Named Arguments as Intersections, Optional Arguments as Unions

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Syntax of λ_{iu} (target)

Types $A, B ::= \top \mid \bot \mid \mathbf{Null} \mid \mathbb{Z} \mid A \to B \mid \{\ell : A\} \mid A \land B \mid A \lor B$ Expressions $e ::= \{\} \mid \mathbf{null} \mid n \mid x \mid \lambda x : A. \ e : B \mid e_1 \ e_2 \mid \{\ell = e\} \mid e.\ell \mid e_1, e_2 \mid e.\ell \mid e_1, e_2 \mid e.\ell \mid$

switch e_0 as x case $A \Rightarrow e_1$ case $B \Rightarrow e_2 \mid letin \ e$

Let-in bindings $letin ::= let x = e in \mid letin_1 \circ letin_2 \mid id$

Syntax of UAENA¹ (source)

Types $\mathcal{A},\mathcal{B}::=\mathbb{Z}\mid\mathcal{A}\rightarrow\mathcal{B}\mid\{\mathcal{P}\}\rightarrow\mathcal{B}\mid\{\mathcal{K}\}$

Named parameter types $\mathcal{P} ::= \ \cdot \ | \ \mathcal{P}; \ \ell : \mathcal{A} \ | \ \mathcal{P}; \ \ell ? : \mathcal{A}$

Named argument types $\mathcal{K} ::= \ \cdot \ | \ \mathcal{K}; \ \ell : \mathcal{A}$

Expressions $\epsilon ::= n \mid x \mid \lambda(x : \mathcal{A}). \; \epsilon \mid \lambda\{\rho\}. \; \epsilon \mid \epsilon_1 \; \epsilon_2 \mid \{\kappa\}$

Named parameters $\rho := \cdot \mid \rho; \ell : \mathcal{A} \mid \rho; \ell = \epsilon$

Named arguments $\kappa := \cdot \mid \kappa; \ell = \epsilon$

¹UAENA = Unnamed Arguments Encoded Named Arguments

From Uaena to λ_{iii}

$$\boxed{\Delta \vdash \epsilon : \mathcal{A} \leadsto e}$$
 (Elaboration)

$$\begin{array}{lll} \text{ELA-Int} & \begin{array}{lll} \text{ELA-Var} \\ \hline \Delta \vdash n : \mathbb{Z} \leadsto n \end{array} & \begin{array}{lll} \text{ELA-Var} \\ \hline x : \mathcal{A} \in \Delta \\ \hline \Delta \vdash x : \mathcal{A} \leadsto x \end{array} & \begin{array}{lll} \text{ELA-Abs} \\ \hline \Delta \vdash \lambda(x : \mathcal{A}) . \ \epsilon : \mathcal{A} \to \mathcal{B} \leadsto \lambda x : |\mathcal{A}|. \ e : |\mathcal{B}| \end{array} \\ \end{array}$$

$$\begin{array}{c} \text{Ela-NField} \\ \Delta \vdash \{\kappa\} : \{\mathcal{K}\} \leadsto e' \\ \Delta \vdash \epsilon : \mathcal{A} \leadsto e \\ \hline \Delta \vdash \{\cdot\} : \{\cdot\} \leadsto \{\} \end{array}$$

$$\Delta \vdash_x \rho : \mathcal{P} \leadsto letin \dashv \Delta'$$
 (Parameter elaboration)

$$\frac{\text{PELA-REQUIRED}}{\Delta \vdash_{x} \cdot : \cdot \rightsquigarrow \mathbf{id} \dashv \Delta} \qquad \frac{\Delta \vdash_{x} \rho : \mathcal{P} \rightsquigarrow letin \dashv \Delta'}{\Delta \vdash_{x} (\rho; \ell : \mathcal{A}) : (\mathcal{P}; \ell : \mathcal{A}) \rightsquigarrow letin \circ \mathbf{let} \ell = x.\ell \mathbf{in} \dashv \Delta', \ell : \mathcal{A}}$$

PELA-OPTIONAL

$$\Delta \vdash_{x} \rho : \mathcal{P} \leadsto letin \dashv \Delta'$$
$$\Delta' \vdash \epsilon : \mathcal{A} \leadsto e$$

 $\overline{\Delta \vdash_x (\rho; \ell = \epsilon) : (\mathcal{P}; \ell? : \mathcal{A})} \rightsquigarrow \overline{letin \circ \mathbf{let} \ell = \mathbf{switch} \, x. \ell \, \mathbf{as} \, y \, \mathbf{case} \, |\mathcal{A}|} \Rightarrow y \, \mathbf{case} \, \mathbf{Null} \Rightarrow e \, \mathbf{in} \, \dashv \, \Delta', \, \ell : \mathcal{A}$

$$\boxed{\Delta \vdash_{e} \mathcal{P} \diamond \mathcal{K} \leadsto e'}$$
 (Parameter matching)

$$\begin{array}{c} \text{PMAT-REQUIRED} \\ \text{PMAT-EMPTY} \\ \hline \Delta \vdash_{e} \cdot \diamond \mathcal{K} \leadsto \{\} \end{array} \begin{array}{c} \mathcal{K} :: \ell \Rightarrow \mathcal{A} \\ \Delta \vdash_{e} \mathcal{P} \diamond \mathcal{K} \leadsto e' \\ \hline \Delta \vdash_{e} (\mathcal{P}; \ell : \mathcal{A}) \diamond \mathcal{K} \leadsto e', \{\ell = e.\ell\} \end{array} \begin{array}{c} \text{PMAT-PRESENT} \\ \mathcal{K} :: \ell \Rightarrow \mathcal{A} \\ \Delta \vdash_{e} \mathcal{P} \diamond \mathcal{K} \leadsto e' \\ \hline \Delta \vdash_{e} (\mathcal{P}; \ell ? : \mathcal{A}) \diamond \mathcal{K} \leadsto e', \{\ell = e.\ell\} \end{array}$$

PMAT-ABSENT
$$\mathcal{K} :: \ell \not\Rightarrow \\
\Delta \vdash_{e} \mathcal{P} \diamond \mathcal{K} \leadsto e' \\
\overline{\Delta} \vdash_{e} (\mathcal{P}; \ell? : \mathcal{A}) \diamond \mathcal{K} \leadsto e'_{g} \{\ell = \mathbf{null}\}$$

$$\mathcal{K} :: \ell \Rightarrow \mathcal{A}$$
 (Successful lookup)

LU-PRESENT
$$\mathcal{K} :: \ell \Rightarrow$$
LU-ABSENT
 $\ell' \neq \ell$ $\mathcal{K} :: \ell \Rightarrow \mathcal{A}$ $(\mathcal{K}; \ell : \mathcal{A}) :: \ell \Rightarrow \mathcal{A}$ $(\mathcal{K}; \ell' : \mathcal{B}) :: \ell \Rightarrow \mathcal{A}$

$$\mathcal{K} :: \ell \Rightarrow$$
 (Failed lookup)

LD-Empty
$$\frac{\ell' \neq \ell \quad \mathcal{K} :: \ell \Rightarrow}{(\mathcal{K}; \ell' : \mathcal{A}) :: \ell \Rightarrow}$$

 $|\mathcal{A}|$ Type translation

$$\begin{split} |\mathbb{Z}| &\equiv \mathbb{Z} \\ |\mathcal{A} \to \mathcal{B}| &\equiv |\mathcal{A}| \to |\mathcal{B}| \\ |\{\mathcal{P}\} \to \mathcal{B}| &\equiv |\mathcal{P}| \to |\mathcal{B}| \\ |\{\mathcal{K}\}| &\equiv |\mathcal{K}| \end{split}$$

 $|\mathcal{P}|$ Parameter type translation

$$\begin{split} |\cdot| &\equiv \top \\ |\mathcal{P}; \, \ell: \mathcal{A}| &\equiv |\mathcal{P}| \wedge \{\ell: |\mathcal{A}|\} \\ |\mathcal{P}; \, \ell?: \mathcal{A}| &\equiv |\mathcal{P}| \wedge \{\ell: |\mathcal{A}| \vee \mathbf{Null}\} \end{split}$$

 $|\mathcal{K}|$ Argument type translation

$$\begin{aligned} |\cdot| &\equiv \top \\ |\mathcal{K}; \, \ell: \mathcal{A}| &\equiv |\mathcal{K}| \wedge \{\ell: |\mathcal{A}|\} \end{aligned}$$

 $|\Delta|$ Typing context translation

$$|\cdot| \equiv \cdot$$

 $|\Delta, x : A| \equiv |\Delta|, x : |A|$

Theorem 1 (Elaboration soundness) If $\Delta \vdash \epsilon : \mathcal{A} \leadsto e$, then $|\Delta| \vdash e : |\mathcal{A}|$.

Example 1

Appendix: Semantics of λ_{iu}

A <: B (Subtyping)

$$\frac{\text{Sub-Top}}{A <: \top} \qquad \frac{\text{Sub-Bot}}{\bot <: A} \qquad \frac{\text{Sub-Null}}{\text{\textbf{Null}} <: \text{\textbf{Null}}} \qquad \frac{\text{Sub-Int}}{\mathbb{Z} <: \mathbb{Z}} \qquad \frac{B_1 <: A_1 \qquad A_2 <: B_2}{A_1 \to A_2 <: B_1 \to B_2}$$

$$\frac{\text{Sub-Rcd}}{A <: B} \underbrace{\frac{\text{Sub-And}}{A <: B \quad A <: C}}_{A <: B \land C} \underbrace{\frac{\text{Sub-AndL}}{A <: C}}_{A \land B <: C} \underbrace{\frac{\text{Sub-AndR}}{B <: C}}_{A \land B <: C} \underbrace{\frac{\text{Sub-Or}}{A \land B <: C}}_{A \land B <: C}$$

SUB-ORL SUB-ORR
$$A <: B$$
 $A <: B \lor C$ $A <: B \lor C$

 $\boxed{\Gamma \vdash e : A}$

$$\frac{\text{Typ-Top}}{\Gamma \vdash \{\} : \top} \qquad \frac{\text{Typ-Null}}{\Gamma \vdash \textbf{null} : \textbf{Null}} \qquad \frac{\text{Typ-Int}}{\Gamma \vdash n : \mathbb{Z}} \qquad \frac{x : A \in \Gamma}{\Gamma \vdash x : A} \qquad \frac{\text{Typ-Abs}}{\Gamma \vdash (\lambda x : A \vdash e : B)} \qquad \frac{\Gamma, x : A \vdash e : B}{\Gamma \vdash (\lambda x : A \cdot e : B) : A \to B}$$

$$\frac{\text{Typ-App}}{\Gamma \vdash e_1 : A \to B} \qquad \frac{\Gamma \vdash e_2 : A}{\Gamma \vdash e_1 e_2 : B} \qquad \frac{\text{Typ-Rcd}}{\Gamma \vdash e : A} \qquad \frac{\Gamma \vdash e : A}{\Gamma \vdash e : A} \qquad \frac{\Gamma \vdash e : \{\ell : A\}}{\Gamma \vdash e : \{\ell : A\}}$$

Typ-Switch

$$\begin{array}{c} \Gamma \vdash e_0 : A \lor B \\ \Gamma, \ x : A \vdash e_1 : C \\ \hline \Gamma \vdash e_1 : A \quad \Gamma \vdash e_2 : B \\ \hline \Gamma \vdash e_1 \circ e_2 : A \land B \end{array} \qquad \begin{array}{c} \Gamma \vdash e_0 : A \lor B \\ \hline \Gamma, \ x : A \vdash e_1 : C \\ \hline \Gamma, \ x : B \vdash e_2 : C \\ \hline \Gamma \vdash \mathbf{switch} \ e_0 \ \mathbf{as} \ x \ \mathbf{case} \ A \Rightarrow e_1 \ \mathbf{case} \ B \Rightarrow e_2 : C \end{array}$$

$$\frac{\text{Typ-Let}}{\Gamma \vdash letin \dashv \Gamma' \qquad \Gamma' \vdash e : A} \qquad \qquad \frac{\text{Typ-Sub}}{\Gamma \vdash e : A \qquad \qquad \frac{\Gamma \vdash e : A}{\Gamma \vdash e : B}}$$

$$\boxed{\Gamma \vdash letin \dashv \Gamma'}$$
(Let-in binding)

$$\begin{array}{ccc} \text{LB-Comp} & & & & & & \\ \Gamma \vdash letin_1 \dashv \Gamma' & & & & \\ \Gamma \vdash letin_2 \dashv \Gamma'' & & & & \\ \hline \Gamma \vdash let x = e \textbf{ in } \dashv \Gamma, \ x : A & & & \hline \Gamma \vdash letin_1 \circ letin_2 \dashv \Gamma'' & & \hline \Gamma \vdash letin_1 \circ letin_2 \dashv \Gamma'' & & \hline \end{array}$$