Practice Set 2

A. The Fibonacci sequence is composed of numbers where each number is the sum of the two previous numbers:

$$F_n = F_{n-1} + F_{n-2}$$
, where $F_0 = 0$, $F_1 = 1$

Using recursion, implement the procedure FIBONACCI(n) which computes the nth Fibonacci number.

- B. Given a sorted array, we can use binary search to find an element in O(lg n) time. Using recursion, implement the procedure BINARY-SEARCH(A, value, start, end) which searches for the element value in the sorted array A from index start to end. The result is the index of given element. For extra practice, implement it again without recursion.
- C. Implement MERGE(A, p, q, r) which merges the sorted subarrays A[p..q] and A[(q+1)..r] back into the array A.
- D. Implement MERGE-SORT(A, p, r) which sorts the elements from p to r in an array A.
- E. Implement MAX-HEAPIFY(A, i, h) which processes the nodes in array A of the subtree at index i with heap size h, to maintain the max-heap property at i.
- F. Implement BUILD-MAX-HEAP(A) which converts an entire array A into a heap.
- G. Implement HEAPSORT(A) using the previous procedures MAX-HEAPIFY and BUILD-MAX-HEAP to sort the array *A*.
- H. *HARD* (CLRS 6.5-9) Give an O(*n* lg *k*)-time algorithm to merge *k* sorted lists into one sorted list, where *n* is the total number of elements in all the input lists. (Hint: Use a min-heap for *k*-way merging.)