

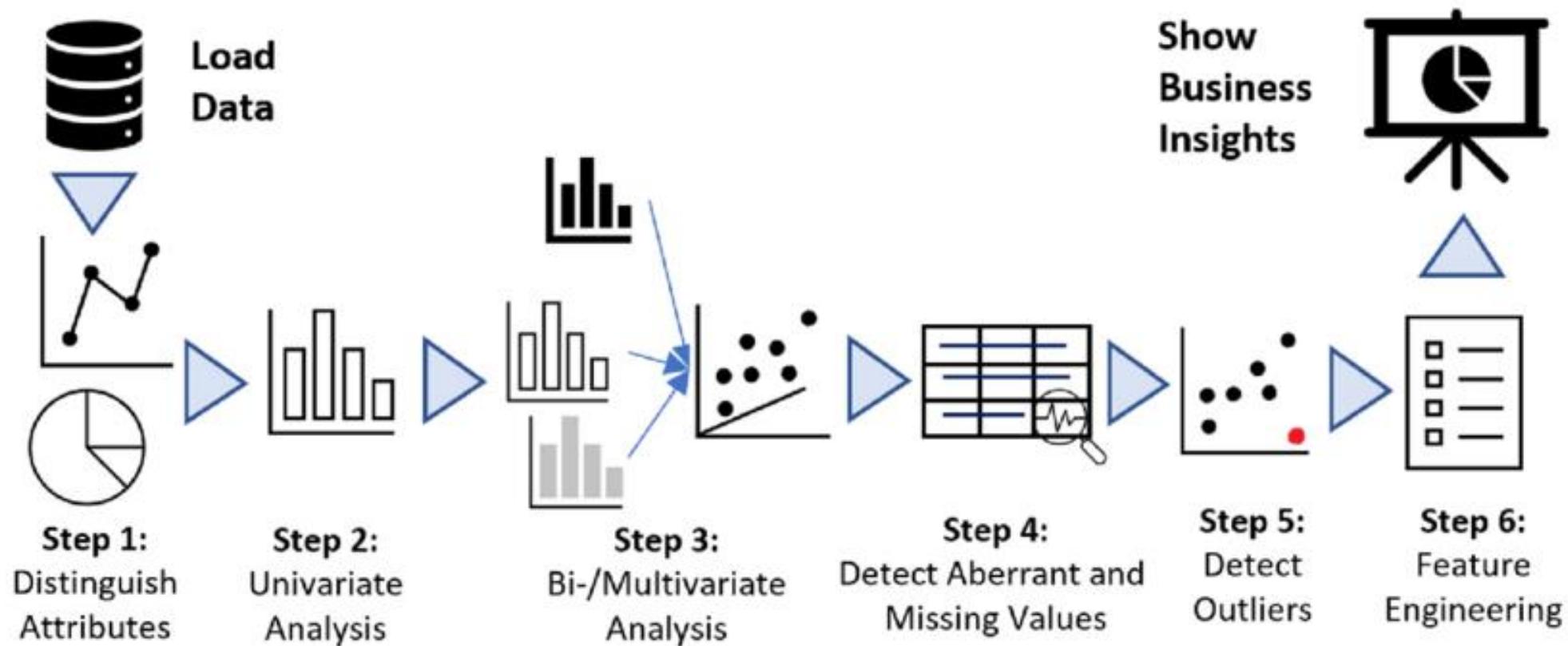
Exploratory Data Analysis

CS 459 Business Intelligence

Summarizing 6-steps of Data Wrangling



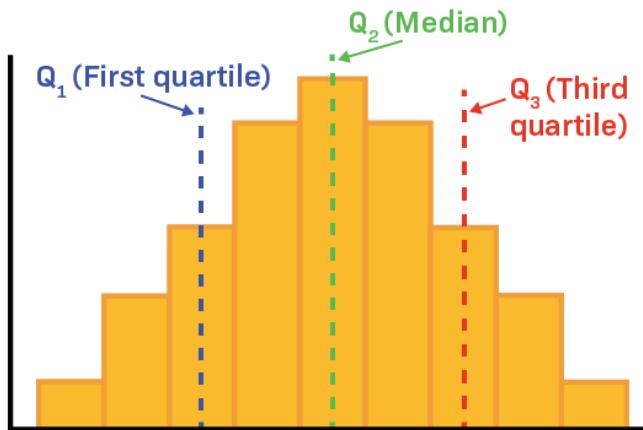
EDA



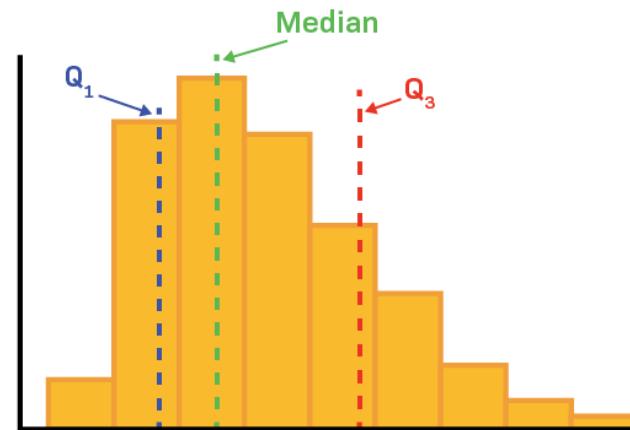
Univariate Analysis

Histograms and Box Plots

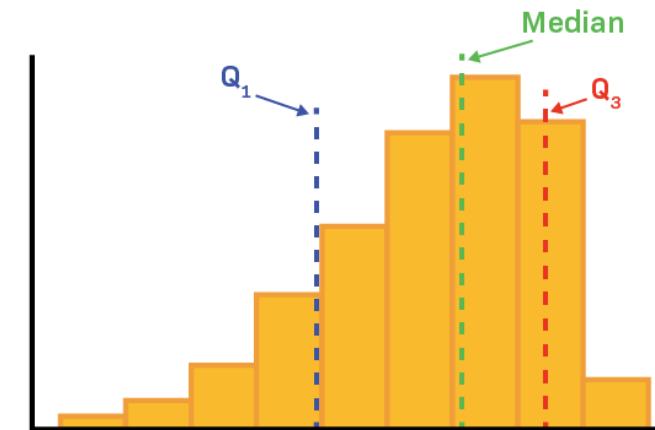
A. Symmetric



B. Right-skewed (or Positive-skewed)



C. Left-skewed (or Negative-skewed)



Multi-Variate Analysis

Bi-variate/ Multivariate Statistical Testing

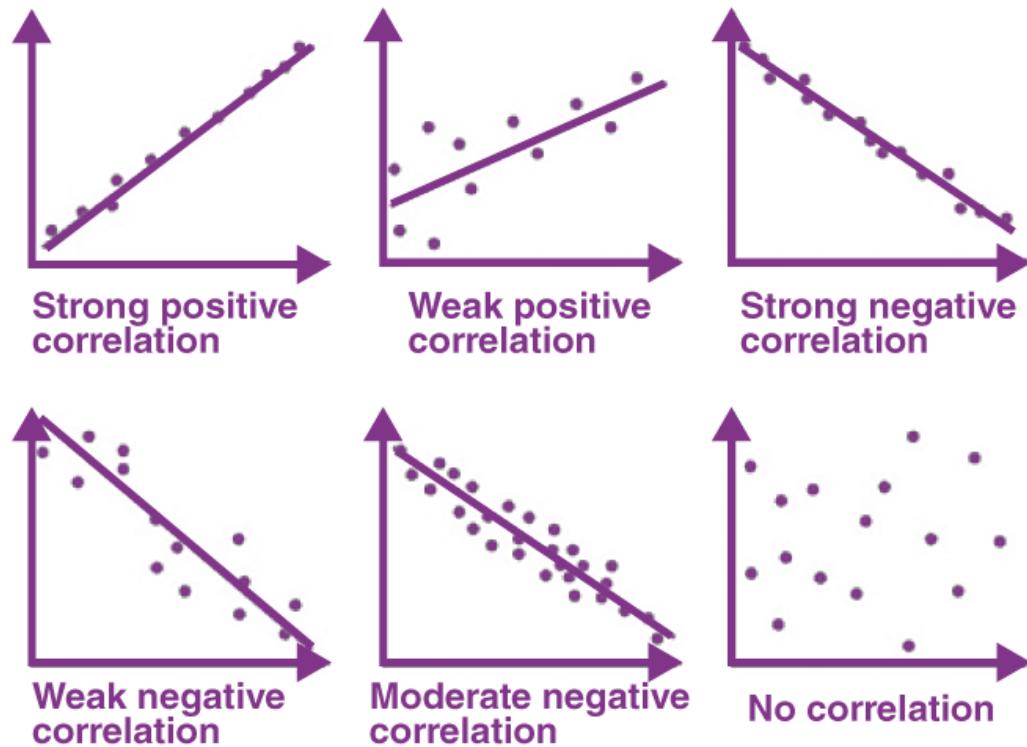
Numerical

Categorical	Numerical	
Categorical	Chi-Square Test	T-test ANOVA
Continuous	Regression	Correlation Test

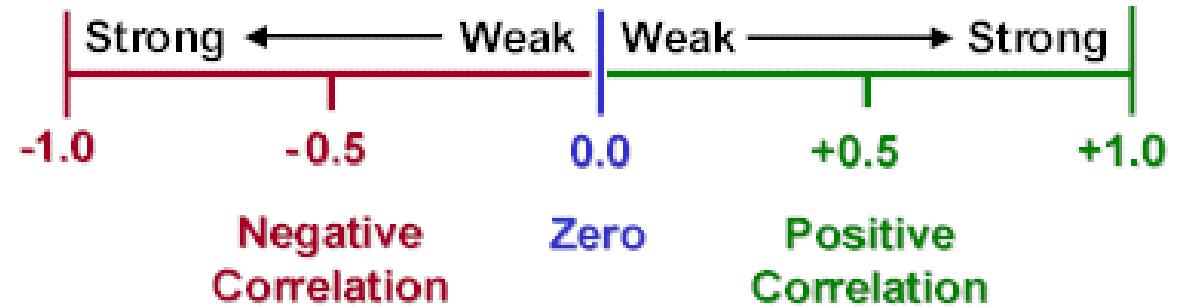
Correlation Testing

- One way to quantify the relationship between two variables is to use the *Pearson correlation* coefficient, which measures the linear association between two variables.
- *Correlation Coefficient*
 - **-1** indicates a perfectly negative linear correlation
 - **0** indicates no linear correlation
 - **1** indicates a perfectly positive linear correlation

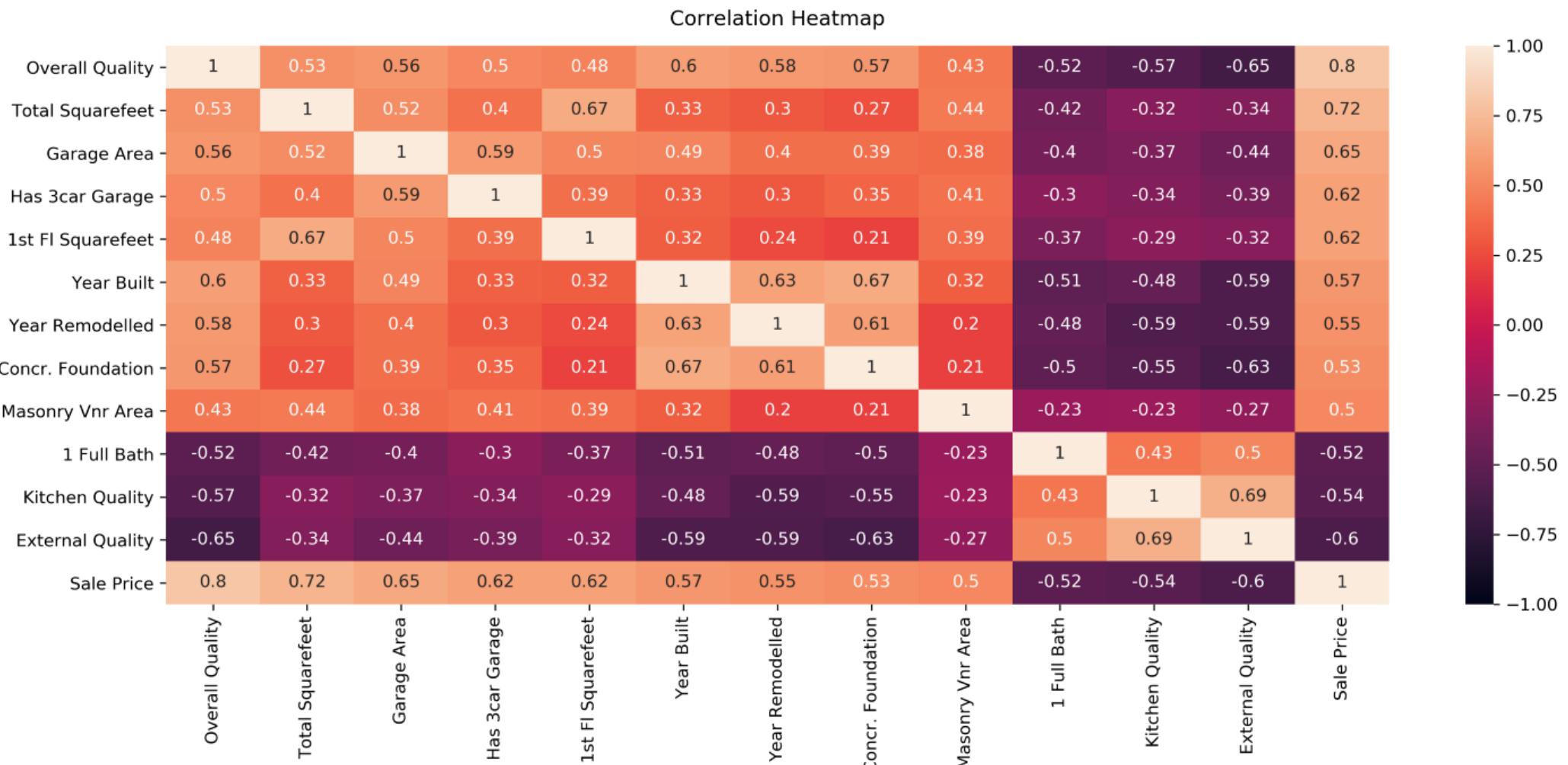
Correlation Analysis



Correlation Coefficient
Shows Strength & Direction of Correlation



Correlation heat map

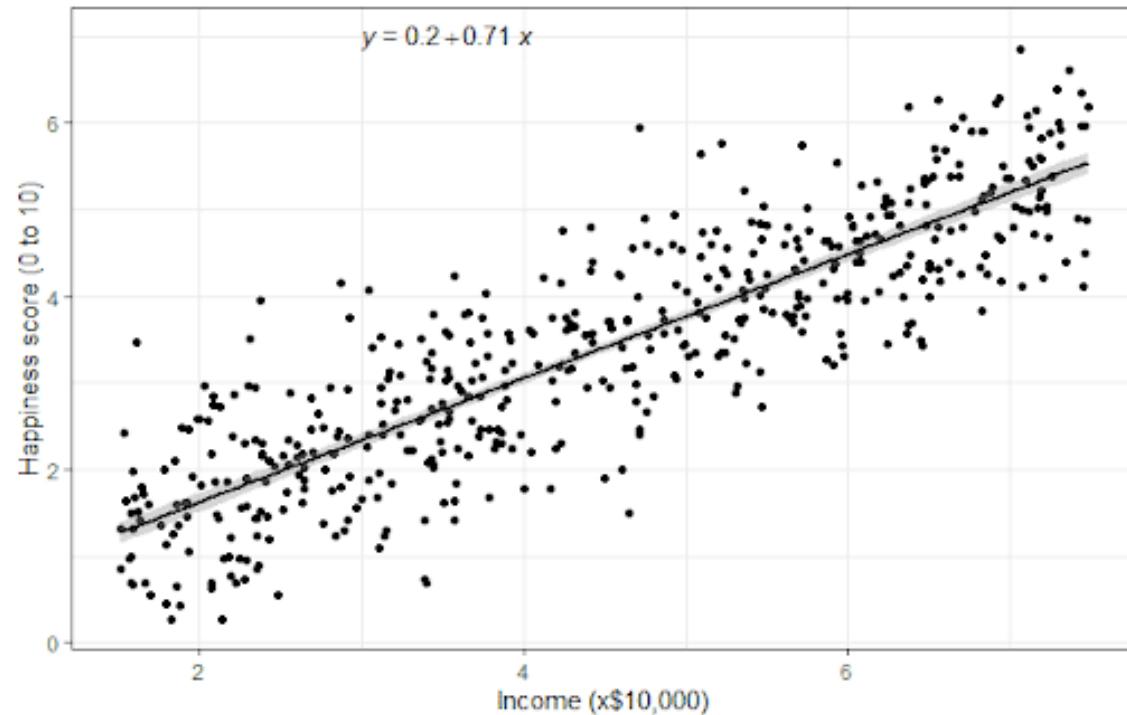


P-value in Hypothesis Testing

- The **p-value** indicates the **strength of evidence against a null hypothesis.**
- Smaller p-value → Stronger evidence against the null hypothesis
- The commonly used threshold (α) is **0.05 (5%)**.
- **If p-value < 0.05:** Reject the null hypothesis and **accept the alternative hypothesis.**
- **If p-value ≥ 0.05: Fail to reject** the null hypothesis (not enough evidence to accept the alternative hypothesis).

Regression

Reported happiness as a function of income



- In statistical modeling, regression analysis is a set of statistical processes for estimating the relationships between a **dependent variable** and **one or more independent variables**.

Regression

- **Linear Regression:**

- Used when the dependent variable is numerical.
- Example: Predicting house prices based on size and location.

- **Logistic Regression:**

- Used when the dependent variable (target) is categorical.
- Example:
 - Predicting whether an email is spam (1) or not (0).
 - Determining if a tumor is malignant (1) or benign (0).

Interpreting Results

R-square value:

- This means that **76.67%** of the variation in the response variable can be explained by the two predictor variables in the model.

```
from sklearn.linear_model import LinearRegression

#initiate linear regression model
model = LinearRegression()

#define predictor and response variables
X, y = df[['x1', 'x2']], df.y

#fit regression model
model.fit(X, y)

#display regression coefficients and R-squared value of model
print(model.intercept_, model.coef_, model.score(X, y))

70.4828205704 [ 5.7945 -1.1576] 0.766742556527
```

$$y = 70.48 + 5.79x_1 - 1.16x_2$$

```

import statsmodels.api as sm

#define response variable
y = df['y']

#define predictor variables
x = df[['x1', 'x2']]

#add constant to predictor variables
x = sm.add_constant(x)

#fit linear regression model
model = sm.OLS(y, x).fit()

#view model summary
print(model.summary())

```

P-value for each variable can also be computed. This gives the statistical significance of each variable when p value is less than 0.05.

OLS Regression Results						
Dep. Variable:	y	R-squared:	0.767			
Model:	OLS	Adj. R-squared:	0.708			
Method:	Least Squares	F-statistic:	13.15			
Date:	Fri, 01 Apr 2022	Prob (F-statistic):	0.00296			
Time:	11:10:16	Log-Likelihood:	-31.191			
No. Observations:	11	AIC:	68.38			
Df Residuals:	8	BIC:	69.57			
Df Model:	2					
Covariance Type:	nonrobust					
	coef	std err	t	P> t	[0.025	0.975]
const	70.4828	3.749	18.803	0.000	61.839	79.127
x1	5.7945	1.132	5.120	0.001	3.185	8.404
x2	-1.1576	1.065	-1.087	0.309	-3.613	1.298
Omnibus:		0.198	Durbin-Watson:			1.240
Prob(Omnibus):		0.906	Jarque-Bera (JB):			0.296
Skew:		-0.242	Prob(JB):			0.862
Kurtosis:		2.359	Cond. No.			10.7

ANOVA - Analysis of Variance

- **ANOVA** is a statistical formula used to compare variances across the means (or average) of different groups.
- A range of scenarios use it to determine if there is any difference between the means of different groups

	fertilizer	weight
1	None	55
2	None	45
3	None	46
4	Biological	64
5	Biological	52
6	Biological	42
7	Chemical	65
8	Chemical	51
9	Chemical	66
10	Chemical	55

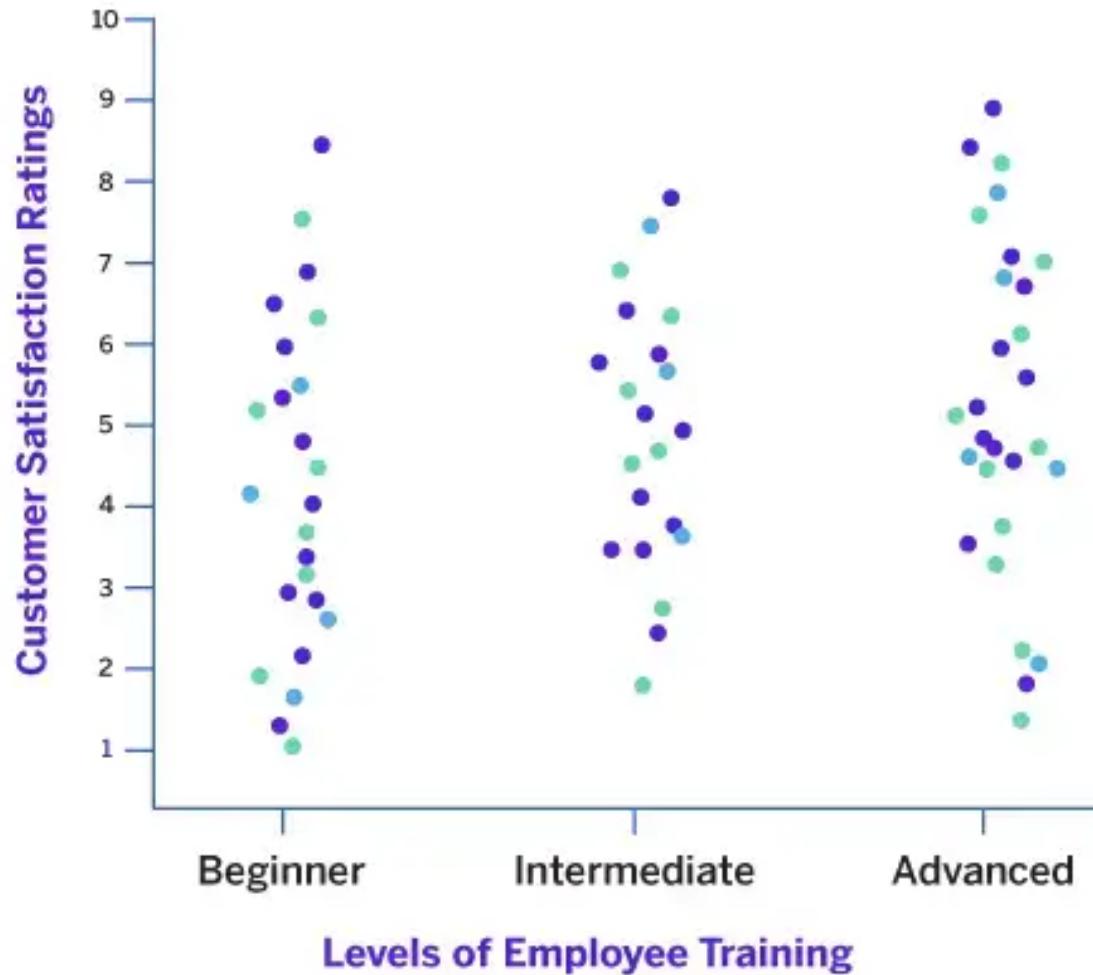
ONE-WAY ANOVA

Population Means Equal?

1 metric outcome variable
3(+) groups of cases

EMPLOYEE TRAINING IMPACT ON CUSTOMER SATISFACTION

qualtrics.^{XM}



Interpreting Results

- A one-way ANOVA uses the following null and alternative hypotheses:
- **H_0 (null hypothesis):** $\mu_1 = \mu_2 = \mu_3 = \dots = \mu_k$
(all the population means are equal)
- **H_1 (alternate hypothesis):** at least one population mean is different from the rest

ANOVA Results

```
from scipy.stats import f_oneway

#perform one-way ANOVA
f_oneway(group1, group2, group3)

(statistic=2.3575, pvalue=0.1138)
```

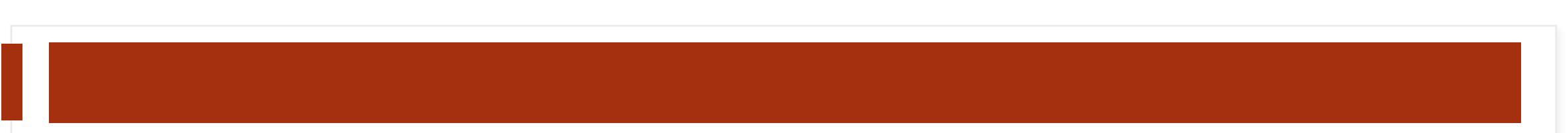
The F test statistic is **2.3575** and the corresponding p-value is **0.1138**.

F-Statistic (Fisher Statistic):

A measure used to test the overall significance of a statistical model by comparing model fit against a baseline model.

- The F-statistic is compared with a critical value or evaluated using the p-value.
- If the **p-value < 0.05**, the model is considered statistically significant (**Reject the null hypothesis**).
- If the **p-value ≥ 0.05**, the model is not statistically significant (**Fail to reject the null hypothesis**).
- **Note:** A large F-statistic generally corresponds to a small p-value, indicating statistical significance.

Head over to
Descriptive Statistics Notebook



Create a Summary Table for the ANOVA Test

Column A	Column B	P-Value	Reject / Fail to Reject	Difference exists / No Difference
Sales	Order Priority	0.22		

Complete Table for ANOVA test

Column A	Column B	P-Value	Reject / Fail to Reject	Difference exists / No Difference
Sales	Order Priority	0.22		
Sales	Ship Mode	0.00		
Sales	Region	0.33		
Sales	Customer Segment	0.63		
Sales	Product Category	4.908931e-168		
Sales	Sub Category	0.00		
Sales	Product Container	0.00		

Tukey Test

- Tukey's test determines the individual means which are significantly different from a set of means.
- Tukey's test is a multiple comparison test and is applicable when there are more than two means being compared (for two means, utilize a t test).
- Typically, Tukey's test is utilized after ANOVA has shown that significant difference exists and this determines where the difference exists.

Interpret ANOVA

```
#enter data for three groups
a = [85, 86, 88, 75, 78, 94, 98, 79, 71, 80]
b = [91, 92, 93, 90, 97, 94, 82, 88, 95, 96]
c = [79, 78, 88, 94, 92, 85, 83, 85, 82, 81]

#perform one-way ANOVA
f_oneway(a, b, c)

F_onewayResult(statistic=5.167774552944481, pvalue=0.012582197136592609)
```

- H₀ : all the population means are equal
- We can see that the overall p-value from the ANOVA table is **0.01258**.

- Since this is less than 0.05, reject null hypothesis which implies that the mean values across each group are not equal.
- Proceed to perform Tukey's Test to determine exactly which group means are different.

Interpreting Tukey

- There is a statistically significant difference between the means of groups *a* and *b* and groups *b* and *c*, but not a statistically significant difference between the means of groups *a* and *c*.

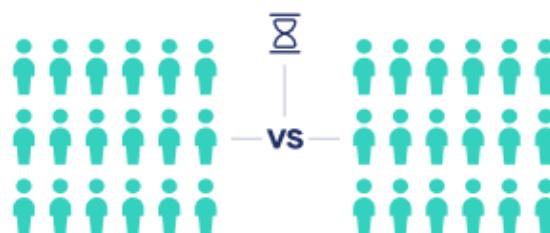
Multiple Comparison of Means - Tukey HSD, FWER=0.05						
group1	group2	meandiff	p-adj	lower	upper	reject

<i>a</i>	<i>b</i>	8.4	0.0158	1.4272	15.3728	True
<i>a</i>	<i>c</i>	1.3	0.8864	-5.6728	8.2728	False
<i>b</i>	<i>c</i>	-7.1	0.0453	-14.0728	-0.1272	True

T-test

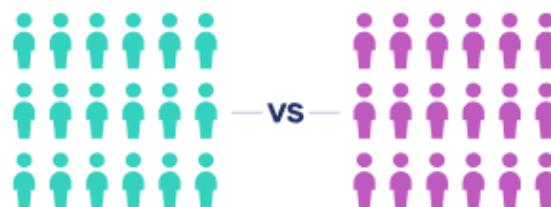
- A t-test is a statistical test that **compares the means of two samples**.
 Null hypothesis: The difference in group means is zero and an alternate hypothesis that the difference in group means is different from zero.

Paired-samples t test



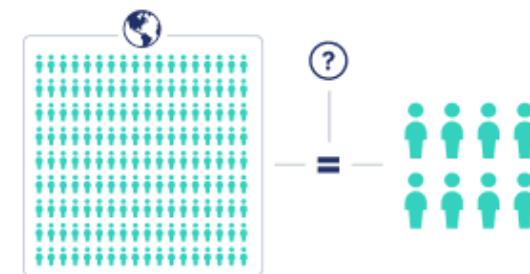
Investigate whether there's a difference within a group between two points in time (within-subjects).

Independent-samples t test



Investigate whether there's a difference between two groups (between-subjects).

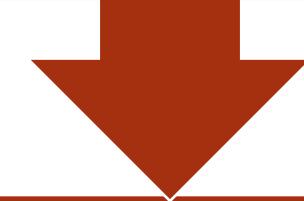
One-sample t test



Investigate whether there's a difference between a group and a standard value or whether a subgroup belongs to a population.

Interpreting Results

Compare **P-value** in the same way.



The **t-value** measures the size of the difference relative to the variation in your sample data. Put another way, T is simply the calculated difference represented in units of standard error. **The greater the magnitude of T, the greater the evidence against the null hypothesis.**

Chi-square

- **Chi-square** is a statistical test used to examine the differences between **categorical variables** from a random sample in order to judge goodness of fit between expected and observed results.
- **Chi-square** is most commonly used by researchers who are studying survey response data because it applies to categorical variables. Demography, consumer and marketing research, political science, and economics are all examples of this type of research
- **Example:** Is gender related to political party preference?



Gender

- Male
- Female

Highest educational level

- Without graduation
- College
- Bachelor's degree
- Master's degree



Gender

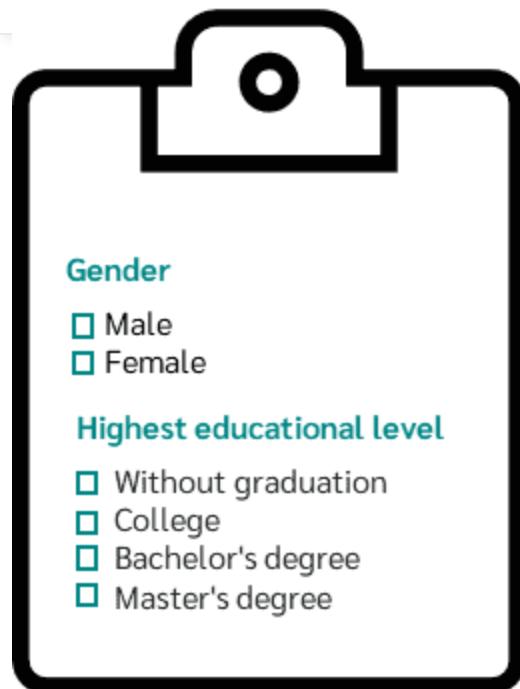
- Male
- Female

Highest educational level

- Without graduation
- College
- Bachelor's degree
- Master's degree



Fall	Gender	Highest educational level
1	Male	College
2	Female	Without graduation
3	Male	Without graduation
4	Male	Bachelor's degree
5	Female	Master's degree
6	Male	Bachelor's degree
7	Female	Master's degree
...



Fall	Gender	Highest educational level
1	Male	College
2	Female	Without graduation
3	Male	Without graduation
4	Male	Bachelor's degree
5	Female	Master's degree
6	Male	Bachelor's degree
7	Female	Master's degree
...



	Female	Male
Without graduation	6	7
College	13	16
Bachelor's degree	16	15
Master's degree	8	11
Total	43	49

Is there a correlation
between gender and the
highest level of education?



Chi²- Test