Mathematical Foundations for Computer Vision and Machine Learning

Byung-Woo Hong

Computer Science Department, Chung-Ang University

Jupyter Notebook

- Create a new notebook for Python 3
- Include your name and the student ID in the notebook
- Write python 3 codes for the given assignment
- Try to separate the codes into meaningful blocks
- Write a comment for each block of codes
- Plot the important intermediate results
- Write a short description for each graphical result
- Use LaTeX for mathematical comments in the notebook
- Save the notebook file as assignment08.ipynb
- Download the notebook as a PDF file assignment08.pdf

github

- Start a project or a directory for the assignment08
- Include the link to the giuhub for the assignment in the notebook
- Upload the notebook assignment08.ipynb to the github after the deadline (Note that your github project is visible to public)

Submission to eclass

- Submit the PDF file assignment08.pdf to eclass
- Deadline is 11:59 pm on next Thursday. No extension
- Score ranges from 0 to 5

Score Table

- The results should be correct
- The codes should be written in a modulated way
- The comment should be made for each block of the codes
- The important intermediate results should be presented
- The link to the github project should be included

Build a binary classifier

- Define a linear bi-partitioning function \tilde{f} to classify digit '0' against all the other digits '1', '2', '3', '4', '5', '6', '7', '8', '9' using the training data at MNIST dataset
- Define the classifier $\hat{f}(x) = \operatorname{sign}(\tilde{f}(x))$ using the sign function:

$$sign(x) = \begin{cases} +1 & \text{if } x \ge 0\\ -1 & \text{if } x < 0 \end{cases}$$

■ Evaluate the performance of the classifier \hat{f} using the testing data at MNIST dataset based on TP(True Positive), FP(False Positive), TN(True Negative) and FN(False Negative)

Build a binary classifier

- Let $x=(x_1,x_2,\cdots,x_{784})$ be a vector that represent an image of the size 28×28
- Let f_i be a feature function such tat $f_i : \mathbb{R}^{784} \to \mathbb{R}$:

$$f_i(x) = x_i$$

■ The partitioning function $\tilde{f}: \mathbb{R}^{784} \to \mathbb{R}$ is defined by:

$$\tilde{f}(x;\theta) = \theta_1 f_1(x) + \theta_2 f_2(x) + \dots + \theta_{784} f_{784}(x)$$

where $\theta = (\theta_1, \theta_2, \cdots, \theta_{784})$ denotes the model parameters



Essential Visualisation

- Plot the value of the model parameters $\theta_1, \theta_2, \cdots, \theta_{784}$ in the image form (28×28)
- Present the evaluation value table (TP, FP, TN, FN)
- Plot the average image (28×28) of True Positive
- lacktriangle Plot the average image (28×28) of False Positive
- Plot the average image (28×28) of True Negative
- Plot the average image (28×28) of False Negative