





(Remark: in the n-D case,

row picture: intersections of

hyperplane

Column picture: Boombination of columns to produce 6).

The Matrix Form of Equations

Let
$$A = \begin{bmatrix} 1 & 2 & 3 & 7^{x_1} \\ 2 & 5 & 2 & 7^{x_2} \\ 6 & -3 & 1 & 7^{x_3} \end{bmatrix} b = \begin{bmatrix} 6 \\ 4 \\ 2 \end{bmatrix}$$

Matrix equation A x = b

Multiplication by rows
$$A \times = \begin{bmatrix} x_1 & x_2 \\ x_2 & x_3 \end{bmatrix}$$

A Multiplication by columns

$$Ax = xu + yv + zv$$

Take 
$$x = \begin{bmatrix} 0 \\ 2 \end{bmatrix}$$
, then

$$A \times = 2 w = 2 \begin{bmatrix} 3 \\ 2 \end{bmatrix} = \begin{bmatrix} 6 \\ 4 \\ 2 \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 0 & 0 & 7 \\ 1 & 0 & 0 & 7 \end{bmatrix}, \quad x = \begin{bmatrix} 4 & 7 \\ 5 & 6 \end{bmatrix}$$

$$A \times = \mathbf{z} + \mathbf{z} \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 4 \\ 4 \end{bmatrix}$$

Let 
$$T = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$$
 identity matrix

$$I = x = 4 \begin{bmatrix} 0 \\ 0 \end{bmatrix} + 5 \begin{bmatrix} 0 \\ 0 \end{bmatrix} + 6 \begin{bmatrix} 0 \\ 0 \end{bmatrix} = x$$

Note: for each vector  $x = \begin{bmatrix} x \\ y \end{bmatrix}$ , we have

Matrix Notation

$$A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} = \begin{bmatrix} A(1,1) & A(1,2) \\ A(2,1) & A(2,2) \end{bmatrix}$$

Review: 1. Row picture for Ax=6

2-D case: two lines meet at a point
3-D case: 23 planes meet at a point

2. Column prictive for  $A \times = b$ combination of columns of  $\times$  gives b.

3. Multiplication by columns:

Ax: a combination of columns of A.