





INFORMAZIONE E BIOINGEGNERIA

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Dipartimento di Elettronica, Informazione e Bioingegneria

Computer Graphics



Computer Graphics

 GLSL, Ray tracing and other Rendering techniques

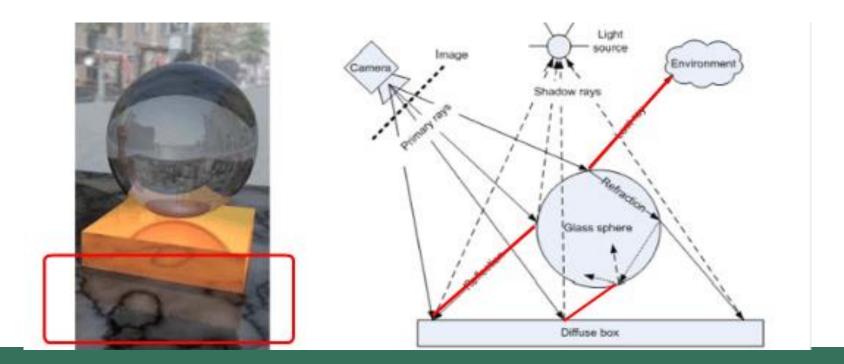
Ray tracing considers for each pixel also the light emitted by other objects in two specific directions: the *mirror reflection* and the *refraction* (for transparent objects).

$$L(x,\omega_r) = L_e(x,\omega_r) + \\ \int L(y,yx)f_r(x,yx,\omega_r)G(x,y)V(x,y)dy$$

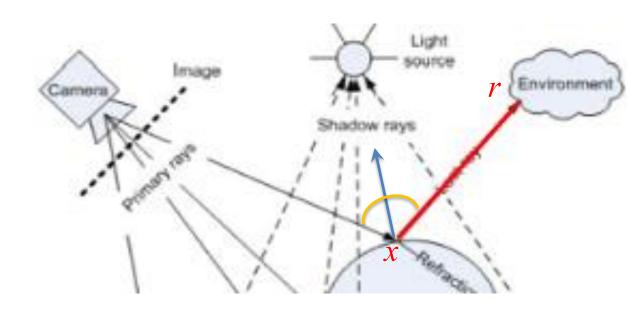
$$L(x,\omega_r) = L_e(x,\omega_r) + \sum_{l} L(l,\overline{lx})f_{r,l}(x,\overline{lx},\omega_r)V(x,l) + \\ \text{Reflection} \qquad \qquad L(r,\overline{rx})f_{r,l}(x,\overline{rx},\omega_r)V(x,r) + \\ L(t,\overline{tx'})f_{t,l}(x',\overline{tx'},\omega_r)V(x,t)$$

For reflection, this direction corresponds to the *mirror direction*: same angle, *but on the other side* with respect to the normal vector of the surface in the hit point.

This allows the reproduction of realistic perfect (mirror) reflections.

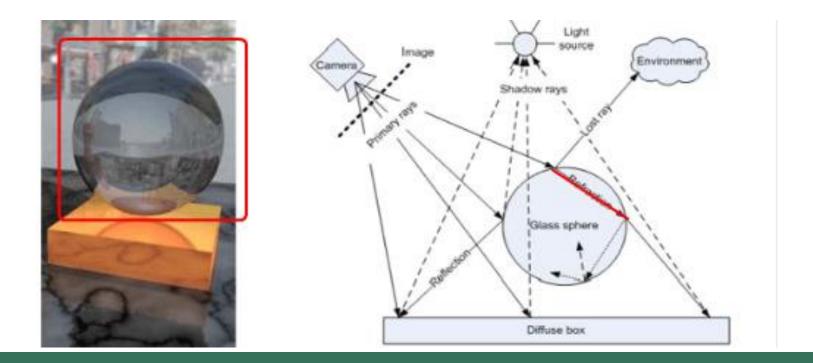


In particular, for each point x, the algorithm looks for the points r on all the objects in the scene, along the mirror direction \overrightarrow{rx} , and selects the one closest to x.



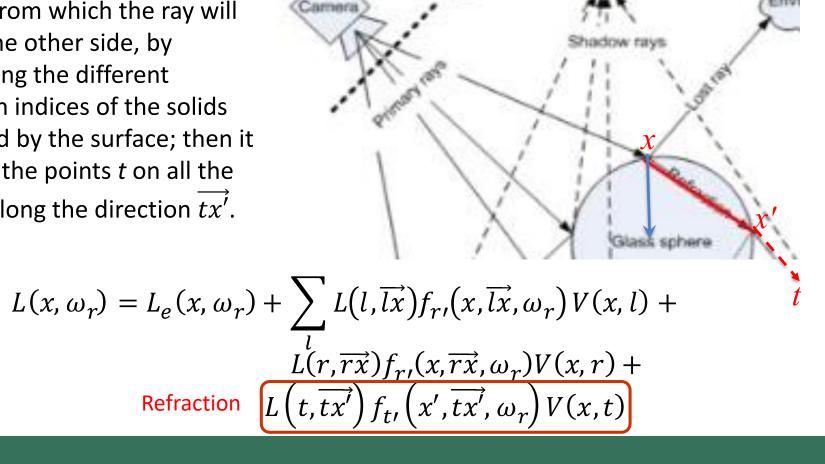
$$\begin{split} L(x,\omega_r) &= L_e(x,\omega_r) + \sum_{l} L(l,\overrightarrow{lx}) f_{r,l}(x,\overrightarrow{lx},\omega_r) V(x,l) + \\ &\text{Reflection} \quad \underbrace{L(r,\overrightarrow{rx}) f_{r,l}(x,\overrightarrow{rx},\omega_r) V(x,r) +}_{L\left(t,\overrightarrow{tx'}\right) f_{t,l}\left(x',\overrightarrow{tx'},\omega_r\right) V(x,t)} \end{split}$$

For refraction, the physical properties of the objects are emulated by considering the *index of refraction* for the material to determine the angle at which the refraction ray is cast.



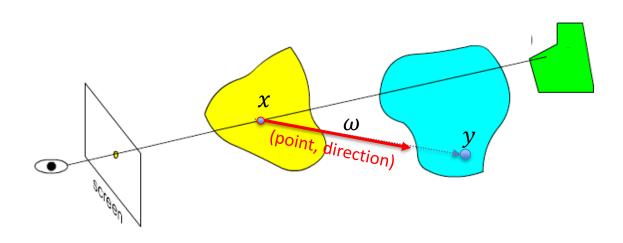
In this case, for each point x, the algorithm first searches for the point x' from which the ray will exit on the other side, by considering the different refraction indices of the solids separated by the surface; then it looks for the points t on all the objects along the direction $\overrightarrow{tx'}$.

Refraction

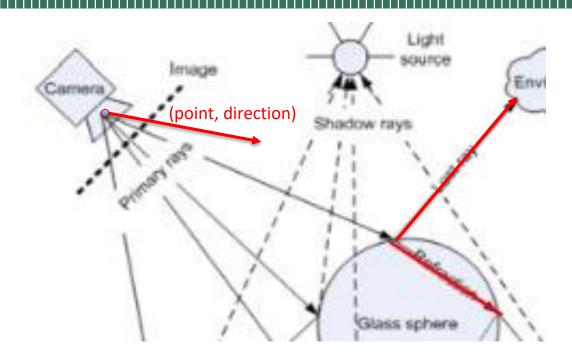


The algorithm relies on a ray-casting procedure that computes the colors seen from a given (point-in-space x, direction ω) couple.

The procedure searches the closest object to point y in the given direction ω , and applies the approximated rendering equation to compute $L(y, \omega)$.



The algorithm starts considering each point on the projection plane (each pixel of the generated image), in the direction of the projection ray, and applies the ray-casting procedure to it.

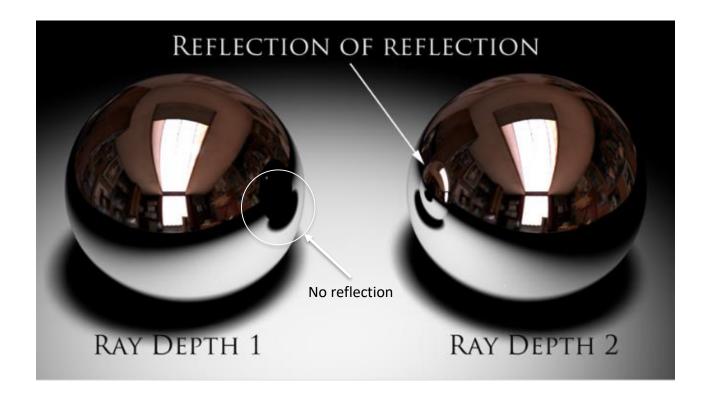


For considering the reflection and refraction part of each pixel, the procedure is called recursively with the computed points and directions.

$$L(x,\omega_r) = L_e(x,\omega_r) + \sum_{t \in \mathcal{L}(t,\overline{tx})} L(t,\overline{tx}) f_{r,t}(x,\overline{tx},\omega_r) V(x,t) + \sum_{t \in \mathcal{L}(t,\overline{tx})} L(t,\overline{tx}) f_{r,t}(x,\overline{rx},\omega_r) V(x,t) + \sum_{t \in \mathcal{L}(t,\overline{tx})} L(t,\overline{tx}) f_{r,t}(x,\overline{rx},\omega_r) V(x,r) + \sum_{t \in \mathcal{L}(t,\overline{tx})} L(t,\overline{tx}) f_{t,t}(x,\overline{tx},\omega_r) V(x,t) + \sum_{t \in \mathcal{L}(t,\overline{tx})} L(t,\overline{tx},\omega_r) V(x,t) + \sum_{t \in \mathcal{$$

refracted from x

The recursion is repeated up to a given number of bounces, called the *ray depth*.



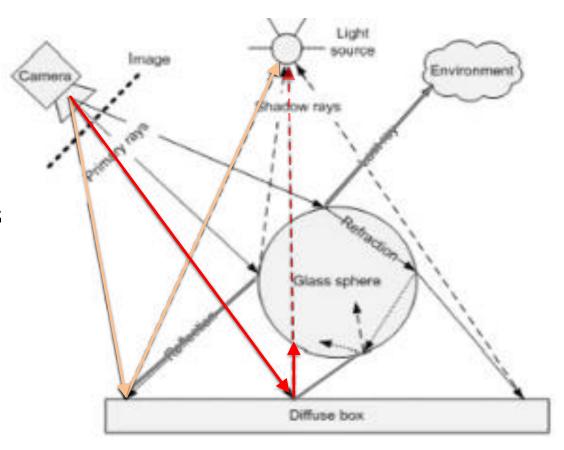
Light sources are still separated from the objects, and the visibility for light sources is also considered. This time however ray tracing is used to determine if a light is visible or not.

$$L(x,\omega_r) = L_e(x,\omega_r) + \\ \int L(y,yx) f_r(x,yx,\omega_r) G(x,y) V(x,y) dy$$

$$L(x,\omega_r) = L_e(x,\omega_r) + \underbrace{\sum_l L(l,\overrightarrow{lx}) f_r(x,\overrightarrow{lx},\omega_r) V(x,l)}_{l} + \\ \text{Reflection} \qquad L(r,\overrightarrow{rx}) f_r(x,\overrightarrow{rx},\omega_r) V(x,r) + \\ \text{Refraction} \qquad L\left(t,\overrightarrow{tx'}\right) f_t(x',\overrightarrow{tx'},\omega_r) V(x,t)$$

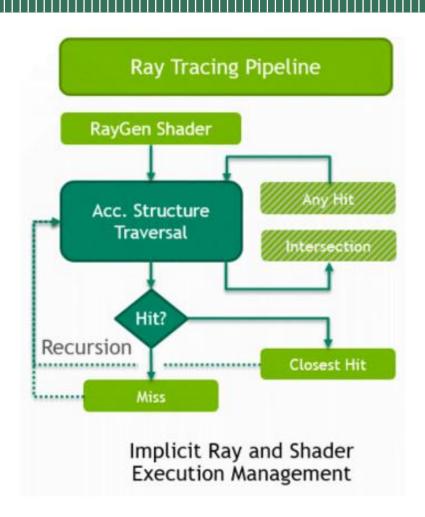
If the reflect ray does not encounter any other object in the direction of the light, then the source is considered.

Otherwise, if it hits another object, the light is considered to be covered, and excluded from the rendering equation.



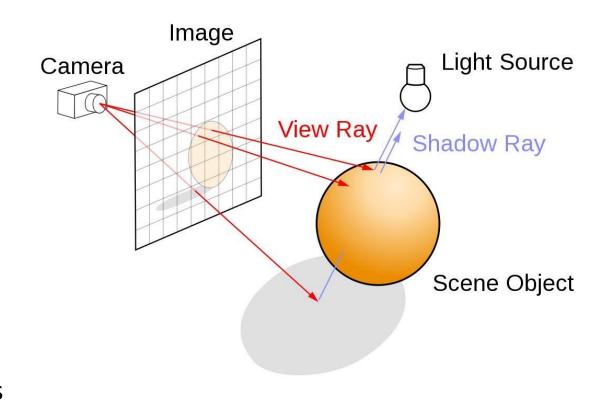
Vulkan and DirectX, have both a specific pipeline to support ray tracing in real time (provided that suitable GPUs are available).

In Vulkan this pipeline is called "the Ray Tracing pipeline".



The ray-tracing pipeline creates images starting from the pixels on screen, and it is not driven by triangles and vertices as the graphic one.

For each fragment on the screen, a ray is cast into the scene, and it is intersected with all the triangles of all the meshes in the 3D environment.

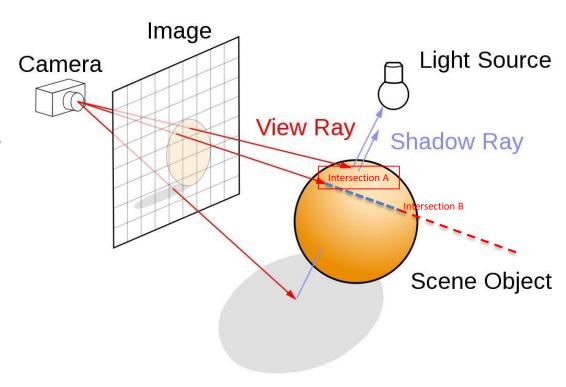


Only the intersection closer to the viewer is considered.

In order to compute its color, extra rays are traced to accurately reproduce reflections and refraction (transparencies).

For the ray-tracing rendering technique just presented, these rays are generally:

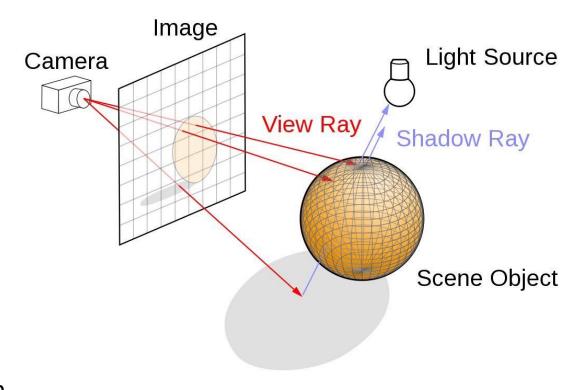
- The perfect reflection ray
- The refraction ray
- The rays connecting the point to the light sources



Determining the intersection with all the triangles in the scene is not a simple task: without special care, it can have complexity o(n) in the number of triangles.

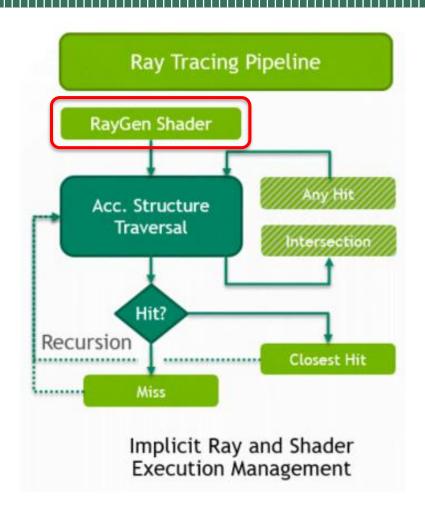
In order to cope with this complexity, special acceleration structures must be provided by the user.

For time constraints we will not be able to present them in depth.

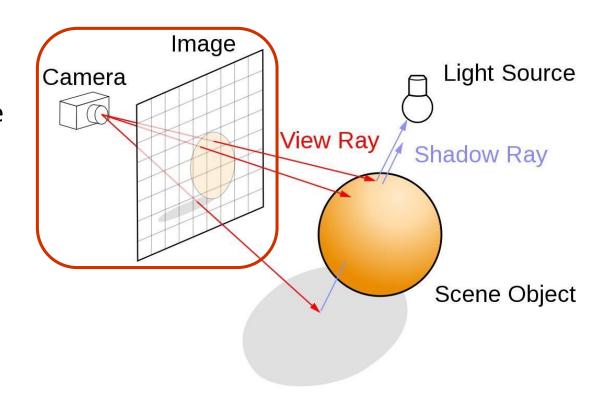


The ray-tracing pipeline requires five shaders to compute and handle all the triangle-ray intersections.

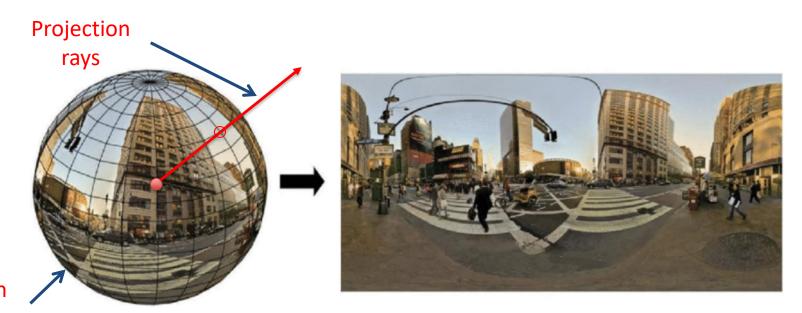
The RayGen shader is executed for each output fragment of the images, and it must determine the starting point and the direction of the corresponding ray in the scene.



It generally just considers each pixel on screen, and cast a ray according to the direction that starts from the camera.



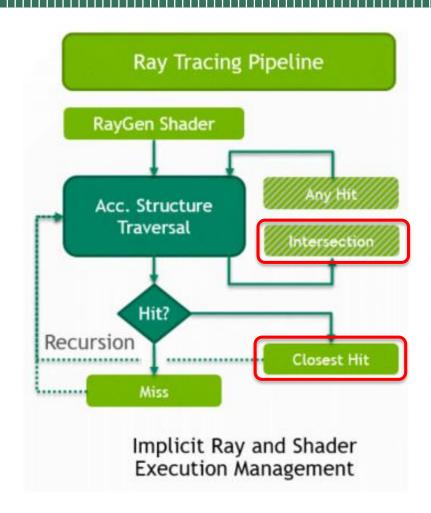
However, user is not constrained to consider a planar projection plane with equally-spaced pixels: cylindrical and spherical projections can be easily implemented by minor changes to the *RayGan* procedure.



Projection surface

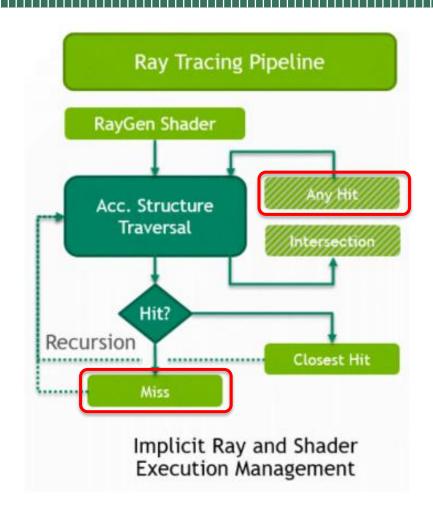
The *Intersection* shader allows to implement custom *ray-triangle intersection* procedures.

The Closest Hit shader is instead called on the point that is closer to the viewer. Its purpose is computing the color of the point, by approximating the rendering equation in a way similar to a fragment shader in the graphics pipeline, and for doing this it can recursively cast other rays.



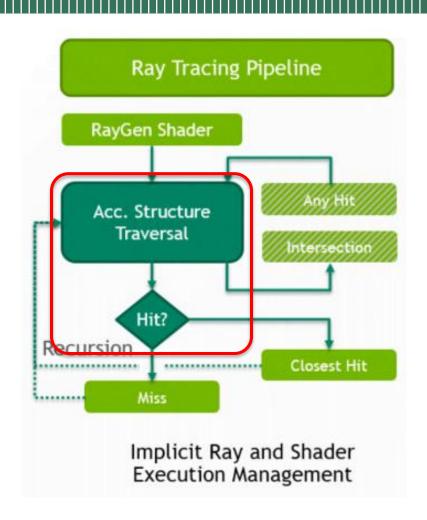
The Any Hit shader is used to filter out intersections that should not be considered, and can for example be used to handle partially transparent objects.

The *Miss* shader is instead called if the ray does not hit any object: generally it is used to draw some sort of background that should appear behind everything else.



The fixed part of the pipeline controls the acceleration structure traversal, and the determination of the closest hit.

Although being powerful, it is very resource demanding and only today's top GPUs can offer decent performance with real time ray tracing.



Ray tracing implementation

The pseudo-code of a ray tracing rendering algorithm is the following:

```
01 for each pixel x on screen do
02   Compute color casting a ray from x according the projection
03 end
```

The ray-casting procedure, is the hearth of the technique:

```
01 Determine the point q of the closest object w.r.t. the ray
02 Set the pixel color C = 0
03 for each light 1 in the scene do
04   if light 1 is not occluded (ray-casting) then
05     Set C = C + contribution of light 1 to q
06   end if
07 end
08 Set C = C + reflection contribution (recursion)
09 Set C = C + refraction contribution (recursion)
```

Ray tracing implementation

In a Ray Tracing pipeline, the *RayGen* Shader, and the *Closest Hit Shader* perform the tasks highlighted in the previous slide.

```
Ray Generation Shader
01 for each pixel x on screen do
02
      Compute color casting a ray from x according the projection
03 end
                  Intersection Shader
                                                        Miss Shader
                                           Hit?
                                      Any hit Shader
01 Determine the point q of the closest object w.r.t. the ray
02 Set the pixel color C = 0
                                                           Closest hit Shader
03 for each light 1 in the scene do
     if light 1 is not occluded (ray-casting) then
04
05
       Set C = C + \text{contribution of light } l \text{ to } q
     end if
06
07 end
08 Set C = C + \text{reflection contribution (recursion)}
09 Set C = C + \text{refraction contribution (recursion)}
```

Ray tracing - discussion

The number of traced rays potentially doubles at every step: this can significantly increase the rendering times. Moreover, it requires computation of the closest intersection using the *acceleration* structure instead of the Z-buffer.

Ray tracing allows including mirror reflection and transparency with refraction: this can be used to realistically reproduce glass, fluid, shiny metals and many other objects.

However, ray tracing is not able to simulate indirect lighting or consider glossy reflections, limiting the level of achievable realism.

Radiosity proposes a different simplification of the rendering equation. In particular it considers only materials that have a constant BRDF.

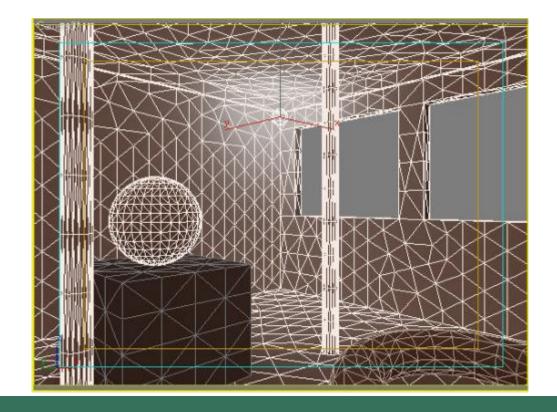
$$f_r(x, \omega_i, \omega_r) = \rho_x$$

The unknowns of the rendering equations are thus reduced to one variable per point of the objects since in this way reflection does not depend on the direction from which it is seen. This unknown is called the *radiosity* of the object (that is the output counterparts of the irradiance).

$$L(x, \omega_r) = L_e(x, \omega_r) + \int L(y, yx) f_r(x, yx, \omega_r) G(x, y) V(x, y) dy$$

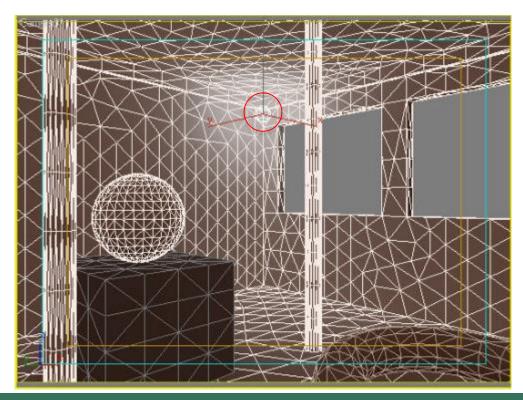
$$L(x) = L_e(x) + \rho_x \int L(y) G(x, y) V(x, y) dy$$

The surfaces of the objects are then split into patches, with one unknown per patch.



Light sources are implemented as patches that emits radiosity.

$$L(x) = L_e(x) + \rho_x \int L(y)G(x,y)V(x,y)dy$$



The rendering equation becomes a (large) system of linear equations that can be solved with an iterative technique.

$$L(x) = L_e(x) + \rho_x \int L(y)G(x,y)V(x,y)dy$$

$$L(x_i) = L_e(x_i) + \rho_{x_i} \sum_{y_j} L(y_j)G(x_i, y_j)V(x_i, y_j)$$

In matrix notation, vector L has one element (per color frequency) per patch, and represents its *radiosity*.

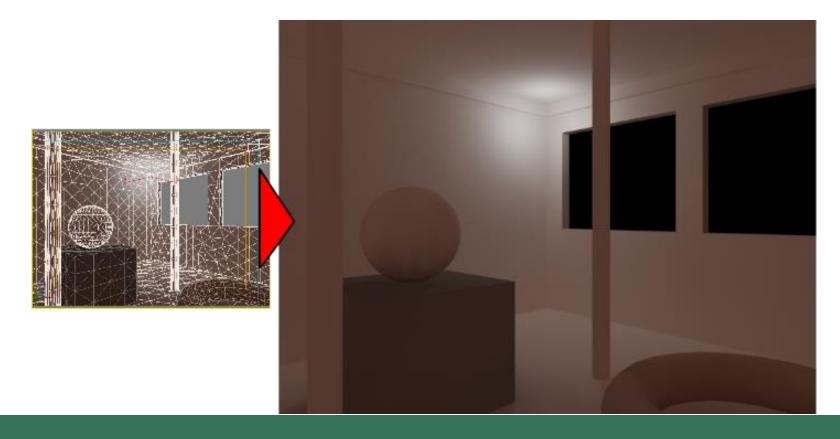
Matrix *R* includes the visibility, the constant BRDF, and the geometric relations between any two patches of scene.

$$L(x_i) = L_e(x_i) + \rho_{x_i} \sum_{y_j} L(y_j) G(x_i, y_j) V(x_i, y_j)$$

$$L(x_i) = L_e(x_i) + \sum_{y_j} L(y_j) R(x_i, y_j) \qquad R(x_i, y_j) = \rho_{x_i} G(x_i, y_j) V(x_i, y_j)$$

$$L = L_e + R \cdot L$$

The solutions of the equations are then interpolated to produce a view of the scene.



The pseudo-code of a radiosity rendering algorithm is the following:

```
01 Discretize the scene, and compute matrix R
02 Compute the solution of equation L = L_e + R \cdot L
03 Render the scene using either scan-line or raytracing
04 Interpolate L to obtain the color for each pixel
```

Indeed the most time consuming steps are steps **01** and **02**. However, once they have been computed, the scene can very quickly be rendered from any point of view.

In most of the cases, the solution of the equation can be computed with a fixed-point iteration, starting from L = 0, and refining its value at every iteration.

```
01 Lold = Lnew = 0

02 Repeat

03 Lold = Lnew

04 Lnew = L_e + R \cdot Lold

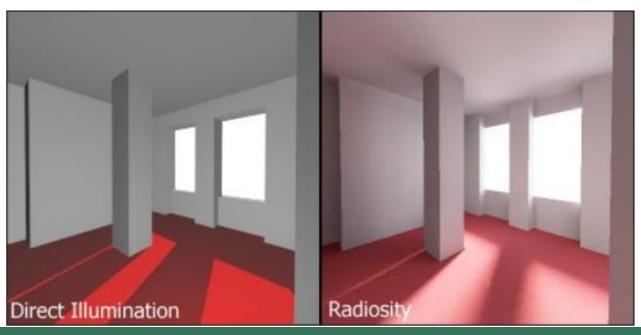
05 Until |Lnew - Lold| > threshold
```

Even if the number of patches is big, the loop converges in a moderate number of iterations.

Radiosity is able to capture indirect illumination effects.

Shadows however are usually very poorly approximated due to the size of the patches.

Mirror reflections and refractions cannot be considered directly, since they greatly depend on the direction from which an object is seen.



Radiosity is usually an off-line technique, and almost never implemented in real time. For this reason Vulkan and other low-level graphics engine have no specific pipelines to support it.

Montecarlo techniques

Photorealistic results can only be achieved by approximating the solution of the complete rendering equation.

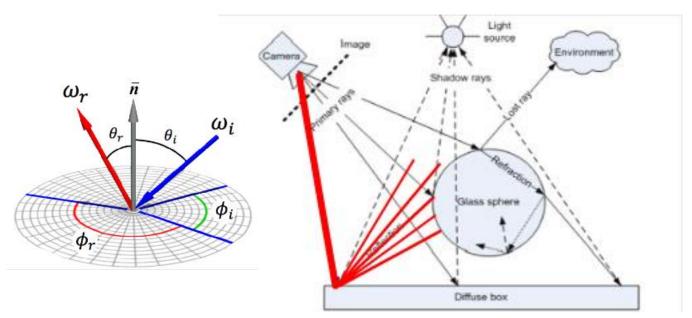
Due to its complexity, *Montecarlo* techniques are usually employed: the integral is computed by averaging several random points and directions chosen from the equations.

Many alternative approaches are possible: each advanced rendering engine exploits one of them.

Montecarlo techniques

Many techniques extend ray tracing: instead of sending a single ray in the mirror direction, a sampling of the *most probable* output directions is considered (*importance sampling*).

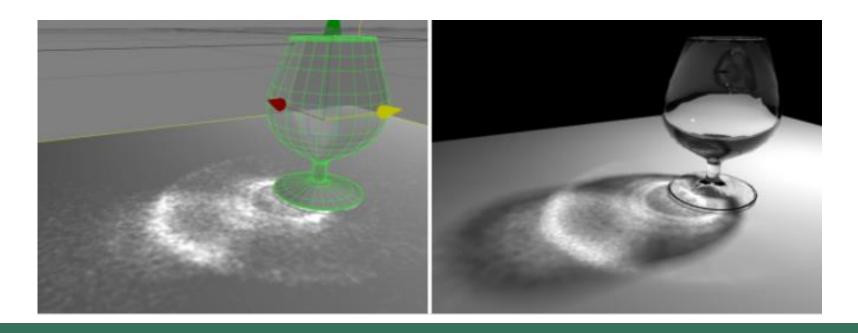
A ray is thus traced for each selected direction, and the radiance is computed using the BRDF of the considered material.



Montecarlo techniques (based on a limited number of rays) are sometimes implemented in real time, using the ray-tracing rendering pipeline.

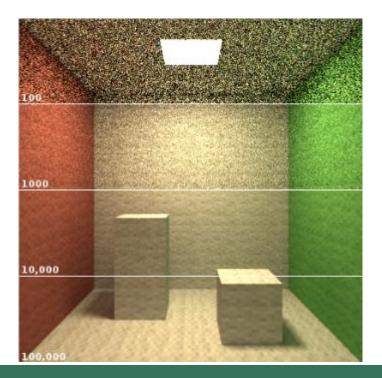
Montecarlo techniques

Photon mapping instead emulates the movements of photons in the scene, considering bounces, focalizations and other advanced phenomenon such as caustics.



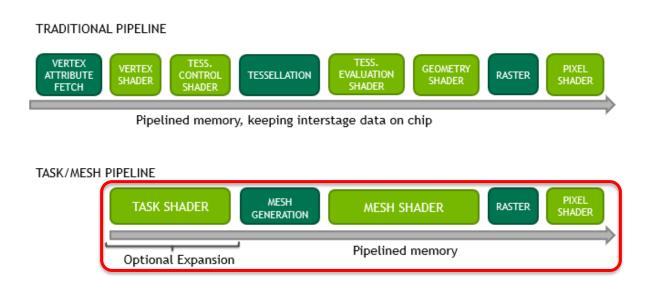
Montecarlo techniques

Due to the randomness that drives the techniques, *Montecarlo* based rendering algorithms tend to produce noisy images, whose effect can only be reduced by increasing the number of rays (and consequently, the rendering time).



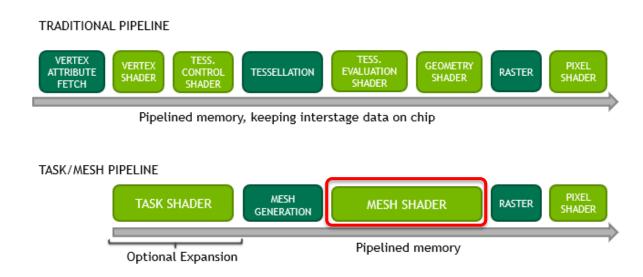
The *Mesh Shader* pipeline is a generalization of the graphics pipeline where no initial fixed part of the pipeline is considered and mesh generation can be entirely handled by the shaders.

MESHLETS



Mesh shaders computes indexed triangle lists, returned as a set of vertices and groups of three indices for each triangle. Vertices are computed in normalized screen coordinates to simplify rasterization.

MESHLETS

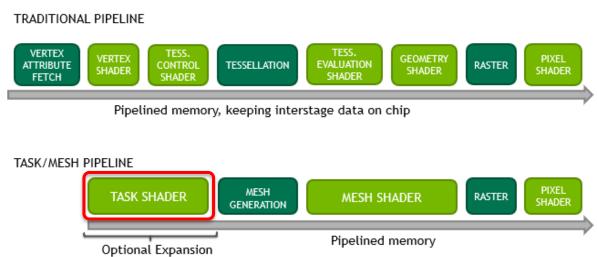


The number of vertices and triangles that a Mesh shader can generate is limited. For this reason each object is divided in a large number of patches so called *Meshlets*.



The purpose of the optional *Task* shader is to subdivide a larger mesh into smaller Meshlets, and control the corresponding *Mesh* shader for generating all the required patches.

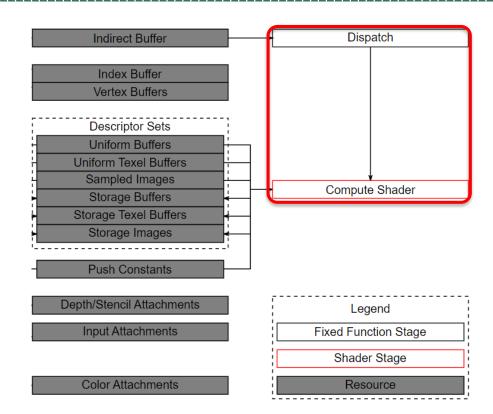
MESHLETS



The Compute pipeline

The *Compute* pipeline is not for rendering images, but for performing GPGPU computations.

In this case the application provides a single shader, the *Compute* Shader, that performs the desired operations.

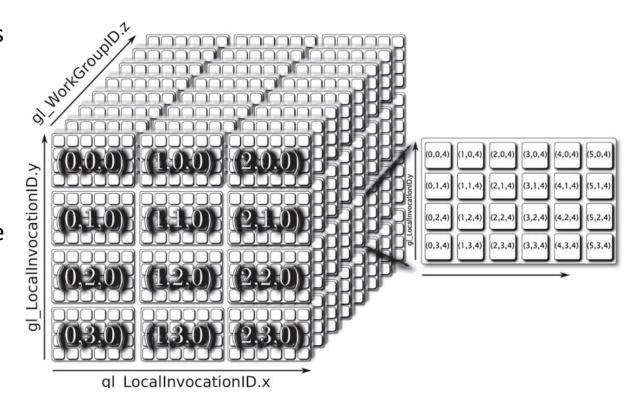


The Compute pipeline

Data is copied into buffers in the GPU memory (if available), and Compute shaders executions are identified by a (up to) tridimensional index.

Using this (vector) index, the shader can refer the data to find the partition on which it can work.

Please follow the GPU course, if you are more interested in the topic!



Programming in GLSL

Most of the BRDF functions, indirect light approximation and light emission models will be implemented using Shaders written with the GLSL language.

We have already seen how we can compile a shader from its GLSL source code to its SPIR-V intermediate representation required by Vulkan.

GLSL is a C-like language, and it is very similar to C, C++, C#, JAVA, JavaScript, PHP and many others.

Running example

To show the features, we will describe an example that computes the *Mandelbrot set* (the most famous fractal) using vertex and fragment shaders.

```
while (x*x + y*y ≤ 2*2 AND iteration < max_iteration) do
    xtemp := x*x - y*y + x0
    y := 2*x*y + y0
    x := xtemp
    iteration := iteration + 1

color := palette[iteration]</pre>
```

Program structure

Vertex shader

Shaders follow the classical convention, having global variables and functions in the main scope of the file.

The entry point of the shader can be user defined in the code that calls it:

however it is generally the

function main().

#version 450

Global definitions

```
layout (set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
} ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
  The main procedure
void main()
    gl Position = ubo.vpMat * ubo.worldMat *
                  vec4(inPosition, 1.0);
    real = inPosition.x * 2.5;
         = inPosition.y * 2.5;
```

Program structure

Vertex shader

Vulkan require that at least GLSL version is supported.

For this reason, a shader source code should start with the #version directive, asking at least for version 4.5

```
#version 450
```

```
layout (set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
} ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
// The main procedure
void main() {
    gl Position = ubo.vpMat * ubo.worldMat *
                  vec4(inPosition, 1.0);
    real = inPosition.x * 2.5;
    img = inPosition.y * 2.5;
```

Comments

Vertex shader

Comments in the code follows the classical *C* notations:

```
// for comments to the end of the line
/* begins a comment block
*/ ends a comment block
```

```
#version 450
layout(set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
} ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
   The main procedure
void main()
    gl Position = ubo.vpMat * ubo.worldMat *
                  vec4(inPosition, 1.0);
    real = inPosition.x * 2.5;
    img = inPosition.y * 2.5;
```

Vertex shader

Blocks are denoted using { }

```
#version 450
layout(set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
 ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
// The main procedure
void main() {
    gl Position = ubo.vpMat * ubo.worldMat *
                  vec4(inPosition, 1.0);
    real = inPosition.x * 2.5;
    img = inPosition.y * 2.5;
```

Variables

Variables are typed and their name follows the same C convention (case sensitive, allowing letters, numbers and underscore, but cannot start with a number).

As in C, variables are local to the block they are defined into.

```
#version 450
                                          Fragment shader
layout(location = 0) in float real;
layout(location = 1) in float img;
layout(location = 0) out vec4 outColor;
layout(set = 0, binding = 1) uniform
GlobalUniformBufferObject {
      float time;
} qubo;
void main() {
      float m real = 0.0f, m img = 0.0f, temp;
      for (i = 0; i < 16; i++) {
            if (m \text{ real } * m \text{ real } + m \text{ img } * m \text{ img } > 4.0)  {
                  break:
            temp = m real * m real - m img * m img + real;
            m img = 2.0 * m real * m img + img;
            m real = temp;
      outColor =
          vec4((float(i % 5) + sin(gubo.time*6.28)) / 5.0,
                 float(i % 10) / 10.0, float(i) / 15.0, 1.0);
```

Variables

Beside type and name, variables can be preceded with a large number of different qualifiers.

Most of them are required to interface them with the pipeline: we will return on that later.

```
#version 450
```

Fragment shader

```
layout(location = 0) in float real;
layout(location = 1) in loat img;
layout(location = 0) out vec4 outColor;
layout(set = 0, binding = 1) uniform
GlobalUniformBufferObject {
      float time;
} aubo;
void main() {
      float m real = 0.0f, m img = 0.0f, temp;
      int i:
      for (i = 0; i < 16; i++) {
            if (m \text{ real } * m \text{ real } + m \text{ img } * m \text{ img } > 4.0)  {
                  break:
            temp = m real * m real - m img * m img + real;
            m img = 2.0 * m real * m img + img;
            m real = temp;
      outColor =
           vec4((float(i % 5) + sin(qubo.time*6.28)) / 5.0,
                 float(i % 10) / 10.0, float(i) / 15.0, 1.0);
```

Data types

GLSL supports a large number of types:

Types [4.1]		Floating-Point O			Opaque Types (cont'd)	Unsigne	d Intege	er Opaqu	е Тур	es (cont'd)
Transparent Types		sampler{1D,2D,3D}	1D, 2D, or 3D texture	iimage2DRect	int. 2D rectangular image	uimage2DI	MSArray	uint 2D mu	lti-samp	le array image
void	no function return value	image{1D,2D,3D} samplerCube	cube mapped texture	isampler[1,2]DArray	integer 1D, 2D array texture	usamplerCubeArray uint		uint cube i	nt cube map array texture	
bool	Boolean	imageCube	cube mapped texture	iimage[1,2]DArray	integer 1D, 2D array image	uimageCubeArray uint		uint cube i	nt cube map array image	
int, uint	signed/unsigned integers	sampler2DRect	rectangular texture	isamplerBuffer	integer buffer texture	Implicit Conversions				
float	single-precision floating-point	image2DRect		iimageBuffer	integer buffer image	int	-> uin		ec2 -	> dvec2
lioat	scalar	sampler{1D,2D}Array	1D or 2D array texture	isampler2DMS	int. 2D multi-sample texture	int, uint	-> floa			> dvec3
double	double-precision floating scalar	image{1D,2D}Array		iimage2DMS	int. 2D multi-sample image	int, uint, flo		uble uv		
vec2, vec3, vec4	floating point vector	samplerBuffer	buffer texture	isampler2DMSArray	int. 2D multi-sample array tex.	ivec2	-> uve			> dvec2
dvec2, dvec3, dvec4	double precision floating-point	imageBuffer	2D multi comple touture	iimage2DMSArray	int. 2D multi-sample array image	ivec3	-> uve			> dvec3
bvec2, bvec3, bvec4	vectors Boolean vectors	sampler2DMS image2DMS	2D multi-sample texture	isamplerCubeArray	int. cube map array texture	ivec4 ivec2	-> uve			> dvec4 > dmat2
· · ·		sampler2DMSArray	2D multi-sample array		' '	ivec3	-> vec			> dmat2
ivec2, ivec3, ivec4 uvec2, uvec3, uvec4	signed and unsigned integer vectors	image2DMSArray	texture	iimageCubeArray	int. cube map array image	ivec4	-> vec			> dmat4
mat2, mat3, mat4	2x2, 3x3, 4x4 float matrix	samplerCubeArray	cube map array texture	Unsigned Intege	r Opaque Types	uvec2	-> vec		nt2x3 - nt2x4 -	4111442710
mat2x2, mat2x3,	2-column float matrix of	imageCubeArray		atomic uint	uint atomic counter	uvec3 uvec4	-> vec		nt2x4 - nt3x2 -	
mat2x4	2, 3, or 4 rows	sampler1DShadow	1D or 2D depth texture	usampler[1,2,3]D	uint 1D. 2D. or 3D texture	ivec2	-> dve		1t3x4 -	
mat3x2, mat3x3, mat3x4	3-column float matrix of 2, 3, or 4 rows	sampler2DShadow	with comparison	uimage[1,2,3]D	uint 1D, 2D, or 3D texture	ivec3	-> dve	ec3 ma	1t4x2 -	> dmat4x2
mat4x2, mat4x3,	4-column float matrix of	sampler2DRectShadov		usamplerCube	uint cube mapped texture	ivec4	-> dve	ec4 ma	at4x3 -	> dmat4x4
mat4x4	2, 3, or 4 rows	sampler1DArrayShadov sampler2DArrayShadov		uimageCube	uint cube mapped image					
dmat2, dmat3,	2x2, 3x3, 4x4 double-precision	samplerCubeShadow	cube map depth texture	usampler2DRect	uint rectangular texture		tion of Basic Types			
dmat4	float matrix	ounipier our contact	with comparison	uimage2DRect	uint rectangular image	Arrays	float[3] foo; float foo[3] // Structures, blocks, and st // can be arrays. Arrays of a			
dmat2x2, dmat2x3, dmat2x4	2-col. double-precision float matrix of 2, 3, 4 rows	samplerCubeArraySha		usampler[1,2]DArray	1D or 2D array texture					
dmat3x2, dmat3x3,	3-col. double-precision float		texture with comparison	uimage[1,2]DArray	1D or 2D array image	Structures				
dmat3x4	matrix of 2, 3, 4 rows	Signed Integer O	paque Types	usamplerBuffer	uint buffer texture		members			
dmat4x2, dmat4x3,	4-column double-precision float		integer 1D, 2D, or 3D texture	uimageBuffer	uint buffer image		} struct-n	<i>ame</i> []; nal variable d	oclaratio	
dmat4x4	matrix of 2, 3, 4 rows	iimage[1,2,3]D	integer 1D, 2D, or 3D image	usampler2DMS	uint 2D multi-sample texture	Blocks				
		isamplerCube integer cube mapped texture		uimage2DMS	uint 2D multi-sample image	Blocks in/out/uniform block-name { // interface matching by block name			•	
		iimageCube integer cube mapped image			1 0		optionally-qualified members			
		isampler2DRect	int. 2D rectangular texture	usampler2DMSArray			} instance	e-name[];		
			Continue ¹		Continue J		// optio	nal instance r	ame, opt	ionally an array

Data types

The most common scalar types are the following:

Types [4.1] Transparent Types					
void	no function return value				
bool	Boolean				
int, uint	signed/unsigned integers				
float	single-precision floating-point scalar				
double	double-precision floating scalar				

Vectors

GLSL has also types for containing vectors of 2, 3 or 4 components. vec n floating points vectors are the most widely used to describe colors and coordinates.

vec2, vec3, vec4	floating point vector
dvec2, dvec3, dvec4	double precision floating-point vectors
bvec2, bvec3, bvec4	Boolean vectors
ivec2, ivec3, ivec4 uvec2, uvec3, uvec4	signed and unsigned integer vectors

Vector elements

Vertex shader

Vector elements can be accessed individually using the "dot" syntax:

```
#version 450
layout(set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
} ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
// The main procedure
void main() {
    gl Position = ubo.vpMat * ubo.worldMat *
                  vec4(inPosition, 1.0);
    real = inPosition.x * 2.5;
    img
           inPosition.y * 2.5;
```

Vector elements

Since vectors can be used to store world coordinates, colors or texture coordinates, several aliases exist for each component:

```
light.x = light.r = light.s = 1.0
light.y = light.g = light.t = 0.9
light.z = light.b = light.p = 0.5
light.w = light.a = light.q = 1.0
```

More than one letter can be used to refer to more elements...

```
vec3 11 = light.xyz;
vec2 12 = light.rb;
```

Elements order can be mixed to shuffle a vector:

```
light.zxy = light.xyz;
```

Matrices

Matrix types are defined as well: again the most commonly used are the 2x2, 3x3 or 4x4 composed by single precision elements.

mat2, mat3, mat4	2x2, 3x3, 4x4 float matrix
mat2x2, mat2x3, mat2x4	2-column float matrix of 2, 3, or 4 rows
mat3x2, mat3x3, mat3x4	3-column float matrix of 2, 3, or 4 rows
mat4x2, mat4x3, mat4x4	4-column float matrix of 2, 3, or 4 rows
dmat2, dmat3, dmat4	2x2, 3x3, 4x4 double-precision float matrix
dmat2x2, dmat2x3, dmat2x4	2-col. double-precision float matrix of 2, 3, 4 rows
dmat3x2, dmat3x3, dmat3x4	3-col. double-precision float matrix of 2, 3, 4 rows
dmat4x2, dmat4x3, dmat4x4	4-column double-precision float matrix of 2, 3, 4 rows

Matrix elements

GLSL uses the column major encoding, and allows to access elements using indices starting from zero in [][] brackets.

Matrix columns can also be accessed as vectors:

GLM and GLSL types

The types defined in the GLM library we used in our C++ source code, have been named to follow the equivalent GLSL conventions: this simplifies the interactions between the shaders and the application code.

GLSL

vec2, vec3, vec4	floating point vector	or	1					
dvec2, dvec3, dvec4	double precision flo vectors	pating-point						
bvec2, bvec3, bvec4	Boolean vectors							
ivec2, ivec3, ivec4 uvec2, uvec3, uvec4 mat2, mat3, mat4	signed and unsigne vectors 2x2, 3x3, glm::m			M (ir	C+	+)		
mat2x2, mat2x3, mat2x4	2-column M1 = t	ranslate(glum::mat4(1,	, .,, lm::mat4(1), ,2,3,4,5,6,7					16);
mat3x2, mat3x3, mat3x4	3-column for (in 2, 3, or 4) for (t i = 0; i int j = 0;	j < 4; j++)	{	[gribau		os-MBP o	
mat4x2, mat4x3, mat4x4	4-column st 2.3. or 41 }	d::cout <<	M1[j][i] <<	"\t";	0	0 1 0	0 0 1	1 2 3
dmat2, dmat3, dmat4	2x2, 3x3, for(:cout << "\ int j = 0; d::cout <<	(t"; j < 4; j++) M2[j][i] <<	{ "\t":	5	13	0 21	1 29
dmat2x2, dmat2x3, dmat2x4	2-col. dou }	:cout << "\			10 15 4	22 31 8	34 47 12	46 63 16
dmat3x2, dmat3x3, dmat3x4		out << "\n'	'; < 4; i++) {		gribau	do@Marco	os-MBP o	ther st
dmat4x2, dmat4x3, dmat4x4	4-column for(int $j = 0$;	j < 4; j++) M[j][i] <<	{				
	}	:cout << "\n'						

Vector and matrix literals

Matrix and vector elements can be constructed using the *type name*, followed by the comma separated list of elements between ()

```
#version 450
                                           Fragment shader
layout(location = 0) in float real;
layout(location = 1) in float img;
layout(location = 0) out vec4 outColor;
layout (set = 0, binding = 1) uniform
GlobalUniformBufferObject {
      float time;
} qubo;
void main() {
      float m real = 0.0f, m img = 0.0f, temp;
      int i:
      for (i = 0; i < 16; i++) {
            if (m \text{ real } * m \text{ real } + m \text{ img } * m \text{ img } > 4.0)  {
                  break:
            temp = m real * m real - m img * m img + real;
            m img = 2.0 * m real * m img + img;
            m real = temp;
      outColor =
           vec4((float(i % 5) + sin(qubo.time*6.28)) / 5.0,
                 float(i % 10) / 10.0, float(i) / 15.0, 1.0)
```

Vector and matrix literals

Vertex shader

Larger vectors can be composed adding elements to shorter ones.

```
#version 450
layout(set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
} ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
// The main procedure
void main() {
    gl Position = ubo.vpMat * ubo.worldMat *
                  vec4(inPosition, 1.0);
    real = inPosition.x * 2.5;
    img = inPosition.y * 2.5;
```

Type Casting

The same syntax can also be used to perform explicit type casting, when available.

```
Fragment shader
layout(location = 0) in float real;
layout(location = 1) in float img;
layout(location = 0) out vec4 outColor;
layout (set = 0, binding = 1) uniform
GlobalUniformBufferObject {
     float time;
} qubo;
void main() {
     float m real = 0.0f, m img = 0.0f, temp;
     int i:
     for (i = 0; i < 16; i++) {
           if (m real * m real + m img * m img > 4.0) {
                 break:
           temp = m real * m real - m img * m img + real;
           m img = 2.0 * m real * m img + img;
           m real = temp;
     outColor =
                float(i % 5) + sin(qubo.time*6.28)) / 5.0,
          vec4(
```

#version 450

loat(i % 10) / 10.0, float(i) / 15.0, 1.0);

Algebraic operations

Vertex shader

Algebraic operations and assignments, including the ones between vector and matrices, is done using the conventional operators.

```
#version 450
layout(set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
} ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
// The main procedure
void main() {
    gl Position = ubo.vpMat * ubo.worldMat
                  vec4(inPosition, 1.0);
    real = inPosition.x * 2.5;
         = inPosition.y * 2.5;
```

GLSL operators

GLSL includes a large set of common C operators:

Operators and Expressions [5.1] The following operators are numbered in order			3.	++ +-~!	prefix increment and decrement unary	11. 12.	 &&	bit-wise inclusive or logical and	
of pred	The following operators are numbered in order of precedence. Relational and equality operators evaluate to Boolean. Also See lessThan(), equal().			*/%	multiplicative	13.	۸۸	logical exclusive or	
evalua	evaluate to Boolean. Also See lessThan(), equal().		5.	+-	additive	14.	П	logical inclusive or	
1.	()	parenthetical grouping	6.	<< >>	bit-wise shift	15.	?:	selects an entire operand	
	[] array subscript		7.	<> <= >=	relational		= += -=	assignment arithmetic assignments	
	[] array subscript () function call, constructor, structure	8.	== !=	equality	16.	*= /= %= <<= >>=			
2.	field, selector, swizzle ++ postfix increment and decrement		9.	&	bit-wise and		&= ^= =	and interior assignments	
			10.	۸	bit-wise exclusive or	17.	,	sequence	

Functions

Functions definitions and function calls follow the classical C convention:

definition:

```
return type name (args, ...)
{...} // function body
```

call:

```
name (args, ...)
```

```
#version 450
                                          Fragment shader
layout(location = 0) in float real;
layout(location = 1) in float img;
layout(location = 0) out vec4 outColor;
layout(set = 0, binding = 1) uniform
GlobalUniformBufferObject {
      float time;
} qubo;
       main procedure
void main()
      float m real = 0.0f, m img = 0.0f, temp;
      int i:
      for (i = 0; i < 16; i++) {
            if (m \text{ real } * m \text{ real } + m \text{ img } * m \text{ img } > 4.0)  {
                  break:
            temp = m real * m real - m img * m img + real;
            m img = 2.0 * m real * m img + img;
            m real = temp;
      outColor =
          vec4((float(i % 5) + sin(gubo.time*6.28)
                float(i % 10) / 10.0, float(i) / 15.0, 1.0);
```

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Built-In Functions Angle & Trig. Functions [8.1] Functions will not result in a divide-by-zero error. If the divisor of a ratio is 0, then results will be undefined. Component-wise operation. Parameters specified as angle are in units of radians. Tf=float, vecn.		Common Functions (cont.) Returns maximum value: Tfd max(Tfd x, Tfd y) Tiu max(Tiu x, Tiu y) Tf max(Tf x, float y) Ti max(Ti x, int y) Td max(Td x, double y) Tu max(Tu x, uint y)	Type Abbreviations for Built-in Functions: In vector types, n is 2, 3, If=float, vecn. Td =double, dvecn. Tfd= float, vecn, double, dvecn. Tb= bool, bve Tu=uint, uvecn. Ti=int, ivecn. Tiu=int, ivecn, uint, uvecn. Tvec=vecn, uvecn, i Within any one function, type sizes and dimensionality must correspond after implicit conversions. For example, float round(float) is supported, but float round(vec4) is				
Tf radians(Tf degrees)	degrees to radians	Returns min(max(x, minVal), maxVal):	Geometric Functions [8.5] These functions operate on vectors as vectors, not component-wise. Tf=float, vecn. Td =double, dvecn. Tfd=float, vecn, double, dvecn.		Integer Functions (cont.)		
Tf degrees(Tf radians) Tf sin(Tf angle)	radians to degrees	Tfd clamp(Tfd x, Tfd minVal, Tfd maxVal) Tf clamp(Tf x, float minVal, float maxVal)			Returns the reversal of the bits of value: Tiu bitfieldReverse(Tiu value)		
Tf cos(Tf angle)	cosine	Td clamp(Td x, double minVal, double maxVal) Tiu clamp(Tiu x, Tiu minVal, Tiu maxVal)	float length(Tf x) double length(Td x)	length of vector	Inserts the bits least-significant bits of insert into base: Tiu bitfieldInsert(Tiu base, Tiu insert, int offset, int bits)		
Tf tan(Tf angle) Tf asin(Tf x)	tangent arc sine	Ti clamp (Ti x, int minVal, int maxVal) Tu clamp (Tu x, uint minVal, uint maxVal)	float distance (Tf p0, Tf p1) double distance (Td p0, Td p1)	distance between points	Returns the number of bits set to 1: Ti bitCount(Tiu value)		
Tf acos(Tf x)	arc cosine	Returns linear blend of x and y: Tfd mix(Tfd x, Tfd y, Tfd a) Ti mix(Ti x, Ti y, Ti a)	float dot (Tf x, Tf y) double dot (Td x, Td y)	dot product	Returns the bit number of the least significant bit: Ti findLSB(Tiu value)		
Tf atan(Tf y, Tf x) Tf atan(Tf y_over_x)	arc tangent	Tf mix(Tf x, Tf y, float a) Tu mix(Tu x, Tu y, Tu a) Td mix(Td x, Td v, double a)	vec3 cross(vec3 x, vec3 y)	cross product	Returns the bit number of the most significant bit: Ti findMSB(Tiu value)		
Tf sinh(Tf x)	hyperbolic sine	Components returned come from x when a components	dvec3 cross(dvec3 x, dvec3 y) Tfd normalize(Tfd x)	normalize vector to length 1	Texture Lookup Functions [8.9]		
Tf cosh(Tf x)	hyperbolic cosine	are true, from y when a components are false:	Tfd faceforward(Tfd N,	returns N if dot(Nref, I) <	Available to vertex, geometry, and fragment		
Tf tanh(Tf x)	hyperbolic tangent	Tfd mix(Tfd x, Tfd y, Tb a) Tb mix(Tb x, Tb y, Tb a) Tiu mix(Tiu x, Tiu y, Tb a)	Tfd I, Tfd Nref)	0, else -N	shaders. See tables on next page.		
Tf asinh(Tf x)	hyperbolic sine	Returns 0.0 if <i>x</i> < <i>edge</i> , else 1.0:	Tfd reflect(Tfd I, Tfd N)	reflection direction I - 2 * dot(N,I) * N	Atomic-Counter Functions [8.10]		
Tf acosh(Tf x)	hyperbolic cosine	Tfd sten(Tfd edge Tfd x)	Tfd refract(Tfd I, Tfd N,	, , , ,	Returns the value of an atomic counter. Atomically increments c then returns its prior value:		
Tf atanh(Tf x)	hyperbolic tangent	Tf step(float edge, Tf x) Td step(double edge, Td x)	float eta)	refraction vector	uint atomicCounterIncrement(atomic_uint c)		
Exponential Functions [8.2] Component-wise operation. Tf=float, vecn.		Clamps and smoothes: Tfd smoothstep(Tfd edge0, Tfd edge1, Tfd x)	Matrix Functions [8.6] N and M are 1, 2, 3, 4. mat matrixCompMult(mat x, mat y) component-wise multiply		Atomically decrements c then returns its prior value: uint atomicCounterDecrement(atomic_uint c)		
Td= double, dvecn. Tfd= Tf, Td Tf $pow(Tf x, Tf y)$ x^y		Tf smoothstep(float edge0, float edge1, Tf x) Td smoothstep(double edge0, double edge1, Td x)			Atomically returns the counter for c: uint atomicCounter(atomic_uint c)		
Tf exp(Tf x)	e _x	Returns true if x is NaN: Tb isnan(Tfd x)	matN outerProduct(vecN c, v dmatN outerProduct(dvecN c		Atomic operations performed on <i>c</i> , where Op may be Add, Subtract, Min, Max, And, Or, Xor:		
Tf log(Tfx)	In	Returns true if x is positive or negative infinity:	matNxM outerProduct(vecM c, vecN r) dmatNxM outerProduct(dvecM c, dvecN r) outer product		uint atomicCounterOp(atomic_uint c, uint data)		

Tb isinf(Tfd x)

matN transnose(matN m)

Atomically swap values of c and data; returns its prior value:

Tf exp2(Tf x)

Conditional statements

The classical **if else** statement, and the ?: in-line syntax can be used to control the execution of a procedure.

```
#version 450
                                        Fragment shader
layout(location = 0) in float real;
layout(location = 1) in float img;
layout(location = 0) out vec4 outColor;
layout(set = 0, binding = 1) uniform
GlobalUniformBufferObject {
     float time;
} qubo;
void main() {
     float m real = 0.0f, m img = 0.0f, temp;
     int i:
     for(i = 0: i < 16: i++) 
           if (m real * m real + m img * m img > 4.0)
                 break:
            temp = m real * m real - m img
           m img = 2.0 * m real * m img + img;
           m real = temp;
     outColor =
          vec4((float(i % 5) + sin(qubo.time*6.28)) / 5.0,
               float(i % 10) / 10.0, float(i) / 15.0, 1.0);
```

Loops

for() and while() loops are also available:

Iteration and Jumps [6.3-4]

iteration and Jumps [0.5-4]					
Function	call by value-return				
Iteration	for (;;) { break, continue } while () { break, continue } do { break, continue } while ();				
Selection	<pre>if () { } if () { } else { } switch () { case integer: break; default: }</pre>				
Entry	void main()				
Jump	break, continue, return (There is no 'goto')				
Exit	return in main() discard // Fragment shader only				

```
#version 450
                                       Fragment shader
layout(location = 0) in float real;
layout(location = 1) in float img;
layout(location = 0) out vec4 outColor;
layout(set = 0, binding = 1) uniform
GlobalUniformBufferObject {
     float time;
} qubo;
void main() {
     float m real = 0.0f, m img = 0.0f, temp;
     int i;
      for (i = 0; i < 16; i++)
            ii(m real * m real + m img * m img > 4.0) {
                 break:
           temp = m real * m real - m img * m img + real;
           m img = 2.0 * m real * m img + img;
           m real = temp;
     outColor =
          vec4((float(i % 5) + sin(qubo.time*6.28)) / 5.0,
               float(i % 10) / 10.0, float(i) / 15.0, 1.0);
```

Loop exit statements

Common C statements for exiting loops can also be used.

Iteration and Jumps [6.3-4] Function call by value-return for (;;) { break, continue } Iteration while () { break, continue } do { break, continue } while (); Selection if () {} if () { } else { } switch () { case integer: ... break; ... default: ... } void main() Entry break, continue, return Jump (There is no 'goto') Exit return in main() discard // Fragment shader only

```
#version 450
                                        Fragment shader
layout(location = 0) in float real;
layout(location = 1) in float img;
layout(location = 0) out vec4 outColor;
layout (set = 0, binding = 1) uniform
GlobalUniformBufferObject {
     float time;
} qubo;
void main() {
     float m real = 0.0f, m img = 0.0f, temp;
     int i:
     for (i = 0; i < 16; i++) {
           if (m real * m real + m img * m img > 4.0) {
           temp = m real * m real - m img * m img + real;
           m img = 2.0 * m real * m img + img;
           m real = temp;
     outColor =
          vec4((float(i % 5) + sin(qubo.time*6.28)) / 5.0,
               float(i % 10) / 10.0, float(i) / 15.0, 1.0);
```

Note on flow control

Please note that flow control statements on the GPU behaves differently than on the CPU.

The SIMD architecture of GPU, which always processes many elements at the same time, have some nasty implications:

- Both the if and else branches are always executed.
- In variable length loops, all executions are conditioned by the longest one in the batch being run concurrently.

This is why it is always a good idea trying to avoid loops (with variable number of iterations) and conditional statements as much as possible.

Shader-pipeline communication

Vertex shader

Communication between the Shaders and the Pipeline occurs through global variables.

```
#version 450
layout(set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
} ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
// The main procedure
void main() {
    gl Position = ubo.vpMat * ubo.worldMat *
                  vec4(inPosition, 1.0);
    real = inPosition.x * 2.5;
    img = inPosition.y * 2.5;
```

Shader-pipeline communication: in and out

Vertex shader

in and out variables are used to interface with the programmable or configurable part of the pipeline.

We will consider the mechanism in detail in the following lessons.

```
#version 450
layout(set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
} ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
// The main procedure
void main() {
    gl Position = ubo.vpMat * ubo.worldMat *
                  vec4(inPosition, 1.0);
    real = inPosition.x * 2.5;
    img = inPosition.y * 2.5;
```

Shader-pipeline communication: built-in variables

Vertex shader

Communication with the fixed part of the pipeline also occurs through some predefined global variables.

For example, in a Vertex shader, $gl_Position$ is a vec4 variable that must be filled with the clipping coordinates of the corresponding vertex.

```
#version 450
layout(set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
} ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
// The main procedure
void main() {
      Position = ubo.vpMat * ubo.worldMat *
                  vec4(inPosition, 1.0);
    real = inPosition.x * 2.5;
         = inPosition.y * 2.5;
```

Shader-pipeline communication: built-in variables

Although gl Position is the most important one, which is always required in any applications using the graphic pipeline, a lot more global variables exit, mainly to interface with other shaders types.

For time constraints, we will not cover them in detail.

> Please also note that some variables have changed name in Vulkan, even if a complete list of the changes is not easy to find.

Built-In Variables [7]

Vertex Language

```
in int gl VertexID;
        gl InstanceID;
       gl BaseInstance
       gl BaseVertex
in int gl DrawID
out gl PerVertex {
  vec4 gl Position;
  float gl PointSize;
  float gl ClipDistance[];
  float gl CullDistance[];
```

Tessellation Control Language

```
in gl PerVertex {
  vec4 gl_Position;
  float gl PointSize;
  float gl ClipDistance[];
  float gl CullDistance[];
} gl in[gl MaxPatchVertices];
in int gl PatchVerticesIn;
in int gl PrimitiveID;
in int gl InvocationID;
out gl PerVertex {
  vec4 gl_Position;
  float gl PointSize;
  float gl ClipDistance[];
  float gl CullDistance[];
} gl_out[];
patch out float gl_TessLevelOuter[4];
patch out float gl TessLevelInner[2];
```

Tessellation Evaluation Language

```
in gl PerVertex {
  vec4 gl Position;
  float gl PointSize:
  float gl_ClipDistance[];
  float gl CullDistance[];
} gl in[gl MaxPatchVertices];
in int gl_PatchVerticesIn;
in int gl_PrimitiveID;
in vec3 gl_TessCoord;
patch in float gl_TessLevelOuter[4];
patch in float gl TessLevelInner[2];
out gl PerVertex {
 vec4 gl Position;
 float gl PointSize:
 float gl ClipDistance[];
  float gl CullDistance[];
```

Geometry Language

```
in gl PerVertex {
  vec4 gl Position;
  float gl PointSize;
  float gl ClipDistance[]:
  float gl CullDistance[];
} gl_in[];
in int gl PrimitiveIDIn;
in int gl InvocationID;
out gl PerVertex {
  vec4 gl Position;
  float gl_PointSize;
  float gl_ClipDistance[];
  float gl CullDistance[];
out int gl PrimitiveID;
```

Fragment Language

out int gl Layer;

out int gl ViewportIndex;

```
in vec4 gl FragCoord;
in bool gl_FrontFacing;
in float gl ClipDistance[];
in float gl CullDistance[];
in vec2 gl PointCoord;
in int gl PrimitiveID:
        gl SampleID;
in vec2 gl_SamplePosition;
        gl_SampleMaskIn[];
        gl_Layer;
        gl ViewportIndex;
in bool gl HelperInvocation;
out float gl_FragDepth;
out int gl SampleMask[];
```

Compute Language

More information in diagram on page 6.

Work group dimensions

in uvec3 gl NumWorkGroups; const uvec3 gl WorkGroupSize; in uvec3 gl LocalGroupSize;

Work group and invocation IDs

in uvec3 gl WorkGroupID; in uvec3 gl_LocalInvocationID;

Derived variables

in uvec3 gl GlobalInvocationID; in uint gl LocalInvocationIndex;

Shader-application communication

Vertex shader

Communication between the Shaders and the application occurs using special types of external variables, usually called *Uniforms*.

The most common on are the *Uniform Variables Blocks*.

```
#version 450
```

```
layout(set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
} ubo;
```

Shader-application communication

Vertex shader

Each block is similar to a C typedef struct element: it has assigned a tag and a name, and it contains a set of components.

In the following lessons, we will focus on the way in which blocks are connected between the shaders and the application.

```
#version 450
layout (set = 0, binding = 0) uniform
UniformBufferObject {
    mat4 worldMat;
    mat4 vpMat;
 ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
// The main procedure
void main() {
    gl Position = ubo.vpMat * ubo.worldMat *
                  vec4(inPosition, 1.0);
    real = inPosition.x * 2.5;
         = inPosition.y * 2.5;
```

Shader-application communication

Vertex shader

Elements of the blocks are accessed in a Shader program exactly as fields of a structure in the C code.

```
#version 450
layout(set = 0, binding = 0) uniform
UniformBufferObject {
       4 worldMat;
     mat4 vpMat;
} ubo;
layout(location = 0) in vec3 inPosition;
layout(location = 0) out float real;
layout(location = 1) out float img;
// The main procedure
void main() {
    gl Position = ubo.vpMat * ubo.worldMat
                   vec4(inrosition, i.Ū);
    real = inPosition.x * 2.5;
    img = inPosition.y * 2.5;
```



Marco Gribaudo

Associate Professor

CONTACTS

Tel. +39 02 2399 3568

marco.gribaudo@polimi.it https://www.deib.polimi.it/eng/home-page

> (Remember to use the phone, since mails might require a lot of time to be answered. Microsoft Teams messages might also be faster than regular mails)