

Data Structures and their Use in Elementary Algorithms

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Preface

Data structures deal with the representation and arrangement of data that we use in computer programs. Based on how we represent data, certain features of our program can be highly efficient or inefficient and, often, limits what our programs can do. Therefore, the study of data structures is essential in computer science education. In fact, a part of the reason we can program modern-day computers so easily is because programming languages allow us to define variables and constants the way we humans understand that languages translate to bits of electrical signals that computers can process. You would be surprised to know that in the early days of computers, users had to write binary numbers (that is, just sequences of zeros and ones) to communicate with the computers. Numbers, characters, and even instructions were just sequences of zeros and ones that users needed to tediously write and then send to the machine to let it do any computation. Imagine how hard and error-prone that mode of programming was. So it is a blessing that we can use data structures whose behavior we easily comprehend when writing computer programs.

Just as big structures in the real world such as roads, buildings, cars, and electrical grids are made of building block elements such as concrete, brick blocks, aluminum, and wires; complex data structures that our programs use are made out of elementary data structures. These elementary data structures are so common that they have been standardized among languages and hardware. *They are typically called primitive data types as there is no structure below them.* For example, bit (aka. A true/false value), byte, character, integer, single-precision fractional number (aka, floating points), double precision fractional numbers are supported by virtually all hardware and programming languages. Larger structures are a combination of these smaller structures and most often a collection of them.

In fact, larger data structures are made of multiple layers of intermediate data structures that go back to primitive data types. For example, to represent a 2D rectangle (a data structure) you need four points (an intermediate data structure) each of which has two integers (for horizontal and vertical placement). Now to compute the total land area covered by a region of rectangular land plots, you would need a collection type data structure that holds all rectangles. Suppose in your computer program you need to know the total number of rectangles frequently. Without any additional info in your collection data structure, you would need to count the rectangles every time you need that information. However, if you keep a counter in the collection that you increase by one every time you add a new rectangular plot, then when querying the total number of rectangles, you could quickly use that counter. So you understand depending on how you structure the data some features may take constant time or involve a lot of computations. Consider another program, where you know that all plots are of the same size. Then you do not need a collection data structure at all. You just need the counter and a single rectangle. This saves a lot of space.

I hope you understand from this simple example, why the choice of data structures is so important. A good grasp of data structures is indispensable for any programming related job and even in hardware design. If you want to do research in computer science in the future then you need a strong foundation on data structures even more. That is why the data structures course is in the program core. I would take it further to say that it is among the few courses that are at the very center of the core program curriculum.

You now understand the pivotal role of data structures in program and hardware design. But what does it mean to have a strong foundation on data structures? It means you are capable of