# Z3++ at SMT-COMP 2023

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## 1 Introduction

Z3++ is a derived SMT solver based on Z3-4.8.15[4]. It participates in the Single Query and Model Validation track of QF\_LIA, QF\_IDL, QF\_NIA and QF\_NRA logics.

For solving QF\_LIA, QF\_IDL and QF\_NIA, a local search solver dedicated for integer arithmetic logic is developed, and it is deeply combined with Z3 by exchanging solving information. In the QF\_NRA division, we implement a feasible region consistency checker before the main search, and implement sample-cell projection [3] in the NLSAT. Additionally, we tune the QF\_NRA tactic with a sophisticated flow. We also implemented a local search solver dedicated for it based on the interval-based information [2], and combined it with Z3.

## 2 Features

In this section, we introduce the new features of Z3++ (compared to Z3) on the divisions we mention in this document.

Integer Arithmetic: We developed a novel local search solver called LA-IA for integer arithmetic, including QF\_LIA, QF\_IDL and QF\_NIA. It is an extended version of LS-LIA [1], which is a local search solver for QF\_LIA (including QF\_IDL). LS-IA directly operates on variables, breaking through the traditional framework. We propose a local search framework by considering the distinctions between Boolean and integer variables. Moreover, we design a novel operator and scoring functions, and propose a two-level operation selection heuristic. LS-IA is deeply combined with Z3 by exchanging information between each other.

QF\_NRA: We noticed that the order of variables to be assigned greatly affects the performance on many instances, so we employ different solving flows, mainly including various heuristic arithmetic variable reordering strategies from CAD. Also, as DPLL(T) framework works particularly well for multilinear instances, we extend the time limit of DPLL(T) for such instances.

As for NRA theory solving, we implement sample-cell projection [3] in NL-SAT explain module. Although the new operator is also a CAD-like projection operator which computes the cell (not necessarily cylindrical) containing a given sample such that each polynomial from the problem is sign-invariant on the cell, it is of singly exponential time complexity.

Also we implement a feasible region consistency checker for clauses which are univariate and unit before the main search. The checker obtains the feasible region of variables through real root isolation and continuously takes the intersection of the regions. If the feasible region of some variable becomes empty, it means the instance is unsatisfiable. Otherwise, the obtained feasible regions are added to the instance as lemmas.

Moreover, we implemented a local search algorithm for SMT(QF\_NRA) [2] by considering the interval-based information, and combined it with Z3.

## 3 Webpage

Further information can be found at https://z3-plus-plus.github.io/

#### 4 Contributors

This project is a result of team work. Shaowei Cai launches and leads the Z3++ project. Shaowei Cai (proposing the local search methodology), Bohan Li (main developer) and Xindi Zhang (code review in early stage, and participates in idea discussions) are contributors to integer arithmetic theories (including QF\_IDL, QF\_LIA, QF\_NIA), and the algorithm is a result of many discussions among them. Mengyu Zhao are main developers for the QF\_NRA division, under the supervisions of Shaowei Cai and Bohua Zhan.

#### References

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