**Z-Tree**

<http://www.ztreesoft.com>

<http://www.patentsencyclopedia.com/app/20140222870>

This document demonstrates the design and implementation of a new data structure, Z-Tree, key-value mapping. This data structure can also be used to sort millions of strings.

In Z-Tree, all keys will be distinguished by bit values.

**Bit Values**

The following table shows some example keys and their bit values. In this document, the ASCII values instead of the UNICODE values will be used to make the demonstration simple.

|  |  |
| --- | --- |
| **Keys** | **Bit Values** |
| 1 | 00110001 |
| a | 01100001 |
| 2 | 00110010 |
| ab | 01100001 01100010 |
| long key | 01101100 01101111 01101110 01100111 00100000 01101011 01100101 01111001 |

**Z-Tree Components**

Z-Tree includes three kinds of nodes, **Key Node**, **Branch Node** and **Value Node**.

Both **Key Node** and **Branch Node** include a pointer pointing to the **Value Nodes** associated with the key. The **Value Nodes** are optional and may vary in different applications. The **Value Node** will not be discussed in detail in this document.

**Key Node**

**Key Node** represents multiple continuous bits. **Key Node** includes a bit buffer together with the start bit index and the end bit index to represent multiple continuous bits.

**Key Node** also includes a pointer pointing to the child **Key Node** or **Branch Node** and another pointer pointing to the **Value Nodes**. Figure 1 shows a **Key Node** with 6 bits “111011” (the pointer to the **Value Nodes** is not shown). Figure 2 shows the **Key Node** definition in C/C++.

111011

Figure 1: Z-Tree Key Node with 6 bits "111011"

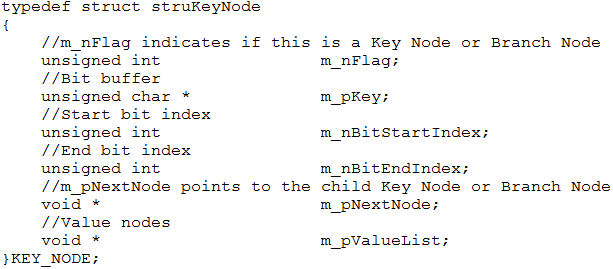


Figure 2: Z-Tree Key Node definition in C/C++

**Branch Node**

**Branch Node** includes two pointers representing bit 0 and bit 1. The first pointer (for bit 0) points to the left child **Key Node** or **Branch Node** andthe second pointer (for bit 1) points to the right child **Key Node** or **Branch Node**. **Branch Node** also includes a pointer pointing to the **Value Nodes**. Figure 3 shows a **Branch Node** (the pointer to the **Value Nodes** is not shown). Figure 4 shows the **Branch Node** definition in C/C++.

0

1

Figure 3: Z-Tree Branch Node

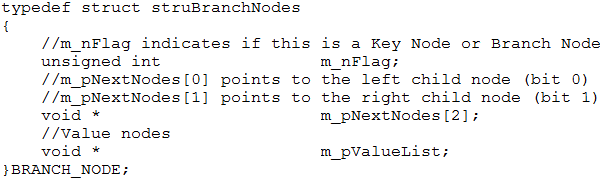


Figure 4: Z-Tree Branch Node definition in C/C++

**Z-Tree Operations**

Z-Tree includes three kinds of operations, adding a key (and associated value) into Z-Tree, finding a key (and associated value) from Z-Tree and traversing Z-Tree to sort over the keys.

Removing a key (and associated value) will not be discussed in this document.

**Add a key (and associated value) into Z-Tree**

When a new key (and associated value) is added into Z-Tree, Z-Tree will perform a loop to compare the bit values of the incoming key and the bit values of the Z-Tree nodes until reaches the end of Z-Tree or the incoming key.

If the current Z-Tree node is a **Branch Node** and the current bit value of the incoming key is 0, Z-tree will go to the left child node.

If the current Z-Tree node is a **Branch Node** and the current bit value of the incoming key is 1, Z-tree will go to the right child node.

If the current Z-Tree node is a **Key Node** and the bit values of the **Key Node** in Z-Tree match the current bit values of the incoming key, Z-tree will go to the child node.

If the current Z-Tree node is a **Key Node** and the bit values of the **Key Node** don't match the current bit values of the incoming key, the **Key Node** in Z-Tree will be split at the first different bit. If the first bit is different, the **Key Node** in Z-Tree will be split into one **Branch Node** and one **Key Node**. If the first different bit is the last bit, the **Key Node** in Z-Tree will be split into one **Key Node** and one **Branch Node**. If the first different bit is in the middle of the Z-Tree **Key Node**, the **Key Node** will be split into one **Key Node**, one **Branch Node** and another **Key Node**. After that, Z-Tree will continue with the loop.

If after reaching the end of the Z-Tree, there is still extra bits in the incoming key, Z-Tree will create a new **Key Node** and append it to the end of Z-Tree.

The value, if there is, will be added to the value list of the last **Key Node** or **Branch Node**.

The time complexity of adding a key (and associated value) is always O (1) because the time complexity depends on the length of bits and is irrelevant to the key number (n).

**Example of adding keys (and associated values) to Z-Tree**

Here are some examples about adding keys (and associated values) to Z-Tree.

Figure 5 shows Z-Tree after adding a key "1" (00110001).

Figure 6 show Z-Tree after adding another key "a" (01100001). Since the second bit is different, the **Key Node** will be split and a **Branch Node** will be inserted at the second bit. Key "1" (00110001) will go to the left child tree (bit 0) and key "a" (01100001) will go to the right child tree (bit 1).

Figure 7 shows Z-Tree after adding another key "2" (00110010). This time the seventh bit is different and will be split.

Figure 8 shows Z-Tree after adding another key "ab" (0110000101100010). A new **Key Node** will be created at the end of Z-Tree.

**00110001**

Figure 5: Z-Tree after adding keys "1" (00110001)

**0**

0

1

**110001**

**100001**

**0**

0

1

**110001**

**100001**

Figure 6: Z-Tree after adding keys "1" (00110001) and "a" (01100001)

**0**

0

1

**1100**

**100001**

0

1

**1**

**0**

Figure 7: Z-Tree after adding keys "1" (00110001), "a" (01100001) and "2" (00110010)

**0**

0

1

**1100**

**100001**

0

1

**1**

**0**

**01100010**

Figure 8: Z-Tree after adding keys "1" (00110001), "a" (01100001), "2" (00110010) and "ab" (0110000101100010)

**2. Find a Key (and associated value) from Z-Tree**

When trying to find a key (and associated value) in Z-Tree. Z-Tree will perform a loop to compare the bit values of the incoming key and the bit values of the Z-Tree nodes until reaches the end of Z-Tree or the incoming key.

If the current Z-Tree node is a **Branch Node** and the current bit value of the incoming key is 0, Z-tree will go to the left child node.

If the current Z-Tree node is a **Branch Node** and the current bit value of the incoming key is 1, Z-tree will go to the right child node.

If the current Z-Tree node is a **Key Node** and the bit values of the **Key Node** match the current bit values of the incoming key, Z-tree will go to the child node.

If the current Z-Tree node is a **Key Node** and the bit values of the **Key Node** don't match the current bit values of the incoming key, Z-tree will return null.

When Z-Tree reaches the end of the incoming key, the value list of the last matching Z-Tree **Key Node** or **Branch Node** will be returned.

The time complexity of finding a key (and associated value) in Z-Tree is always O (1) since there is no collision between the bit values of different keys.

Figure 9 shows how to find a key "1" (and the associated value) in Z-Tree following the bit values of the key "1" (00110001).

**0**

0

1

**1100**

**100001**

0

1

**1**

**0**

**01100010**

Figure 9: Find key "1" (00110001) and the associated values in Z-Tree

**3. Traverse Z-Tree to sort over the keys**

Figure 10 shows that the keys in Z-Tree are already sorted automatically. One can sort over the keys by traversing the **Key Node** and **Branch Node** recursively. The following steps show how to sort over the keys in ascending order.

If the current node has **Value Nodes**, output the values.

If the current node is a **Branch Node**, traverse the left child tree and then traverse the right child tree.

If the current node is a **Key Node** and has a child node, go on to traverse the child tree.

The time complexity of sorting with Z-Tree is O (n) which is the fastest among all sorting algorithms.

**0**

0

1

**1100**

**100001**

0

1

**1**

**0**

**01100010**

Figure 10: The keys in Z-Tree are sorted automatically

**Advantages of Z-Tree**

Z-Tree has many advantages when compared with hash table and other data structures.

1. Z-Tree will distinguish keys by bit values instead of hash code. Since the different keys must have different bit values, there is no collision between different keys. The time complexity of adding/finding a key in Z-Tree is always O (1).
2. Z-Tree can grow automatically. There is no need to worry about the bucket size. By comparison, hash table needs to copy keys/values from one bucket to another bucket when it is growing.
3. Since the keys in Z-Tree are sorted automatically, one can use Z-Tree to sort millions of keys. The time complexity of sorting with Z-Tree is O (n) which is the fastest among all sorting algorithms.
4. When two keys have the same prefix, they can share the same **Key Nodes** and **Branch Nodes** for the prefix. For example, for the two keys, “Hello Tom” and “Hello Jack”, the prefix “Hello ” will be saved in the same **Key Nodes** or **Branch Nodes**. This feature can help to reduce the memory usage. While loading a file into Z-Tree, the memory size allocated for Z-Tree may be even less than the file size. That is why one can use Z-Tree to sort files of several GB.
5. Z-Tree can be used to find all keys started with a prefix conveniently. For example, one can find all keys started with “Hello” in Z-Tree.
6. Z-Tree can also be used to save binary keys and values.