The third report

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```
library(simstudy)
## Loading required package: data.table
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:data.table':
##
##
       between, first, last
## The following objects are masked from 'package:stats':
##
       filter, lag
## The following objects are masked from 'package:base':
       intersect, setdiff, setequal, union
##
library(caret)
## Loading required package: lattice
## Loading required package: ggplot2
```

Generate Dataset

```
def <- defData(varname = "mu1", dist = "nonrandom", formula = 5, id = "idnum")
def <- defData(def,varname = "mu2", dist = "nonrandom", formula = 2, id = "idnum")
def <- defData(def,varname = "mu3", dist = "nonrandom", formula = 3, id = "idnum")
def <- defData(def,varname = "mu4", dist = "nonrandom", formula = 4, id = "idnum")
def <- defData(def,varname = "x0", dist = "nonrandom", formula = 1, id = "idnum")
def <- defData(def,varname = "x1", formula = "mu1", variance=1)
def <- defData(def,varname = "x2", formula = "mu2", variance=1)
def <- defData(def,varname = "x3", formula = "mu4", variance=1)
def <- defData(def,varname = "y1", formula = "mu4", variance=1)
def <- defData(def, varname = "y1", formula = "2*x0+4*x3", variance = 1)
def <- defData(def, varname = "y2", formula = "2*x0+4*x3+8*x4", variance = 1)
def <- defData(def, varname = "y3", formula = "2*x0+9*x1+4*x3+8*x4", variance = 1)
def <- defData(def, varname = "y4", formula = "2*x0+9*x1+6*x2+4*x3+8*x4", variance = 1)
def <- defData(def, varname = "y4", formula = "2*x0+9*x1+6*x2+4*x3+8*x4", variance = 1)
def <- defData(def, varname = "y4", formula = "2*x0+9*x1+6*x2+4*x3+8*x4", variance = 1)
def <- defData(def, varname = "y4", formula = "2*x0+9*x1+6*x2+4*x3+8*x4", variance = 1)
def <- defData(def, varname = "y4", formula = "2*x0+9*x1+6*x2+4*x3+8*x4", variance = 1)</pre>
```

This simulation shows that leave-one-out cross validation at least works really well on model selection in this case, in fact, it always chooses the true model (100 out of 100 times) no matter what the true model is. Maybe the reason is that our dataset has only 40 observations. But it kind of doesn't agree with the simulation result in the paper.

leave-one-out cross

```
####sample size=1500
loocv=function(fit){
  h=lm.influence(fit)$h
  mean((residuals(fit)/(1-h))^2)
}
md < -c()
for(i in 1:100){
dt <- genData(1500, def)
fit1 <- lm(y1 \sim x3, data = dt)
fit2 \leftarrow lm(y1 \sim x1+x3, data = dt)
fit3 <- lm(y1 \sim x2+x3, data = dt)
fit4 \leftarrow lm(y1 \sim x3+x4, data = dt)
fit5 <- lm(y1 \sim x1+x2+x3, data = dt)
fit6 <- lm(y1 \sim x1+x3+x4, data = dt)
fit7 <- lm(y1 ~ x2+x3+x4, data = dt)
fit8 <- lm(y1 \sim x1+x2+x3+x4, data = dt)
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4),loocv(fit5),loocv(fit6),loocv(fit7),loocv(fit8))
md<-c(md, which.min(a))</pre>
table(md)
## md
## 1 2 3 4 5 6 7
## 75 8 6 4 1 2 4
md < -c()
for(i in 1:100){
 dt <- genData(1500, def)
fit1 <- lm(y2 \sim x3+x4, data = dt)
fit2 <- lm(y2 ~ x1+x3+x4, data = dt)
fit3 <- lm(y2 \sim x2+x3+x4, data = dt)
fit4 \leftarrow lm(y2 \sim x1+x2+x3+x4, data = dt)
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4))</pre>
md<-c(md, which.min(a))
table(md)
```

md

```
## 1 2 3 4
## 74 11 14 1
md < -c()
for(i in 1:100){
  dt <- genData(1500, def)
fit1 <- lm(y3 \sim x3+x4, data = dt)
fit2 <- lm(y3 \sim x1+x3+x4, data = dt)
fit3 <- lm(y3 \sim x2+x3+x4, data = dt)
fit4 <- lm(y3 ~ x1+x2+x3+x4, data = dt)
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4))</pre>
md<-c(md, which.min(a))</pre>
table(md)
## md
## 2 4
## 83 17
md < -c()
for(i in 1:100){
dt <- genData(1500, def)
fit1 <- lm(y4 \sim x1+x2+x4, data = dt)
fit2 <- lm(y4 ~ x1+x3+x4, data = dt)
fit3 <- lm(y4 \sim x2+x3+x4, data = dt)
fit4 \leftarrow lm(y4 \sim x1+x2+x3+x4, data = dt)
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4))</pre>
md<-c(md, which.min(a))
}
table(md)
## md
##
## 100
####sample size=1000
loocv=function(fit){
  h=lm.influence(fit)$h
  mean((residuals(fit)/(1-h))^2)
}
md < -c()
for(i in 1:100){
dt <- genData(1000, def)
fit1 <- lm(y1 \sim x3, data = dt)
```

```
fit2 <- lm(y1 \sim x1+x3, data = dt)
fit3 <- lm(y1 \sim x2+x3, data = dt)
fit4 <- lm(y1 \sim x3+x4, data = dt)
fit5 <- lm(y1 \sim x1+x2+x3, data = dt)
fit6 <- lm(y1 \sim x1+x3+x4, data = dt)
fit7 <- lm(y1 ~ x2+x3+x4, data = dt)
fit8 <- lm(y1 \sim x1+x2+x3+x4, data = dt)
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4),loocv(fit5),loocv(fit6),loocv(fit7),loocv(fit8))
md<-c(md,which.min(a))
table(md)
## md
## 1 2 3 4 5 7
## 59 7 14 14 3 3
md < -c()
for(i in 1:100){
 dt <- genData(1000, def)
fit1 <- lm(y2 \sim x3+x4, data = dt)
fit2 <- lm(y2 \sim x1+x3+x4, data = dt)
fit3 <- lm(y2 \sim x2+x3+x4, data = dt)
fit4 \leftarrow lm(y2 \sim x1+x2+x3+x4, data = dt)
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4))
md<-c(md, which.min(a))
table(md)
## md
## 1 2 3 4
## 69 17 11 3
md < -c()
for(i in 1:100){
 dt <- genData(1000, def)
fit1 \leftarrow lm(y3 \sim x3+x4, data = dt)
fit2 <- lm(y3 ~ x1+x3+x4, data = dt)
fit3 <- lm(y3 \sim x2+x3+x4, data = dt)
fit4 \leftarrow lm(y3 \sim x1+x2+x3+x4, data = dt)
```

```
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4))</pre>
md<-c(md,which.min(a))
table(md)
## md
## 2 4
## 84 16
md < -c()
for(i in 1:100){
 dt <- genData(1500, def)
fit1 <- lm(y4 \sim x1+x2+x4, data = dt)
fit2 <- lm(y4 \sim x1+x3+x4, data = dt)
fit3 <- lm(y4 \sim x2+x3+x4, data = dt)
fit4 <- lm(y4 ~ x1+x2+x3+x4, data = dt)
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4))</pre>
md<-c(md, which.min(a))
}
table(md)
## md
##
## 100
sample size=40 1000 simulations
loocv=function(fit){
  h=lm.influence(fit)$h
  mean((residuals(fit)/(1-h))^2)
}
md1 < -c()
for(i in 1:1000){
dt <- genData(40, def)</pre>
fit1 \leftarrow lm(y1 \sim x3, data = dt)
fit2 \leftarrow lm(y1 \sim x1+x3, data = dt)
fit3 <- lm(y1 \sim x2+x3, data = dt)
fit4 <- lm(y1 \sim x3+x4, data = dt)
fit5 <- lm(y1 \sim x1+x2+x3, data = dt)
fit6 <- lm(y1 \sim x1+x3+x4, data = dt)
fit7 <- lm(y1 ~ x2+x3+x4, data = dt)
```

```
fit8 <- lm(y1 \sim x1+x2+x3+x4, data = dt)
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4),loocv(fit5),loocv(fit6),loocv(fit7),loocv(fit8))
md1<-c(md1,which.min(a))
table(md1)
## md1
## 1 2 3 4 5 6
## 589 111 114 110 17 22 31
md2 < -c()
for(i in 1:1000){
 dt <- genData(40, def)
fit1 <- lm(y2 \sim x3+x4, data = dt)
fit2 <- lm(y2 \sim x1+x3+x4, data = dt)
fit3 <- lm(y2 \sim x2+x3+x4, data = dt)
fit4 <- lm(y2 ~ x1+x2+x3+x4, data = dt)
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4))
md2<-c(md2,which.min(a))
table(md2)
## md2
         2 3
## 691 142 143 24
md3<-c()
for(i in 1:1000){
 dt <- genData(40, def)
fit1 <- lm(y3 \sim x3+x4, data = dt)
fit2 <- lm(y3 ~ x1+x3+x4, data = dt)
fit3 <- lm(y3 \sim x2+x3+x4, data = dt)
fit4 <- lm(y3 \sim x1+x2+x3+x4, data = dt)
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4))</pre>
md3<-c(md3,which.min(a))
}
table(md3)
## md3
##
   2
## 803 197
```

```
md4<-c()
for(i in 1:1000){
 dt <- genData(40, def)</pre>
fit1 <- lm(y4 \sim x1+x2+x4, data = dt)
fit2 <- lm(y4 ~ x1+x3+x4, data = dt)
fit3 <- lm(y4 \sim x2+x3+x4, data = dt)
fit4 \leftarrow lm(y4 \sim x1+x2+x3+x4, data = dt)
a<-c(loocv(fit1),loocv(fit2),loocv(fit3),loocv(fit4))</pre>
md4<-c(md4,which.min(a))
}
table(md4)
## md4
## 1000
table(md1)
## md1
        2 3 4 5 6
                            7
                                  8
## 589 111 114 110 17 22 31
table(md2)
## md2
## 1 2 3 4
## 691 142 143 24
table(md3)
## md3
## 2 4
## 803 197
table(md4)
## md4
## 4
## 1000
####MCCV
fitControl <-
trainControl(
 method = "LGOCV",
  p = 0.375
)
md1<-c()
for(i in 1:100){
dt <- genData(40, def)</pre>
fit1 \leftarrow train(y1 \sim x3, data = dt,
            method="lm",
```

```
trControl = trainControl(method = "LGOCV",p = 0.375))
fit2 \leftarrow train(y1 ~ x1+x3, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit3 \leftarrow train(y1 ~ x2+x3, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit4 \leftarrow train(y1 \sim x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit5 \leftarrow train(y1 ~ x1+x2+x3, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit6 <- train(y1 \sim x1+x3+x4, data = dt,
              method="lm",
               trControl = trainControl(method = "LGOCV",p = 0.375))
fit7 <- train(y1 \sim x2+x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit8 \leftarrow train(y1 ~ x1+x2+x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
a<-c(fit1$results$RMSE,fit2$results$RMSE,fit3$results$RMSE,
     fit4$results$RMSE,fit5$results$RMSE,fit6$results$RMSE,
     fit7$results$RMSE,fit8$results$RMSE)
md1<-c(md1,which.min(a))
}
table(md1)
## md1
## 1 2 3 4 7
## 66 12 11 9 2
md2 < -c()
for(i in 1:100){
dt <- genData(40, def)</pre>
fit1 <- train(y2 \sim x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit2 <- train(y2 ~ x1+x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
```

```
fit3 <- train(y2 \sim x2+x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit4 <- train(y2 \sim x1+x2+x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
a<-c(fit1$results$RMSE,fit2$results$RMSE,fit3$results$RMSE,
     fit4$results$RMSE)
md2<-c(md2,which.min(a))
}
table(md2)
## md2
## 1 2 3 4
## 70 13 13 4
md3 < -c()
for(i in 1:100){
dt <- genData(40, def)</pre>
fit1 <- train(y3 \sim x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit2 <- train(y3 \sim x1+x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit3 \leftarrow train(y3 ~ x2+x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit4 \leftarrow train(y3 ~ x1+x2+x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
a<-c(fit1$results$RMSE,fit2$results$RMSE,fit3$results$RMSE,
     fit4$results$RMSE)
md3<-c(md3,which.min(a))
}
table(md3)
## md3
## 2 4
## 87 13
md4 < -c()
for(i in 1:100){
dt <- genData(40, def)
fit1 <- train(y4 \sim x1+x2+x4, data = dt,
```

```
method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit2 <- train(y4 \sim x1+x3+x4, data = dt,
              method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit3 <- train(y4 \sim x2+x3+x4, data = dt,
             method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
fit4 <- train(y4 ~ x1+x2+x3+x4, data = dt,
             method="lm",
              trControl = trainControl(method = "LGOCV",p = 0.375))
a<-c(fit1$results$RMSE,fit2$results$RMSE,fit3$results$RMSE,
     fit4$results$RMSE)
md4<-c(md4,which.min(a))
}
table(md4)
## md4
## 4
## 100
table(md1)
## md1
## 1 2 3 4 7
## 66 12 11 9 2
table(md2)
## md2
## 1 2 3 4
## 70 13 13 4
table(md3)
## md3
## 2 4
## 87 13
table(md4)
## md4
## 4
## 100
```