a conserved quantity that guides our intuition; and baroclinic instability, a fluid instability that is uniquely geophysical and drives ocean eddies and atmospheric storms. See the schedule on the second page for more details.

#### Instructor

Yi Zhang (y.zhang@nyu.edu) Assistant Professor in Mathematics/Atmosphere Ocean Science

## Logistics

- Class time: Tuesday and Thursday, 2:00–3:15 PM, Warren Weaver Hall 517
- Office hours: Tuesday and Thursday, 3:15–4:15 PM, Warren Weaver Hall 909

#### Assessment

Completion of four problem sets and a take-home final exam.

#### References

- Atmospheric and Oceanic Fluid Dynamics, G. Vallis (Cambridge, any edition)
- Waves in the Ocean and Atmosphere, J. Pedlosky (Springer, 2003)
- Lectures on Geophysical Fluid Dynamics, R. Salmon (Oxford, 1998)
- Atmosphere-Ocean Dynamics, A. Gill (Academic 1982)

# Lecture Schedule

Week	Dates	Topics / Notes
1	9/2, 9/4	Introduction to fluid dynamics and the idea of GFD: continuum approximation, label space and Lagrangian/Eulerian perspectives, material derivatives. (Vallis 1.1)
2	9/9, 9/11	Mass conservation, momentum equation, rotating reference frame, spherical coordinate, hydrostatic balance, primitive equations, fplane and beta-plane approximations, shallow water model. (Vallis 1.2–1.3, 2.1–2.3, 3.1). <b>Problem Set 1</b>
3	9/16, 9/18	Shallow water system: geostrophic balance, potential vorticity, shallow water gravity waves, inertia—gravity waves. (Vallis 3.5, 3.7, 3.8; Pedlosky 13)
4	9/23, 9/25	Shallow water system (continued): Kelvin waves, geostrophic adjustment, geostrophic scaling, quasi-geostrophic equations. (Vallis 3.8, 3.9, 5.1, 5.3; Pedlosky 13, 14, 15)
5	9/30, 10/2	Rossby waves in a single-layer shallow water model: dispersion relation, propagation mechanism, group velocity, energy propagation diagram, energy flux equation. (Vallis 6.2, 6.4; Pedlosky 16). <b>Problem Set 2</b>
6	10/7, 10/9	Asymptotic derivation of the quasi-geostrophic equations, two-layer shallow water model, reduced-gravity model, rigid-lid approximation, thermal wind balance. (Vallis 3.3, 3.5, 5.3.1)
7	10/16	Two-layer QG equations, Rossby waves in the two-layer QG model. (Vallis 5.3.2, 6.4.4)
8	10/21, 10/23	Barotropic instability: parallel shear flows, piecewise shear flows, Rayleigh's equation, jump conditions, edge waves, interaction of edge waves generating instability. (Vallis 9.1, 9.2). <b>Problem Set 3</b>
9	10/28, 10/30	Necessary conditions for barotropic instability – Rayleigh's and Fjortoft's criteria; baroclinic instability in a two-layer QG model. (Vallis 9.3, 9.6)
10	11/4, 11/6	Boussinesq and anelastic approximations, continuously stratified QG PV equation, baroclinic instability in stratified fluids (Eady's model). (Vallis 2.4, 2.5, 5.4, 9.5)
11	11/11, 11/13	Charney–Stern–Pedlosky criterion, internal gravity waves: dispersion relation, parcel interpretation, reflection, topographic generated waves. (Vallis 9.4, 7.3). <b>Problem Set 4</b>
12	11/18, 11/20	Vorticity equation, "frozen-in" property of vorticity, Ertel's PV, potential temperature, Kelvin's circulation theorem, shallow water PV from the "frozen-in" property. (Vallis 4.1, 4.2, 4.3, 4.5, 4.6)
13	11/25	3D incompressible turbulence: triad interactions, Kolmogorov theory, inertial range, viscous scale. (Vallis 11.1, 11.2)
14	12/2, 12/4	2D incompressible turbulence: conservation of enstrophy, inverse energy cascade, 2D turbulence with beta effect, mechanism of midlatitude atmospheric jet production: vorticity budget, Rossby wave momentum flux. (Vallis 11.3, 15.1)
15	12/5-12/12	Take-home final exam