

# Studies on Domain Walls, Cosmic Strings, and Their Gravitational Wave Signatures

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<https://yzhxxzxy.github.io>

Based on Qing-Quan Zeng, Xi He, ZHY, Jiaming Zheng, arXiv:2501.10059

Shi-Qi Ling, ZHY, arXiv:2502.16576



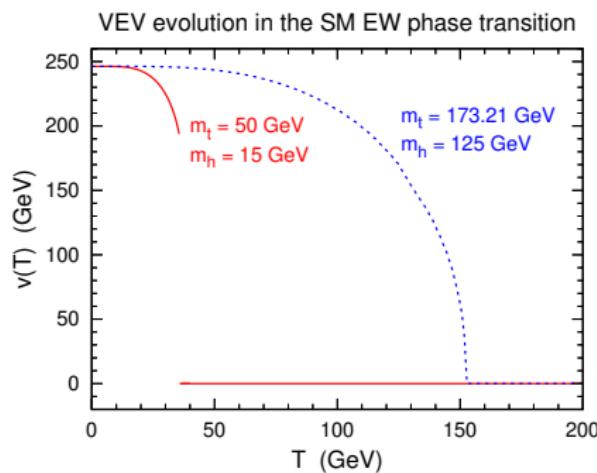
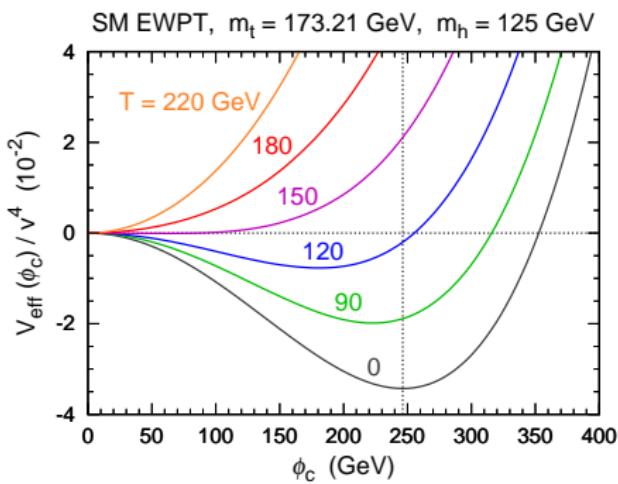
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# Cosmological Phase Transition

 Spontaneously broken symmetries in field theories can be restored at sufficiently high temperatures due to thermal corrections to the effective potential

 In the history of the Universe, spontaneous symmetry breaking manifests itself as a cosmological phase transition



# Topological Defects

 Consider that **some scalar fields** acquire nonzero **vacuum expectation values** (VEVs), which **break** a **symmetry group  $G$**  to a **subgroup  $H$**

 The **manifold** consisting of all **degenerate vacua** is the **coset space  $G/H$**

 The **topology** of the **vacuum manifold  $G/H$**  can be characterized by its  **$n$ -th homotopy group  $\pi_n(G/H)$** , which are formed by the homotopy classes of the mappings from an  **$n$ -dimensional sphere  $S^n$**  into  $G/H$

 A **nontrivial  $\pi_n(G/H)$**  leads **topological defects** [Kibble, J. Phys. A9 (1976) 1387], as commonly predicted in **grand unified theories**

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**Nontrivial  $\pi_0(G/H)$ :** two or more disconnected components

**Domain walls** (2-dim topological defects)

**Nontrivial  $\pi_1(G/H)$ :** incontractable closed paths

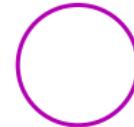
**Cosmic strings** (1-dim topological defects)

**Nontrivial  $\pi_2(G/H)$ :** incontractable spheres

**Monopoles** (0-dim topological defects)



$$\pi_0(G/H) = \mathbb{Z}_2$$



$$\pi_1(G/H) = \mathbb{Z}$$

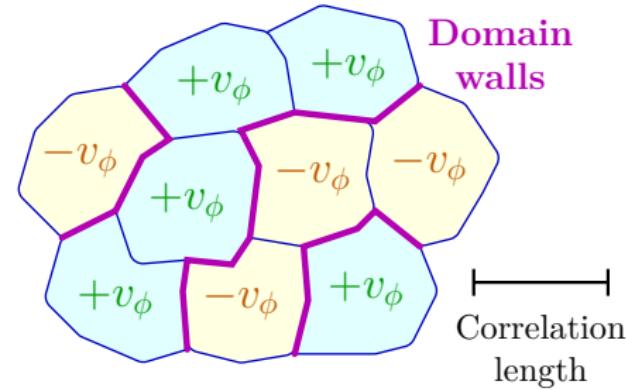
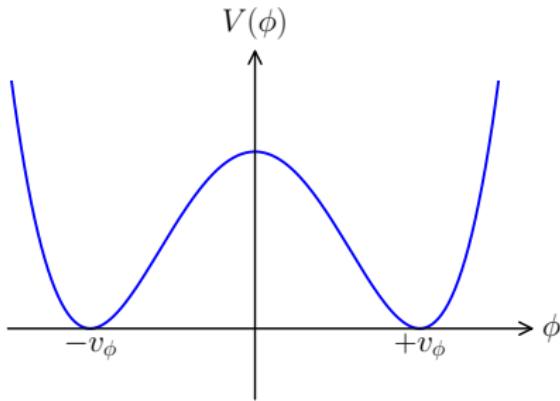
# Domain Walls

⌚ Domain walls (DWs) are two-dimensional topological defects which could be formed when a discrete symmetry of the scalar potential is spontaneously broken in the early Universe

-II They are boundaries separating spatial regions with different degenerate vacua

🚫 Stable DWs are thought to be a cosmological problem [Zeldovich, Kobzarev, Okun, Zh.Eksp.Teor.Fiz. 67 (1974) 3]

⚠ As the Universe expands, the DW energy density decreases slower than radiation and matter, and would soon dominate the total energy density



# Collapsing Domain Walls



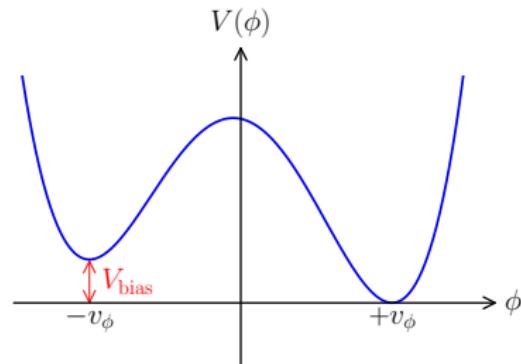
It is **allowed** if **DWs collapse** at a very early epoch [Vilenkin, PRD 23 (1981) 852; Gelmini, Gleiser, Kolb, PRD 39 (1989) 1558; Larsson, Sarkar, White, hep-ph/9608319, PRD]

Such **unstable DWs** can be realized if the **discrete symmetry is explicitly broken** by a **small potential term** that gives an **energy bias**  $V_{\text{bias}}$  among the minima of the potential

The bias induces a **volume pressure force** acting on the DWs that leads to their collapse

**Collapsing DWs** can produce significant **GWs** [Preskill et al., NPB 363 (1991) 207; Gleiser, Roberts, astro-ph/9807260, PRL; Hiramatsu, Kawasaki, Saikawa, 1002.1555, JCAP]

A **stochastic gravitational wave background (SGWB)** would be formed and remain to the present time



# Spontaneously Broken $Z_2$ Symmetry

 We study the dynamics of **DWs** formed through the **spontaneous breaking** of an **approximate  $Z_2$  symmetry** in a **scalar field**  $\phi$ , focusing on the influence of **quantum** and **thermal corrections** induced by a  **$Z_2$ -violating Yukawa coupling** to **Dirac fermions**  $f$  in the **thermal bath** [QQ Zeng, X He, ZHY, JM Zheng, 2501.10059]

$$\mathcal{L} = \frac{1}{2} \partial_\mu \phi \partial^\mu \phi + i \bar{f} \gamma^\mu \partial_\mu f - m_f \bar{f} f - y \phi \bar{f} f - V_0(\phi)$$

$$V_0(\phi) = -\frac{1}{2} \mu_\phi^2 \phi^2 + \frac{1}{3} \mu_3 \phi^3 + \frac{1}{4} \lambda_\phi \phi^4, \quad \mu_\phi^2 > 0, \quad \lambda_\phi > 0$$

 The small **couplings**  $y$  and  $\mu_3$  **explicitly violate** the  **$Z_2$  symmetry**  $\phi \rightarrow -\phi$

 Considering the **Coleman-Weinberg correction**  $V_{\text{CW}}(\phi)$  and **finite-temperature correction**  $V_T(\phi, T)$  at one-loop level, the **effective potential** becomes

$$V(\phi, T) = V_0(\phi) + V_{\text{CW}}(\phi) + V_T(\phi, T)$$

 The **vacuum expectation value (VEV)**  $v_\phi$  of  $\phi$  corresponds to

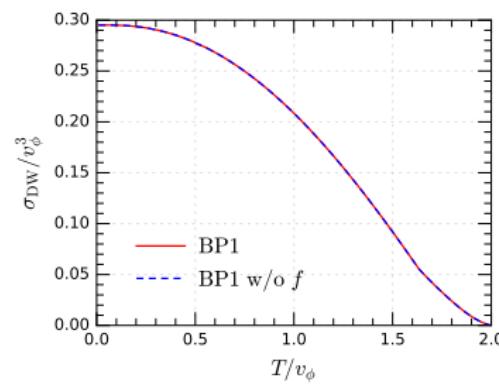
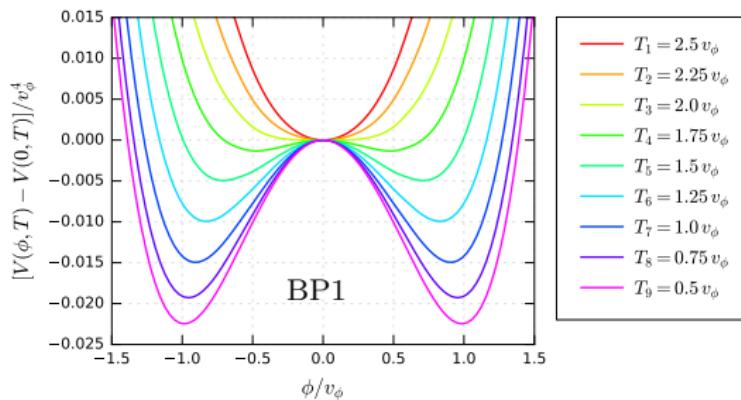
$$\left. \frac{\partial}{\partial \phi} [V_0(\phi) + V_{\text{CW}}(\phi)] \right|_{\phi=v_\phi} = 0$$

# Potential Evolution and DW Tension

By solving the equation of motion for the **DW solution** and integrating the energy density, the **DW tension**  $\sigma_{\text{DW}}$ , i.e., **energy per unit area**, can be obtained

We choose **three benchmark points** (BPs) to highlight remarkable features

	$v_\phi$ [GeV]	$\mu_3/v_\phi$	$\lambda_\phi$	$y$	$m_f/v_\phi$
<b>BP1</b>	$2 \times 10^9$	$-10^{-17}$	0.1	$2.5 \times 10^{-5}$	$4 \times 10^{-5}$
<b>BP2</b>	$5 \times 10^4$	$-10^{-27}$	0.1	$-9 \times 10^{-8}$	$10^{-7}$
<b>BP3</b>	$1.5 \times 10^{11}$	$-1.2148 \times 10^{-13}$	0.1	$3 \times 10^{-4}$	$4 \times 10^{-4}$



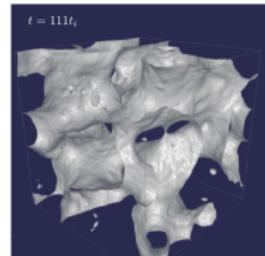
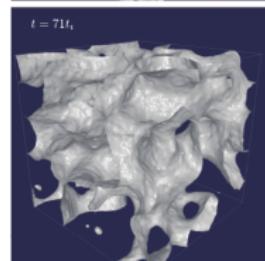
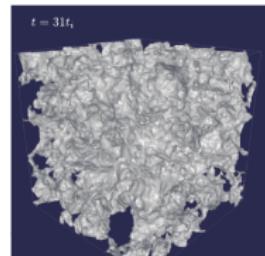
# Evolution of Domain Walls

After DWs are created, the **tension**  $\sigma_{\text{DW}}$  acts to **stretch** them up to the **horizon size** if the **friction**  $F_f$  is **small**, and they would enter the **scaling regime** with **energy density**  $\rho_{\text{DW}} = \frac{\mathcal{A}\sigma_{\text{DW}}}{t}$

$\mathcal{A} \approx 0.8 \pm 0.1$  is a numerical factor given by lattice simulation

$\rho_{\text{DW}} \propto t^{-1}$  implies that DWs are **diluted more slowly** than **radiation** and **matter** as the Universe expands

If DWs are **stable**, they would soon **dominate** the evolution of the Universe, **conflicting** with cosmological observations



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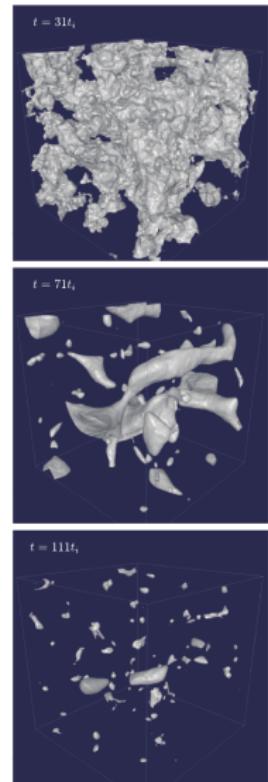
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⚠ However, the **potential bias**  $V_{\text{bias}}(T) = V(\phi_-, T) - V(\phi_+, T)$  between the false and true vacua  $\phi_-$  and  $\phi_+$  provides a **pressure**  $p_V(T) \sim V_{\text{bias}}(T)$  acting on the DWs, against the **tension force per unit area**  $p_T(T) \sim \rho_{\text{DW}}(T)$

⚠ This makes the **DWs collapse** and the **false vacuum domains shrink**

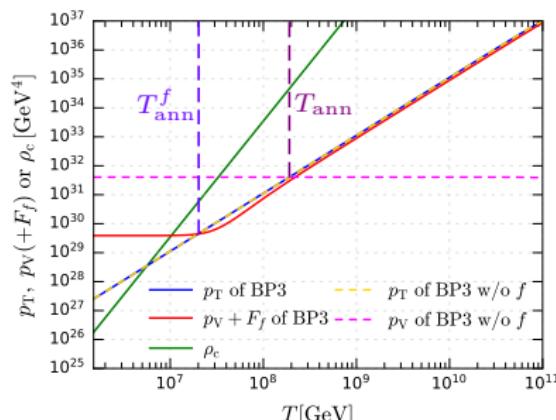
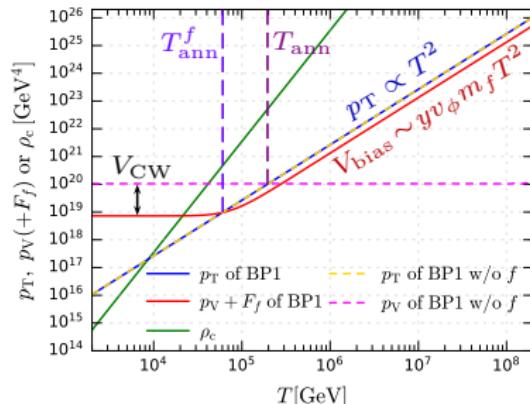
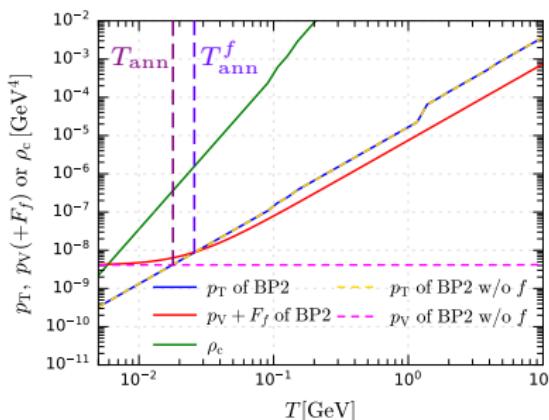
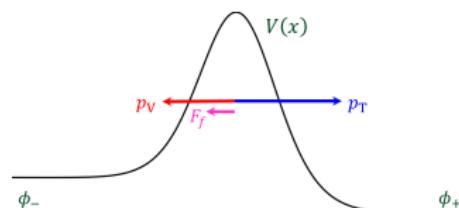


[Hiramatsu et al., 1002.1555]

# Annihilation Temperature

The **domain walls collapse** at the **annihilation temperature  $T_{\text{ann}}$**  when

$$p_V(T_{\text{ann}}) + F_f(T_{\text{ann}}) \simeq p_T(T_{\text{ann}})$$



# SGWB Spectrum from Collapsing DWs

 The **SGWB spectrum** is commonly characterized by  $\Omega_{\text{GW}}(f) = \frac{f}{\rho_c} \frac{d\rho_{\text{GW}}}{df}$

  $\rho_{\text{GW}}$  is the **GW energy density**, and  $\rho_c$  is the critical energy density

 The SGWB from **collapsing DWs** can be estimated by **numerical simulations**

[Hiramatsu, Kawasaki, Saikawa, 1002.1555, 1309.5001, JCAP]

 The **present SGWB spectrum** induced by collapsing DWs can be evaluated by

$$\Omega_{\text{GW}}(f) h^2 = \Omega_{\text{GW}}^{\text{peak}} h^2 \times \begin{cases} \left(\frac{f}{f_{\text{peak}}}\right)^3, & f < f_{\text{peak}} \\ \frac{f_{\text{peak}}}{f}, & f > f_{\text{peak}} \end{cases}$$

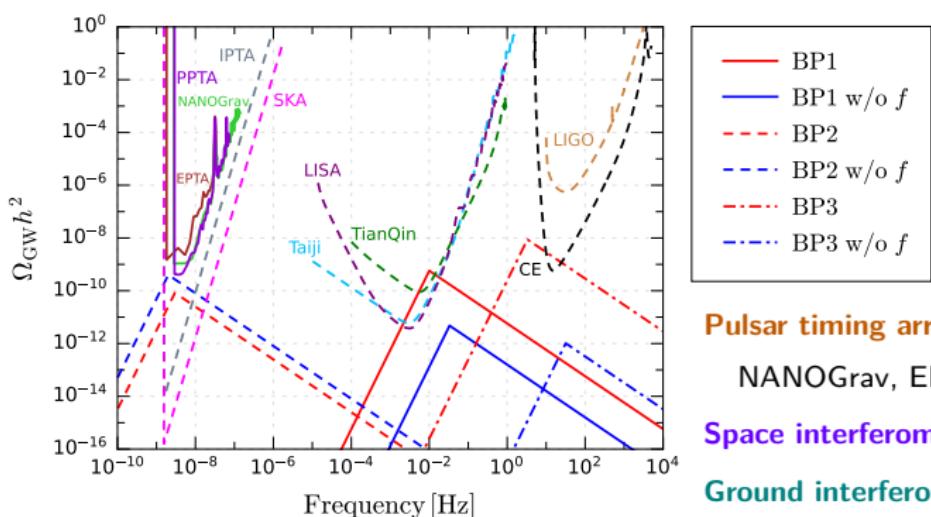
$$\Omega_{\text{GW}}^{\text{peak}} h^2 = 7.2 \times 10^{-18} \tilde{\epsilon}_{\text{GW}} \mathcal{A}^2 \left[ \frac{g_{*s}(T_{\text{ann}})}{10} \right]^{-4/3} \left[ \frac{\sigma_{\text{DW}}(T_{\text{ann}})}{1 \text{ TeV}^3} \right]^2 \left( \frac{T_{\text{ann}}}{10 \text{ MeV}} \right)^{-4}$$

$$f_{\text{peak}} = 1.1 \times 10^{-9} \text{ Hz} \left[ \frac{g_*(T_{\text{ann}})}{10} \right]^{1/2} \left[ \frac{g_{*s}(T_{\text{ann}})}{10} \right]^{-1/3} \frac{T_{\text{ann}}}{10 \text{ MeV}}$$

  $\tilde{\epsilon}_{\text{GW}} = 0.7 \pm 0.4$  is derived from numerical simulation

# SGWB Spectra with and without the Fermion

- 🏓 A decrease of  $T_{\text{ann}}$  by one order of magnitude would increase  $\Omega_{\text{GW}}^{\text{peak}} h^2$  by four orders of magnitude and decrease  $f_{\text{peak}}$  by one order of magnitude
- 🏸 The differences between the SGWB spectra predicted by the scenarios with and without the fermion could potentially be verified by future GW experiments



**Pulsar timing arrays (PTAs):**

NANOGrav, EPTA, PPTA, IPTA, SKA

**Space interferometers:** LISA, TianQin, Taiji

**Ground interferometers:** LIGO, CE

# Cosmic Strings from U(1) Gauge Symmetry Breaking

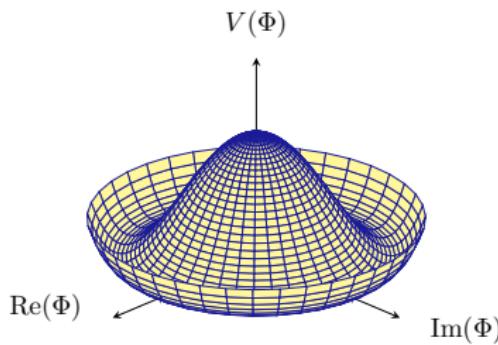
💡 Consider the **Abelian Higgs model** with a **complex scalar field**  $\Phi$

$$\mathcal{L} = (D^\mu \Phi)^\dagger (D_\mu \Phi) - V(\Phi) - \frac{1}{4} X^{\mu\nu} X_{\mu\nu}, \quad V(\Phi) = -\mu_\phi^2 |\Phi|^2 + \frac{\lambda_\Phi}{2} |\Phi|^4$$

💡 The covariant derivative of  $\Phi$  is  $D_\mu \Phi = (\partial_\mu - iq_\Phi g_X X_\mu) \Phi$

💡 The field strength tensor of the **U(1)<sub>X</sub> gauge field**  $X^\mu$  is  $X_{\mu\nu} = \partial_\mu X_\nu - \partial_\nu X_\mu$

🧸 Assume a **Mexican-hat potential**  $V(\Phi)$  with **degenerate vacua**  $\langle \Phi \rangle = v_\Phi e^{i\varphi} / \sqrt{2}$



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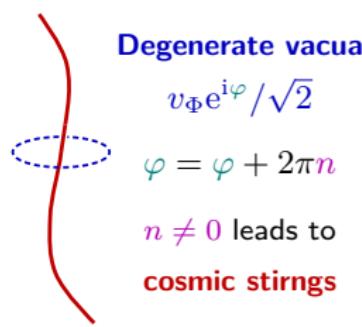
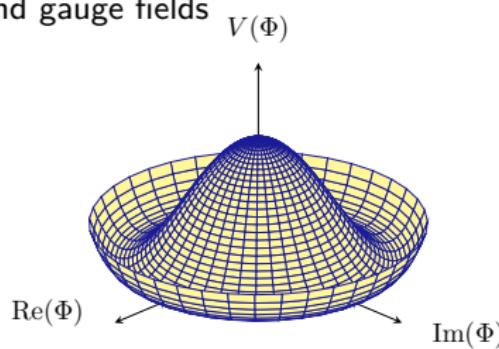
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 The **spontaneous breaking** of the **U(1)<sub>X</sub> gauge symmetry** in the early Universe would induce **cosmic strings (CSs)**, which are concentrated with energies of the scalar and gauge fields



# Cosmic String Tension

 A **network of cosmic strings** would be formed in the early Universe after the spontaneous breaking of the  $U(1)_X$  gauge symmetry

 The **tension** of **cosmic string  $\mu$**  (energy per unit length) can be estimated as

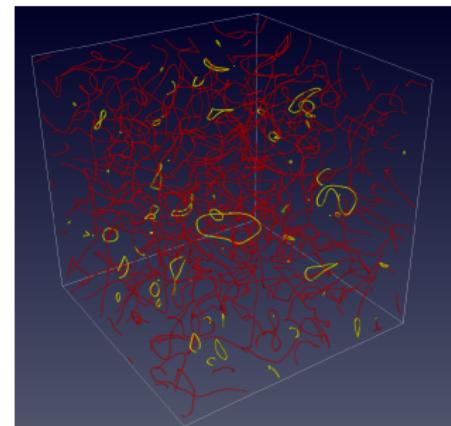
$$\mu \simeq \begin{cases} 1.19\pi v_\Phi^2 b^{-0.195}, & 0.01 < b < 100, \\ \frac{2.4\pi v_\Phi^2}{\ln b}, & b > 100, \end{cases}$$

$$b \equiv \frac{2q_\Phi^2 g_X^2}{\lambda_\Phi}$$

[Hill, Hodges, Turner, PRD 37, 263 (1988)]

 As  $\mu \propto v_\Phi^2$ , a **high symmetry-breaking scale**  $v_\Phi$  would lead to cosmic strings with **high tension**

 Denoting  $G$  as the **Newtonian constant of gravitation**, the **dimensionless quantity  $G\mu$**  is commonly used to describe the **tension** of cosmic strings



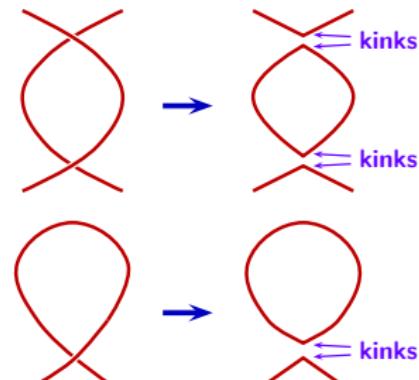
[Kitajima, Nakayama, 2212.13573, JHEP]

# Gravitational Waves from Cosmic Strings

According to the analysis of string dynamics, the intersections of long strings could produce closed loops, whose size is smaller than the Hubble radius

Cosmic string loops could further fragment into smaller loops or reconnect to long strings

Loops typically have localized features called “cusps” and “kinks”



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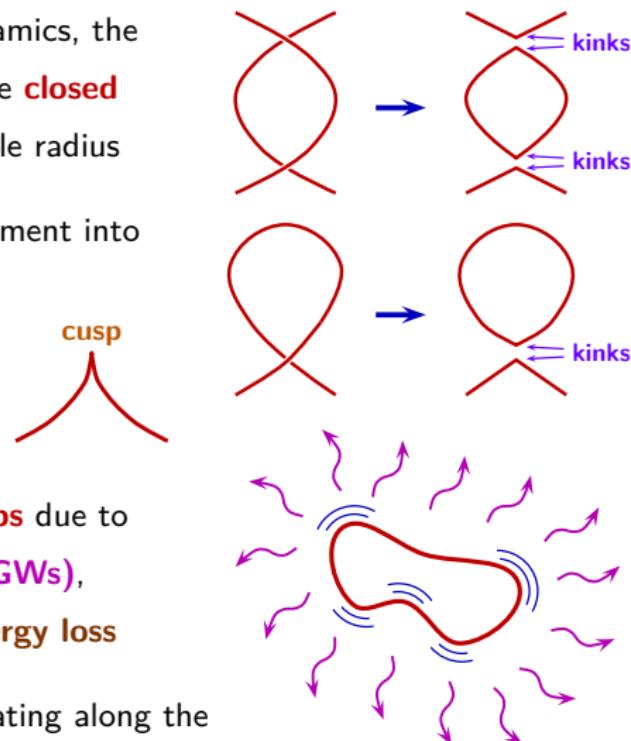
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The **relativistic oscillations** of the **loops** due to their **tension** emit **Gravitational Waves (GWs)**, and the loops would **shrink** because of **energy loss**

Moreover, the **cusps** and **kinks** propagating along the loops could produce **GW bursts** [Damour & Vilenkin, gr-qc/0004075, PRL]



# Power of Gravitational Radiation

🎻 At the **emission time**  $t_e$ , a **cosmic string loop** of **length**  $l$  emits GWs with **frequencies**  $f_e = \frac{2n}{l}$

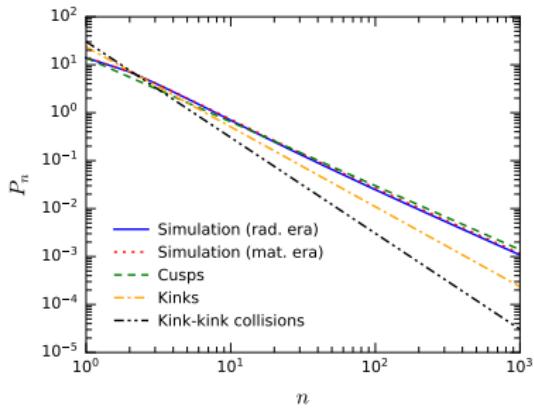
🎵  $n = 1, 2, 3, \dots$  denotes the **harmonic modes** of the loop oscillation

🎺 Denoting  $P_n$  as the **power of gravitational radiation** for the harmonic mode  $n$  in units of  $G\mu^2$ , the total power is given by  $P = G\mu^2 \sum_n P_n$

🎹 According to the **simulation** of **smoothed cosmic string loops** [Blanco-Pillado & Olum, 1709.02693, PRD],  $P_n$  for loops in the **radiation** and **matter** eras are obtained

🥁 The **total dimensionless power**  $\Gamma = \sum_n P_n$  is estimated to be  $\sim 50$

🎸 For comparison, analytic studies imply  $P_n \simeq \frac{\Gamma}{\zeta(q)n^q}$  with  $q = \frac{4}{3}, \frac{5}{3}, 2$  for **cusps**, **kinks**, and **kink-kink collisions**



# Stochastic GW Background Induced by Cosmic Strings

 The **energy** of **cosmic strings** is converted into the **energy** of **GWs**, and an **SGWB** is formed due to **incoherent superposition**

 The **SGWB energy density**  $\rho_{\text{GW}}$  per unit frequency at the present is

$$\frac{d\rho_{\text{GW}}}{df} = G\mu^2 \int_{t_{\text{ini}}}^{t_0} a^5(t) \sum_n \frac{2n P_n}{f^2} n_{\text{CS}} \left( \frac{2na(t)}{f}, t \right) dt$$

  $n_{\text{CS}}(l, t)$  is the **number density per unit length** of **CS loops** with length  $l$  at cosmic time  $t$

  $a(t)$  is the **scale factor** satisfying  $\frac{da(t)}{dt} = a(t)H(t)$  and  $a(t_0) = 1$

  $H(t)$  is the **Hubble rate** and  $t_{\text{ini}}$  is the cosmic time when the GW emissions start

 The **SGWB spectrum** is commonly represented by

$$\Omega_{\text{GW}}(f) = \frac{f}{\rho_c} \frac{d\rho_{\text{GW}}}{df}, \quad \rho_c \equiv \frac{3H_0^2}{8\pi G}$$

# Velocity-dependent One-scale Model

 The evolution of the **CS network** can be described using the **velocity-dependent one-scale (VOS) model** [Martins & Shellard, hep-ph/9507335, PRD]

 The parameters are the **correlation length  $L$**  and the **root-mean-square velocity  $v$**  of string segments; the **energy density** of **long strings** is expressed as  $\rho = \mu/L^2$

 Introducing a **dimensionless quantity**  $\xi \equiv L/t$ , the evolution equations are

$$t\dot{\xi} = H(1+v^2)t\xi - \xi + \frac{1}{2}\tilde{c}v, \quad t\dot{v} = (1-v^2)\left[\frac{k(v)}{\xi} - 2Htv\right]$$

$$\tilde{c} \simeq 0.23, \quad k(v) = \frac{2\sqrt{2}}{\pi}(1-v^2)(1+2\sqrt{2}v^3)\frac{1-8v^6}{1+8v^6}$$

 The solutions converge to **constant values** [Marfatia & YL Zhou, 2312.10455, JHEP]:

$$\xi_r = 0.271, \quad v_r = 0.662, \quad \text{radiation-dominated (RD) era}$$

$$\xi_m = 0.625, \quad v_m = 0.582, \quad \text{matter-dominated (MD) era}$$

 This implies that the CS network quickly evolves into a **linear scaling regime** characterized by  $L \propto t$

# Loop Production Functions

 The **CS loop number density** is given by  $n_{\text{CS}}(l, t) = \frac{1}{a^3(t)} \int_{t_{\text{ini}}}^t \mathcal{P}(l', t') a^3(t') dt'$

 Motivated by **numerical simulations** [Blanco-Pillado, Olum & Shlaer, 1309.6637, PRD], the **loop production functions** can be approximated as

$$\mathcal{P}_r(l, t) = \frac{\mathcal{F}_r \tilde{c} v \delta(\alpha_r \xi - l/t)}{\gamma_v \alpha_r \xi^4 t^5}, \quad \text{RD era}$$

$$\mathcal{P}_m(l, t) = \frac{\mathcal{F}_m \tilde{c} v \Theta(\alpha_m \xi - l/t)}{\gamma_v (l/t)^{1.69} \xi^3 t^5}, \quad \text{MD era}$$

  $\gamma_v = (1 - v^2)^{-1/2}$  is the Lorentz factor

 At the **loop production time**  $t_*$ , we have

$$l_* = l + \Gamma G \mu (t - t_*), \quad \alpha_r \xi_* \simeq 0.1 \text{ and } \alpha_m \xi_* \simeq 0.18$$

 Adopting  $\mathcal{F}_r = 0.1$  and  $\mathcal{F}_m = 0.36$ , the obtained **loop number densities** in the **RD** and **MD eras** **agrees** with the **simulation results** in the **scaling regime**

# Loop Production Functions

Orange: The **CS loop number density** is given by  $n_{\text{CS}}(l, t) = \frac{1}{a^3(t)} \int_{t_{\text{ini}}}^t \mathcal{P}(l', t') a^3(t') dt'$

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$$\mathcal{P}_r(l, t) = \frac{\mathcal{F}_r \tilde{c} v \delta(\alpha_r \xi - l/t)}{\gamma_v \alpha_r \xi^4 t^5}, \quad \text{RD era}$$

$$\mathcal{P}_m(l, t) = \frac{\mathcal{F}_m \tilde{c} v \Theta(\alpha_m \xi - l/t)}{\gamma_v (l/t)^{1.69} \xi^3 t^5}, \quad \text{MD era}$$

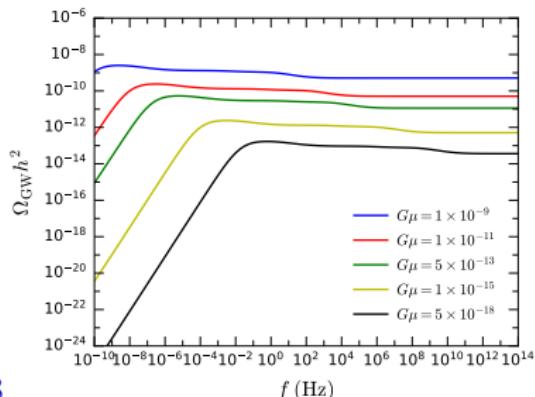
Apple:  $\gamma_v = (1 - v^2)^{-1/2}$  is the Lorentz factor

Cherry: At the **loop production time**  $t_*$ , we have

$$l_* = l + \Gamma G \mu (t - t_*), \quad \alpha_r \xi_* \simeq 0.1 \text{ and } \alpha_m \xi_* \simeq 0.18$$

Pear: Adopting  $\mathcal{F}_r = 0.1$  and  $\mathcal{F}_m = 0.36$ , the obtained **loop number densities** in the **RD** and **MD eras** **agrees** with the **simulation results** in the **scaling regime**

Avocado: The **SGWB spectra** in the  $\Lambda$ **CDM cosmological model** is further calculated



# Early Cosmic History

 Cosmological observations can **hardly** date back to eras **prior to big bang nucleosynthesis** (BBN)

 **Various hypotheses** beyond the standard cosmic history **predating BBN** are possible, such as an **early matter-dominated (EMD) era**, a **kination-dominated era**, and an **intermediate inflationary era**

 Traditional **electromagnetic detection** methods are **ineffective** when the Universe was **opaque to photons**

# Early Cosmic History

- 💡 Cosmological observations can hardly date back to eras **prior to big bang nucleosynthesis (BBN)**
- 💡 **Various hypotheses** beyond the standard cosmic history **predating BBN** are possible, such as an **early matter-dominated (EMD) era**, a **kination-dominated era**, and an **intermediate inflationary era**
- ⚠ Traditional **electromagnetic detection** methods are **ineffective** when the Universe was **opaque to photons**
- ⚠ Nonetheless, **GWs** can **propagate freely** through space, preserving information from the early Universe and reaching us in the present day
- ⚠ We study how the **SGWB spectrum** originated from a preexisting **CS network** is modified by an **EMD era** [SQ Ling & ZHY, 2502.16576]



# Origin of the Early Matter-dominated Era

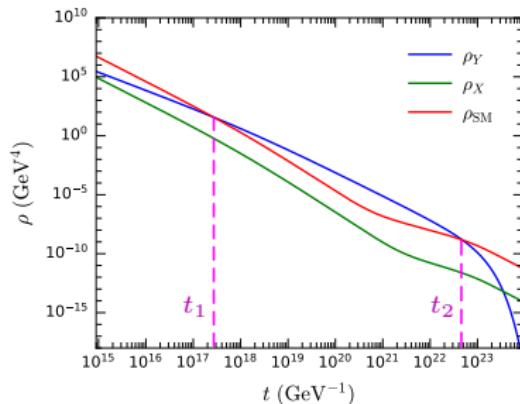
- 🐓 Consider **dark matter (DM) dilution mechanism** as the origin of the **EMD era**
- 🐓 Thermal production of a **light DM candidate  $X$**  with low annihilation cross sections typically results in an **overproduction problem**
- 🐒 DM overproduction can be **mitigated** by **entropy injection** from the **decays** of a **diluton particle  $Y$** , which **dominates** the Universe for a period, inducing an **EMD era**
- 🦅 Taking the **minimal left-right symmetric model** as an example, where the lightest and next-to-lightest right-handed neutrinos  $N_1$  and  $N_2$  can serve as  $X$  and  $Y$
- 🦉 The related Boltzmann equations are

$$\frac{d\rho_Y}{dt} + 3H\rho_Y = -\Gamma_Y \rho_Y$$

$$\frac{d\rho_X}{dt} + 4H\rho_X = yB_X \Gamma_Y \rho_Y$$

$$\frac{d\rho_{SM}}{dt} + 4H\rho_{SM} = (1 - yB_X)\Gamma_Y \rho_Y$$

[Nemevšek & Y Zhang, 2206.11293, PRL]

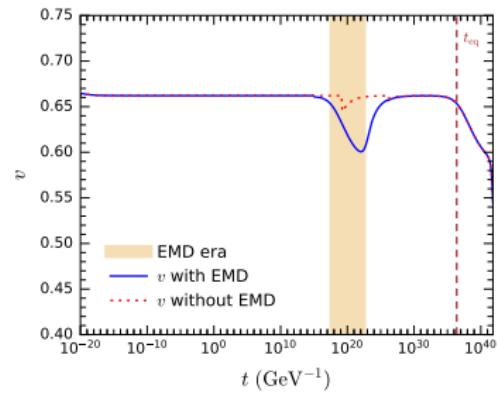
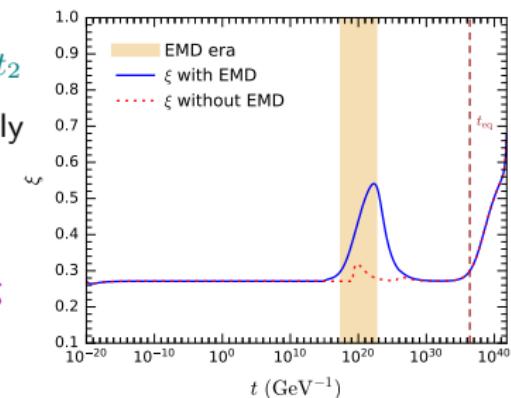
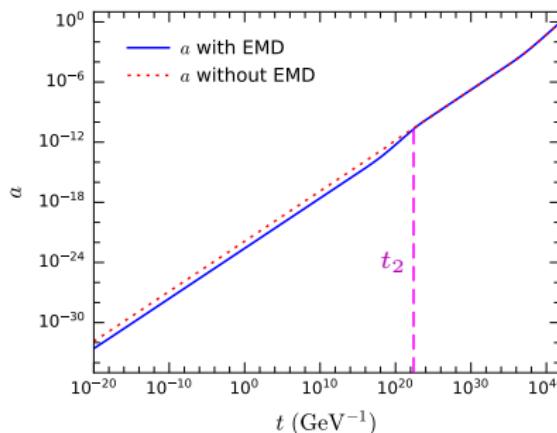


# Impact on the Scale Factor and the VOS Parameters

Compared with the  **$\Lambda$ CDM model**, the presence of the **EMD era** reduces the **scale factor  $a$  before  $t_2$**

$a \propto t^{2/3}$  during an **MD era** increases more rapidly than  $a \propto t^{1/2}$  during an **RD era**, and  $a$  is **smaller** at the **onset** of the **EMD era** to ensure  $a(t_0) = 1$

Moreover, the **EMD era** introduces a **nonscaling effect** to the evolution of the **CS network**



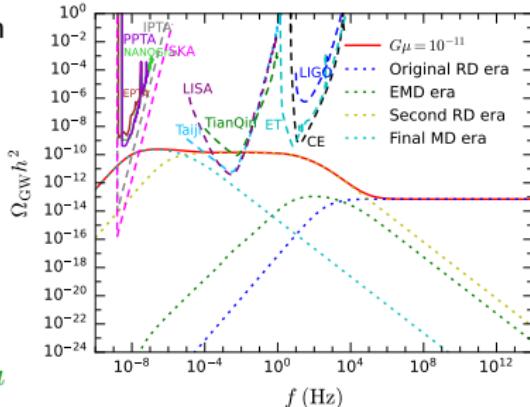
# Imprints in the SGWB spectrum

Affected by the **EMD era**, the SGWB spectrum displays a **suppression** at **high frequencies**

This corresponds to the contributions from CS loops formed in the **original RD** and **EMD eras**

The **lengths** of the generated **CS loops** are **positively correlated** with the **scale factor  $a$**

Since the **EMD era reduces the scale factor  $a$  before  $t_2$** , the CS loops with a given **initial length  $l$** , which is related to the **GW emission frequency** by  $f_e = 2n/l$ , are **formed at a later time**, when the **energy densities** of both CS loops and the emitted GWs are **reduced**



# Imprints in the SGWB spectrum

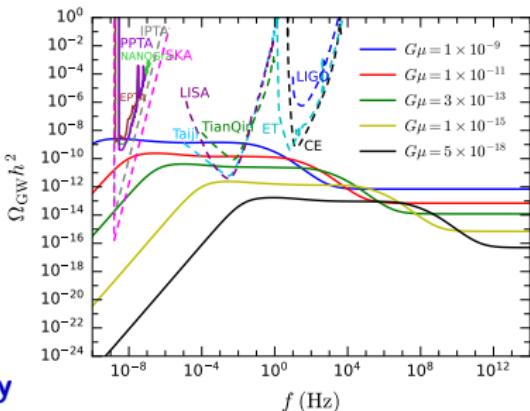
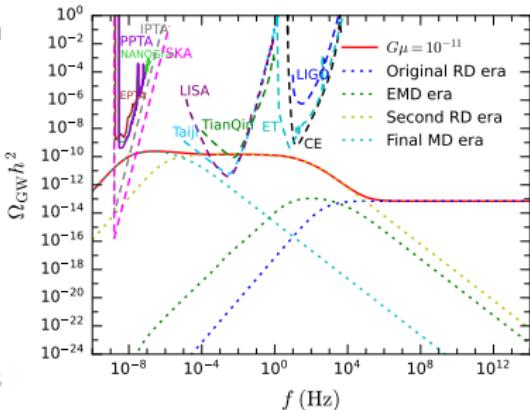
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For a **smaller CS tension**, the **loop lifetime is extended** and the **average length at  $t_2$  is smaller**, causing **suppression** to begin at a **higher frequency**



# Summary

- In the early Universe, the **spontaneous breaking of symmetries** could lead to **topological defects**, such as **domain walls** and **cosmic strings**
- **Cosmic strings** or **collapsing domain walls** may result in a **stochastic GW background**, which could be probed in GW experiments
- We consider **quantum** and **thermal corrections** to the **effective potential** and explore their impact on the **dynamics** of **domain walls** and the resulting **GW signatures**
- We investigate how an **early matter-dominated era** in cosmic history influences the **dynamics** of **cosmic strings** and the produced **GW spectrum**

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Thanks for your attention!

# Friction on the Domain Walls

⚠️ The interaction between a **domain wall** and the  $f$  **fermions** in the **thermal bath** induces **friction** on the wall as it moves in the plasma

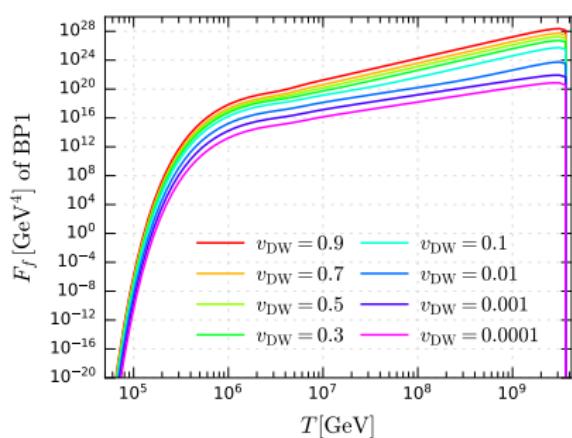
🔍 The **friction force** per unit area exerted on the **DW** is

$$F_f = \frac{2}{\pi^2} \frac{1}{1 - v_{DW}^2} \int_0^{+\infty} \int_{-\infty}^{+\infty} R(p_x) \frac{(p_x - \omega v_{DW})^2}{\omega - p_x v_{DW}} \frac{1}{e^{\omega/T} + 1} p_\perp dp_x dp_\perp$$

◆ The **reflection probability**  $R(p_x)$  can be estimated by considering one-dimensional scattering of a free particle off a step potential

🍰  $F_f$  decreases exponentially due to the **Boltzmann suppression** at low temperatures

🧁 The friction is **negligible** when evaluating the **annihilation temperature**  $T_{\text{ann}}$  for the BPs



# Values of $T_{\text{ann}}$ , $f_{\text{peak}}$ , and $\Omega_{\text{GW}}(f_{\text{peak}})h^2$ for the BPs

	$T_{\text{ann}}$ [GeV]	$f_{\text{peak}}$ [Hz]	$\Omega_{\text{GW}}(f_{\text{peak}})h^2$
BP1	$6.02 \times 10^4$	$1.00 \times 10^{-2}$	$5.77 \times 10^{-10}$
BP1 w/o $f$	$2.00 \times 10^5$	$3.32 \times 10^{-2}$	$4.77 \times 10^{-12}$
BP2	$2.62 \times 10^{-2}$	$2.98 \times 10^{-9}$	$8.36 \times 10^{-11}$
BP2 w/o $f$	$1.77 \times 10^{-2}$	$2.01 \times 10^{-9}$	$4.01 \times 10^{-10}$
BP3	$1.98 \times 10^7$	3.30	$8.77 \times 10^{-9}$
BP3 w/o $f$	$1.90 \times 10^8$	$3.17 \times 10^1$	$1.02 \times 10^{-12}$

# DM Dilution Mechanism

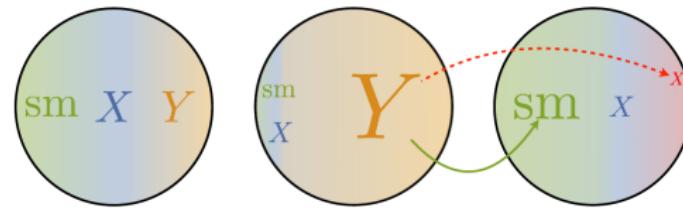
🎯 A **long-lived dilutor**  $Y$  has mass  $m_Y$  **much larger** than  $m_X$  can effectively address the **overproduction problem** of  $X$  particles

↗ First, during the **RD era**, both  $Y$  and  $X$  particles **decouple relativistically** at a similar temperature, resulting in comparable yields,  $Y_Y \simeq Y_X$

⑧ Second, because of  $m_Y \gg m_X$ ,  $Y$  **particles** become **nonrelativistic** at a relatively high temperature, while  $X$  **particles** remain **relativistic**

🎃 Consequently,  $Y$  **particles** quickly **dominate** the energy density of the Universe, initiating an **EMD era**

🎈 Finally, when the **lifetime** of  $Y$  **particles** comes to an end, they **decay** into SM particles and  $X$  particles, **injecting entropy** and consequently **diluting** the **energy density**  $\rho_X$  of  $X$  particles



[Nemevšek & Y Zhang,  
2206.11293, PRL]

# Minimal Left-right Symmetric Model

The **DM candidate** is  $X = N_1$ , and the **dilutor** is  $Y = N_2$ , which undergoes a three-body decay mediated by a **right-handed gauge boson**  $W_R^\pm$  into two charged leptons  $\ell\ell'$  and one  $N_1$

The related **right-handed charged current interactions** are described by

$$\mathcal{L}_1 = \frac{g}{\sqrt{2}} W_R^\mu \left( \sum_{i=1}^2 \bar{N}_i \gamma_\mu V_{\text{PMNS}}^{R\dagger} \ell_R + \bar{u}_R \gamma_\mu V_{\text{CKM}}^R d_R \right) + \text{H.c.}$$

$N_2$  **decay channels** include  $N_2 \rightarrow N_1 \ell\ell'$ ,  $N_2 \rightarrow \ell q\bar{q}'$ , and  $N_2 \rightarrow \ell W$

**Benchmark parameters** used in the previous slides:

$$m_{N_2} = 200 \text{ GeV}, \quad m_{N_1} = 6.5 \text{ keV}, \quad m_{W_R} = 5 \times 10^7 \text{ GeV}, \quad \tan \beta = 0.5$$

$$\Gamma_{N_2} = 2.22 \times 10^{-23} \text{ GeV}, \quad B_X = 4.41 \times 10^{-3}, \quad y = 0.35,$$

$B_X$  is the **branching ratio** of the decay channel  $N_2 \rightarrow N_1 \ell\ell'$

$y$  is the **energy fraction** carried away by the  $X$  particle from the  $Y$  particle

# Effects of the Dilutor Decay Width and Mass

- A smaller dilutor decay width  $\Gamma_Y$  corresponds to a longer duration of the EMD era, leading to stronger suppression effects at high frequencies
- A larger dilutor mass  $m_Y$  implies that the EMD era occurs earlier, and hence a higher frequency at which the suppression of the GW spectrum commences

