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# A First Physical-World Trajectory Prediction Attack via LiDAR-induced Deceptions in Autonomous Driving

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## Abstract

Trajectory prediction forecasts nearby agents' moves based on their historical trajectories. Accurate trajectory prediction (or prediction in short) is crucial for autonomous vehicles (AVs). Existing attacks compromise the prediction model of a victim AV by *directly* manipulating the historical trajectory of an attacker AV, which has limited real-world applicability. This paper, for the first time, explores an *indirect* attack approach that induces prediction errors via attacks against the perception module of a victim AV. Although it has been shown that physically realizable attacks against LiDAR-based perception are possible by placing a few objects at strategic locations, it is still an open challenge to find an object location from the vast search space in order to launch effective attacks against prediction under varying victim AV velocities.

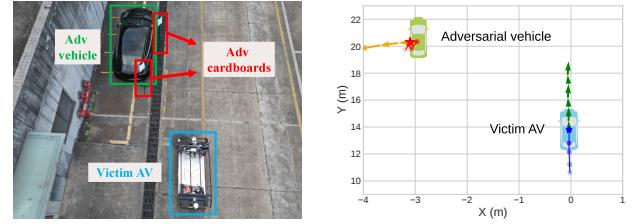
Through analysis, we observe that a prediction model is prone to an attack focusing on a single point in the scene. Consequently, we propose a novel two-stage attack framework to realize the single-point attack. The first stage of prediction-side attack efficiently identifies, guided by the distribution of detection results under object-based attacks against perception, the state perturbations for the prediction model that are effective and velocity-insensitive. In the second stage of location matching, we match the feasible object locations with the found state perturbations. Our evaluation using a public autonomous driving dataset shows that our attack causes a collision rate of up to 63% and various hazardous responses of the victim AV. The effectiveness of our attack is also demonstrated on a real testbed car<sup>1</sup>. To the best of our knowledge, this study is the first security analysis spanning from LiDAR-based perception to prediction in autonomous driving, leading to a realistic attack on prediction. To counteract the proposed attack, potential defenses are discussed.

## 1 Introduction

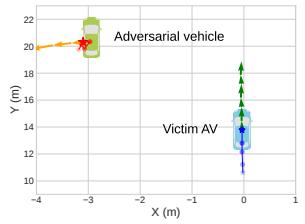
Autonomous vehicles (AVs) are transforming transportation systems worldwide. Autonomous driving (AD) systems, e.g.,

<sup>\*</sup>Equal contribution

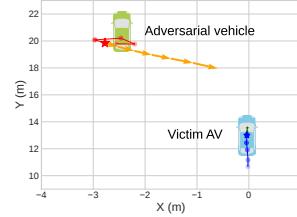
<sup>1</sup>A demo video of our attack on a real testbed car is available at [https://1drv.ms/v/s!Aoc\\_mWfaEyaGbrdCPNS9oKMjm9Q?e=f1GA6u](https://1drv.ms/v/s!Aoc_mWfaEyaGbrdCPNS9oKMjm9Q?e=f1GA6u).



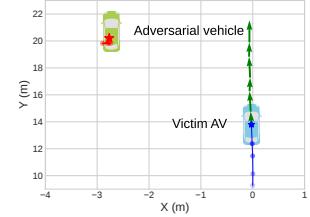
(a) A scene with adversarial cardboards placed around a parked car.



(b) Random object locations cause a prediction error posing no threat.



(c) Brute-force search finds object threatening victim vehicle.



(d) No longer threatening for victim vehicle approaching at higher speed.

Figure 1: A motivation experiment.

Autoware.AI [1], typically consist of perception, prediction, and planning modules. In this AD system pipeline, the perception module utilizes sensors, such as LiDAR, to detect and track on-road objects; the prediction module forecasts the future trajectories of nearby agents; the planning module determines the AV's future driving behavior. The predicted trajectories are particularly vital for the subsequent planning module as they significantly influence an AV's driving behavior. The existing studies [9, 47, 61] directly compromise the prediction module of a victim AV by manipulating the historical trajectory of an attacker agent nearby, which is usually a vehicle. In these attacks, the attacker's vehicle must drive according to a specific *adversarial driving trajectory* to mislead the victim AV's prediction module into generating wrong future trajectory prediction for the attacker's vehicle. However, it is hard to precisely drive the attacker's vehicle along a pre-computed trajectory due to kinematic constraints. Moreover, such adversarial trajectories are designed based on

a restrictive assumption that the victim AV would drive at a certain velocity.

To address these limitations, in this paper, we explore the possibility of indirectly compromising the prediction module via perturbing the perception module of the victim AV such that the perception errors can induce the prediction module to predict a wrong trajectory of a nearby agent. The existing physically-realizable attacks against the LiDAR perception [10, 38, 44, 45] provide a basis for such indirect attack on the prediction module. Among them, object-based attacks, which use specific shapes or common objects to introduce additional adversarial LiDAR points captured by the victim AV, have lower logistics overhead in attack implementation. However, the impact of the perturbed bounding box attributes (including coordinates, dimensions, and heading) as a result of the object-based attack on the subsequent prediction in the AD pipeline has never been systematically studied.

To study the feasibility of compromising the prediction model indirectly via object-based attacks to induce dangerous driving decisions, we conduct a motivation experiment on our custom-built real testbed AV. We employ an object-based attack method from [66], due primarily to its practicality, to plan the locations for placing two *adversarial cardboards* around a car parked roadside, called *adversarial vehicle*, as shown in Fig. 1(a). Then, the victim AV running the LiDAR-based AD pipeline drives by. Fig. 1(b) shows that random object placement may result in a wrongly predicted trajectory of the adversarial vehicle, which stays stationary in reality. However, as the predicted trajectory points to the left, it imposes no threat on the victim AV. Then, we employ brute-force search to find the locations of the two adversarial cardboards that lead to a collision between the victim AV’s original trajectory and the adversarial vehicle’s trajectory predicted by the victim AV. The search is based on the victim AV’s original trajectory. As shown in Fig. 1(c), the attack-induced illusive collision leads to a sudden brake decided by the victim AV’s planning module. This result shows the existence of object-based attacks that generate threatening effects penetrating the AV pipeline. However, when the victim AV runs at a varied velocity causing a deviation from the spatio-temporal trajectory assumed by the attacker’s brute-force search, the attack becomes no threatening as shown in Fig. 1(d). This paper aims to design an efficient attack approach to identify locations for placing adversarial objects that lead to hazardous responses of the victim AV regardless of its driving velocity.

Our vulnerability analysis via experiments shows that the AV’s trajectory prediction is prone to substantial perception errors when the moving victim AV is at a point in the scene. Based on this observation, we choose to reduce the attack design space to focus on a fixed *attack point* and perturb the victim AV’s perception to induce prediction errors, when it arrives at the attack point. This strategy greatly reduces the search space yet largely preserves the potential of the attack in leading to the victim AV’s hazardous responses. However,

as the historical LiDAR frames captured before the victim AV arrives at the attack point form a part of the prediction model’s input, the victim AV’s velocity still affects the effectiveness of the single-point attack. In addition, the exhaustive search for the locations of multiple adversarial objects in the 3D proximity space of the adversarial vehicle, while considering all possible victim AV’s velocity values for robustness to velocity variations, still incur undesirable overhead.

To address the above two issues related to the single-point attack strategy, we design a novel two-stage attack framework. In the stage of *prediction-side attack*, we maximize attack effectiveness by searching for input state perturbations for the prediction model that maximize the interference between the predicted trajectory of the adversarial vehicle and the victim AV’s planned trajectory. To maintain attack effectiveness across various velocity conditions, we employ the Expectation over Transformation (EoT) technique. Our experiment shows that, with object-based attacks, the perturbed detection results (i.e., bounding boxes) of the adversarial vehicle exhibit distributional patterns. Thus, we utilize the distribution to guide the optimization of the state perturbations for the prediction model, which improves the efficiency of attack design. We use the Projected Gradient Descent (PGD) method to iteratively search for the state perturbations and select the perturbations that lead to collisions. However, the optimized state perturbations may not translate to feasible perturbed detection results caused by the placement of adversarial objects. To achieve attack feasibility, in the stage of *location matching*, we employ the Hungarian algorithm to match the adversarial locations with the optimized state perturbations and further refine the candidate adversarial locations by probing in their close vicinity for reducing the matching cost.

We conduct experiments on both the nuScenes [6] autonomous driving dataset and our real testbed AV. In the dataset-based experiments, our attack achieves a collision rate of up to 63%, effectively inducing various hazardous responses of the victim, including sudden brakes, accelerations, and unexpected lane changes, in the presence of object displacement errors and object size variations. In the physical-world experiments with our custom-built testbed AV, our attack is effective in various velocity conditions and achieves the highest attack success rate compared with the random location and the brute-force sampling attacks. The experiments also show that our attack is robust against object displacement errors and variations in the victim AV’s direction.

Our main contributions can be summarized as follows:

- We design and launch the first physical-world attack on the AD system’s trajectory prediction by strategically placing objects to indirectly induce prediction errors, leading to hazardous responses of the victim AV.
- We find that the prediction model is susceptible to the single-point attack. Built upon this, we design a novel two-stage attack framework that efficiently identifies adversarial locations for object placement, leading to

- effective, velocity-insensitive, and feasible attacks.
- Our attack is evaluated on both a public autonomous driving dataset and a custom-built real-world testbed AV, achieving consistently higher threats compared with the baselines and attack robustness. Additionally, we propose potential defenses to mitigate the threat.

## 2 Background and Related Work

### 2.1 Autonomous Driving System

A typical AD system consists of perception, trajectory prediction, and motion planning modules, as detailed below.

**LiDAR-based Perception**, known for its precision in acquiring environmental data, is widely adopted in the default pipeline of open-source AD systems [5] and in commercial solutions [50, 51]. This process starts with 3D object detection, which analyzes a LiDAR point cloud to identify objects around the ego vehicle. Modern AD perception utilizes deep learning models, denoted by  $M_{det}(\cdot)$ , to process LiDAR point cloud  $D$  and produce a set of 3D bounding boxes  $\mathbf{B} = M_{det}(D)$ . A bounding box  $\mathbf{b} \in \mathbf{B}$ , characterized by coordinates, dimensions, heading, and a confidence score, represents a detected object. Existing 3D object detection methods can be divided into Bird’s Eye View (BEV)-based [56], voxel-based [55, 57], and point-based [43]. They respectively map point clouds into 2D representation, discretize 3D space into voxels, and operate on raw point cloud directly. Detected objects are tracked over time by an object tracking model  $M_{track}$ .

**Trajectory Prediction** forecasts the future trajectories of road agents (vehicles and pedestrians) based on their current and historical states perceived over  $H$  time steps denoted by  $\mathbf{X} = (\mathbf{X}^{-H+1}, \dots, \mathbf{X}^0)$ , where  $\mathbf{X}^t = (\mathbf{x}_1^t, \dots, \mathbf{x}_{N_a}^t)$  represents the states of  $N_a$  agents at time step  $t$  and each  $\mathbf{x}_i^t$  includes an agent’s coordinates, velocity, acceleration, and heading. The trajectory prediction for a horizon of  $T$  time steps by a predictor  $M_{pred}(\cdot)$  is  $\mathbf{Y} = (\mathbf{Y}^1, \dots, \mathbf{Y}^T) = M_{pred}(\mathbf{X})$ , where  $\mathbf{Y}^t = (\mathbf{y}_1^t, \dots, \mathbf{y}_{N_a}^t)$  is the predicted coordinates of the  $N_a$  agents at time step  $t$ . Existing trajectory predictors employ recurrent neural networks [28, 31], graph neural networks [29, 59], and transformers [30, 63]. Recent generative predictors such as Trajectron++ [39] and AgentFormer [58], which perform conditional sampling and selection, have shown superior performance and are therefore employed in this work.

**Motion Planning** takes into account road agents’ current states  $\mathbf{X}^0$  and trajectory prediction results  $\mathbf{Y}$  to plan a safe, efficient, and feasible future trajectory  $\mathbf{P} = M_{plan}(\mathbf{X}^0, \mathbf{Y})$  for the ego vehicle. Existing solutions can be divided into sampling-based [26], control-based [15], graph search-based [17], and learning-based methods [41, 60].

### 2.2 Adversarial Attacks

Deep learning models are shown to be vulnerable to adversarial examples [12, 19, 27, 32, 37, 42, 46, 48, 53, 62], which are

perturbed input samples that mislead the model to generate erroneous outputs. Specifically, given a model  $M(\cdot)$ , for a benign input  $x$  with ground truth label  $y$ , the attack searches for a minimal perturbation  $\delta$  such that  $M(x + \delta) \neq y$  (non-targeted attack) or  $M(x + \delta) = y'$  (targeted attack), where  $y'$  is the target label. Adversarial examples may pose great threat on the safety-critical AD systems that employ deep learning models for perception and prediction. In what follows, we review the existing adversarial attacks on LiDAR-based perception, trajectory prediction, and motion planning, respectively.

The attacks on LiDAR-based perception are studied in both simulations [20, 21] and physical environments. Physical-space attacks fall into two groups: *laser-based* [7, 10, 25, 38, 40, 44, 45] and *object-based* [8, 49, 64, 66]. The former, also known as spoofing, injects fake points by intercepting LiDAR’s emitted laser pulses using a receiver and then transmitting counterfeit pulses back to the LiDAR sensor with a manipulated delay. However, such attacks require precise timing and specialized equipment, making them costly and conspicuous. Object-based attacks use physical objects to mislead LiDAR detection models. For example, in [66], a vehicle can be hidden from LiDAR detection by placing common objects at computed adversarial locations near the vehicle. Both laser-based and object-based attacks usually hide or create objects by manipulating bounding box confidence scores. Yet, their effects on bounding box parameters (coordinates, dimensions, and heading) and the impact of induced errors in estimating these parameters on subsequent AD modules remain largely unexplored. This work considers object-based attacks that are more realistic for real-world deployments.

In the tracking module, tracker hijacking attacks [13, 22–24, 34, 54] perturb camera image inputs to manipulate bounding box parameters. A primary goal of these attacks is object move-in, which manipulates the tracker of a roadside object towards the road center, potentially inducing falsified trajectories similar to ours due to pipeline effects. However, these studies focus exclusively on the tracking module, while our attack optimizes such effects in the downstream trajectory prediction module. Unlike these studies that focus on camera-only systems, our attack applies to LiDAR-based perception, introducing unique challenges and attack vectors that necessitate new methodologies.

The attacks on trajectory prediction perturb the input states of the adversarial vehicle and mislead the victim AV’s prediction model. However, existing methods either neglect the kinematic laws governing the adversarial vehicle [47, 61] or disregard the driving uncertainties of the victim AV, including speed variations [9, 11], which could alter the adversarial vehicle’s input states during the attack. Differently, this paper plans the object-based attacks that generate pipeline effect on LiDAR-based perception and then trajectory prediction.

There are a few studies focusing on physical attacks against motion planning. The work [52] uses common road objects to trigger a Semantic Denial-of-Service in the motion planning

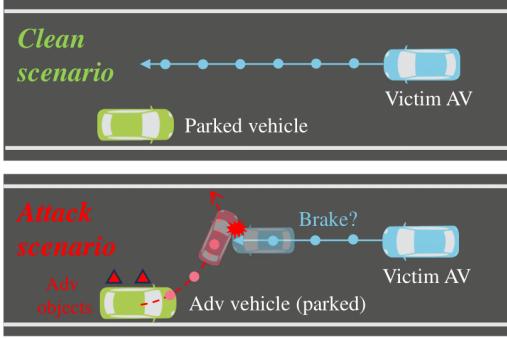


Figure 2: Our attack scenario. Solid blue arrows are victim AV’s planned trajectories; dash red arrow is adversarial vehicle’s future trajectory predicted by the victim AV.

module, causing emergency stops or critical driving decision failures. In comparison, this paper targets the trajectory prediction module in AD systems. Regarding methods, the work in [52] exploits flaws in programming code logic, while our attack focuses on vulnerabilities in learning-based perception and prediction models, highlighting a distinct approach in exploiting AD systems’ weaknesses.

### 3 Threat Model

**Attack Goal.** We consider an attack scenario depicted in Fig. 2, where a static adversarial vehicle is parked on the roadside, while a victim AV is driving and approaching it on the adjacent lane. Such a scenario is common in urban driving environments, such as street parking, industrial areas, and parking lots. We assume that the victim AV runs the AD pipeline of LiDAR-based perception, trajectory prediction, and motion planning. The attack goal is to manipulate the victim AV’s perception, such that the prediction forecasts an erroneous moving trajectory for the static adversarial vehicle and causes the victim AV’s motion planning to decide a hazardous driving strategy. This can be motivated by intentional harm towards an individual, unhealthy competition among solution vendors aiming to undermine the safety reputation of rivals’ self-driving products, or the intent to disrupt traffic mobility by causing traffic jams [36]. The manipulation of the victim AV’s perception is achieved by placing some adversarial common objects, e.g., cardboards, around the adversarial vehicle. The key for the perception manipulation is to identify the *adversarial locations* for placing the adversarial objects, such that the victim AV’s LiDAR-based perception generates inaccurate bounding boxes over time for the adversarial vehicle. The attack aims at misleading the victim AV to produce a falsified trajectory of the adversarial vehicle that intersects the victim AV’s planned trajectory. As a result, the victim AV re-plans the motion to avoid the illusive collision with safety-undermining driving decisions, including emergent braking, sudden acceleration and/or lane change.

**Attacker Capabilities.** We assume that the attacker is capable of placing objects around an adversarial vehicle, which can be the attacker’s own car or a random car parked on the roadside. We consider a realistic but challenging setting in which the attacker has no access to the real-time data (e.g., LiDAR point cloud) collected by the victim AV. We consider the white-box attacker that has comprehensive knowledge of the victim AV’s AD pipeline. This enables the attacker to query and analyze  $M_{det}(\cdot)$ ,  $M_{track}$ , and  $M_{pred}(\cdot)$  for crafting attacks. To obtain these three models, the attacker can use social engineering on the system designers of the car manufacturers or reverse-engineer a vehicle identical to the victim AV. For the vehicles employing open-source AD systems [1, 2], the overhead of obtaining the three models  $M_{det}(\cdot)$ ,  $M_{track}$ , and  $M_{pred}(\cdot)$  can be lower. Before launching the attack, the attacker gathers data by driving a LiDAR-equipped vehicle to mimic the victim AV’s behavior. The attacker uses the data to determine the locations for placing the objects.

## 4 Challenges and Problem Definition

### 4.1 Attack Challenges

Challenges to identify effective adversarial locations include:

**Challenge C1: Maximizing Attack Effectiveness.** Inducing errors in predicting the adversarial vehicle’s trajectory, quantified by metrics such as average displacement error (ADE) and final displacement error (FDE), as in the literature, does not necessarily imply a threat to the victim AV. An erroneously predicted moving trajectory for an adversarial vehicle that is stationary in reality, if not intersecting the victim’s planned trajectory, poses no actual danger. To maximize attack effectiveness, a meaningful objective is to minimize the distance between the adversarial vehicle’s predicted trajectory and the victim AV’s planned trajectory.

**Challenge C2: Velocity-Induced Uncertainty in Attack Effectiveness.** The victim AV may drive by the adversarial vehicle at varying velocities. When the victim AV’s velocity is different from that used for attack construction, the victim AV’s perception results and the consequent predicted trajectory of the adversarial vehicle may differ from those expected by the attacker. Thus, should the victim AV deviate from its expected trajectory, the effectiveness of the pre-determined adversarial locations may be reduced.

**Challenge C3: Vast Search Space for Adversarial Locations.** Given the non-differentiable processes within the AD system’s independent modules, employing gradient-based optimization to achieve the attack goal presents significant difficulties. A straightforward approach would be exhaustively sampling a multitude of locations in the vicinity of the adversarial vehicle in order to identify the most effective set of adversarial locations. However, such a brute-force sampling approach faces efficiency challenges, particularly in time-sensitive scenarios. For instance, if an attacker can only

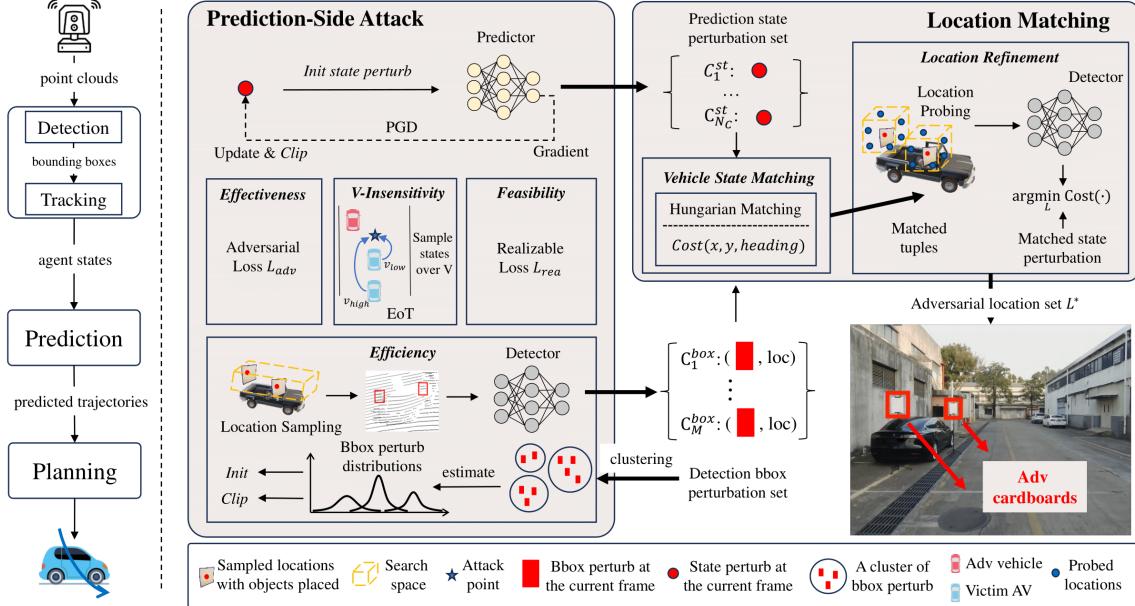


Figure 3: Our proposed inverse attack framework for identifying the adversarial locations to place objects (cardboards in red boxes). The framework operates within the AD system pipeline, which is outlined on the left for reference.

determine the victim AV’s route after it departs, it has limited time to plan and deploy the attack. First, even if we restrict the search area to only the top of the adversarial vehicle and its immediate surroundings, the search space is still extensive and grows exponentially with the number of adversarial objects. Second, if the search further accounts for the victim AV’s velocity as an additional dimension to address **C2**, the search space is even larger.

## 4.2 Problem Definition

We aim to identify a set of adversarial locations  $L = \{l_n | n = 1, \dots, N_L\}$ , where  $l_n \in \mathbb{R}^3$  is the 3D coordinates of the  $n$ -th adversarial location and  $N_L$  is the number of locations we consider, to achieve the attack goal. Inspired by the finding **F1** in Section 5.2, we propose to establish a fixed *attack point* and manipulate the prediction of the adversarial vehicle when the victim AV reaches this point. In this way, the perception of the adversarial vehicle at the attack point is independent of the victim AV’s velocity. We let  $t = 0$  denote the time step when the victim AV arrives at the attack point. The point cloud frame captured by the victim AV’s LiDAR at  $t = 0$  is referred to as the *current frame*. We formulate the problem of identifying  $L$  as:

$$\begin{aligned} \arg \max_L & \mathbb{E}_{v \in V} [\text{Interference}(\tilde{\mathbf{Y}}^v, \mathbf{P}^v)], \\ \text{s.t. } & \tilde{\mathbf{Y}}^v = M_{pred}(\tilde{\mathbf{X}}^v), \\ & \tilde{\mathbf{X}}^v = M_{track}(\{M_{det}(D_t^v(L)) | t = -H + 1, \dots, 0\}), \end{aligned} \quad (1)$$

where  $v$  is the victim AV’s velocity sampled from a range  $V$ ;  $D_t^v(L)$  is the LiDAR point cloud captured by the victim

AV with velocity  $v$  at time step  $t$  when the adversarial objects are placed at  $L$ ; the  $\{M_{det}(D_t^v(L)) | t = -H + 1, \dots, 0\}$  is the sequence of the victim AV’s detection results regarding the adversarial vehicle over  $H$  time steps;  $\tilde{\mathbf{X}}^v$  represents the adversarial vehicle’s states observed by the victim AV, determined by the tracking model  $M_{track}(\cdot)$  based on the detection results;  $\tilde{\mathbf{Y}}^v$  is the trajectory of the adversarial vehicle predicted by the victim AV;  $\mathbf{P}^v$  is the original planned trajectory of the victim AV;  $\text{Interference}(\tilde{\mathbf{Y}}^v, \mathbf{P}^v)$  represents the interference between the trajectories  $\tilde{\mathbf{Y}}^v$  and  $\mathbf{P}^v$ . One meaningful definition of the interference is the reciprocal of the average distance between the adversarial vehicle moving on  $\tilde{\mathbf{Y}}^v$  and the victim AV moving on  $\mathbf{P}^v$ . In the above formulation, the quantities with the superscript  $v$  are affected by the victim AV’s velocity  $v$ .

## 5 Attack Design

To achieve the attack goal defined in Eq. 1 while addressing the attack challenges summarized in Section 4.1, we design a novel two-stage attack framework as shown in Fig. 3. This framework aims to identify adversarial locations for placing objects that mislead the victim AV into forecasting a falsified future trajectory of the adversarial vehicle, inducing dangerous driving behaviors conducted by the victim AV.

### 5.1 Approach Overview

Our attack framework is built upon two key insights. First, the widespread use of learning-based models in AD systems, which are vulnerable to adversarial inputs, presents a potential attack surface to impact downstream modules such as trajectory prediction through pipeline effects. Second, in contrast to

Table 1: Average distance between predicted trajectory of adversarial vehicle and victim AV’s planned trajectory. A smaller distance indicates a higher collision risk.

Model	Average Distance (m)					
	Clean		Attacked Frame Index			
	-4	-3	-2	-1	0	
Trajectron++	6.3	6.1	6.1	5.9	3.0	2.7
AgentFormer	6.3	5.9	5.8	5.8	5.0	3.9

the brute-force forward sampling attack that is inefficient and often gets stuck in local optima, our inverse attack strategy effectively exploits vulnerabilities in the prediction module for enhanced effectiveness and efficiency.

At a high level, our framework compromises modules from prediction to perception. It initiates by conducting adversarial attacks on the prediction module to generate adversarial states, i.e., the adversarial inputs of the trajectory prediction module that can mislead the module into forecasting a falsified future trajectory of the adversarial vehicle. Then, we conduct object-based attacks on the perception module, which generates adversarial locations. Placing objects at these locations can mislead the perception module to generate the adversarial bounding box perturbations, resulting in the desired adversarial states in the previous step.

The first stage, called *prediction-side attack* as detailed in Section 5.3, is designed to find state perturbations that mislead the victim AV’s prediction model. Firstly, we address the attack effectiveness challenge C1 by minimizing the distance between the predicted trajectory of the adversarial vehicle and the planned trajectory of the victim AV. Secondly, we propose a fix-point attack based on a key finding F1 presented in Section 5.2 that the trajectory prediction models are especially susceptible to the adversarial attack at the current frame. Together with the Expectation over Transformation (EoT) technique applied to various velocities of the victim AV, we address the velocity-insensitivity challenge C2. Thirdly, we address the vast search space challenge C3 by utilizing a feasible set of detection results to guide the searching for effective state perturbations against the prediction model, which is based on a key finding F2 presented in Section 5.2, i.e., the detection results under object-based attacks are limited and exhibit distributional patterns. Lastly, we employ the Projected Gradient Descent (PGD) method to iteratively update the state perturbations and select the perturbations that lead to collisions.

The second stage, called *location matching* as detailed in Section 5.4, finds the adversarial locations for placing common objects that can implement the state perturbations found by the prediction-side attack.

## 5.2 Findings

We conduct experiments to gain key insights for the design of our attack, as detailed below.

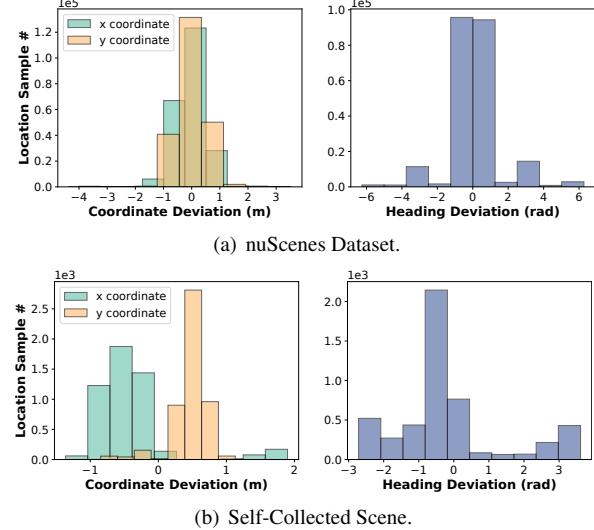


Figure 4: Histogram of coordinates and heading perturbations in nuScenes dataset scenes and a self-collected real-world scene under object-based attacks.

**Finding F1: Trajectory prediction models are vulnerable to single-point attack at the current frame.** To address challenge C2, we conduct a vulnerability analysis of two representative trajectory prediction models: Trajectron++ [39] and AgentFormer [58]. Both models take five historical states as input to predict the future trajectory. We apply the PGD method to perturb each of the five historical states. We add random noises to the remaining states to simulate noisy conditions in practice. The PGD attack minimizes the average distance between the predicted trajectory of the adversarial vehicle and the victim AV’s planned trajectory. Then, we measure this average distance under both clean and single-point attack scenarios. The results presented in Table 1 show that perturbing the current state (i.e.,  $t = 0$ ) achieves the smallest average distance, indicating the highest threat for collision. The reasons are two-fold. First, models such as Trajectron++ sequentially process input states using LSTM, which relies heavily on the most recent input state. Second, models including AgentFormer transform input states into a local coordinate system centered on the current frame. Thus, a small perturbation on the current state has the largest impact on the prediction result. The finding reveals that for a trajectory prediction model  $M_{pred}(\cdot)$  and a sequence of  $H$  input states  $\mathbf{X} = (\mathbf{X}^{-H+1}, \dots, \mathbf{X}^0)$ , the model is particularly susceptible to adversarial attacks targeting the current state  $\mathbf{X}^0$ , despite variations in historical states due to say different velocities. Therefore, by focusing the design of the attack on a fixed *attack point* that the victim AV arrives at, we can simplify the problem and preserve the potential of the attack in inducing victim AV’s hazardous responses.

**Finding F2: 3D object detection results under attack exhibit distributional patterns that help improve attack efficiency.** We follow the approach in [66] to compromise

LiDAR-based 3D object detection systems. The principle behind this attack is that strategic placement of adversarial objects distorts the vehicle’s perceived shape, perturbing the object detector’s geometric feature recognition. To analyze the resulting bounding box perturbations, we conduct experiments to launch attacks on 100 driving scenes from the nuScenes dataset [6] and a self-collected real-world driving scene. For each driving scene, we uniformly sample 500 candidate locations around the adversarial vehicle to place objects and record the resulted *bounding box perturbation* in five consecutive frames, which is defined as the deviation of the bounding box for the adversarial vehicle with and without attack. To be more specific, we measure the deviations of the  $x$  and  $y$  coordinates and the heading  $h$  of the bounding box, which serve as the inputs to the downstream trajectory prediction. Based on the experiment results in Fig. 4, we can observe that the bounding box perturbations caused by placing adversarial objects exhibit distributional patterns. The deviations of  $x$  and  $y$  coordinates are primarily distributed within the interval [-1, 1]. The distribution of heading deviations exhibits distinct clusters. Note that heading deviations of around  $\pm 1$  rad mean that the adversarial vehicle is perceived to have a heading close to its actual heading, while deviations of  $\pm 3$  rad indicate a heading in the opposite direction. This finding is key to address the vast search space challenge C3. This is because, instead of exhaustive location sampling, we only need a limited number of location probes to recognize the bounding box perturbation distribution, thus improving efficiency in finding adversarial locations.

### 5.3 Prediction-Side Attack

To mislead victim AV’s trajectory prediction model, we need to identify the *state perturbation* at the current time step, which is added to the input states of the prediction model. It is denoted by  $\delta^{\text{st}} = \{\delta_x^{\text{st}}, \delta_y^{\text{st}}, \delta_h^{\text{st}}\}$ , where  $x$ ,  $y$ , and  $h$  indicate  $x$  coordinate,  $y$  coordinate, and heading, respectively. Now, we discuss the considerations when designing  $\delta^{\text{st}}$  to address the three challenges presented in Section 4.1.

**Attack Effectiveness.** To find the state perturbation at the current time step that can address challenge C1 and achieve the attack goal defined in Eq. 1, we propose *Adversarial Loss*  $\mathcal{L}_{\text{adv}} = \|\tilde{Y}^v - P^v\|_2$ , which maximizes attack effectiveness by minimizing the  $\ell_2$  distance between the predicted trajectory of the adversarial vehicle  $\tilde{Y}^v$  and the original planned trajectory  $P^v$  of the victim AV.

**Attack Efficiency.** Given the vast search space as mentioned in challenge C3 in Section 4.1, finding a physically feasible state perturbation achieved by placing objects around the adversarial vehicle is costly. To address this, we rely on the finding F2 and leverage a set of physically feasible detection results under object-based attack to efficiently guide the searching for the effective state perturbation. Specifically, we evenly sample a small number of locations around the adversarial vehicle to derive a *bounding box perturbation* set

---

#### Algorithm 1 Prediction-side Attack

```

Require: Prediction model  $M_{\text{pred}}(\cdot)$ , victim AV’s original
planned trajectory  $P$ , bbox perturbation set  $C^{\text{box}}$ , bbox
perturbation clusters  $R$ , victim AV’s velocity range  $V$ 
1: for  $r$  in  $R$  do
2:   for  $e \leftarrow 1$  to  $E$  do
3:     Init  $\delta_i^{\text{st}} \sim \mathcal{N}(\mu_i^r, \sigma_i^r), i \in \{x, y, h\}$ ;
4:     for  $\text{iter} \leftarrow 1$  to  $I$  do
5:       for  $v \sim V$  do
6:         Simulate historical states to estimate  $\tilde{X}^v$ ;
7:         Trajectory prediction  $\tilde{Y}^v = M_{\text{pred}}(\tilde{X}^v)$ ;
8:         Compute loss  $\mathcal{L} = \mathcal{L}_{\text{adv}} + \mathcal{L}_{\text{rea}}$ ;
9:       end for
10:      Update  $\delta_i^{\text{st}}$  with PGD using avg.  $\mathcal{L}$  over  $V$ ;
11:      Clip  $\delta_i^{\text{st}}$  into  $[\mu_i^r - 2\sigma_i^r, \mu_i^r + 2\sigma_i^r], i \in \{x, y, h\}$ ;
12:    end for
13:    Inference  $\tilde{Y} = M_{\text{pred}}(X + \delta^{\text{st}})$ ;
14:    if collision between  $\tilde{Y}$  and  $P$  then
15:       $C^{\text{st}} \leftarrow C^{\text{st}} \cup \{\delta^{\text{st}}\}$ ;
16:    end if
17:  end for
18: end for
19: return State perturbation set  $C^{\text{st}}$ 

```

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$C^{\text{box}}$ . Each element in this set consists of a bounding box perturbation  $\delta^{\text{box},m} = \{\delta_x^{\text{box}}, \delta_y^{\text{box}}, \delta_h^{\text{box}}\}$  and its corresponding location set  $L_m$ . Based on the distribution of the bounding box heading perturbation, we divide  $C^{\text{box}}$  into a set of clusters  $R$ . For each cluster  $r$  in  $R$ , the bounding box perturbation  $\delta_i^{\text{box}}$  follows the distribution  $\mathcal{N}(\mu_i^r, \sigma_i^r)$ , where  $i \in \{x, y, h\}$ . Then, for each  $r$  in  $R$ , we leverage the estimated bounding box perturbation distribution to constrain the searching for the state perturbation by the following two steps. (1) At the start of each attack epoch, we initialize the state perturbation  $\delta_i^{\text{st}}$  from the estimated distribution  $\mathcal{N}(\mu_i^r, \sigma_i^r)$ ,  $i \in \{x, y, h\}$ , and then conduct iterative updates for attack optimization. At the end of each update, we clip  $\delta_i^{\text{st}}$  within the range  $[\mu_i^r - 2\sigma_i^r, \mu_i^r + 2\sigma_i^r]$  for  $i \in \{x, y, h\}$ . (2) We define a *Realizable Loss* as  $\mathcal{L}_{\text{rea}} = \|\delta^{\text{st}} - \underset{\delta^{\text{box}} \in C^{\text{box}}}{\text{argmin}} \|\delta^{\text{st}} - \delta^{\text{box}}\|_1\|_1$ , aiming

to minimizes the  $\ell_1$  distance between  $\delta^{\text{st}}$  and its closest  $\delta^{\text{box}}$  in  $C^{\text{box}}$ . An advantage of constraining the state perturbation within multiple clusters is that the generated perturbations are diversified, which enhances the probability of finding adversarial locations capable of achieving the desired perturbation.

**Velocity-Insensitivity.** To address challenge C2, we rely on the finding F1 and aim to identify a state perturbation  $\delta^{\text{st}}$  effective for the victim AV passing the attack point at various velocities. To achieve this, we employ the Expectation over Transformation (EoT) technique [4]. Specifically, we compute the expected sum of adversarial and realizable losses over a range of possible adversarial and victim AV input states associated with various velocities. To simulate the historical

states of the victim AV, we fix the current frame at the attack point and backtrack the vehicle’s motion using a kinematic model to obtain historical frames, ensuring compliance with vehicle dynamics. For the adversarial vehicle, we randomly sample states from the bounding box perturbation distribution. In each iteration, we update the state perturbation using the average losses across sampled velocities.

**Optimization Procedure.** To summarize, we propose the optimization problem in Eq. 2.

$$\begin{aligned} \arg \min_{\delta^{\text{st}}} \quad & \mathbb{E}_{v \in V} [\mathcal{L}_{\text{adv}}(\tilde{Y}^v, P^v) + \mathcal{L}_{\text{rea}}(\tilde{X}^v, C^{\text{box}})], \\ \text{s.t.} \quad & \tilde{Y}^v = M_{\text{pred}}(\tilde{X}^v), \quad \tilde{X}^v = X^v + \delta^{\text{st}}, \\ & \delta_i^{\text{st}} \in [\mu_r^i - 2\sigma_r^i, \mu_r^i + 2\sigma_r^i], \forall i \in \{x, y, h\}. \end{aligned} \quad (2)$$

The attack procedure is summarized in Alg. 1. The goal is to identify a set of candidate state perturbations, denoted as  $C^{\text{st}} = \{\delta^{\text{st},n}\}_{n=1}^{N_c}$ , that are effective and velocity-insensitive. Given the bounding box perturbation set  $C^{\text{box}}$  and corresponding distribution clusters  $R$ , for each cluster  $r$  in  $R$ , we conduct multiple attack epochs starting from initializing  $\delta^{\text{st}}$  within its respective distribution (line 3). We compute the average loss on different victim AV’s velocities and use it to iteratively update  $\delta^{\text{st}}$  with the PGD method (lines 5-10). At the end of each iteration, we clip  $\delta^{\text{st}}$  to its distribution range (line 11). Due to the randomness in initialization and optimization, the candidate  $\delta^{\text{st}}$  may not lead to a successful attack. To select effective state perturbations for forming the set  $C^{\text{st}}$ , we utilize the criteria in [14] to evaluate collision likelihood between the adversarial vehicle’s predicted trajectory  $\tilde{Y}$  and the victim AV’s planned trajectory  $P$ . In particular, a collision is defined when the outer circumferences of both vehicles intersect. We choose only perturbations that cause collisions to form the final set  $C^{\text{st}}$  (lines 13-15).

## 5.4 Location Matching

In prediction-side attack, we efficiently identify a set of state perturbations of the adversarial vehicle that are effective and velocity-insensitive. To launch a successful attack in the real world, we must also identify an adversarial location set  $L^*$  that can achieve the desired state perturbations. To achieve this feasibility, we adopt a two-step solution, including the *Vehicle State Matching* and *Location Refinement*. The procedure is illustrated in Alg. 2.

**Vehicle State Matching.** In this step, we utilize the sampled bounding box perturbation set  $C^{\text{box}}$  in Section 5.3 to estimate the object locations that can achieve the desired state perturbations. Specifically, we employ the Hungarian algorithm to find the matched bounding box perturbation  $\hat{\delta}^{\text{box},n}$  and its corresponding adversarial location set  $\hat{L}_n$  in  $C^{\text{box}}$  with each desired state perturbation  $\delta^{\text{st},n}$  in  $C^{\text{st}}$ . The cost matrix for the Hungarian algorithm is defined as:

$$\text{cost}(m, n) = \sum_{i \in \{x, y, h\}} w_i \cdot |\delta_i^{\text{box},m} - \delta_i^{\text{st},n}|. \quad (3)$$

---

### Algorithm 2 Location Matching

---

**Require:** State perturb set  $C^{\text{st}}$ , bbox perturb set  $C^{\text{box}}$

```

1: // Vehicle State Matching
2:  $N_C \leftarrow$  size of  $C^{\text{st}}$ ,  $M \leftarrow$  size of  $C^{\text{box}}$ ;
3: Init. cost matrix of size  $N_C \times M$ ;
4: for  $n \leftarrow 1$  to  $N_C$  do
5:   for  $m \leftarrow 1$  to  $M$  do
6:     Calculate  $\text{cost}(m, n) \leftarrow \sum_{i \in \{x, y, h\}} w_i \cdot |\delta_i^{\text{box},m} - \delta_i^{\text{st},n}|$ ;
7:   end for
8: end for
9: Apply Hungarian Algorithm to  $\text{cost}$ ;
10: Generate matched tuples  $(\hat{\delta}^{\text{box},n}, \hat{L}_n, \delta^{\text{st},n})_{n=1}^{N_C}$ ;
11:
12: // Location Refinement
13:  $L^* \leftarrow$  null;
14: for each tuple  $(\hat{\delta}^{\text{box},n}, \hat{L}_n, \delta^{\text{st},n})$  do
15:   Init.  $f_{\min} \leftarrow$  current cost,  $L_{\min} \leftarrow \hat{L}_n$ ;
16:   for each location set  $L$  near  $\hat{L}_n$  do
17:     Calculate cost  $f = \sum_{i \in \{x, y, h\}} w_i \cdot |\delta_i^{\text{box},L} - \delta_i^{\text{st},n}|$ ;
18:     if  $f < f_{\min}$  then
19:        $f_{\min} \leftarrow f$ ,  $L_{\min} \leftarrow L$ ;
20:     end if
21:   end for
22:    $L^* \leftarrow L^* \cup \{L_{\min}\}$ ;
23: end for
24: return Adversarial location set  $L^*$ 

```

---

Here,  $\text{cost}(m, n)$  is the matching cost between the  $m$ -th bounding box perturbation  $\delta_i^{\text{box},m}$  and the  $n$ -th state perturbation  $\delta_i^{\text{st},n}$ , for  $i \in \{x, y, h\}$ . The  $w_i$  represents the pre-set weights corresponding to  $\{x, y, h\}$ , where elements with larger normalized perturbation in  $\delta^{\text{st}}$  are assigned greater weights. For instance, if a desired state perturbation has a larger normalized  $\delta_x^{\text{st}}$  value compared with the normalized  $\delta_y^{\text{st}}$  and  $\delta_h^{\text{st}}$ , we will assign a larger weight to  $x$ . This is inspired by our empirical observation that a larger perturbation is more related to the change of a prediction result. For each desired state perturbation, this step finds all the matched bounding box perturbation and its corresponding location set, generating matched tuples  $(\hat{\delta}^{\text{box},n}, \hat{L}_n, \delta^{\text{st},n})$ , for  $n = 1, \dots, N_c$ .

**Location Refinement.** Due to the limited samples in  $C^{\text{box}}$ , the bounding box perturbation  $\hat{\delta}^{\text{box},n}$  matched in the above Vehicle State Matching step might not precisely align with the desired state perturbations  $\delta^{\text{st},n}$ . This step aims to refine candidate adversarial locations, thereby further aligning the corresponding bounding boxes towards the desired state perturbations. Specifically, we search for refined adversarial location set in close proximity to  $\hat{L}_n$ , aiming to reduce the cost  $f = \sum_{i \in \{x, y, h\}} w_i \cdot |\delta_i^{\text{box},L} - \delta_i^{\text{st},n}|$ , where  $\delta_i^{\text{box},L}$  is a bounding box perturbation after placing objects at  $L$  near  $\hat{L}_n$ . We ran-

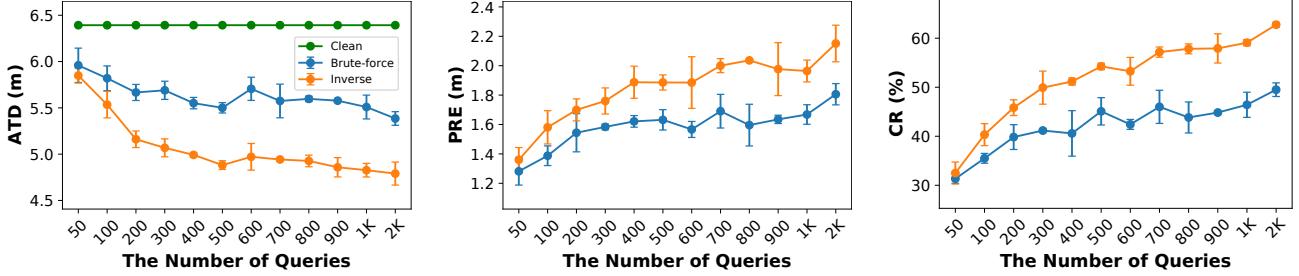


Figure 5: Average Trajectory Distance (ATD), Planning-Response Error (PRE), and Collision Rate (CR) under clean, brute-force sampling attack, and our inverse attack scenarios.

domly probe multiple locations in the vicinity of  $\hat{L}_n$ . The probing space is defined as small cubes centered around each  $\hat{l}_n$  in  $\hat{L}_n$ , as shown in Fig. 3. We set the cube size to be nearly equal to the voxel size of the LiDAR detector, allowing for moderate detection shifts. Finally, the refined location set leading to the smallest cost value is selected to form the final adversarial location set  $L^*$ .

## 6 Experiments on Dataset

In this section, we evaluate our attack using a public real-world autonomous driving dataset. This data-driven evaluation quantifies the effectiveness and robustness of our attack.

### 6.1 Experiment Setting

**Dataset.** We select 100 driving scenes from the nuScenes dataset [6], a large-scale autonomous driving dataset consisting of extensive data and labels covering both perception and prediction. The scene selection criteria are as follows. We select driving scenes aligned with our specified attack scenario, in which the ego vehicle approaches a static vehicle parked on the roadside. The parked vehicle is viewed as the adversarial vehicle; the ego vehicle serves as the victim AV. In each scene, we ensure that the victim AV starts with a minimum separation of 20 meters from the adversarial vehicle and reaches an attack point at a distance of less than 10 meters. During the attack planning, we leverage the annotated key frames captured at 2 Hz in the nuScenes dataset to identify the adversarial location set. We then evaluate these locations on frames that simulate various velocities of the victim AV, selected via a kinematic model from the unannotated nuScenes dataset sampled at 20 Hz. We simulate variations in the victim AV’s velocities at 1.5x, 1.25x, 0.75x, and 0.5x of the original recorded speed.

**AD Models.** We employ representative models for the victim AV’s AD system. We use PIXOR [56] for LiDAR-based detection, CenterPoint Tracker [57] for tracking, Trajectron++ [39] for trajectory prediction, and a Model Predictive Control (MPC)-based planner [15] for motion planning. Note that Trajectron++ is a widely used and open-source prediction model on the nuScenes dataset. We train both PIXOR and Trajectron++ using their default configurations.

**Adversarial Object.** Following [66], we simulate adversarial objects at three adversarial locations. Each object is represented by a random point cluster with a radius of 0.2 m. The number of points in each cluster is set to 4. During the location sampling step to derive  $C^{\text{box}}$ , the search space is a  $4 \times 4 \times 1 \text{ m}^3$  cube above the adversarial vehicle. In the location refinement, we reduce the search space to a sphere with a radius of 0.1 m, allowing for more precise adjustments.

**Evaluation Metrics.** We employ the following three metrics to measure the attack performance:

**Average Trajectory Distance (ATD):** This is the average distance between the predicted trajectory of the adversarial vehicle and the victim AV’s original planned trajectory. It inversely quantifies the efficacy for the interference of the adversarial vehicle’s trajectory to the victim AV. A smaller ATD suggests a larger interference.

**Planning-Response Error (PRE):** The average displacement error between the victim AV’s planned trajectories in the presence and absence of attack, respectively. A greater PRE signifies an increased tendency for the victim AV to deviate from its original action.

**Collision Rate (CR):** The proportion of the adversarial vehicle’s predicted trajectories that intersect with the victim AV’s planned trajectories in any future frame. Such intersections imply hazardous driving actions by the victim AV.

**Baseline: Brute-Force Sampling.** This straightforward baseline samples numerous locations around the adversarial vehicle and identifies the location set that results in the smallest ATD as the adversarial location set. We employ this customized baseline because there is no existing attack that can achieve the goal of this work.

### 6.2 Attack Effectiveness

Fig. 5 shows the error bars representing the mean and standard deviation of ATD, PRE, and CR values achieved by three repeated experiments. “The number of queries” refers to the maximum number of queries the attacker can make to the victim’s AD system. For instance, if the number of queries is set to 100, the attacker is limited to sample at most 100 locations around the adversarial vehicle and restricted to a total of 100 queries across all interactions with the victim AV’s detection, tracking, prediction, and planning models. From

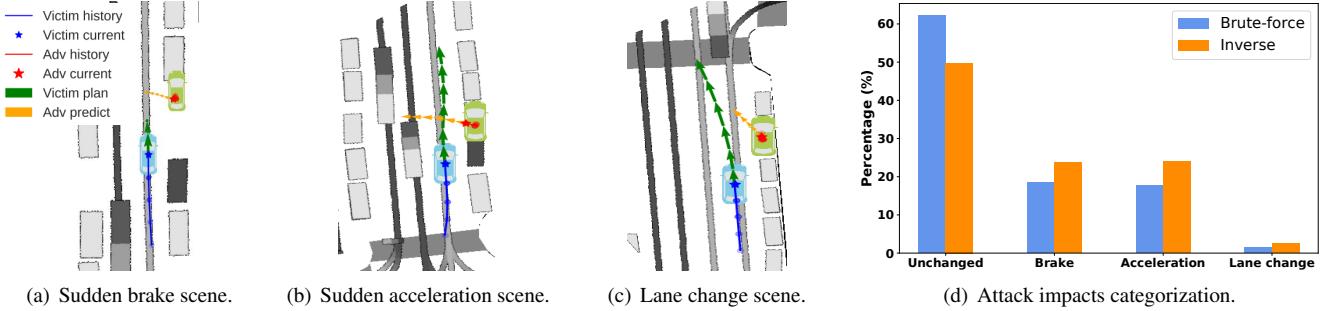


Figure 6: The attack impacts are categorized into *unchange*, *sudden brake*, *sudden acceleration*, and *lane change*, with the latter three indicate hazardous driving behaviors.

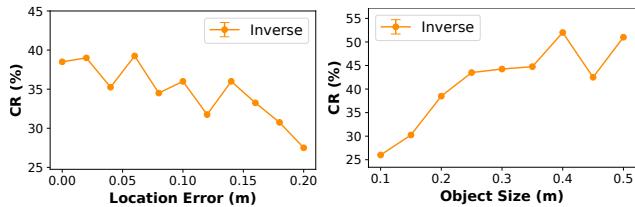


Figure 7: Attack robustness  
against object displacement.

the results, we can see that our method with 2,000 queries achieves the best attack performance, with the lowest ATD (4.7 m), the highest PRE (2.2 m), and the highest CR (63%). We can also observe that the attack performance is better for both brute-force sampling and our inverse attacks when the number of queries is larger. Notably, under the same number of queries, our method consistently outperforms the brute-force sampling. In particular, our method with 400 queries results in a higher CR than the brute-force sampling with 2,000 queries, indicating a reduction of the attack overhead by a factor of five.

To illustrate the attack impact, we categorize the victim AV’s driving behaviors under attacks into four categories, i.e., *unchange*, *sudden brake*, *sudden acceleration*, and *lane change*. Note that the victim AV’s original driving behavior is moving forward within its current lane. Thus, the latter three behaviors are considered hazardous because they deviate from the victim AV’s original driving intent. The categorization is based on the metrics of Maximum Lateral Deviation (MLaD) and Longitudinal Deviation (MLoD). MLaD measures the lateral deviation between the victim AV’s planned trajectories in the presence and absence of attack, while MLoD measures the longitudinal deviation. A trajectory with an MLoD greater or smaller than  $\pm 2$  m is categorized as a sudden acceleration or brake. An MLaD greater or smaller than  $\pm 1$  m indicates a left or right lane change. Figs. 6(a), 6(b), and 6(c) visualize three representative scenes of sudden brake, sudden acceleration, and lane change, respectively. Fig. 6(d) displays the categorization results for 400 victim AV’s planned trajectories under attacks. These trajectories are generated on 100 driving

scenes at four different velocities. The number of queries is set to 100. The results show that our method induces hazardous driving behaviors of the victim AV for more than 50% of the trajectories, while the brute-force method results in 12% fewer hazardous trajectories. This suggests that our attack not only induces errors in trajectory prediction but also forces the victim AV’s planning module to adopt unsafe maneuvers as corrective measures to avert potential collisions with the adversarial vehicle’s incorrectly predicted future trajectory.

### 6.3 Attack Robustness

**Robustness against Object Displacement.** In real-world deployment, precisely placing objects at pre-computed locations may be challenging. To evaluate the robustness of our attack against object displacement errors, we randomly shift the identified adversarial locations and evaluate our attack’s effectiveness. In this experiment, we use the adversarial location set generated by our attack method with a limit of 100 queries. Fig. 7 illustrates CR as the location shift changes from 0 to 0.2 m in intervals of 0.02 m. The corresponding ATD and PRE results are presented in Appendix B.1. The results show that ATD gradually increases, while PRE and CR decrease, as the location shift increases. This is because when the shift exceeds the grid cell/voxel size of the object detector, the additional point clusters caused by the objects might be assigned to a different grid cell/voxel than the originally intended one, leading to a detection bounding box that deviates from the desired state perturbation. However, within the grid cell/voxel size limit of 0.1 m, the location sets generated by our attack demonstrate relative robustness, making them deployable in real-world scenarios.

**Robustness against Object Size.** In this work, the attacker launches the attack by placing objects, such as cardboards or boxes, at designated locations. These objects vary in size and shape. To evaluate robustness of our attack against object size variations, we generate random point clusters with varying radius, ranging from 0.1 m to 0.5 m, and position them at same adversarial locations. Following the setting in [66], we set the number of points in each cluster proportional to the square of the object size. Fig. 8 illustrates the CR under different

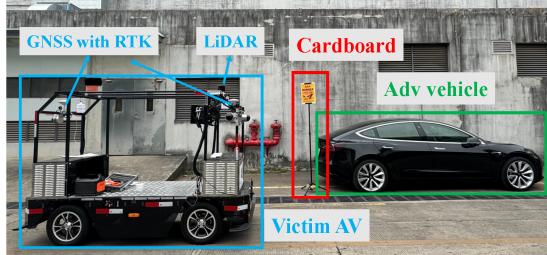


Figure 9: Experimental setup for physical world attack.

object sizes. The corresponding ATD and PRE results are presented in Appendix B.1. We can observe that a smaller object size results in weaker attack performance, indicated by a higher ATD and lower PRE and CR. This is because smaller objects induce fewer points, leading to limited perturbing effect in detection results. Object sizes in the range of 0.2m to 0.4m demonstrate stable, optimal performance across all metrics. However, the performance declines and becomes much more random beyond this range. This is likely due to larger objects occupying numerous grid cells/voxels, resulting in a significant deviation from the original detection results.

#### 6.4 Attack Transferability

We also evaluate the transferability of our attack under the black-box scenario. In this experiment, we assume the victim AV uses AgentFormer as its trajectory prediction model. We assume a black-box condition where the attacker generates locations of adversarial objects based on Trajectron++ and uses these locations to compromise the target model, i.e., AgentFormer. The results (see Appendix B.1) indicate that our attack effectively compromises a different predictor, achieving a maximum CR of 31% with 500 queries. Similar to the white-box results, our attack consistently outperforms the brute-force approach across different numbers of queries, demonstrating its superior transferability and efficiency.

## 7 Experiments in Physical World

### 7.1 Experimental Settings

**Testbed Car.** As illustrated in Fig. 9, our testbed car includes a LiDAR and a Global Navigation Satellite System receiver (GNSS) with Real-Time Kinematic (RTK). The testbed car serves as both the attacker’s data collection car during the attack planning stage and the victim AV during the evaluation. We integrate the commonly used Robosense Helios-32 LiDAR for perception, featuring 32 lines and a 10Hz frame rate. The LiDAR is mounted on the top front center of the testbed car at the height of 1.6m from the ground. We use the BYNAV X1 high Precision GNSS/INS Receiver with RTK to construct accurate coordinates for prediction and planning, achieving centimeter-level precision in vehicle localization by correcting GPS errors with differential signals. Our testbed

car uses the same models as in the dataset-based experiments for perception, prediction, and planning.

**Adversarial Vehicle and Objects.** Our proposed attack does not have any requirements on the size or color of the adversarial vehicle, which can be any car parked on the roadside. In our experiments, we use a black Tesla Model 3 as the adversarial vehicle. For the adversarial objects, we utilize two cardboards measuring 0.3m in width and 0.42m in height, equivalent to the standard A3 paper size. During the attack planning phase, to simulate realistic point clusters of cardboards akin to those captured in the real world, we use the ray-casting method [3] to sample points. In the attack deployment phase, each cardboard is mounted on a tripod for flexible placement at various locations around the adversarial vehicle. The cardboards are tilted at a 45° angle to face the side of the victim AV. While our experiments use white cardboards for better visibility, they can be substituted with ubiquitous roadside objects, such as billboards, for stealthiness.

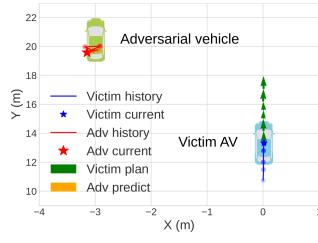
**Attack Planning and Deployment.** During the attack planning phase, we establish a start point as the origin of the global coordinate system. The testbed car, acting as the attacker’s data collection car, drives from the start point and passes by the attack point at a velocity of 5 km/h, simultaneously collecting the LiDAR point cloud and the corresponding GNSS data. The input states to the prediction model are computed in this global coordinate system, originating at the start point. Specifically, we transform the GNSS data in geodetic coordinates (latitude, longitude, altitude) into ENU (East, North, Up) coordinates based on this origin. This conversion enables us to obtain the states of victim AV and combine these coordinates with detection results to obtain the adversarial vehicle’s states. Based on the collected data in the absence of attack, we derive two adversarial locations aiming to mislead the victim AV’s trajectory prediction. Considering the practicality of placing the cardboards, we limit the location search space to the vicinity of the adversarial vehicle. Specifically, we define the side search region to be  $5.2 \times 0.4 \times 0.8 \text{ m}^3$ , matching the length of the adversarial vehicle, and the rear/front search regions to be  $0.4 \times 2.2 \times 0.8 \text{ m}^3$ , aligning with the vehicle’s width. During the attack deployment, the cardboards are positioned at the decided adversarial locations. The testbed car, now acting as the victim AV, drives from the start point established during the attack planning phase towards the attack point at various velocities to collect LiDAR point cloud and GNSS data. The collected data under attack are then fed into the victim AV’s AD system for evaluation.

### 7.2 Attack Effectiveness

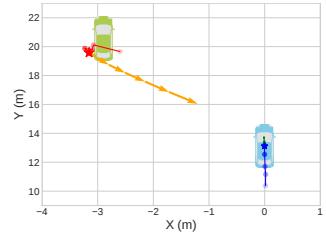
In this section, we evaluate our attack’s effectiveness in two real-world scenarios, where the victim AV drives on the road with an adversarial vehicle parked either on its left or right side, referred to as the “left-side scenario” and the “right-side scenario”, respectively. We compare our attack with the random location attack and the brute-force sampling attack. An



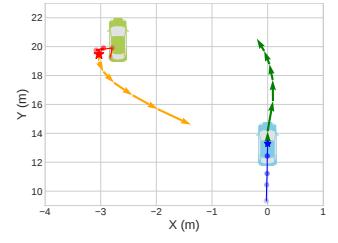
(a) Left-side scenario with adversarial objects deployed (victim AV’s view).



(b) Result of left-side scenario when no adversarial objects are deployed.



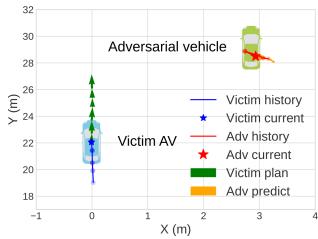
(c) Result of left-side attack(ours) at a velocity of 5 km/h. Success ratio: 5/5.



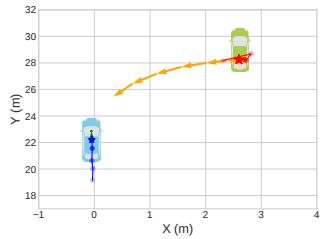
(d) Result of left-side attack(ours) at a velocity of 10 km/h. Success ratio: 4/5.



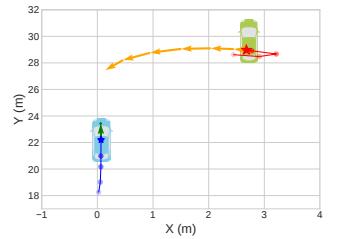
(e) Right-side scenario with adv ob- jects deployed (victim AV’s view).



(f) Result of right-side scenario when no adversarial objects are deployed.



(g) Result of right-side attack(ours) at a velocity of 5 km/h. Success ratio: 4/5.



(h) Result of right-side attack(ours) at a velocity of 10 km/h. Success ratio: 5/5.

Figure 10: Two real-world scenarios with a parked black Tesla car as the adversarial vehicle. The adversarial objects (cardboards) placed at the locations computed by our inverse attack are highlighted with red boxes. The attack results are illustrated in grid maps, where the blue car represents the victim AV and the green car represents the adversarial vehicle.

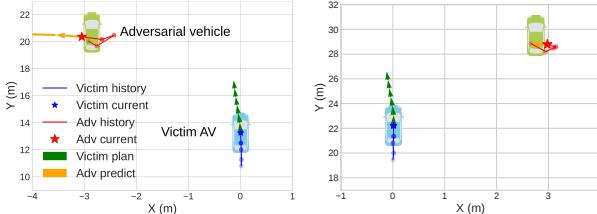
attack is viewed as successful when the PRE exceeds a threshold of 1 m, which is a significant change in the victim AV’s planning decision due to the erroneously predicted trajectory.

**Inverse Attack (Ours).** In these experiments, we place objects at the adversarial locations identified by our attack during the attack planning phase, using data collected at a velocity of 5 km/h. We then evaluate the effectiveness of these locations when the victim AV drives at velocities of 5 km/h or 10 km/h, with slight variations for each trial, capturing the uncertainties encountered in real driving environments. Figs. 10(a) and 10(e) present the scenarios when our attack is deployed. Corresponding LiDAR point clouds perceived by the victim AV under attack can be found in Appendix B.2. In non-attack scenarios, the adversarial vehicle is predicted static and thus poses no threat to the victim AV’s trajectory planning, as depicted in Figs. 10(b) and 10(f). In the left-side scenario, our attack succeeds in five out of five trials at an evaluation velocity of 5 km/h. Fig. 10(c) shows a successful attack where our attack misleads the victim AV at a velocity of 5 km/h to predict a future trajectory heading towards itself, forcing the victim AV to an emergency brake. Our attack, utilizing adversarial locations planned using data at a velocity of 5 km/h, succeeds in four out of five trials at an evaluation velocity of 10 km/h. Fig. 10(d) presents a successful example, where our attack induces a similar prediction error as in the scene at a velocity of 5 km/h in Fig. 10(c), demonstrating our attack’s velocity insensitivity. In the right-side scenario, the planned adversarial locations achieve four successes out of five trials at an evaluation velocity of 5 km/h and five out of five at 10 km/h. Example successful attack scenes at velocities

of 5 km/h and 10 km/h are shown in Figs. 10(g) and 10(h), with similar trajectory prediction errors and the same sudden brake decision taken by the victim AV in both scenes. In both left- and right-side scenarios, successful attack examples at different evaluation velocities demonstrate similar perception errors at the current time step, as marked by red stars in Fig. 10. This indicates the effectiveness of single-point attack in inducing prediction error at the current frame. Detailed quantitative results, including comparisons of ATD and PRE, are presented in Appendix B.2.

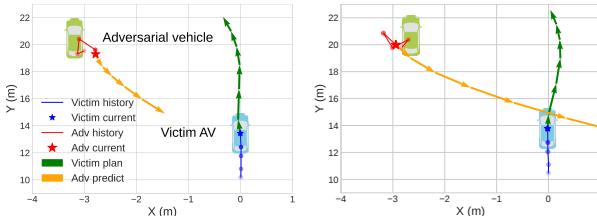
**Baseline 1: Random Location Attack.** In this set of experiments, adversarial cardboards are randomly placed around the adversarial vehicle. Some example scenes are shown in Appendix B.2. In both left-side and right-side random location attack scenarios, our evaluation yields no successful attacks out of five trials. Fig. 11(a) illustrates a left-side attack example where cardboards, randomly placed on the right side of the adversarial vehicle, cause a predicted trajectory of the adversarial vehicle moving to the left of the victim AV, posing a limited threat. Fig. 11(b) shows a right-side attack example with cardboards randomly placed at the rear, leading to a static predicted trajectory of the adversarial vehicle with no threat to the victim AV. The results demonstrate that, objects placed at random locations may affect the predicted trajectories of the adversarial vehicle, while failing to achieve the attack goal defined in Eq. 1. This underscores the importance of strategic object placement at adversarial locations, which is facilitated by our inverse attack.

**Baseline 2: Brute-force Sampling Attack.** We evaluate the attack effectiveness of the brute-force sampling method



(a) Result of left-side random location attack. Success ratio: 0/5. (b) Result of right-side random location attack. Success ratio: 0/5.

Figure 11: Random location attack results.



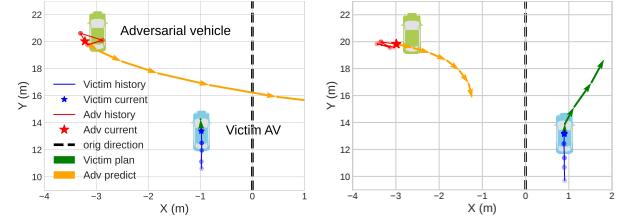
(a) Result of coordinate shift (0.1m). (b) Result of orientation shift. Success ratio: 3/5.

Figure 12: Robustness against object displacement errors induced by shifts in object coordinates or orientations.

using locations derived from data at a velocity of 5 km/h in the planning phase. The evaluation is conducted in the left-side scenario at velocities of 5 km/h and 10 km/h. This method achieves a success ratio of three out of five trials at both velocities. The reason for the reduced attack success ratio compared with our inverse attack, even under the less challenging condition at a velocity of 5 km/h, is likely due to small fluctuations in the victim AV’s velocity between trials. These variations can render velocity-sensitive adversarial locations ineffective, leading to attack failures due to minor discrepancies from the original scene in the attack planning phase.

### 7.3 Attack Robustness

**Robustness against Object Displacement.** When deploying cardboards at the adversarial locations, there may be deviations in their 3D coordinates and orientations. To evaluate our attack’s robustness against these deviations, we conduct experiments to randomly shift each cardboard’s 3D coordinates and orientation, respectively. The experiments are performed in the left-side attack scenario, with the victim AV driving at a velocity of 5 km/h. Some example scenes are illustrated in Appendix B.2. To simulate the shifts, we move each cardboard 0.1 m from its planned location in random directions. Results show that shifting cardboards’ coordinates by 0.1 m leads to three successful attacks out of five trials. Fig. 12(a) illustrates an example successful attack, achieving a similar attack result as in the original attack scene in Fig. 10(d). This robustness is due to the majority of points, even after shifting, still falling within the same grid cell or voxel after LiDAR detection processing. However, when the shift increases to 0.3 m, which exceeds the grid cell/voxel size, the attack success ratio drops



(a) Result of victim AV in left driving direction. Success ratio: 2/5. (b) Result of victim AV in right driving direction. Success ratio: 3/5.

Figure 13: Robustness against various driving directions of the victim AV.

to one out of five trials. To simulate orientation shifts, the cardboards are rotated randomly within  $[-30^\circ, 30^\circ]$ . In all five trials, our attack is successful. Fig. 12(b) shows a successful attack. This robustness may stem from the observation that, despite substantial orientation shifts, the points on a cardboard mostly remain within the original grid or shift to an adjacent grid, resulting in similar perception and prediction outcomes. To summarize, the adversarial locations identified by our inverse attack remain effective within a reasonable range of object displacement errors induced by coordinate and orientation shifts.

**Robustness against Varied Driving Direction.** During the evaluation, the victim AV remains in the same lane as in the planning phase. However, it may not maintain a perfectly straight path and occasionally steer slightly to the left or right. To evaluate the robustness of our inverse attack against the variations in victim AV’s driving direction, we conduct an experiment in the left-side scenario at a velocity of 5 km/h, with example scenes shown in Appendix B.2. With the planned adversarial locations unchanged, we shift the victim AV’s starting and attack point by 1 m to the left or right of their original positions, simulating the victim AV going slightly rightward or leftward. When shifting the victim AV’s driving direction to the left, two out of five attack trials are successful. When shifting to the right, the attack success ratio is three out of five. Figs. 13(a) and 13(b) show example successful attack results. When shifting to the left direction, the victim AV is forced to brake urgently due to the reduced distance from the predicted trajectory of the adversarial vehicle, while shifting to the right direction leads to a lane change to avoid intersection with the adversarial vehicle’s predicted trajectory.

## 8 Discussions

### 8.1 A Potential Defense

This work shows that a lack of awareness for adversarial vehicle states can lead to hazardous results, which our proposed attack exploits. As depicted in Fig. 4, in a sequence of adversarial states under attack, the coordinates are typically perturbed within a reasonable range ( $\pm 1$ m), but the heading shows significant volatility. For instance, an adversar-

ial vehicle’s heading might abruptly reverse from one frame to the next, which violates the vehicle physical dynamics. Inspired by this, we propose a *heading-centric adversarial state detector* based on the kinematic bicycle model as the defense for our proposed attack. It scrutinizes the discrepancy between observed and physically plausible heading changes across consecutive frames. Given a wheelbase  $L_w$  and a maximum steering angle  $\theta_{\max}$ , following the kinematic bicycle model, the expected maximum heading change is denoted as  $\Delta h_{\max} = \frac{v\Delta t \tan(\theta_{\max})}{L_w}$ , where  $v$  represents the vehicle’s velocity and  $\Delta t$  is the time interval between two consecutive frames. A scene is labeled adversarial if the observed heading changes in at least two frames exceed the calculated  $\Delta h_{\max}$ . This serves as a criterion for detecting abnormal behaviors, such as those of a vehicle under object-based attacks. As the defense, the detected adversarial states are replaced with the states predicted by the kinematic bicycle model using preceding states. We evaluate the detector on 400 attack scenes under the same experiment setting as in Section 6. We set  $L_w$  at 2.5 m and  $\theta_{\max}$  at 1 rad, following standard vehicle configurations. The results show that, 44.5% (178/400) attacked scenes are detected. With defense, the ATD changes from 5.45 m to 6.03 m, PRE from 1.51 m to 1.15 m, and CR from 40% to 25%.

## 8.2 Other Possible Defenses

Based on the nature of our attack mechanisms, three types of existing general defense approaches might be applied. We discuss and evaluate the effectiveness of such defenses against our attack strategy.

*Spatial-temporal consistency checks:* Recent studies [16, 33, 35] have explored spatial-temporal consistency checks to detect perception attacks. PercepGuard [33] is a representative method that leverages the spatial-temporal properties of bounding boxes across different classes to detect anomalies. In our experiments, PercepGuard detects anomalies in 4 out of 400 attack scenes, with a limit of 100 queries, under the same settings as in the dataset-based experiments. Unlike typical attacks that aim to induce object disappearance, creation, or misclassification, our attack subtly perturbs bounding boxes, presenting a challenge for spatial-temporal checks.

*Adversarial training:* Following adversarial training [19], we fine-tune the Trajectron++ predictor with adversarial states generated by our attacks for an additional 10 epochs. After training, the CR decreases from 40% to 35%, while the mean Final Displacement Error increases from 2.18m to 2.22m in clean scenes. This illustrates a trade-off between robustness and accuracy in the trajectory prediction model. Moreover, effective adversarial training requires the defender to know the attack methods, which is not always possible.

*MC-dropout:* We also explore MC-dropout [18], a technique that introduces randomness into the perception model during inference, thus disrupting the matching between bounding box perturbations and adversarial states. Implementing MC-dropout with 5 runs led to a reduction in the collision

rate from 40% to 18%. However, this defense significantly increases the computational overhead during inference, impacting the real-time performance capabilities of AD systems.

In conclusion, existing methods can partially defend against our attack but also introduce some additional overhead. Our proposed lightweight defense method checks key adversarial states against vehicle dynamics, achieving a good balance of efficacy and cost.

## 8.3 Limitations and Future Work

**Single-Point Attack Impact.** A limitation of our attack is its diminishing impact once the victim AV passes the attack point. For example, a victim AV brakes suddenly at the attack point may resume normal behavior in subsequent frames. This occurs because the current frame at the attack point becomes one of the historical frames as the victim moves, being less effective as shown in finding **F1** in Section 5.2. To address this limitation, developing a temporally effective attack to maintain consistent impact over time is interesting.

**Different Attack Scenarios.** Another limitation is that our attack focuses on the driving scenario where a victim AV passes a roadside-parked adversarial vehicle. Future work can explore other common scenarios, such as an adversarial vehicle stopped at an intersection, potentially impacting more vehicles in dense traffic scenarios. Moreover, it is interesting to extend our attack to scenarios where both the adversarial vehicle and the victim AV are moving. In these cases, drones can act as movable adversarial objects, utilizing advanced drone localization and tracking technologies. This approach opens up an opportunity for a continuous and dynamic attack, adapting to the changing positions of the adversarial vehicle.

**Attack Multi-sensor Fusion.** Our attack can be extended to multi-sensor fusion systems by optimizing existing perception attacks for different sensing modalities. For example, we can use adversarial objects with specific shapes and textures to compromise both LiDAR and camera perceptions, akin to techniques discussed in [8, 65]. Specifically, the shape and texture attributes of the adversarial objects can be randomly sampled to create the bounding box perturbation set. Then, our prediction-side attack methodology can be applied to generate a set of adversarial states. Lastly, a matching and refining phase is applied, where the shape and texture parameters are adjusted to optimize the attack’s effectiveness across sensors.

## 9 Conclusion

In this paper, we investigate the possibility of compromising trajectory prediction in autonomous driving systems via physically realizable object-based LiDAR attacks on perception modules. We find that prediction models are vulnerable to single-point attacks. Building on this insight, we introduce a novel two-stage attack framework that efficiently identifies an effective, velocity-insensitive, and feasible adversarial location set. By strategically placing objects at these locations,

the attacker can manipulate the victim vehicle to predict a wrong trajectory of a nearby agent, potentially inducing hazardous victim AV responses. We evaluate the proposed attack framework on both a public autonomous driving dataset and a custom-built real testbed car. The results demonstrate that our proposed attack consistently achieves the highest threat across various driving conditions and shows robustness against different types of noise.

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## Appendix

### A Generalizability Across Models

To extend our analysis beyond Trajectron++, the primary trajectory prediction model utilized in this study, we apply our attack to AgentFormer [58], another advanced trajectory predictor, to assess its generalizability. We follow the same experimental settings as those used in the dataset-based experiments, and the AgentFormer model is also trained on the nuScenes dataset using its default configuration. Fig. 14 compares the Average Trajectory Distance (ATD), Planning-Response Error (PRE), and Collision Rate (CR) metrics between our inverse attack method and the brute-force sampling method when applied to the victim AV system utilizing AgentFormer. The number of queries ranges from 100 to 500. The results show that our inverse attack consistently outperforms the brute-force sampling method on three metrics across all query limitations. These outcomes, similar to those presented in Fig. 5, further demonstrating the generalizability of our attack.

## B Supplementary Experiments

### B.1 Experiments on Dataset

Fig. 15 shows the Average Trajectory Distance (ATD) and Planning-Response Error (PRE) of our inverse attack method under varied object displacements. Fig. 16 demonstrates how different object sizes affect the ATD and PRE metrics of our inverse attack method. Fig. 17 illustrates the ATD, PRE, and CR metrics in the attack transferability experiments, where

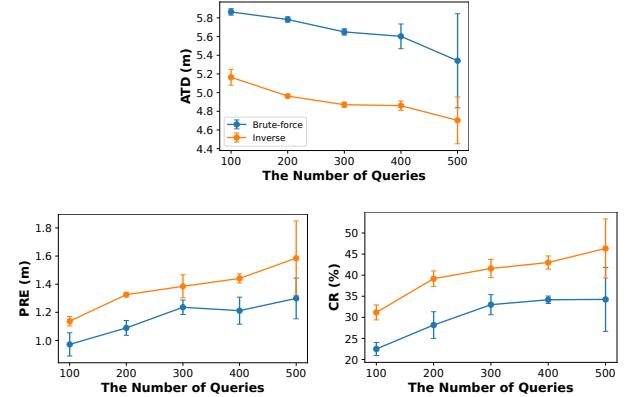


Figure 14: ATD, PRE and CR under brute-force sampling attack and our inverse attack on victim AV using AgentFormer trajectory predictor.

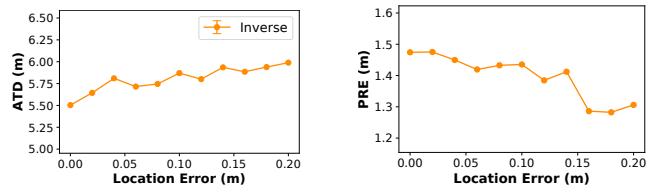


Figure 15: Attack robustness against object displacement.

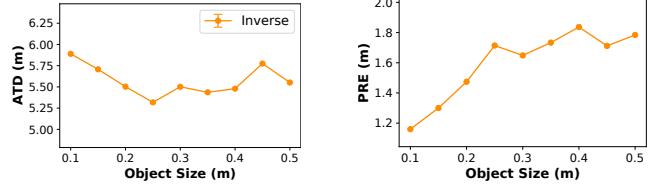


Figure 16: Attack robustness against object size.

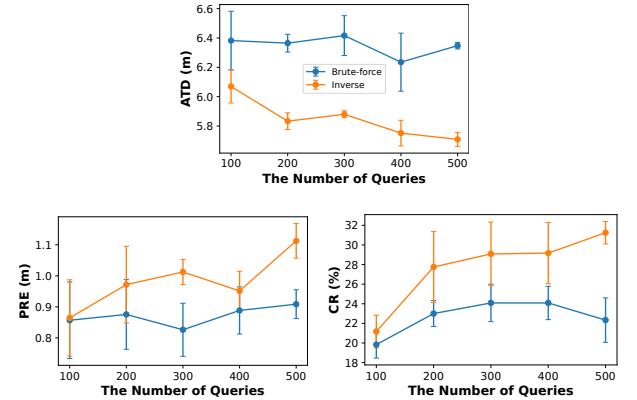


Figure 17: ATD, PRE, and CR under brute-force sampling attack and our inverse attack in the black-box scenario. The attack is planned using Trajectron++ predictor and evaluated on the AgentFormer model.

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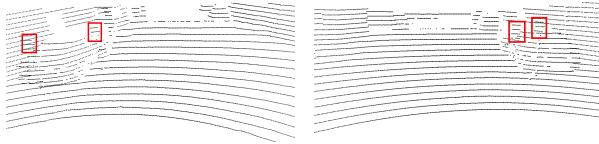


(a) Testbed car equipped with LiDAR and GNSS.



(b) Cardboards affixed to tripods.

Figure 18: Physical-world experiment setup.



(a) Point cloud view of the left-side attack scene. (b) Point cloud view of the right-side attack scene.

Figure 19: LiDAR point cloud view of two real-world attack scenarios.

Table 2: ATD and PRE under clean scenario and our inverse attack at velocities of 5 km/h and 10 km/h.

Scenario	Left			Right		
	Clean	5km/h	10km/h	Clean	5km/h	10km/h
ATD	4.78	3.50	4.12	4.71	3.14	3.62
PRE	0.00	1.36	2.01	0.00	1.17	1.83

## B.2 Experiments in Physical World

**Experimental Settings** Fig. 18 provides a detailed view of the testbed car and cardboards used in the physical-world experiment. The top LiDAR, marked in the green box, is responsible for collecting point cloud data. The GNSS Receiver with RTK, highlighted in blue, enables precise localization of the testbed car, facilitating the construction of an accurate coordinate system essential for prediction and planning. Regarding the cardboards, we design them to mimic traffic signs and billboards, which are common in driving scenarios, thereby enhancing the stealthiness of our attack.

**Attack Effectiveness** Figs. 19(a) and 19(b) depict the LiDAR point cloud views captured by the victim AV (our testbed car) in the left- and right-side attack scenarios, respectively. Notably, cardboards, outlined in red boxes, contribute additional point clusters to the collected LiDAR point cloud data. These point clusters serve as the basis of our attack, inducing perception and prediction errors. Table 2 presents the ATD and PRE metrics in the absence and presence of our inverse attack, across evaluation velocities of 5 km/h and 10 km/h,



(a) Left-side scenario under random location attack.



(b) Right-side scenario under random location attack.

Figure 20: Random location attack scenes.



(a) Orientation shift scene.



(b) Coordinate shift (0.3m) scene.

Figure 21: Scenes with object displacement errors induced by shifts in object coordinates or orientations.



(a) Driving direction to left.



(b) Driving direction to right.

Figure 22: Scenes under various driving directions of the victim AV.

within both the left- and right-side scenarios. The results indicate that, compared to the clean scenario (without attack), our inverse attack significantly reduces ATD and increases PRE, quantitatively demonstrating its effectiveness.

**Attack Robustness** Fig. 20 shows example scenes of the random location attack, with their corresponding results presented in Fig. 11. In each trial, we sample a varied set of adversarial locations beyond those depicted, including positions beside and behind the adversarial vehicle.

Fig. 21 illustrates example scenes with object displacements. Specifically, in Fig. 21(a), the cardboards are adjusted to face forward, deviating from their initial orientations toward the victim vehicle. In Fig. 21(b), the coordinates of cardboards are shifted by 0.3 m from the predetermined adversarial locations, notably moving them toward the road. In real-world deployment, attackers equipped with distance-measuring devices, such as a tape measure, can precisely place objects at specific adversarial locations.

The example scenes depicting various driving directions of the victim AV are presented in Fig. 22, with the associated attack results shown in Fig. 13.