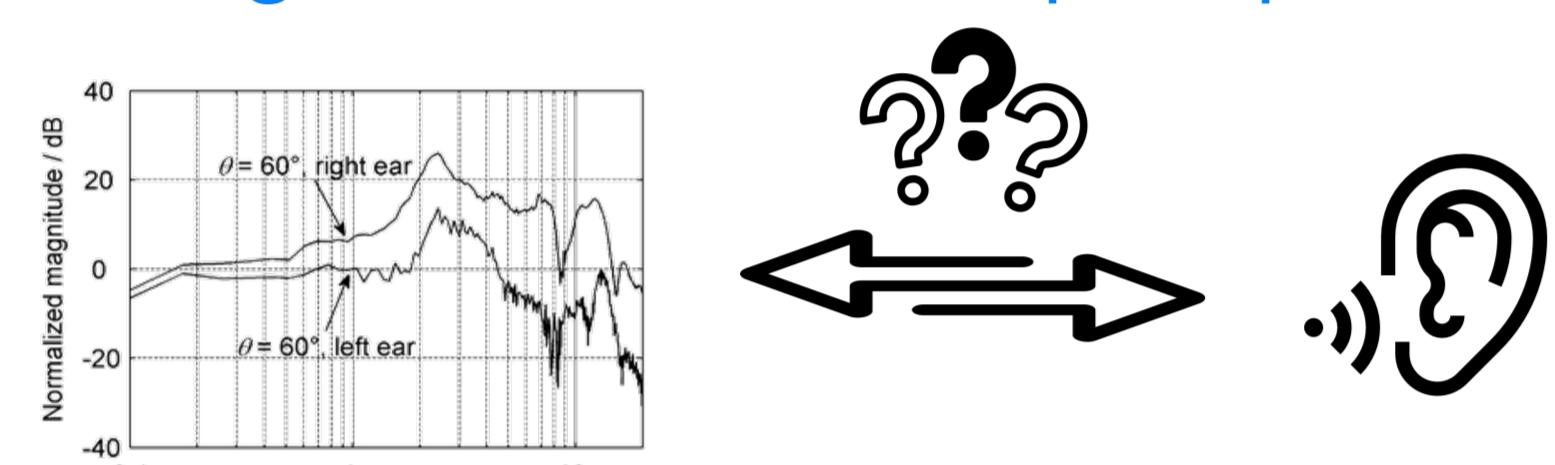


## TL;DR

Beyond spectral reconstruction, we learn a perception-informed HRTF latent space by preserving perceptual relations among HRTFs.

### Research question:

- We investigate: how well do existing learned HRTF representations preserve perceptual relations.
- We improve: the latent HRTF representations to align them with human perception.



### Proposed solution:

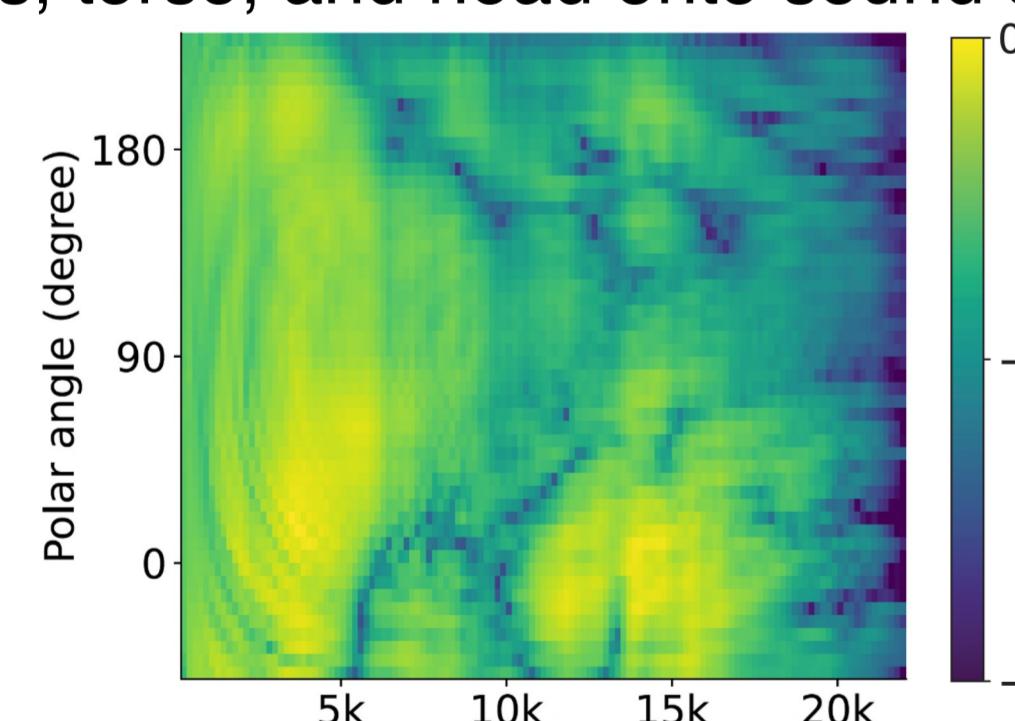
- Perceptual metric-based loss function
- Supervision via Metric Multidimensional Scaling (MMDS)

### Application:

HRTF personalization

## PRELIMINARIES

**Head-related transfer functions (HRTFs)** are a set of functions of **frequency** at different **azimuth** and **elevation** angles, describing the **spatial filtering effect** of the ears, torso, and head onto sound sources.



### Spectral distance: Spectral Difference Error (SDE)

$$SDE_k(H, \hat{H}) = \frac{1}{L} \sum_{\theta, \phi} \left| 20 \cdot \log_{10} \left( \frac{H(\theta, \phi, k)}{\hat{H}(\theta, \phi, k)} \right) \right|$$

### Computational Auditory Modeling

- **Coloration**: Predicted Binaural Coloration (PBC) [1]
- **Externalization**: Auditory Externalization Perception (AEP) [2]
- **Localization**: Difference of Root Mean Square Error in Polar Angles (DRMSP) [3]

### Pearson Correlation

$$\rho_{A,B} = \frac{\mathbb{E}[(A - \mu_A)(B - \mu_B)]}{\sigma_A \sigma_B}$$

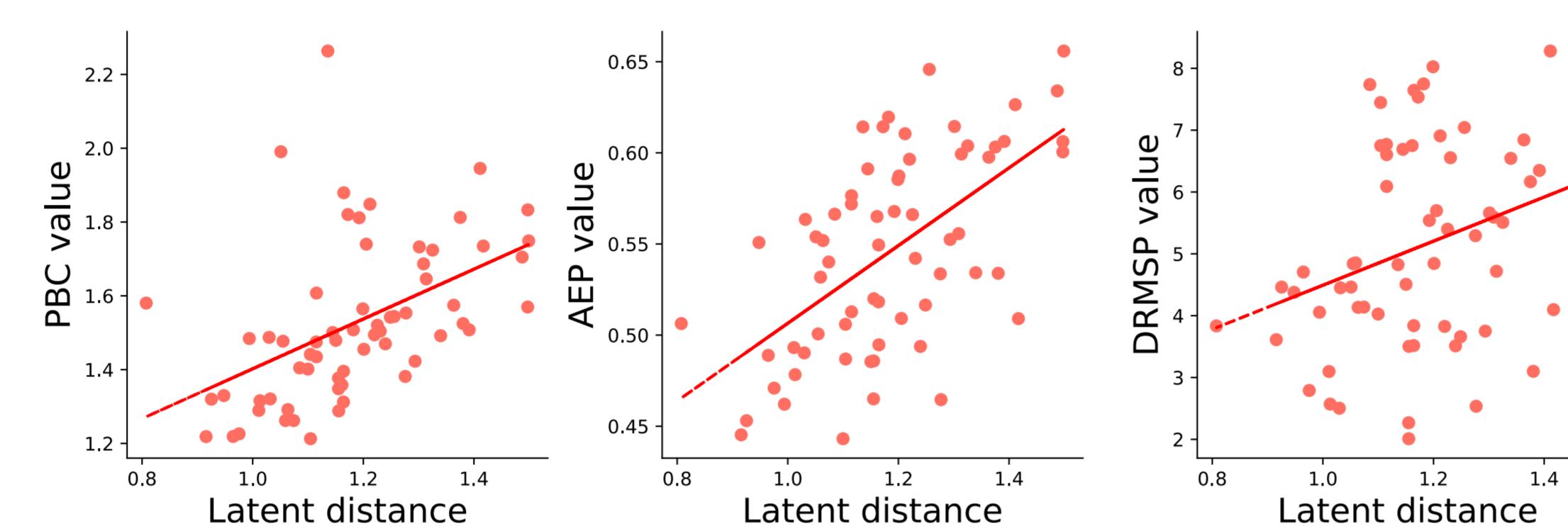
## CASE STUDY: Do Existing Learned HRTF Representations Preserve Perceptual Relations?

**Dataset:** SS2 HRTF dataset [4]

- Setup:**
- 1) Learning with spectral reconstruction
  - 2) Compute pairwise latent distance across subjects
  - 3) Compute pairwise perceptual distance across subjects

### Correlation between latent space and the perceptual metrics

Model: Implicit Neural Representations; Anchor: one subject



### Pearson correlation results for three perceptual metrics

Models	Partitions	PBC	AEP	DRMSP
Convolutional Autoencoder [5]	train	0.60±0.11	0.71±0.08	0.43±0.13
	test	-0.15±0.21	0.07±0.31	-0.10±0.27
Implicit Neural Representations [6]	train	0.60±0.09	0.60±0.14	0.40±0.15
	test	0.71±0.22	0.55±0.23	0.41±0.27
Correlation with SDE:		0.78	0.73	0.37

Minimizing spectral distance leads to limited perceptual correlation.

## EXPERIMENTS: Improving Latent Representation Alignment with Perception-Informed Space

Comparing Pearson correlation and reconstruction error for the proposed methods and the baseline.  
PBC metric; Both losses applied; SS2 dataset

Methods	Pearson Correlation ↑		Reconstruction Error		
	Ground-truth (GT)	Reconstructed	SDE (dB) ↓	PBC ↓	
train	test	train	test	train	test
Proposed Baseline	$L_2 + L_{\text{Align}} + L_{\text{PBC}}$	0.93±0.02	0.80±0.14	0.95±0.01	0.86±0.13
	$L_2$	0.60±0.09	0.71±0.22	0.78±0.06	0.80±0.14
Ablation study	$L_2 + L_{\text{Align}}$	0.96±0.01	0.78±0.14	0.87±0.04	0.82±0.13
	$L_2 + L_{\text{PBC}}$	0.64±0.10	0.71±0.21	0.77±0.08	0.83±0.17

- Our proposed method achieves better alignment with perception-informed space.
- The perceptual correlation learned in training transfer to test subjects (unseen).
- $L_{\text{Align}}$  and  $L_{\text{PBC}}$  complement each other, and MMDS supervision ( $L_{\text{Align}}$ ) dominates.

### AEP / DRMSP metric; MMDS supervision loss; SS2 dataset

Methods	Pearson correlation ↑		SDE (dB) ↓		
	train GT	test GT	train	test	
AEP	$L_2 + L_{\text{Align}}$	0.76±0.09	0.67±0.16	1.09	1.65
	$L_2$	0.60±0.14	0.55±0.23	0.82	1.51
DRMSP	$L_2 + L_{\text{Align}}$	0.96±0.02	0.70±0.20	0.91	1.74
	$L_2$	0.40±0.15	0.41±0.27	0.82	1.51

- Our proposed correlation improvement method generalizes to externalization and localization.

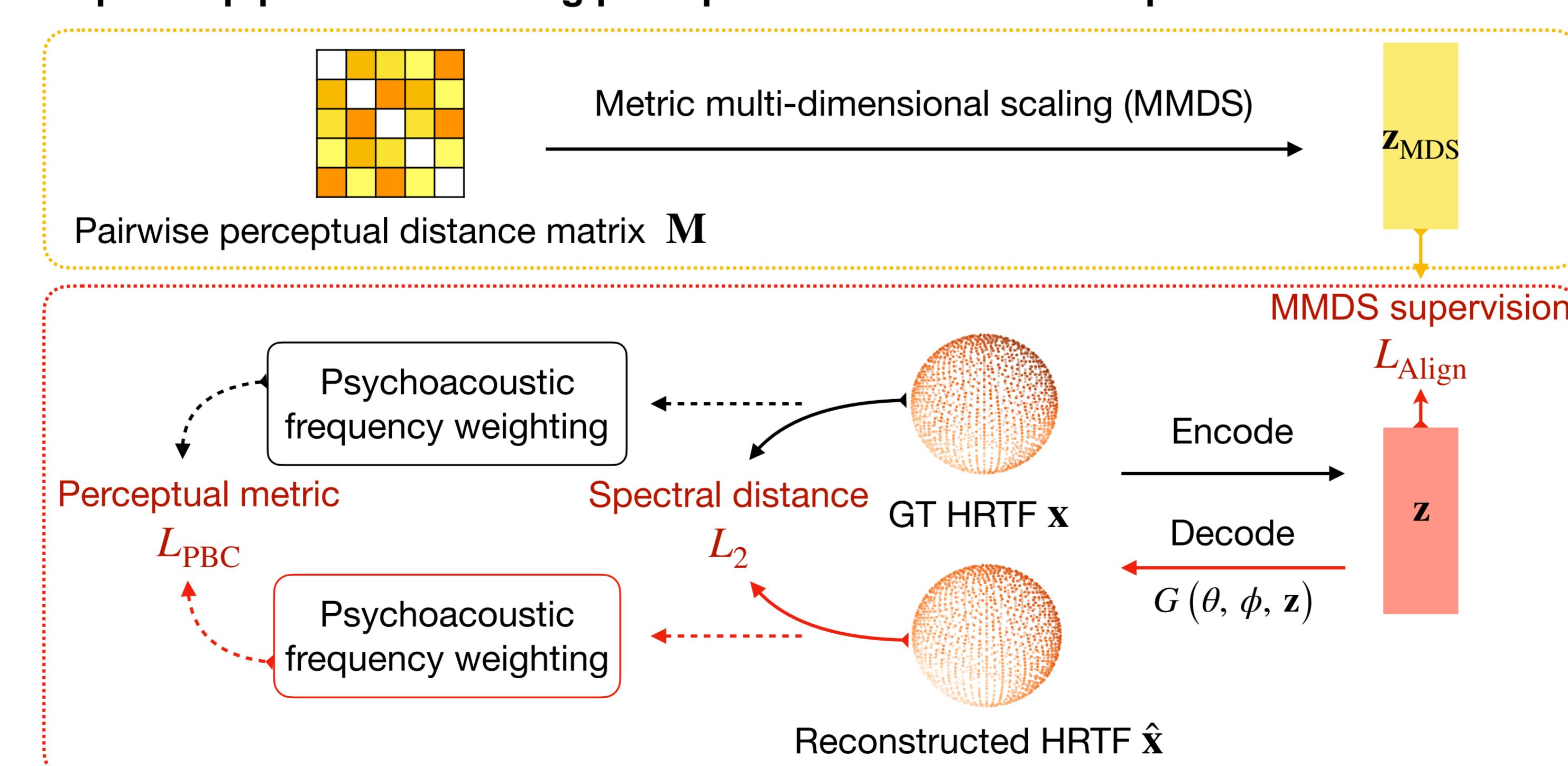
### PBC metric; Both losses applied; HUTUBS dataset

Methods	Pearson correlation ↑		SDE (dB) ↓	
	train GT	test GT	train	test
$L_2 + L_{\text{Align}} + L_{\text{PBC}}$	0.98±0.01	0.71±0.13	0.29	1.60
	0.58±0.12	0.62±0.14	0.42	1.45

- Our proposed correlation improvement method generalizes to HUTUBS dataset.

## METHOD: Aligning with Perception-Informed Space

### Proposed pipeline of learning perception-informed HRTF representations



### Loss functions

$$L = L_2 + \alpha L_{\text{Align}} + \beta L_{\text{PBC}}$$

### PBC loss (only when the metrics is differentiable)

$$L_{\text{PBC}} = \text{PBC}(x, \hat{x})$$

### Metric Multidimensional Scaling (MMDS) supervision (can be applied to every metric)

$$L_{\text{Align}} = \|z - z_{\text{MDS}}\|_2$$

## APPLICATION: Personalized HRTF Selection

For each of the test (unseen) subjects, we select the nearest HRTFs from the training subjects, based on the learned latent representations.

Methods	Best candidate		Top 5 candidates		
	Metrics ↓	SDE (dB) ↓	Metrics ↓	SDE (dB) ↓	
PBC	$L_2 + L_{\text{Align}} + L_{\text{PBC}}$	1.21	2.11	1.31	2.17
	$L_2$	1.30	2.07	1.38	2.19
AEP	$L_2 + L_{\text{Align}}$	0.49	2.17	0.50	2.27
	$L_2$	0.48	2.07	0.51	2.19
DRMSP	$L_2 + L_{\text{Align}}$	3.20	2.12	3.61	2.26
	$L_2$	4.21	2.07	4.42	2.19

HRTFs selected by our methods consistently yield lower perceptual distances.

## REFERENCES

- [1] McKenzie, Thomas, et al. "Predicting the colouration between binaural signals." *Applied Sciences* 2022.
- [2] Baumgartner, Robert, and Piotr Majdak. "Decision making in auditory externalization perception: model predictions for static conditions." *Acta Acustica* 2021.
- [3] Barumerli, Roberto, et al. "A Bayesian model for human directional localization of broadband static sound sources." *Acta Acustica* 2023.
- [4] Warnecke, Michaela, et al. "Sound Sphere 2: A high-resolution HRTF database." *AES AVAR* 2024.
- [5] Zhao, Jiale, Dingding Yao, and Junfeng Li. "Head-Related Transfer Function Upsampling With Spatial Extrapolation Features." *IEEE TASLP* 2025.
- [6] Zhang, You, Yuxiang Wang, and Zhiyao Duan. "HRTF field: Unifying measured HRTF magnitude representation with neural fields." *IEEE ICASSP* 2023.

